

Modeling

September 28, 2020

```
[1]: import pandas as pd
import numpy as np
%matplotlib notebook
import matplotlib.pyplot as plt
from datetime import datetime
import statsmodels.api as sm
from statsmodels.tsa.arima_model import ARIMA
```

```
[3]: # HIT (BA)
hit_HT = pd.read_csv('./hit/hit_HT.csv')
hit_HH = pd.read_csv('./hit/hit_HH.csv')
hit_KT = pd.read_csv('./hit/hit_KT.csv')
hit_LG = pd.read_csv('./hit/hit_LG.csv')
hit_LT = pd.read_csv('./hit/hit_LT.csv')
hit_NC = pd.read_csv('./hit/hit_NC.csv')
hit_OB = pd.read_csv('./hit/hit_OB.csv')
hit_SK = pd.read_csv('./hit/hit_SK.csv')
hit_SS = pd.read_csv('./hit/hit_SS.csv')
hit_WO = pd.read_csv('./hit/hit_WO.csv')

ba_HT = hit_HT.iloc[:, [1, 2]]
ba_HH = hit_HH.iloc[:, [1, 2]]
ba_KT = hit_KT.iloc[:, [1, 2]]
ba_LG = hit_LG.iloc[:, [1, 2]]
ba_LT = hit_LT.iloc[:, [1, 2]]
ba_NC = hit_NC.iloc[:, [1, 2]]
ba_OB = hit_OB.iloc[:, [1, 2]]
ba_SK = hit_SK.iloc[:, [1, 2]]
ba_SS = hit_SS.iloc[:, [1, 2]]
ba_WO = hit_WO.iloc[:, [1, 2]]
```

```
[4]: # PIT (ER)
pit_HT = pd.read_csv('./pit/pit_HT.csv')
pit_HH = pd.read_csv('./pit/pit_HH.csv')
pit_KT = pd.read_csv('./pit/pit_KT.csv')
pit_LG = pd.read_csv('./pit/pit_LG.csv')
pit_LT = pd.read_csv('./pit/pit_LT.csv')
```

```

pit_NC = pd.read_csv('./pit/pit_NC.csv')
pit_OB = pd.read_csv('./pit/pit_OB.csv')
pit_SK = pd.read_csv('./pit/pit_SK.csv')
pit_SS = pd.read_csv('./pit/pit_SS.csv')
pit_WO = pd.read_csv('./pit/pit_WO.csv')
er_HT = pit_HT.iloc[:,[1,2]]
er_HH = pit_HH.iloc[:,[1,2]]
er_KT = pit_KT.iloc[:,[1,2]]
er_LG = pit_LG.iloc[:,[1,2]]
er_LT = pit_LT.iloc[:,[1,2]]
er_NC = pit_NC.iloc[:,[1,2]]
er_OB = pit_OB.iloc[:,[1,2]]
er_SK = pit_SK.iloc[:,[1,2]]
er_SS = pit_SS.iloc[:,[1,2]]
er_WO = pit_WO.iloc[:,[1,2]]

```

```

[5]: # PIT (WLS)
wls_HT = pit_HT.iloc[:,[1,3]]
wls_HH = pit_HH.iloc[:,[1,3]]
wls_KT = pit_KT.iloc[:,[1,3]]
wls_LG = pit_LG.iloc[:,[1,3]]
wls_LT = pit_LT.iloc[:,[1,3]]
wls_NC = pit_NC.iloc[:,[1,3]]
wls_OB = pit_OB.iloc[:,[1,3]]
wls_SK = pit_SK.iloc[:,[1,3]]
wls_SS = pit_SS.iloc[:,[1,3]]
wls_WO = pit_WO.iloc[:,[1,3]]

```

```

[6]: #
def modeling(data,order,steps,trend='c'): # , arima , ,
    data = data.iloc[:,1] #
    model = ARIMA(data,order=order)
    model_fit = model.fit(trend=trend,full_output=True,disp=True)
    print("{}\n".format(model_fit.summary()))
    fore = model_fit.forecast(steps=steps)
    f = pd.DataFrame(fore[0])
    f.index = pd.RangeIndex(start=len(data),stop=len(data)+steps,step=1)
    model_fit.plot_predict()
    plt.plot(f)
    print(" ",f)

```

1

HH 10 HT 12 KT 9 LG 7 LT 9 NC 7 OB 12 SK 9 SS 11 WO 9

2 BA(hit)

HH 2,0,2 HT 1,0,2 KT 2,1,0 LG 2,0,0 LT 2,0,4 NC 1,0,0 OB 1,0,4 SK 2,1,0 SS 0,2,1 WO 4,0,3

```
[7]: # BA
modeling(ba_HH, (2,0,2),10)
```

ARMA Model Results						
=====						
Dep. Variable:	BA		No. Observations:		112	
Model:	ARMA(2, 2)		Log Likelihood		384.622	
Method:	css-mle		S.D. of innovations		0.008	
Date:	Sun, 27 Sep 2020		AIC		-757.245	
Time:	00:52:20		BIC		-740.934	
Sample:	0		HQIC		-750.627	
=====						
	coef	std err	z	P> z	[0.025	0.975]

const	0.2348	0.008	30.579	0.000	0.220	0.250
ar.L1.BA	0.3913	0.240	1.631	0.103	-0.079	0.862
ar.L2.BA	0.4922	0.229	2.147	0.032	0.043	0.942
ma.L1.BA	0.0673	0.234	0.288	0.774	-0.391	0.526
ma.L2.BA	0.2853	0.117	2.447	0.014	0.057	0.514
Roots						
=====						
	Real	Imaginary	Modulus		Frequency	

