

Visualizing association among two or more quantitative variables -

When we want to show more than two variables at once, we may use a bubble chart, a scatter plot or a correlogram. For example, measurements of different animal's, such height, weight, length, and daily energy demands. In this paper we also perform dimensionality reduction, in the form of principal component analysis.

Scatter plot-

Let's start with example, I'm taking a dataset of measurements performed on 123 blue jay birds.

The dataset contains information such as head length, the skull size, and the body mass of each bird. We expect that there are relationship between these variables. For example, birds with longer bills would be expected have larger skull size, and birds with higher body mass should have larger bits and skulls than birds with lower body mass.

Plotting the above relation -

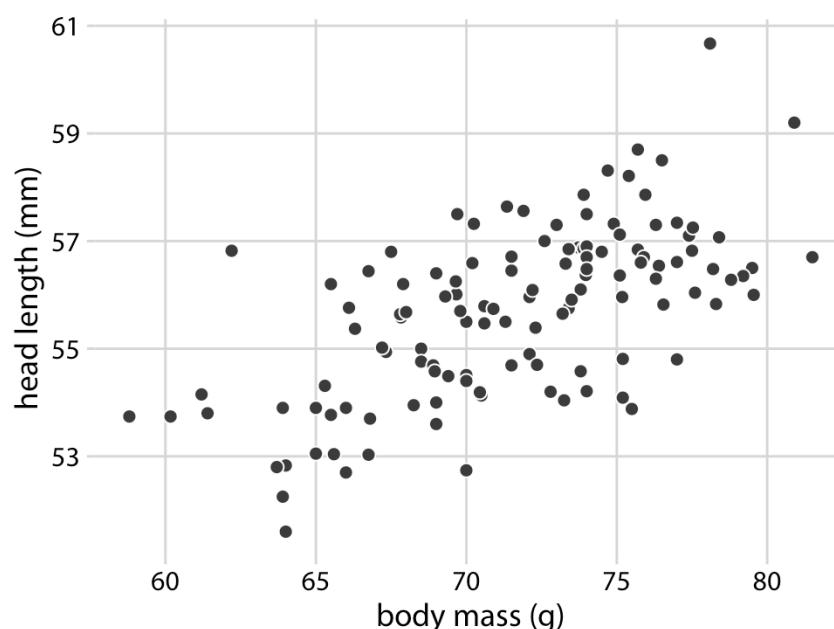
Relation - head length against body mass.

