

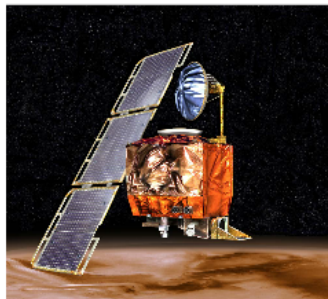


Units of Measure

✗ $42 \text{ m/s} + 137.8 \text{ ft/s}$

✓ $45 \text{ kg} * 10 \text{ m/s}^2 == 450 \text{ N}$

Accidents



Mars Climate Orbiter

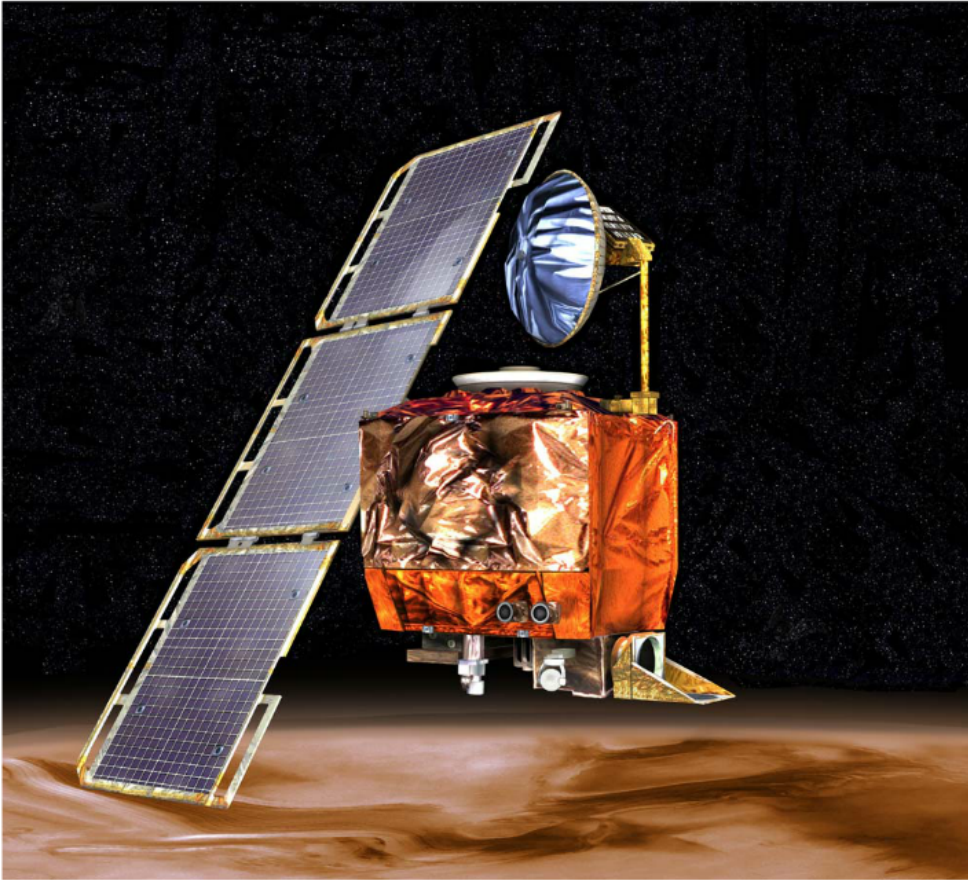
lbs·s ↔ N·s

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lbs·s \leftrightarrow N·s



compile time only

unit inference

Declaration

user defined units

```
[<Measure>] type m  
[<Measure>] type s
```

```
[<Measure>] type N = kg m/s^2
```

Generics

```
let sqr (x:float<_>) = x*x  
// sqr: float<'u> -> float<'u^2>
```

```
let variance xs = let m = mean xs  
  in mean_by (fun x -> sqr(x-m)) xs  
// variance: float<'u> list -> float<'u^2>
```

Usage

```
let gravity = 9.81<m/s^2> // acceleration  
let windowHeight = 5.6 m
```

```
let impactSpeed = sqrt(2 * gravity * windowHeight)  
// impactSpeed: float<m/s>
```

Parametrized Types

```
type Vector2< [<Measure>] 'u> =  
  { x: float<'u>; y: float<'u> }
```

```
let center = { x = 4.0<m>; y = 3.2<_> }  
// center: Vector2<m>
```



F#

compile time only

unit inference

Declaration

user defined units

[<Measure>] type m

[<Measure>] type s

[<Measure>] type N = kg m/s²

Usage

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C++ - Boost.Unit

Template Metaprogramming

Operator Overloading

No Runtime Overhead

Concepts

Base Dimension	length, time
Base Unit	meter, second
Unit	$m^2 \cdot s$
System	SI-System
Quantity	42 m/s

Usage

```
quantity<length, double> dx(2.0 * si::meter);
```

```
quantity<length, measurement<double>>  
  u(measurement<double>(4.52, 0.02)*meters);
```

Unit System Agnostic

Homogeneous vs Heterogeneous Systems

```
template<class System, class Y>  
quantity<unit<energy_dimension, System>, Y>  
work(quantity<unit<force_dimension, System>, Y> F,  
      quantity<unit<length_dimension, System>, Y> dx)  
{ return F*dx; }
```

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Concepts

Base Dimension

length, time

Base Unit

meter, second

Unit

$\text{m}^2 \cdot \text{s}$

System

SI-System

Quantity

42 m/s

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