AR.1	1.0823	+0.0000j	1.0823		0.0000	
AR.2	-1.8773	+0.0000j	1.8773		0.5000	
MA.1	-0.1179	-1.8686j	1.8723		-0.2600	
MA.2	-0.1179	+1.8686j	1.8723		0.2600	

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```
0
112 0.230051
113 0.237423
114 0.233488
115 0.235576
116 0.234457
117 0.235047
118 0.234727
119 0.234892
```

```
120 0.234799
121 0.234843
```

```
[26]: # BA
modeling(ba_HT,(1,0,2),12,'c')
```

ARMA Model Results

```
=====
Dep. Variable:          BA    No. Observations:          109
Model:                  ARMA(1, 2)    Log Likelihood          347.943
Method:                  css-mle    S.D. of innovations          0.010
Date:                   Sat, 26 Sep 2020    AIC          -685.887
Time:                   01:02:26    BIC          -672.430
Sample:                 0    HQIC          -680.430
=====
```

```
=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          0.2620      0.009     29.878      0.000      0.245      0.279
ar.L1.BA        0.9280      0.056     16.543      0.000      0.818      1.038
ma.L1.BA        0.1414      0.112      1.265      0.206     -0.078      0.361
ma.L2.BA       -0.4062      0.117     -3.467      0.001     -0.636     -0.177
=====
```

Roots

```
=====
              Real      Imaginary      Modulus      Frequency
-----
AR.1          1.0776      +0.0000j      1.0776      0.0000
MA.1          -1.4045      +0.0000j      1.4045      0.5000
MA.2          1.7527      +0.0000j      1.7527      0.0000
=====
```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```
0
109 0.286989
110 0.285649
111 0.283947
112 0.282368
113 0.280903
114 0.279544
115 0.278282
116 0.277111
117 0.276025
118 0.275017
```

```
119 0.274081
120 0.273213
```

```
[27]: #KT BA
modeling(ba_KT,(2,1,0),9,'nc')
```

```

                        ARIMA Model Results
=====
Dep. Variable:          D.BA    No. Observations:          110
Model:                  ARIMA(2, 1, 0)    Log Likelihood          355.761
Method:                  css-mle    S.D. of innovations          0.010
Date:                    Sat, 26 Sep 2020    AIC          -705.523
Time:                    01:02:32    BIC          -697.421
Sample:                  1    HQIC          -702.237

=====
                        coef    std err          z      P>|z|      [0.025    0.975]
-----
ar.L1.D.BA      0.2161      0.098      2.216      0.027      0.025      0.407
ar.L2.D.BA      0.1811      0.097      1.861      0.063     -0.010      0.372

                        Roots
=====
                        Real      Imaginary      Modulus      Frequency
-----
AR.1           1.8279      +0.0000j      1.8279      0.0000
AR.2          -3.0212      +0.0000j      3.0212      0.5000
=====

```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
111 0.287613
112 0.288108
113 0.288326
114 0.288463
115 0.288532
116 0.288571
117 0.288592
118 0.288604
119 0.288610

```

```
[28]: #LG BA
modeling(ba_LG,(2,0,0),7)
```

ARMA Model Results

```

=====
Dep. Variable:          BA    No. Observations:          113
Model:                  ARMA(2, 0)    Log Likelihood          367.203
Method:                  css-mle    S.D. of innovations          0.009
Date:                    Sat, 26 Sep 2020    AIC          -726.407
Time:                    01:02:41    BIC          -715.497
Sample:                  0    HQIC          -721.980
=====

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          0.2787      0.005     61.489      0.000      0.270      0.288
ar.L1.BA        1.1319      0.128      8.839      0.000      0.881      1.383
ar.L2.BA       -0.3237      0.128     -2.521      0.012     -0.575     -0.072
=====

```

Roots

```

=====
              Real          Imaginary          Modulus          Frequency
-----
AR.1          1.7484          -0.1799j          1.7576          -0.0163
AR.2          1.7484          +0.1799j          1.7576           0.0163
=====

```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
113 0.272637
114 0.274004
115 0.275347
116 0.276423
117 0.277207
118 0.277746
119 0.278103

```

```
[42]: # BA
      modeling(ba_LT,(2,0,4),9)
```

ARMA Model Results

```

=====
Dep. Variable:          BA    No. Observations:          110
Model:                  ARMA(2, 4)    Log Likelihood          377.968
Method:                  css-mle    S.D. of innovations          0.008
Date:                    Sat, 26 Sep 2020    AIC          -739.936
Time:                    01:06:10    BIC          -718.333
=====

```

Sample: 0 HQIC -731.174

	coef	std err	z	P> z	[0.025	0.975]
const	0.2668	0.006	45.199	0.000	0.255	0.278
ar.L1.BA	1.7050	0.139	12.262	0.000	1.433	1.978
ar.L2.BA	-0.8043	0.138	-5.815	0.000	-1.075	-0.533
ma.L1.BA	-0.5370	0.147	-3.647	0.000	-0.826	-0.248
ma.L2.BA	-0.1005	0.116	-0.866	0.387	-0.328	0.127
ma.L3.BA	-0.0451	0.102	-0.443	0.658	-0.245	0.154
ma.L4.BA	0.4827	0.091	5.301	0.000	0.304	0.661

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	1.0600	-0.3461j	1.1151	-0.0502
AR.2	1.0600	+0.3461j	1.1151	0.0502
MA.1	0.9096	-0.6024j	1.0910	-0.0931
MA.2	0.9096	+0.6024j	1.0910	0.0931
MA.3	-0.8628	-0.9981j	1.3193	-0.3634
MA.4	-0.8628	+0.9981j	1.3193	0.3634

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
110 0.264672
111 0.263119
112 0.260621
113 0.263019
114 0.265325
115 0.267327
116 0.268886
117 0.269935
118 0.270468

```