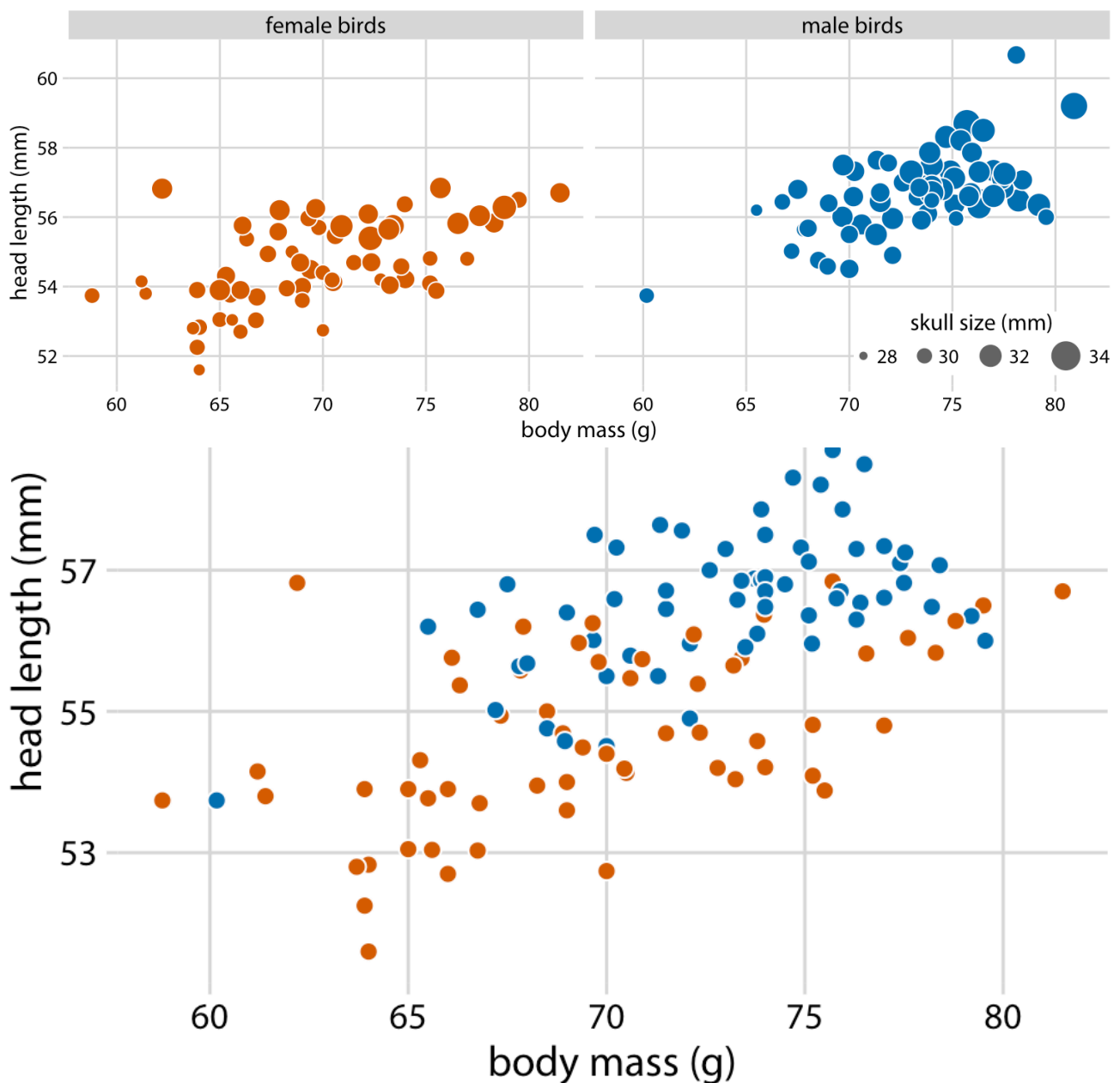
X-axis: head length

Y-axis: body mass

Dot: each bird is shown by one dot

There is a trend for birds, the birds with longest head falls close to the maximum body mass observed, and the bird with shortest head falls close to the minimum mass observed.





