



Matrices, Lists, Dataframes, S3 and S4 Objects.

Elements of the R language

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Matrices

A **matrix** is a 2-dimensional data structure, like vector, it consists of elements of the same type. A matrix has *rows* and *columns*.

Say, we want to construct this matrix in R:

$$\mathbf{X} = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

```
X <- matrix(1:9, # a sequence of numbers to fill in
            nrow=3, # three rows (alt. ncol=3)
            byrow=T) # populate matrix by row
```

X

```
##      [,1] [,2] [,3]
## [1,]    1    2    3
## [2,]    4    5    6
## [3,]    7    8    9
```

Matrices — indexing

Elements of a matrix are retrieved using the '[]' notation, like we have seen for vectors. Here, we have to specify 2 dimensions -- the row and the column:

```
X[1,2] # Retrieve element from the 1st row, 2nd column  
X[3,] # Retrieve the entire 3rd row  
X[,2] # Retrieve the 2nd column
```

```
## [1] 2  
## [1] 7 8 9  
## [1] 2 5 8
```

Matrices — indexing cted.

```
X[c(1,3),] # Retrieve rows 1 and 3  
X[c(1,3),c(3,1)]
```

```
##      [,1] [,2] [,3]  
## [1,]    1    2    3  
## [2,]    7    8    9  
##      [,1] [,2]  
## [1,]    3    1  
## [2,]    9    7
```

Matrices — dimensions

To check the dimensions of a matrix, use `dim()`:

```
X  
dim(X) # 3 rows and 3 columns
```

```
##      [,1] [,2] [,3]  
## [1,]    1    2    3  
## [2,]    4    5    6  
## [3,]    7    8    9  
## [1] 3 3
```

Nobody knows why `dim()` does not work on vectors... use `length()` instead.

Matrices — operations

Usually the functions that work for a vector also work for matrices. To order a matrix with respect to, say, 2nd column:

```
X <- matrix(sample(1:9,size = 9), nrow = 3)
ord <- order(X[,2])
X[ord,]
```

```
##      [,1] [,2] [,3]
## [1,]    2    7    6
## [2,]    4    8    1
## [3,]    3    9    5
```

Matrices — transposition

To **transpose** a matrix use `t()`:

```
X
t(X)
```

```
##      [,1] [,2] [,3]
## [1,]    2    7    6
## [2,]    3    9    5
## [3,]    4    8    1
##      [,1] [,2] [,3]
## [1,]    2    3    4
## [2,]    7    9    8
## [3,]    6    5    1
```

Nobody knows why `dim()` does not work on vectors... use `length()` instead.

Matrices — operations 2

To get the diagonal, of the matrix:

```
X
diag(X) # get values on the diagonal
```

```
##      [,1] [,2] [,3]
## [1,]    2    7    6
## [2,]    3    9    5
## [3,]    4    8    1
## [1] 2 9 1
```

Matrices — operations, triangles

To get the upper or the lower triangle use **upper.tri()** and **lower.tri()** respectively:

```
X # print X
upper.tri(X) # which elements form the upper triangle
X[upper.tri(X)] <- 0 # set them to 0
X # print the new matrix
```

```
##      [,1] [,2] [,3]
## [1,]    2    7    6
## [2,]    3    9    5
## [3,]    4    8    1
##      [,1] [,2] [,3]
## [1,] FALSE TRUE  TRUE
## [2,] FALSE FALSE TRUE
## [3,] FALSE FALSE FALSE
##      [,1] [,2] [,3]
## [1,]    2    0    0
## [2,]    3    9    0
## [3,]    4    8    1
```

Matrices — multiplication

Different types of matrix multiplication exist:

```
A <- matrix(1:4, nrow = 2, byrow=T)
B <- matrix(5:8, nrow = 2, byrow=T)
A * B # Hadamard product
A %*% B # Matrix multiplication
# A %x% B # Kronecker product
# A %o% B # Outer product (tensor product)
```

```
##      [,1] [,2]
## [1,]    5   12
## [2,]   21   32
##      [,1] [,2]
## [1,]   19   22
## [2,]   43   50
```

Matrices — outer

Outer product can be useful for generating names

```
outer(letters[1:4], LETTERS[1:4], paste, sep="-")
```

```
##      [,1] [,2] [,3] [,4]  
## [1,] "a-A" "a-B" "a-C" "a-D"  
## [2,] "b-A" "b-B" "b-C" "b-D"  
## [3,] "c-A" "c-B" "c-C" "c-D"  
## [4,] "d-A" "d-B" "d-C" "d-D"
```

