

⑦ $x := 1;$ A $C_1; C_2$
 if $\underbrace{\neg(y=x)}_b$ then $\{y := x + x; z := y\}$ else $\underbrace{z := x * x}_{D_1}$ } Prog

interpretação
semântica
denotacional

$$\begin{aligned}
 &\rightarrow S_{ds}[\text{Prog}] \\
 &= S_{ds}[A; \text{if } b \text{ then } C_1; C_2 \text{ else } D_1] \sim \\
 &= S_{ds}[\text{if } b \text{ then } C_1; C_2 \text{ else } D_1] \circ S_{ds}[A] \sim \\
 &= \text{cond}(B[b], S_{ds}[C_1; C_2], S_{ds}[D_1]) \circ S_{ds}[A] \sim \\
 &= \text{cond}(B[b], S_{ds}[C_1; C_2], S_{ds}[D_1], \underbrace{s[x \mapsto 1]}_{s_1}) \\
 &= \begin{cases} S_{ds}[C_1; C_2] \sim_1 & \text{se } B[b]_{s_1} = \text{tt} \\ S_{ds}[D_1] \sim_1 & \text{se } B[b]_{s_1} = \text{ff} \end{cases} \\
 &= \begin{cases} \overbrace{s_1[y \mapsto A[x+x]_{s_1}][z \mapsto A[y]_{s_2}]}^{s_2} \sim & B[b]_{s_1} = \text{tt} \\ s_1[z \mapsto A[x*x]_{s_1}] \sim & B[b]_{s_1} = \text{ff} \end{cases} \\
 &= \begin{cases} s[x \mapsto 1][y \mapsto 2][z \mapsto 2] \sim & \neg(s_1, x = s_1, y) \Rightarrow \text{sg} \\ s[x \mapsto 1][z \mapsto 1] \sim & s_1, x = s_1, y \end{cases} \\
 &= \begin{cases} s[x \mapsto 1][y \mapsto 2][z \mapsto 2] \sim & s, y \neq 1 \\ s[x \mapsto 1][z \mapsto 1] \sim & s, y = 1 \end{cases}
 \end{aligned}$$