```
[57]: #NC BA
modeling(ba_NC,(1,0,0),7)
```

ARMA Model Results

Dep. Variable:	BA	No. Observations:	110
Model:	ARMA(1, 0)	Log Likelihood	387.947

```

Method:          css-mle   S.D. of innovations      0.007
Date:           Sat, 26 Sep 2020   AIC                -769.895
Time:           01:23:43   BIC                  -761.793
Sample:         0   HQIC                  -766.609

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          0.2722      0.018     15.150      0.000      0.237      0.307
ar.L1.BA       0.9666      0.030     32.672      0.000      0.909      1.025

```

Roots

```

=====
              Real          Imaginary          Modulus          Frequency
-----
AR.1          1.0345          +0.0000j          1.0345          0.0000

```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
110  0.283605
111  0.283224
112  0.282855
113  0.282498
114  0.282154
115  0.281821
116  0.281499

```

```

[56]: #OB BA
      modeling(ba_OB,(1,0,4),12)

```

ARMA Model Results

```

=====
Dep. Variable:          BA   No. Observations:          112
Model:                ARMA(1, 4)   Log Likelihood          360.897
Method:              css-mle   S.D. of innovations          0.010
Date:           Sat, 26 Sep 2020   AIC                -707.794
Time:           01:23:34   BIC                -688.764
Sample:         0   HQIC                -700.073

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          0.2846      0.007     42.242      0.000      0.271      0.298

```


ar.L1.BA	0.6462	0.134	4.827	0.000	0.384	0.909
ma.L1.BA	0.4539	0.123	3.687	0.000	0.213	0.695
ma.L2.BA	0.2091	0.104	2.008	0.045	0.005	0.413
ma.L3.BA	0.5663	0.105	5.418	0.000	0.361	0.771
ma.L4.BA	0.4175	0.110	3.812	0.000	0.203	0.632

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	1.5474	+0.0000j	1.5474	0.0000
MA.1	0.5428	-0.9918j	1.1306	-0.1703
MA.2	0.5428	+0.9918j	1.1306	0.1703
MA.3	-1.2211	-0.6188j	1.3689	-0.4253
MA.4	-1.2211	+0.6188j	1.3689	0.4253

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

0

```
112 0.259467
113 0.263392
114 0.268439
115 0.273813
116 0.277620
117 0.280081
118 0.281671
119 0.282698
120 0.283362
121 0.283791
122 0.284069
123 0.284248
```

```
[60]: #SK BA
modeling(ba_SK, (2, 1, 0), 9, 'nc')
```

ARIMA Model Results

Dep. Variable:	D.BA	No. Observations:	113
Model:	ARIMA(2, 1, 0)	Log Likelihood	346.393
Method:	css-mle	S.D. of innovations	0.011
Date:	Sat, 26 Sep 2020	AIC	-686.786
Time:	01:39:35	BIC	-678.604
Sample:	1	HQIC	-683.466

	coef	std err	z	P> z	[0.025	0.975]
ar.L1.D.BA	0.8073	0.107	7.513	0.000	0.597	1.018
ar.L2.D.BA	-0.2627	0.142	-1.850	0.064	-0.541	0.016
Roots						
	Real	Imaginary	Modulus	Frequency		
AR.1	1.5367	-1.2023j	1.9512	-0.1057		
AR.2	1.5367	+1.2023j	1.9512	0.1057		

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
114 0.219258
115 0.218620
116 0.218825
117 0.219158
118 0.219373
119 0.219460
120 0.219473
121 0.219460
122 0.219447

```

```
[19]: #SS BA
modeling(ba_SS,(0,2,1),11,'nC')
```

ARIMA Model Results						
Dep. Variable:	D.BA	No. Observations:	111			
Model:	ARIMA(1, 1, 1)	Log Likelihood	387.744			
Method:	css-mle	S.D. of innovations	0.007			
Date:	Sat, 26 Sep 2020	AIC	-767.487			
Time:	16:44:52	BIC	-756.649			
Sample:	1	HQIC	-763.091			
	coef	std err	z	P> z	[0.025	0.975]
const	0.0036	0.003	1.125	0.260	-0.003	0.010
ar.L1.D.BA	0.9661	0.040	24.015	0.000	0.887	1.045
ma.L1.D.BA	-0.8399	0.071	-11.882	0.000	-0.978	-0.701

Roots				
	Real	Imaginary	Modulus	Frequency
AR.1	1.0350	+0.0000j	1.0350	0.0000
MA.1	1.1906	+0.0000j	1.1906	0.0000

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
112 0.292387
113 0.295782
114 0.299184
115 0.302594
116 0.306011
117 0.309434
118 0.312865
119 0.316302
120 0.319745
121 0.323194
122 0.326649

```

```
[69]: #WO BA
modeling(ba_WO,(4,0,3),9)
```

ARMA Model Results						
Dep. Variable:	BA	No. Observations:	117			
Model:	ARMA(4, 3)	Log Likelihood	411.833			
Method:	css-mle	S.D. of innovations	0.007			
Date:	Sat, 26 Sep 2020	AIC	-805.667			
Time:	01:43:23	BIC	-780.807			
Sample:	0	HQIC	-795.574			
	coef	std err	z	P> z	[0.025	0.975]
const	0.2678	0.001	321.423	0.000	0.266	0.269
ar.L1.BA	0.7107	0.073	9.680	0.000	0.567	0.855
ar.L2.BA	0.4449	0.108	4.126	0.000	0.234	0.656
ar.L3.BA	0.6768	0.099	6.833	0.000	0.483	0.871
ar.L4.BA	-0.9008	0.066	-13.661	0.000	-1.030	-0.772
ma.L1.BA	0.2300	0.097	2.374	0.018	0.040	0.420

ma.L2.BA	-0.4161	0.095	-4.373	0.000	-0.603	-0.230
ma.L3.BA	-0.8139	0.102	-7.958	0.000	-1.014	-0.613