Expand grid

But `expand.grid()` is more convenient when you want, e.g. generate combinations of variable values:

```
expand.grid(height = seq(120, 121),  
            weight = c('1-50', '51+'),  
            sex = c("Male", "Female"))
```

```
##   height weight  sex  
## 1    120   1-50  Male  
## 2    121   1-50  Male  
## 3    120    51+  Male  
## 4    121    51+  Male  
## 5    120   1-50 Female  
## 6    121   1-50 Female  
## 7    120    51+ Female  
## 8    121    51+ Female
```

Matrices — apply

Function **apply** is a very useful function that applies a given function to either each value of the matrix or in a column/row-wise manner. Say, we want to have mean of values by column:

```
X  
apply(X, MARGIN=2, mean) # MARGIN=1 would do it for rows
```

```
##      [,1] [,2] [,3]  
## [1,]    2    0    0  
## [2,]    3    9    0  
## [3,]    4    8    1  
## [1] 3.0000000 5.6666667 0.3333333
```

Matrices — apply cted.

And now we will use *apply()* to replace each element it a matrix with its deviation from the mean squared:

```
X
my.mean <- mean(X)
apply(X, MARGIN=c(1,2),
      function(x, my.mean) (x - my.mean)^2,
      my.mean)
```

```
##      [,1] [,2] [,3]
## [1,]    2    0    0
## [2,]    3    9    0
## [3,]    4    8    1
##      [,1] [,2] [,3]
## [1,]    1    9    9
## [2,]    0   36    9
## [3,]    1   25    4
```

Matrices — useful fns.

While *apply()* is handy, it is a bit slow and for the most common statistics, there are special functions col/row Sums/Mean:

```
X
colSums(X)
```

```
##      [,1] [,2] [,3]
## [1,]    2    0    0
## [2,]    3    9    0
## [3,]    4    8    1
## [1]  9 17  1
```

These functions are faster!

Matrices — adding rows/columns

One may wish to add a row or a column to an already existing matrix or to make a matrix out of two or more vectors of equal length:

```
x <- c(1,1,1)
y <- c(2,2,2)
cbind(x,y)
rbind(x,y)
```

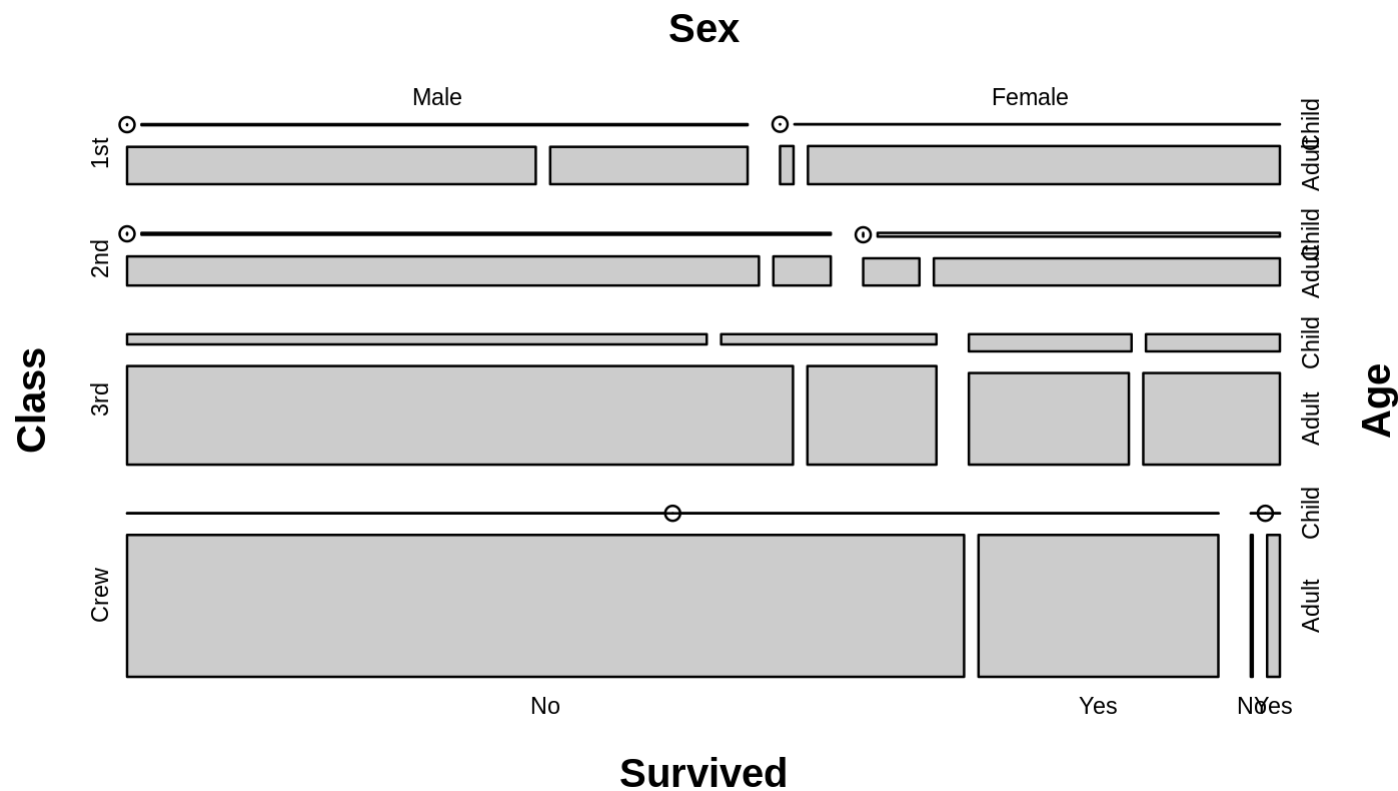
```
##      x y
## [1,] 1 2
## [2,] 1 2
## [3,] 1 2
##    [,1] [,2] [,3]
## x     1     1     1
## y     2     2     2
```