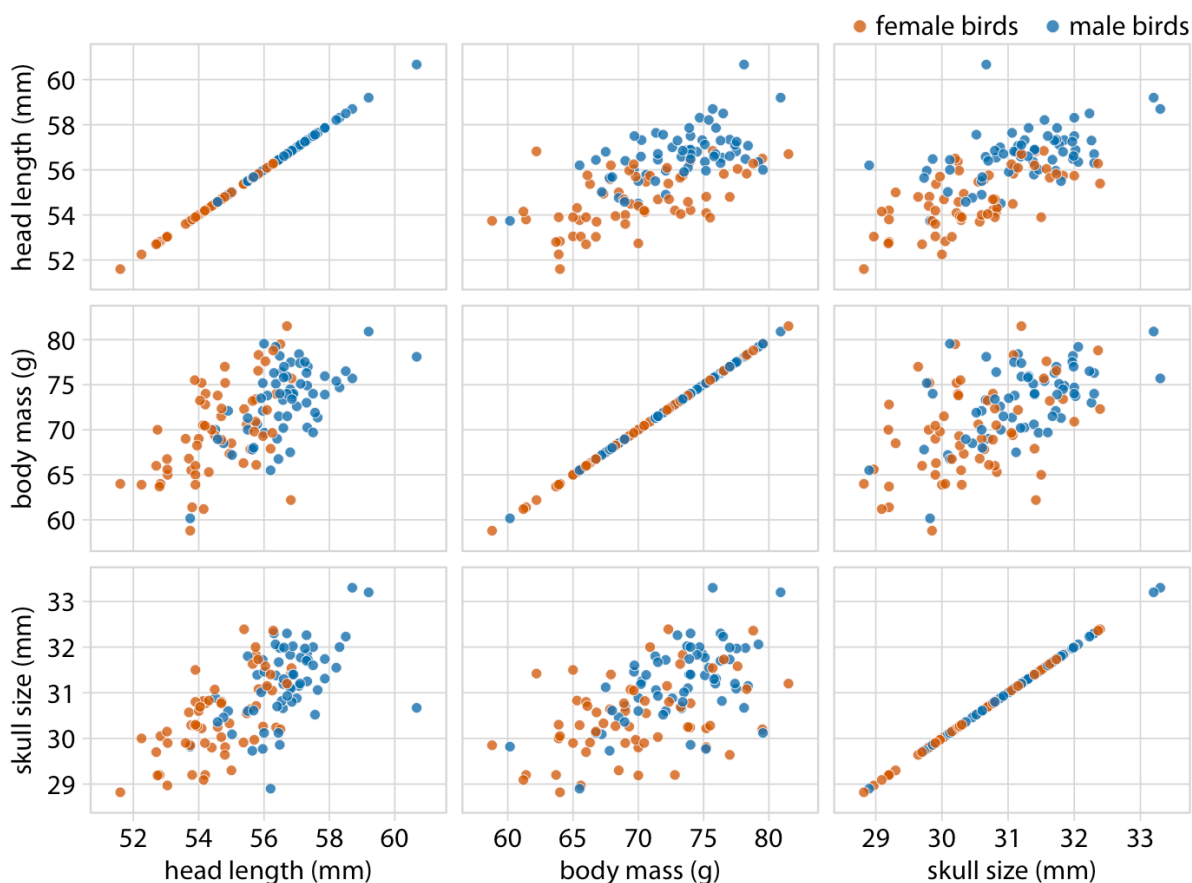
The dataset contains both male and female birds we can show the same relation separately for each sex by using colour of dots. Now, we can see the new trend over a trend that females tends to have shorter heads than males. At the same time, females tend to be lighter than males on average.

Bubble chart -

Bubble charts have disadvantage that they show the same types of variables, quantitative variable with two different types of scales, position and size. This makes it difficult to visually ascertain the strength of association between variables.

Because the head length is defined as the distance from the tip of the bill to the back of the head, a larger head length could imply a longer bill, as larger skull, or both. For showing more than two variables (body mass, head length, and skull size) we can use size of dots (referred as bubbles) for skull size variable that shows size of skull size based on size of bubble (dot) as we already using x-axis for body mass and y-axis for head length.

As an alternative to bubble chart it may be preferable to show an **all-against-all matrix of scatter plot** where each individual plot shows two data dimension. This figure shows clearly that the relationship between skull size



and body mass is comparable for female and male except that the female birds tend to be smaller.

Correlogram -

Visualisation of correlation coefficient is called correlograms. When we have more than three to four quantitative variables we use correlograms. It is more useful to quantify the amount of association between pairs of variables and visualize the quantity rather than data. Calculate the correlation coefficient r ($-1 < r < 1$) that measure relation between two variables.

