# **SUMMARY**

USC ID/s: 1290146248\_2212208812\_8841152462

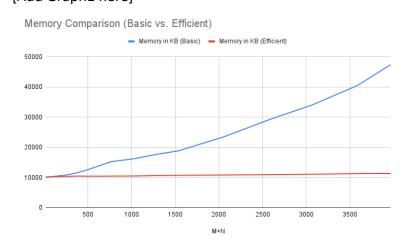
# **Datapoints**

| M+N  | Time in MS (Basic) | Time in MS (Efficient) | Memory in<br>KB (Basic) | Memory in<br>KB (Efficient) |
|------|--------------------|------------------------|-------------------------|-----------------------------|
| 16   | 0.5998611450195312 | 0.6871223449707031     | 10136                   | 10132                       |
| 64   | 2.86102294921875   | 3.492116928100586      | 10204                   | 10216                       |
| 128  | 5.658864974975586  | 11.647939682006836     | 10408                   | 10284                       |
| 256  | 18.890857696533203 | 31.792879104614258     | 10832                   | 10332                       |
| 384  | 30.737876892089844 | 63.09986114501953      | 11592                   | 10468                       |
| 512  | 55.70030212402344  | 121.00100517272949     | 12716                   | 10404                       |
| 768  | 113.09123039245605 | 253.27181816101074     | 15252                   | 10446                       |
| 1024 | 222.2001552581787  | 428.9369583129883      | 16180                   | 10484                       |
| 1280 | 323.6548900604248  | 635.7378959655762      | 17616                   | 10628                       |
| 1536 | 475.71301460266113 | 906.5980911254883      | 18824                   | 10708                       |
| 2048 | 828.8929462432861  | 1590.142011642456      | 23384                   | 10816                       |
| 2560 | 1313.7898445129395 | 2483.47806930542       | 28996                   | 10924                       |
| 3072 | 1877.3260116577148 | 3771.138906478882      | 34100                   | 11064                       |
| 3584 | 2453.4738063812256 | 5527.33302116394       | 40464                   | 11272                       |
| 3968 | 3243.7970638275146 | 6127.490043640137      | 47416                   | 11316                       |

# Insights

As the input size increase, the time and space usage increase faster in the basic version, as well as the time usage of the efficient version, but the memory usage of the efficient version seems proportional to the increase in the input size. From the datapoints we can find out that the time usage of the efficient version is always greater than (at least equal) the time usage of the basic version because we can either optimize the time or space. For the efficient version, we optimized the space usage at the expense of time usage.

Graph1 – Memory vs Problem Size (M+N) [Add Graph1 here]



## Nature of the Graph (Logarithmic/Linear/Polynomial/Exponential)

Basic: Polynomial O(mn) Efficient: Linear O(m + n)

### **Explanation:**

We can clearly see that the cost of memory is optimized when the problem size increases. This is because, for the recursive calls in the efficient algorithm, we work on one recursive call at a time and reuse the memory space from one call to the next. In contrast, we spend an m \* n space to record all possible matching in DP.

Graph2 – Time vs Problem Size (M+N) [Add Graph2 here]



Nature of the Graph (Logarithmic/Linear/Polynomial/Exponential)

Basic: Polynomial O(mn) Efficient: Polynomial O(mn)

#### **Explanation:**

Although the times complexity of both algorithm are the same, in real world, the efficient version spend more time than the basic ones. Since we optimized the space complexity in the efficient version, we sacrifice a little bit more time (a constant factor) on recursive calls by getting a huge decrease in memory usage.

#### Contribution

<1290146248\_2212208812\_8841152462>: <Equal Contribution>