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	-0.6402	-0.8019j	1.0261	-0.3572
AR.2	-0.6402	+0.8019j	1.0261	0.3572
AR.3	1.0158	-0.1501j	1.0269	-0.0234
AR.4	1.0158	+0.1501j	1.0269	0.0234
MA.1	1.0000	-0.0000j	1.0000	-0.0000
MA.2	-0.7556	-0.8110j	1.1084	-0.3694
MA.3	-0.7556	+0.8110j	1.1084	0.3694

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
117 0.250726
118 0.252510
119 0.254042
120 0.255702
121 0.258116
122 0.260001
123 0.262158
124 0.264667
125 0.266512

```

3 ER(PIT)

HH 201 HT 112 KT 010//414 LG 102 LT 100 NC 210 OB 211 SK 011 SS 010//302 WO 101

```
[71]: #HH ER
modeling(er_HH, (2,0,1), 10)
```

ARMA Model Results

Dep. Variable:	ER	No. Observations:	110
Model:	ARMA(2, 1)	Log Likelihood	-44.164
Method:	css-mle	S.D. of innovations	0.354
Date:	Sat, 26 Sep 2020	AIC	98.328
Time:	01:44:40	BIC	111.830
Sample:	0	HQIC	103.804

	coef	std err	z	P> z	[0.025	0.975]
const	4.2368	1.270	3.336	0.001	1.748	6.726
ar.L1.ER	1.9676	0.048	40.773	0.000	1.873	2.062
ar.L2.ER	-0.9720	0.048	-20.345	0.000	-1.066	-0.878
ma.L1.ER	-0.9144	0.137	-6.669	0.000	-1.183	-0.646

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	1.0122	-0.0658j	1.0143	-0.0103
AR.2	1.0122	+0.0658j	1.0143	0.0103
MA.1	1.0937	+0.0000j	1.0937	0.0000

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
110 4.168585
111 4.116964
112 4.067313
113 4.019792
114 3.974548
115 3.931715
116 3.891412
117 3.853743
118 3.818799
119 3.786654

```

```
[74]: #HT ER
modeling(er_HT,(1,1,2),12,'NC')
```

ARIMA Model Results

Dep. Variable:	D.ER	No. Observations:	108
Model:	ARIMA(1, 1, 2)	Log Likelihood	-74.501
Method:	css-mle	S.D. of innovations	0.479
Date:	Sat, 26 Sep 2020	AIC	157.002
Time:	01:45:08	BIC	167.731
Sample:	1	HQIC	161.352

	coef	std err	z	P> z	[0.025	0.975]
--	------	---------	---	------	--------	--------

ar.L1.D.ER	-0.8058	0.169	-4.773	0.000	-1.137	-0.475
ma.L1.D.ER	1.1079	0.128	8.638	0.000	0.857	1.359
ma.L2.D.ER	0.6470	0.076	8.467	0.000	0.497	0.797
Roots						
=====						
	Real	Imaginary		Modulus	Frequency	

AR.1	-1.2411	+0.0000j		1.2411	0.5000	
MA.1	-0.8562	-0.9014j		1.2432	-0.3709	
MA.2	-0.8562	+0.9014j		1.2432	0.3709	

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
109 4.330714
110 4.674135
111 4.397421
112 4.620385
113 4.440730
114 4.585489
115 4.468848
116 4.562832
117 4.487104
118 4.548123
119 4.498956
120 4.538572

```

```
[11]: #KT ER
modeling(er_KT,(4,1,4),9,'nc')
```

```

C:\Users\user\Anaconda3\lib\site-packages\statsmodels\base\model.py:548:
HessianInversionWarning: Inverting hessian failed, no bse or cov_params
available
'available', HessianInversionWarning)

```

ARIMA Model Results			
=====			
Dep. Variable:	D.ER	No. Observations:	111
Model:	ARIMA(4, 1, 4)	Log Likelihood	-26.198
Method:	css-mle	S.D. of innovations	0.295
Date:	Sat, 26 Sep 2020	AIC	70.396
Time:	16:37:02	BIC	94.782
Sample:	1	HQIC	80.288

	coef	std err	z	P> z	[0.025	0.975]
ar.L1.D.ER	-0.7634	0.102	-7.502	0.000	-0.963	-0.564
ar.L2.D.ER	-0.5596	0.117	-4.771	0.000	-0.790	-0.330
ar.L3.D.ER	-0.6014	0.127	-4.723	0.000	-0.851	-0.352
ar.L4.D.ER	-0.7099	0.106	-6.712	0.000	-0.917	-0.503
ma.L1.D.ER	0.6127	0.063	9.685	0.000	0.489	0.737
ma.L2.D.ER	0.5129	0.058	8.894	0.000	0.400	0.626
ma.L3.D.ER	0.6127	0.067	9.155	0.000	0.482	0.744
ma.L4.D.ER	1.0000	0.069	14.476	0.000	0.865	1.135

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	0.4525	-1.0043j	1.1015	-0.1826
AR.2	0.4525	+1.0043j	1.1015	0.1826
AR.3	-0.8762	-0.6272j	1.0775	-0.4011
AR.4	-0.8762	+0.6272j	1.0775	0.4011
MA.1	0.4755	-0.8797j	1.0000	-0.1711
MA.2	0.4755	+0.8797j	1.0000	0.1711
MA.3	-0.7819	-0.6235j	1.0000	-0.3929
MA.4	-0.7819	+0.6235j	1.0000	0.3929

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
112 3.875421
113 3.809631
114 3.766659
115 3.670642
116 3.856234
117 3.840842
118 3.836983
119 3.805084
120 3.709103