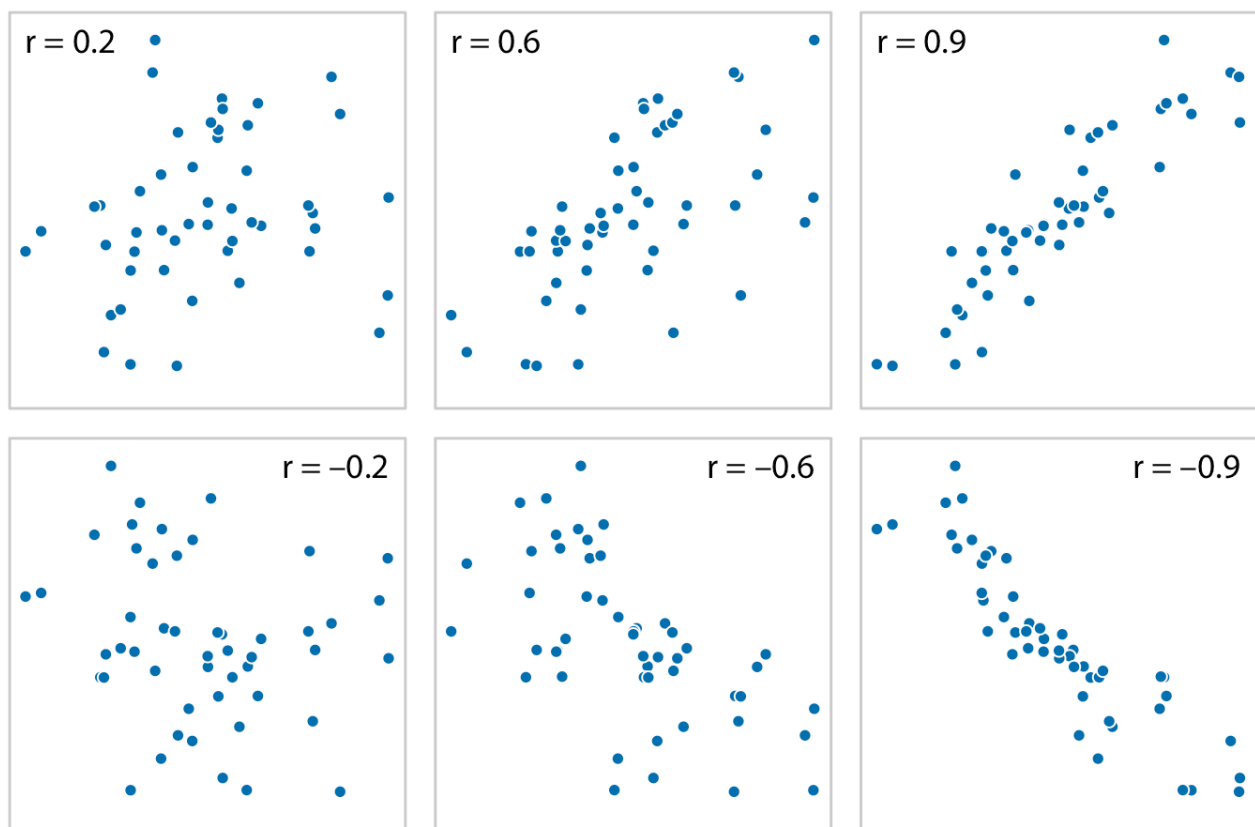
Value, $r = 0$ means there is no relation.

$r = -1, 1$ indicate a perfect relation

the sign of r shows whether the variable are correlated or anti-correlated .