Matrices — more dimensions

```
dim(Titanic)
```

```
## [1] 4 2 2 2
```

```
library(vcd)
mosaic(Titanic, gp_labels=gpar(fontsize=7))
```



Lists — collections of various data types

A list is a collection of elements that can be of various data types:

```
name <- c('R2D2', 'C3PO', 'BB8')
weight <- c(21, 54, 17)
data <- list(name=name, weight)
data
data$name
data[[1]]
```

```
## $name
## [1] "R2D2" "C3PO" "BB8"
##
## [[2]]
## [1] 21 54 17
##
## [1] "R2D2" "C3PO" "BB8"
## [1] "R2D2" "C3PO" "BB8"
```

Lists — collections of various data types

Elements of a list can also be different data structures:

```
weight <- matrix(sample(1:9, size = 9), nrow=3)
data <- list(name, weight)
data
data[[2]][3]
```

```
## [[1]]
## [1] "R2D2" "C3PO" "BB8"
##
## [[2]]
##      [,1] [,2] [,3]
## [1,]    9    8    4
## [2,]    6    7    5
## [3,]    1    3    2
##
## [1] 1
```

Data frames

A **data frame** or a **data table** is a data structure very handy to use. In this structure elements of every column have the same type, but different columns can have different types. Technically, a data frame is a list of vectors...

```
df <- data.frame(c(1:5),  
                LETTERS[1:5],  
                sample(c(TRUE, FALSE), size = 5,  
                      replace=T))
```

df

```
##      c.1.5. LETTERS.1.5. sample.c.TRUE..FALSE...size...5..replace...T.  
## 1      1      A                                TRUE  
## 2      2      B                                TRUE  
## 3      3      C                                FALSE  
## 4      4      D                                TRUE  
## 5      5      E                                FALSE
```

Data frames — cted.

As you have seen, columns of a data frame are named after the call that created them. Not always the best option...

```
df <- data.frame(no=c(1:5),  
                 letter=c('a','b','c','d','e'),  
                 isBrown=sample(c(TRUE, FALSE),  
                                size = 5,  
                                replace=T))
```

df

```
##   no letter isBrown  
## 1  1      a  FALSE  
## 2  2      b   TRUE  
## 3  3      c   TRUE  
## 4  4      d   TRUE  
## 5  5      e   TRUE
```

Data frames — accessing values

As you have seen, columns of a data frame are named after the call that created them. Not always the best option...

```
df[1,] # get the first row
df[,2] # the first column
df[2:3, 'isBrown'] # get rows 2-3 from the isBrown column
df$letter[1:2] # get the first 2 letters
```

```
## no letter isBrown
## 1 1      a FALSE
## [1] "a" "b" "c" "d" "e"
## [1] TRUE TRUE
## [1] "a" "b"
```

Data frames — factors

An interesting observation:

```
df$letter  
df$letter <- as.character(df$letter)  
df$letter
```

```
## [1] "a" "b" "c" "d" "e"  
## [1] "a" "b" "c" "d" "e"
```


Data frames — factors cted.