```

```
[12]: #LG ER
modeling(er_LG,(1,0,2),7)
```

ARMA Model Results

Dep. Variable:	ER	No. Observations:	113
Model:	ARMA(1, 2)	Log Likelihood	-40.403
Method:	css-mle	S.D. of innovations	0.343
Date:	Sat, 26 Sep 2020	AIC	90.805
Time:	11:30:18	BIC	104.442
Sample:	0	HQIC	96.339

	coef	std err	z	P> z	[0.025	0.975]
const	4.3780	0.260	16.836	0.000	3.868	4.888
ar.L1.ER	0.8058	0.076	10.620	0.000	0.657	0.955
ma.L1.ER	0.3068	0.108	2.844	0.004	0.095	0.518
ma.L2.ER	0.3041	0.091	3.337	0.001	0.125	0.483

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	1.2410	+0.0000j	1.2410	0.0000
MA.1	-0.5045	-1.7418j	1.8133	-0.2949
MA.2	-0.5045	+1.7418j	1.8133	0.2949

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
113 4.774576
114 4.698293
115 4.636097
116 4.585980
117 4.545595
118 4.513053
119 4.486832

```

```
[14]: #LT ER
modeling(er_LT,(1,0,0),9)
```

ARMA Model Results

Dep. Variable:	ER	No. Observations:	110
Model:	ARMA(1, 0)	Log Likelihood	-36.496
Method:	css-mle	S.D. of innovations	0.334
Date:	Sat, 26 Sep 2020	AIC	78.992
Time:	11:31:06	BIC	87.093

Sample: 0 HQIC 82.278

	coef	std err	z	P> z	[0.025	0.975]
const	4.3589	0.382	11.401	0.000	3.610	5.108
ar.L1.ER	0.9216	0.045	20.657	0.000	0.834	1.009
Roots						
	Real	Imaginary	Modulus	Frequency		
AR.1	1.0850	+0.0000j	1.0850	0.0000		

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
110 4.847453
111 4.809163
112 4.773873
113 4.741349
114 4.711374
115 4.683748
116 4.658287
117 4.634821
118 4.613195

```

```
[17]: #NC ER
modeling(er_NC,(2,1,0),7,'nc')
```

ARIMA Model Results

Dep. Variable:	D.ER	No. Observations:	109
Model:	ARIMA(2, 1, 0)	Log Likelihood	-33.920
Method:	css-mle	S.D. of innovations	0.330
Date:	Sat, 26 Sep 2020	AIC	73.839
Time:	11:31:58	BIC	81.913
Sample:	1	HQIC	77.114

	coef	std err	z	P> z	[0.025	0.975]
ar.L1.D.ER	0.1692	0.102	1.653	0.098	-0.031	0.370
ar.L2.D.ER	0.2153	0.102	2.102	0.036	0.015	0.416

Roots				
	Real	Imaginary	Modulus	Frequency
AR.1	1.7979	+0.0000j	1.7979	0.0000
AR.2	-2.5840	+0.0000j	2.5840	0.5000

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
110 3.933432
111 3.898275
112 3.877997
113 3.866998
114 3.860772
115 3.857351
116 3.855432

```

```
[20]: #OB ER
modeling(er_OB,(2,1,1),12,'NC')
```

ARIMA Model Results				
Dep. Variable:	D.ER	No. Observations:	111	
Model:	ARIMA(2, 1, 1)	Log Likelihood	-57.156	
Method:	css-mle	S.D. of innovations	0.402	
Date:	Sat, 26 Sep 2020	AIC	122.312	
Time:	11:32:21	BIC	133.150	
Sample:	1	HQIC	126.709	

	coef	std err	z	P> z	[0.025	0.975]
ar.L1.D.ER	0.7220	0.153	4.720	0.000	0.422	1.022
ar.L2.D.ER	-0.7015	0.108	-6.519	0.000	-0.912	-0.491
ma.L1.D.ER	-0.5594	0.135	-4.139	0.000	-0.824	-0.295

Roots				
	Real	Imaginary	Modulus	Frequency
AR.1	0.5146	-1.0774j	1.1940	-0.1791
AR.2	0.5146	+1.0774j	1.1940	0.1791
MA.1	1.7878	+0.0000j	1.7878	0.0000

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

0
112 4.246179
113 4.185770
114 4.125197
115 4.123841
116 4.165354
117 4.196275
118 4.189478
119 4.162880
120 4.148446
121 4.156683
122 4.172755
123 4.178580

```
[13]: #SK ER  
modeling(er_SK,(0,1,1),9,'NC')
```

```

              ARIMA Model Results
=====
Dep. Variable:          D.ER    No. Observations:          113
Model:                ARIMA(0, 1, 1)    Log Likelihood          -39.492
Method:                css-mle    S.D. of innovations          0.343
Date:                  Sat, 26 Sep 2020    AIC              82.984
Time:                  16:37:48    BIC              88.439
Sample:                1    HQIC              85.198

=====
              coef    std err          z      P>|z|      [0.025      0.975]
-----
ma.L1.D.ER      0.2533      0.105      2.420      0.016      0.048      0.459
              Roots
=====
              Real      Imaginary      Modulus      Frequency
-----
MA.1          -3.9473      +0.0000j      3.9473      0.5000
=====
```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```
0
114 5.956982
115 5.956982
116 5.956982
117 5.956982
118 5.956982
119 5.956982
120 5.956982
121 5.956982
122 5.956982
```

```
[15]: #SS ER
      modeling(er_SS,(3,0,2),11,'C')
```

