

Can you divide that

The problem is based on the properties of divisibility being applied on some basic relationships between factorials.

The factorial of a number x_i is divisible by the factorial of y if x_i is greater than or equal to y because $(y!) = (k * x_i!)$.

The properties of divisibility state that if some integers x, y, z are all divisible by some number k , then $(x + y + z)$ is also divisible by k .

So using the above 2 properties, it's safe to conclude that all numbers of above the given number y can be ignored while finding your answer.

Then it seems obvious that factorials of numbers smaller than y can never be divided by the factorial of y .

However there is of the property of factorials that states $((n+1)*n!) = (n+1)!$. This means that even if the number is smaller, with enough repetitions of them in A , the smaller numbers can also become equivalent to a number greater than or equal to y in the context of this problem.

So to solve the problem, you can count the occurrences of each number, and iterating from the smallest possible number, you can divide the count by number+1 and add the quotient to the count of number+1 ($cnt_{n+1} += \text{floor}(cnt_n / (n+1))$). If the count of a number smaller than y leaves a remainder when it's divided by number+1, the sum of the factorials cannot be divisible by y .