# **Connecting Islands**



The newly formed city X is depicted using an M x M grid of cells. The **bottom-left** corner cell of the grid is (0,0) while the **top-right** corner cell of the grid is (M-1, M-1). Each cell is either land or ocean, but not both. If you are in a land cell you can walk to any one of 4 of neighboring (left, right, up or down) land cells from there. You can not walk into an ocean cell. Also, you can't walk outside of the grid.

There are **N** islands in the city right now. And the islands are **rectangular shaped**. Therefore the island can be defined by its bottom-left cell position and upper-right cell position. In a given island, if bottom-left corner cell is **(x1,y1)** and upper-right corner cell is **(x2,y2)** then the total number of cells in that island is **(x2-x1+1)** \* **(y2-y1+1)**. Also, any given land cell in the grid is a part of exactly one island.

The cost of converting an ocean cell to a land cell is 1. Write a program to find the minimum cost required to connect all lands so that you can walk from any land cell to any other land cell in the city.

### **Input Format**

The first line of the input has  $\mathbf{2}$  integers  $\mathbf{M}$  and  $\mathbf{N}$ , the size of the grid  $\mathbf{8}$  the number of islands in the city respectively. Each of the next  $\mathbf{N}$  lines contains  $\mathbf{4}$  integers  $\mathbf{x1_i}$ ,  $\mathbf{y1_i}$ ,  $\mathbf{x2_i}$ ,  $\mathbf{y2_i}$  separated by spaces, representing the  $\mathbf{i^{th}}$  island in the city.

#### **Constraints**

- $0 \le x1_i \le x2_i < M$
- $0 \le y1_i \le y2_i < M$

Subtask 1: 20 points

• 1 < M, N < 20

Subtask 2: 30 points

• 21 < M, N < 100

Subtask 3: 40 points

- $101 < M < 10^5$
- $101 < N < 10^3$

Subtask 4: 10 points

- $101 \le M \le 10^5$
- $101 < N < 10^4$

#### Limits

- Time Limit: 3s
- Memory Limit: 256MB

#### **Output Format**

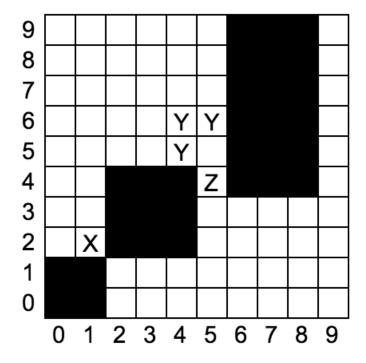
Output just **one** integer representing your answer, the **minimum cost** required to connect all land cells.

## Sample Input 0

```
10 3
0 0 1 1
2 2 4 4
6 4 8 9
```

## Sample Output 0

## Explanation 0



Converting cell  ${\bf X}$  and  ${\bf Z}$  as land cells result in connecting all land cells.

Alternatively, we could have converted cells marked in  $\mathbf{Y}$  instead of  $\mathbf{Z}$ . But that will result in a total cost of 4 which is not optimum.