ARMA Model Results

```
=====
Dep. Variable:          ER    No. Observations:          111
Model:                ARMA(3, 2)  Log Likelihood          -23.193
Method:                css-mle   S.D. of innovations          0.287
Date:                  Sat, 26 Sep 2020  AIC                60.386
Time:                  16:38:31   BIC                 79.353
Sample:                0        HQIC                 68.081
=====
```

```
=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          4.7447        0.293      16.181      0.000         4.170         5.319
ar.L1.ER        0.3011        0.056       5.422      0.000         0.192         0.410
ar.L2.ER       -0.4125        0.052      -7.953      0.000        -0.514        -0.311
ar.L3.ER        0.8692        0.056     15.587      0.000         0.760         0.978
ma.L1.ER        0.7992        0.042     19.195      0.000         0.718         0.881
ma.L2.ER        0.9998        0.039     25.313      0.000         0.922         1.077
=====
```

Roots

```
=====
              Real      Imaginary      Modulus      Frequency
-----
AR.1         -0.3149      -0.9709j         1.0207         -0.2999
AR.2         -0.3149      +0.9709j         1.0207          0.2999
AR.3          1.1043      -0.0000j         1.1043         -0.0000
MA.1         -0.3997      -0.9168j         1.0001         -0.3154
MA.2         -0.3997      +0.9168j         1.0001          0.3154
=====
```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```
0
111 6.036718
112 5.958781
113 5.813561
114 5.688741
115 5.643319
116 5.554905
117 5.438527
118 5.400473
119 5.360173
120 5.262579
121 5.216741
```

```
[27]: #WO ER
modeling(er_WO,(1,0,1),9)
```

ARMA Model Results

```
=====
Dep. Variable:          ER    No. Observations:          117
Model:                  ARMA(1, 1)    Log Likelihood          -37.002
Method:                  css-mle    S.D. of innovations          0.327
Date:                   Sat, 26 Sep 2020    AIC          82.004
Time:                   11:35:06    BIC          93.052
Sample:                 0    HQIC          86.489
=====
```

```
=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const         3.7488        0.985        3.805      0.000        1.818        5.680
ar.L1.ER       0.9635        0.033       29.261      0.000        0.899        1.028
ma.L1.ER       0.3425        0.098        3.484      0.000        0.150        0.535
=====
```

Roots

```
=====
              Real      Imaginary      Modulus      Frequency
-----
AR.1          1.0378      +0.0000j        1.0378        0.0000
MA.1         -2.9196      +0.0000j        2.9196        0.5000
=====
```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

0

```

117  5.194384
118  5.141680
119  5.090896
120  5.041965
121  4.994817
122  4.949388
123  4.905616
124  4.863439
125  4.822801

```

4 WLS

HH 302 HT 010//212 KT 010//414 LG 102 LT 103 NC 010/110 OB 411 SK 010/100 SS 010/100
WO 100

```

[30]: #HH WLS
      modeling(wls_HH,(3,0,2),10)

```

ARMA Model Results

```

=====
Dep. Variable:          WLS      No. Observations:          110
Model:                ARMA(3, 2)  Log Likelihood          156.282
Method:                css-mle    S.D. of innovations      0.057
Date:                  Sat, 26 Sep 2020  AIC                  -298.564
Time:                  11:36:23    BIC                     -279.661
Sample:                0          HQIC                     -290.897
=====

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          0.3988      0.144       2.769      0.006      0.117      0.681
ar.L1.WLS       0.3508      0.110       3.196      0.001      0.136      0.566
ar.L2.WLS      -0.0066      0.146      -0.045      0.964     -0.292      0.279
ar.L3.WLS       0.5745      0.115       4.985      0.000      0.349      0.800
ma.L1.WLS       0.3426      0.032     10.722      0.000      0.280      0.405
ma.L2.WLS       0.9555      0.079     12.038      0.000      0.800      1.111
=====

```

Roots

```

=====
              Real      Imaginary      Modulus      Frequency
-----
AR.1          1.0382      -0.0000j      1.0382      -0.0000
AR.2         -0.5134      -1.1887j      1.2948      -0.3149
AR.3         -0.5134      +1.1887j      1.2948       0.3149
MA.1         -0.1793      -1.0072j      1.0230      -0.2780
MA.2         -0.1793      +1.0072j      1.0230       0.2780
=====

```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

0

```
110 0.286332
111 0.300901
112 0.304992
113 0.301925
114 0.309193
115 0.314113
116 0.314029
117 0.318142
118 0.322412
119 0.323835
```

```
[16]: #HT WLS
      modeling(wls_HT,(2,1,2),12,'nc')
```

ARIMA Model Results

```
=====
Dep. Variable:          D.WLS    No. Observations:          108
Model:                 ARIMA(2, 1, 2)    Log Likelihood          164.589
Method:                css-mle    S.D. of innovations          0.053
Date:                  Sat, 26 Sep 2020    AIC          -319.178
Time:                  16:39:00    BIC          -305.768
Sample:                1    HQIC          -313.741
=====
```

```
=====
              coef    std err          z      P>|z|      [0.025      0.975]
-----
ar.L1.D.WLS      0.1407      0.042      3.329      0.001      0.058      0.224
ar.L2.D.WLS     -0.8400         nan         nan         nan         nan         nan
ma.L1.D.WLS     -0.1790      0.155     -1.152      0.249     -0.483      0.125
ma.L2.D.WLS      0.7419      0.150      4.960      0.000      0.449      1.035
=====
```

Roots

```
=====
              Real      Imaginary      Modulus      Frequency
-----
AR.1          0.0838      -1.0879j      1.0911      -0.2378
AR.2          0.0838      +1.0879j      1.0911       0.2378
MA.1          0.1206      -1.1547j      1.1610     -0.2334
MA.2          0.1206      +1.1547j      1.1610       0.2334
=====
```

C:\Users\user\Anaconda3\lib\site-packages\statsmodels\base\model.py:548:

```

HessianInversionWarning: Inverting hessian failed, no bse or cov_params
available
    'available', HessianInversionWarning)
C:\Users\user\Anaconda3\lib\site-packages\statsmodels\tsa\arima_model.py:1490:
RuntimeWarning: invalid value encountered in sqrt
    return np.sqrt(np.diag(-inv(hess)))
C:\Users\user\Anaconda3\lib\site-
packages\scipy\stats\_distn_infrastructure.py:1932: RuntimeWarning: invalid
value encountered in less_equal
    cond2 = cond0 & (x <= _a)

<IPython.core.display.Javascript object>

```

```

<IPython.core.display.HTML object>

```

```

0
109 0.669300
110 0.682648
111 0.682595
112 0.671375
113 0.669841
114 0.679050
115 0.681634
116 0.674263
117 0.671055
118 0.676795
119 0.680297
120 0.675969

```

```

[17]: #KT WLS
      modeling(wls_KT,(4,1,4),9,'nc')

```

```

C:\Users\user\Anaconda3\lib\site-packages\statsmodels\base\model.py:548:
HessianInversionWarning: Inverting hessian failed, no bse or cov_params
available
    'available', HessianInversionWarning)

```

```

                        ARIMA Model Results
=====
Dep. Variable:          D.WLS      No. Observations:          111
Model:                 ARIMA(4, 1, 4)  Log Likelihood          190.780
Method:                css-mle      S.D. of innovations       0.042
Date:                  Sat, 26 Sep 2020  AIC                      -363.560
Time:                  16:39:32      BIC                      -339.174
Sample:                1           HQIC                      -353.667
=====

```

	coef	std err	z	P> z	[0.025	0.975]

ar.L1.D.WLS	-0.3149	0.096	-3.277	0.001	-0.503	-0.127
ar.L2.D.WLS	-0.0887	0.097	-0.913	0.361	-0.279	0.102
ar.L3.D.WLS	-0.3893	0.074	-5.292	0.000	-0.533	-0.245
ar.L4.D.WLS	-0.8091	0.087	-9.276	0.000	-0.980	-0.638
ma.L1.D.WLS	0.4172	0.064	6.487	0.000	0.291	0.543
ma.L2.D.WLS	0.2645	0.078	3.377	0.001	0.111	0.418
ma.L3.D.WLS	0.4171	0.065	6.391	0.000	0.289	0.545
ma.L4.D.WLS	0.9999	0.065	15.395	0.000	0.873	1.127

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	0.6169	-0.8262j	1.0311	-0.1479
AR.2	0.6169	+0.8262j	1.0311	0.1479
AR.3	-0.8575	-0.6535j	1.0782	-0.3964
AR.4	-0.8575	+0.6535j	1.0782	0.3964
MA.1	0.5626	-0.8268j	1.0001	-0.1549
MA.2	0.5626	+0.8268j	1.0001	0.1549
MA.3	-0.7712	-0.6366j	1.0000	-0.3902
MA.4	-0.7712	+0.6366j	1.0000	0.3902

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
112 0.731450
113 0.739907
114 0.719804
115 0.707352
116 0.702117
117 0.705853
118 0.726253
119 0.731611
120 0.730896

```

```
[35]: #LG WLS
modeling(wls_LG,(1,0,2),7)
```

ARMA Model Results

Dep. Variable:	WLS	No. Observations:	113
Model:	ARMA(1, 2)	Log Likelihood	161.686
Method:	css-mle	S.D. of innovations	0.057

```

Date:          Sat, 26 Sep 2020    AIC          -313.373
Time:          11:40:46           BIC          -299.736
Sample:        0                  HQIC         -307.839

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          0.6066        0.047      12.980      0.000        0.515        0.698
ar.L1.WLS       0.7576        0.088       8.580      0.000        0.585        0.931
ma.L1.WLS       0.4890        0.081       6.017      0.000        0.330        0.648
ma.L2.WLS       0.6457        0.095       6.782      0.000        0.459        0.832

```

Roots

```

=====
              Real          Imaginary      Modulus      Frequency
-----
AR.1          1.3199          +0.0000j          1.3199          0.0000
MA.1          -0.3786          -1.1854j          1.2444          -0.2992
MA.2          -0.3786          +1.1854j          1.2444          0.2992
-----

```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
113  0.596592
114  0.598490
115  0.600457
116  0.601947
117  0.603075
118  0.603931
119  0.604579

```

```

[37]: #LT WLS
      modeling(wls_LT,(1,0,3),9)

```

ARMA Model Results

```

=====
Dep. Variable:          WLS    No. Observations:          110
Model:                ARMA(1, 3)    Log Likelihood          192.675
Method:                css-mle    S.D. of innovations          0.041
Date:                Sat, 26 Sep 2020    AIC          -373.350
Time:                11:41:11    BIC          -357.147
Sample:                0    HQIC          -366.778

```

	coef	std err	z	P> z	[0.025	0.975]
const	0.5777	0.099	5.835	0.000	0.384	0.772
ar.L1.WLS	0.9494	0.037	25.675	0.000	0.877	1.022
ma.L1.WLS	-0.0277	0.099	-0.280	0.780	-0.221	0.166
ma.L2.WLS	0.1947	0.097	1.999	0.046	0.004	0.386
ma.L3.WLS	0.2718	0.088	3.090	0.002	0.099	0.444

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	1.0533	+0.0000j	1.0533	0.0000
MA.1	0.5660	-1.2924j	1.4109	-0.1843
MA.2	0.5660	+1.2924j	1.4109	0.1843
MA.3	-1.8484	-0.0000j	1.8484	-0.5000

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
110 0.434011
111 0.417183
112 0.419772
113 0.427759
114 0.435342
115 0.442542
116 0.449377
117 0.455867
118 0.462028

