with the classical choice of Bmin and Bmax, here we calculate

$$\int_{B_{min}}^{B_{max}} u(t, x_i + y)k(y)d(y) \tag{1}$$

as

$$\int_{B_{min}+x_i}^{B_{max}+x_i} u(t,z)k(z-x_i)d(z)$$
 (2)

using the variable change z = x + y.