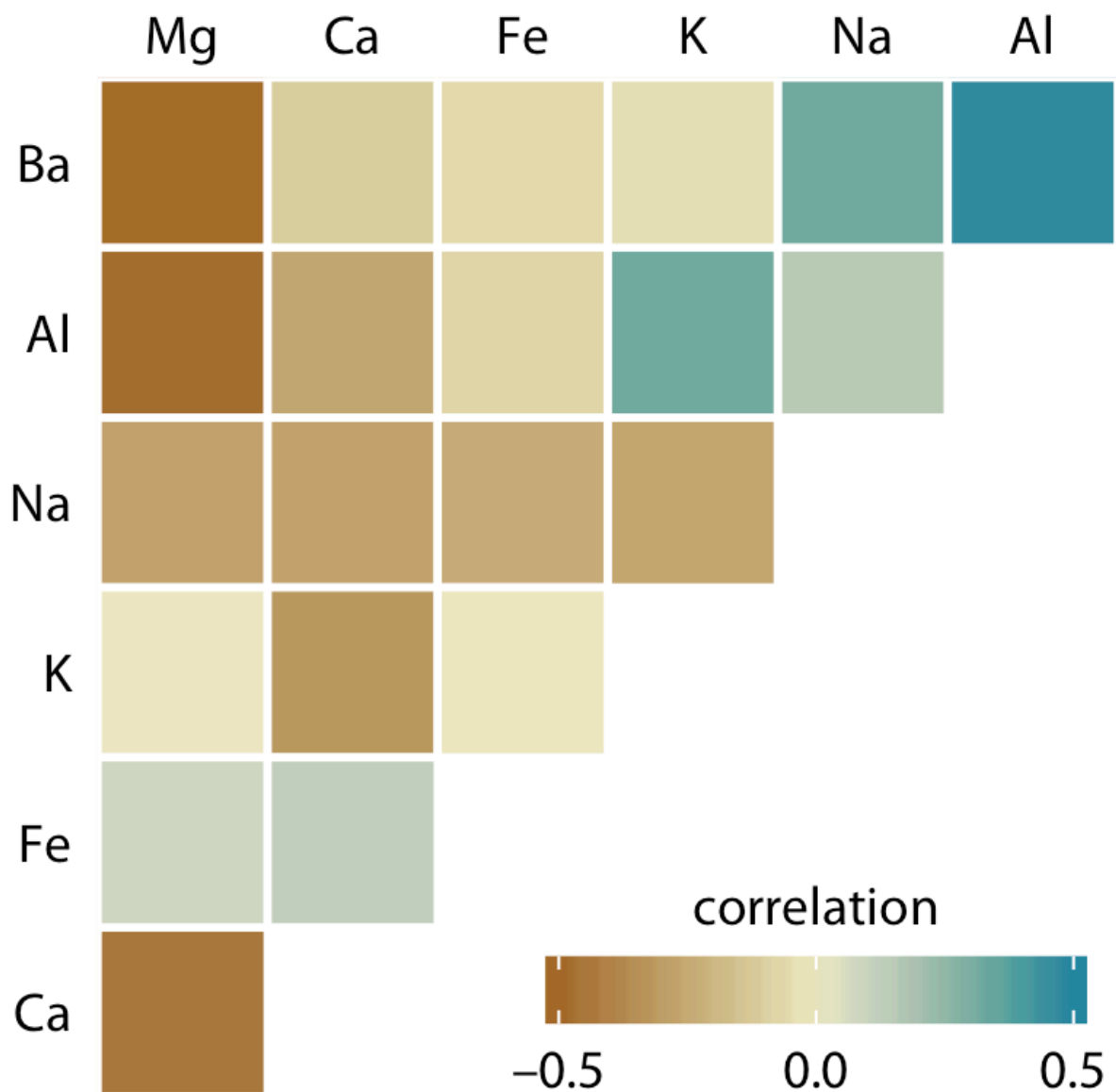
Correlated - larger value in one variable coincide with larger values in other variable.

Anti-correlated - larger values in one variable coincide with smaller values in other variable.