```

```
[9]: #NC WLS
modeling(wls_NC,(1,1,0),7,'NC')
```

ARIMA Model Results

```

=====
Dep. Variable:          D.WLS      No. Observations:          109
Model:                ARIMA(1, 1, 0)  Log Likelihood          193.556
Method:                css-mle      S.D. of innovations        0.041
Date:                  Sat, 26 Sep 2020  AIC                      -383.111
Time:                  13:08:09      BIC                      -377.728
Sample:                1            HQIC                      -380.928
=====

```

	coef	std err	z	P> z	[0.025	0.975]
--	------	---------	---	------	--------	--------

ar.L1.D.WLS	-0.1317	0.094	-1.394	0.163	-0.317	0.053
Roots						
	Real	Imaginary	Modulus	Frequency		
AR.1	-7.5924	+0.0000j	7.5924	0.5000		

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
110 0.562
111 0.562
112 0.562
113 0.562
114 0.562
115 0.562
116 0.562

```

```
[12]: #OB WLS
modeling(wls_OB,(4,1,1),12,'nc')
```

ARIMA Model Results						
Dep. Variable:	D.WLS	No. Observations:	111			
Model:	ARIMA(4, 1, 1)	Log Likelihood	160.125			
Method:	css-mle	S.D. of innovations	0.057			
Date:	Sat, 26 Sep 2020	AIC	-308.249			
Time:	13:09:16	BIC	-291.992			
Sample:	1	HQIC	-301.654			
	coef	std err	z	P> z	[0.025	0.975]
ar.L1.D.WLS	0.7943	0.159	4.981	0.000	0.482	1.107
ar.L2.D.WLS	-0.4144	0.142	-2.913	0.004	-0.693	-0.136
ar.L3.D.WLS	0.7517	0.142	5.279	0.000	0.473	1.031
ar.L4.D.WLS	-0.6329	0.128	-4.947	0.000	-0.884	-0.382
ma.L1.D.WLS	-0.7910	0.150	-5.271	0.000	-1.085	-0.497
Roots						
	Real	Imaginary	Modulus	Frequency		

AR.1	-0.4476	-0.9891j	1.0857	-0.3176
AR.2	-0.4476	+0.9891j	1.0857	0.3176
AR.3	1.0414	-0.5060j	1.1578	-0.0720
AR.4	1.0414	+0.5060j	1.1578	0.0720
MA.1	1.2643	+0.0000j	1.2643	0.0000

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

0

```

112 0.469447
113 0.494425
114 0.501232
115 0.519926
116 0.530825
117 0.521045
118 0.518503
119 0.516900
120 0.502430
121 0.495881
122 0.497079
123 0.490883

```

```
[14]: #SK WLS
modeling(wls_SK,(1,0,0),9)
```

ARMA Model Results

```

=====
Dep. Variable:          WLS    No. Observations:          114
Model:                ARMA(1, 0)    Log Likelihood          156.880
Method:                css-mle    S.D. of innovations          0.061
Date:                  Sat, 26 Sep 2020    AIC          -307.759
Time:                  13:12:08    BIC          -299.551
Sample:                0    HQIC          -304.428
=====

```

	coef	std err	z	P> z	[0.025	0.975]
const	0.3089	0.049	6.346	0.000	0.214	0.404
ar.L1.WLS	0.8891	0.046	19.532	0.000	0.800	0.978

Roots

	Real	Imaginary	Modulus	Frequency

AR.1	1.1247	+0.0000j	1.1247	0.0000
------	--------	----------	--------	--------

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
114 0.330332
115 0.327959
116 0.325850
117 0.323975
118 0.322307
119 0.320824
120 0.319506
121 0.318334
122 0.317292

```

```
[18]: #SS WLS
modeling(wls_SS,(1,0,0),11,'NC')
```

ARMA Model Results

Dep. Variable:	WLS	No. Observations:	111
Model:	ARMA(1, 0)	Log Likelihood	175.680
Method:	css-mle	S.D. of innovations	0.049
Date:	Sat, 26 Sep 2020	AIC	-347.359
Time:	13:14:21	BIC	-341.940
Sample:	0	HQIC	-345.161

	coef	std err	z	P> z	[0.025	0.975]
ar.L1.WLS	0.9915	0.008	127.531	0.000	0.976	1.007

Roots

	Real	Imaginary	Modulus	Frequency
AR.1	1.0086	+0.0000j	1.0086	0.0000

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
111 0.385696
112 0.382420
113 0.379171
114 0.375950
115 0.372757
116 0.369591
117 0.366451
118 0.363338
119 0.360252
120 0.357192
121 0.354158

```

```
[19]: #WO WLS
modeling(wls_WO,(1,0,0),9)
```

```

=====
                        ARMA Model Results
=====
Dep. Variable:                WLS      No. Observations:                117
Model:                        ARMA(1, 0)  Log Likelihood                179.554
Method:                        css-mle    S.D. of innovations                0.052
Date:                          Sat, 26 Sep 2020  AIC                -353.109
Time:                          13:14:38    BIC                -344.822
Sample:                        0          HQIC                -349.744
=====

              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          0.6209      0.071       8.744      0.000       0.482       0.760
ar.L1.WLS       0.9385      0.038      24.473      0.000       0.863       1.014

                        Roots
=====
              Real      Imaginary      Modulus      Frequency
-----
AR.1          1.0655      +0.0000j       1.0655       0.0000
-----

```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

0
117 0.480210
118 0.488853
119 0.496965
120 0.504579

```

121	0.511725
122	0.518432
123	0.524726
124	0.530634
125	0.536178