To treat characters as characters at data frame creation time, one can use the **stringsAsFactors** option set to TRUE:

```
df <- data.frame(no=c(1:5),  
                 letter=c("a","b","c","d","e"),  
                 isBrown=sample(c(TRUE, FALSE),  
                                size = 5,  
                                replace=T),  
                 stringsAsFactors = TRUE)  
df$letter
```

```
## [1] a b c d e  
## Levels: a b c d e
```

Well, as you see, it did not work as expected...

Data frames — names

To get or change row/column names:

```
colnames(df) # get column names
rownames(df) # get row names
rownames(df) <- letters[1:5]
rownames(df)
df['b', ]
```

```
## [1] "no"      "letter"  "isBrown"
## [1] "1" "2" "3" "4" "5"
## [1] "a" "b" "c" "d" "e"
##   no letter isBrown
## b  2      b    TRUE
```

Data frames — merging

A very useful feature of R is merging two data frames on certain key using **merge**:

```
df1 <- data.frame(no=c(1:5),  
                  letter=c("a","b","c","d","e"))  
df2 <- data.frame(no=c(1:5),  
                  letter=c("A","B","C","D","E"))  
merge(df1, df2, by='no')
```

```
##   no letter.x letter.y  
## 1  1      a      A  
## 2  2      b      B  
## 3  3      c      C  
## 4  4      d      D  
## 5  5      e      E
```

Objects — type vs. class

An object of class **factor** is internally represented by numbers:

```
size <- factor('small')  
class(size) # Class 'factor'  
mode(size) # Is represented by 'numeric'  
typeof(size) # Of integer type
```

```
## [1] "factor"  
## [1] "numeric"  
## [1] "integer"
```

Objects — structure

Many functions return **objects**. We can easily examine their **structure**:

```
his <- hist(1:5, plot=F)
str(his)
object.size(his) # How much memory the object consumes
```

```
## List of 6
## $ breaks   : int [1:5] 1 2 3 4 5
## $ counts   : int [1:4] 2 1 1 1
## $ density  : num [1:4] 0.4 0.2 0.2 0.2
## $ mids     : num [1:4] 1.5 2.5 3.5 4.5
## $ xname    : chr "1:5"
## $ equidist: logi TRUE
## - attr(*, "class")= chr "histogram"
## 1240 bytes
```

Objects — fix

We can easily modify values of object's **attributes**:

```
attributes(his)
attr(his, "names")
#fix(his) # Opens an object editor
```

```
## $names
## [1] "breaks"    "counts"    "density"   "mids"      "xname"     "equidist"
##
## $class
## [1] "histogram"
##
## [1] "breaks"    "counts"    "density"   "mids"      "xname"     "equidist"
```

Lists as S3 classes

A list that has been named, becomes an S3 class:

```
my.list <- list(numbers = c(1:5),  
               letters = letters[1:5])  
class(my.list)  
class(my.list) <- 'my.list.class'  
class(my.list) # Now the list is of S3 class
```

```
## [1] "list"  
## [1] "my.list.class"
```

However, that was it. We cannot enforce that *numbers* will contain numeric values and that *letters* will contain only characters. S3 is a very primitive class.

S3 classes

For an S3 class we can define a *generic function* applicable to all objects of this class.

```
print.my.list.class <- function(x) {  
  cat('Numbers:', x$numbers, '\n')  
  cat('Letters:', x$letters)  
}  
print(my.list)
```

```
## Numbers: 1 2 3 4 5  
## Letters: a b c d e
```

But here, we have no error-proofing. If the object will lack *numbers*, the function will still be called:

```
class(his) <- 'my.list.class' # alter class  
print(his) # Gibberish but no error...
```

```
## Numbers:  
## Letters:
```


S3 classes — still useful?

Well, S3 class mechanism is still in use, esp. when writing **generic** functions, most common examples being *print* and *plot*. For example, if you plot an object of a `Manhattan.plot` class, you write *plot(gwas.result)* but the true call is: *plot.manhattan(gwas.result)*. This makes life easier as it requires less writing, but it is up to the function developers to make sure everything works!

S4 class mechanism

S4 classes are more advanced as you actually define the structure of the data within the object of your particular class:

```
setClass('gene',  
        representation(name='character',  
                        coords='numeric')  
        )  
my.gene <- new('gene', name='ANK3',  
              coords=c(1.4e6, 1.412e6))
```

S4 class — slots

The variables within an S4 class are stored in the so-called **slots**. In the above example, we have 2 such slots: *name* and *coords*. Here is how to access them:

```
my.gene@name # access using @ operator  
my.gene@coords[2] # access the 2nd element in slot coords
```

```
## [1] "ANK3"  
## [1] 1412000
```

See you at the next lecture!

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Created: 16-Sep-2021 • Roy Francis • SciLifeLab • NBIS