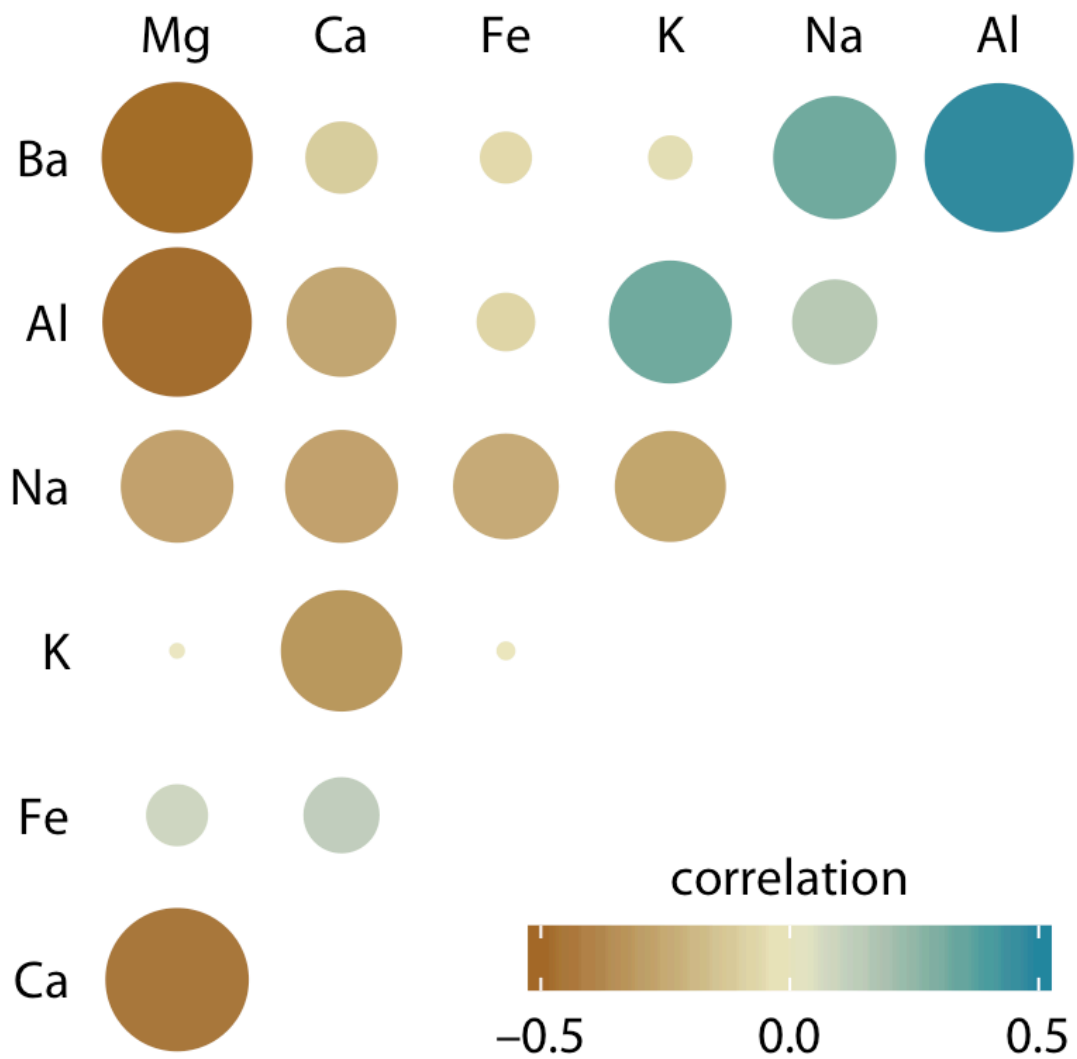


We will consider a dataset of over 200 glass fragments. For each glass fragments, we have measurements about its composition, expressed as the percentage in weight of various mineral oxide. There are seven different oxides for which we have measurements, yielding a total of $6 + 5 + 4 + 3 + 2 + 1 = 21$ pairwise correlations. We can display these 21 correlation at once

as matrix of coloured tiles, where each tile represents one correlation coefficient. By correlograms we see that magnesium is negatively correlated with nearly all. Other oxides, and that aluminium and barium have strong positive correlation.



One weakness of the correlation is that low correlation. I.e. correlation with absolute value near zero, are not as visually suppressed as they should be. For example magnesium(Mg) and potassium(k) have correlation coefficient nearly zero. To overcome this limitation, we can display correlation as a coloured circle and scale the circle size based on their correlation coefficient value. Value near absolute zero have smaller circle.



Remember -

scatter plot - show relation **between 2 variables**.

Bubble chart - show relation **between 3 variables**.

Correlogram - show relation **between more than 3 or 4 variables**.

