# Day 4: Algebra Review

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Math Camp 2021

Questions?

Concluding CH 1 of Moore & Siegel – moving to Ch 2  $\,$ 

### Algebra Review

#### Properties

- Associative property: (a + b) + c = a + (b + c) and (a \* b) \* c = a \* (b \* c)
- **Commutative property** a + b = b + a and a \* b = b \* a
- ▶ Distributive property a(b+c) = ab + ac
- ▶ Identity property x + 0 = x and x \* 1 = x
- ▶ Inverse property -x + x = 0. Multiplicative inverse exists, but not for all numbers  $x^{-1} * x = 1$

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2. 
$$m^2 + 3m + 2 =$$

3. 
$$x^2 + 5x + 6 =$$

4. 
$$25 - x^2 =$$

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- 2.  $2x^2 + 7x + 3$
- 3.  $6y^2 + y 2$

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$$6y^2 + y - 2(2y - 1)(3y + 2)$$

### Inequalities

### Relations: Intervals & Inequalities

Interval notation can be used to express ranges of numbers :

[a, b]	$a \le x \le b$	Square brackets include end points (closed
		interval)
(a,b)	a < x < b	Parenthesis mean exclude end points
		(open interval)
$\{a,b\}$		Typically used for sets - not inequali-
		ties/intervals

#### Relations

### Graph the following:

- ▶ 4 < *x*
- ► *y* > 12
- ▶ 3 < *z* < 7
- **▶** (3,9)
- **▶** [-7, 2)

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Solve like regular equations but FLIP inequality when multiplying by negative values.

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#### EX:

▶ 
$$3x < 4x + 2$$

$$\triangleright$$
 60 $x > -10(x + 7)$ 

$$-6(x+8) < 12$$

### Absolute Value

Solve for TWO possibilities: quantity is positive or negative. EX: |x-3| > 4

- ▶ Quantity is positive: drop bars, solve like usual: x 3 > 4, x > 7
- ▶ Quantity is negative: then, really have x 3 < -4 Solve to find x < -1

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Solution: x < -1 OR x > 7 Try: |2x - 3| > 9

### **Factorial**

The factorial, !, multiplies a number by each subsequent number down to one.

For example, 4! = 4 \* 3 \* 2 \* 1

You can also divide and multiply factorials:  $\frac{3!}{4!} = \frac{3*2*1}{4*3*2*1} = \frac{1}{4}$ 

CANNOT ADD THE NUMBERS!! (e.g.  $6!3! \neq 9!$ )

We can use factorials to help us understand ways of combining elements: e.g. suppose you are forming a committee of 3 people from a group of 5. How many ways can we do that?

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We could also calculate them using the binomial function:

$$\binom{5}{3} = \frac{5!}{3!2!} = \frac{5*4}{2} = 10$$

Try  $\binom{4}{2}$  with population A,B,C,D. Using the general formula:  $\binom{N}{k} = \frac{N!}{k!(N-k)!}$ 

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You may have different populations and different treatments – how many different groups would you need to test the possible combinations?

Relations allow comparison of variables and expressions – some may be more or less specific in how they assign or specify these relationships between the range(y) and domain(x). Suppose we have a domain as follows  $\{apple, kiwi, lime\}$  and a range of  $\{4, 5\}$ .

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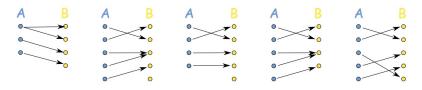


Figure 1:

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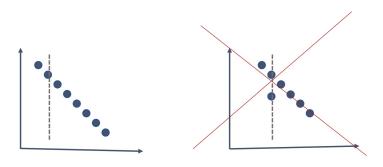


Figure 2: "Vertical line test"

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You can also combine functions, e.g. f(x) = x and  $g(x) = x^3$  can be combined to produce  $f \circ g(x) = f(g(x))$ .

Table 3.1 from book (pg 49)

Term	Meaning
Identity	Elements in domain are mapped to identical
function	elements in codomain
Inverse func-	Function that when composed with original
tion	function returns identity function
Surjective	Every value in codomain produced by value
(onto)	in domain
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Why do we care?

We care about whether a function is surjective, injective, or bijective because we will know if we can trace back what produced what we have.

https://www.mathsisfun.com/sets/injective-surjective-bijective.html

- ▶ We can see that both functions are surjective each 'covers' the codomains
- In the case of g(x), we can see that it is injective, while f(x) is not
- ► Thus, f(x) is not bijective but g(x) is (both surjective and injective) thus, it is invertible (to be defined)

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Composite functions, 
$$f \circ g(x) = f(g(x))$$
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We can see that we only get one y value for each x and that, depending on the domain/codomain, the function is surjective as well, making this function bijective and have a legitimate inverse.

# Monotonic Function Terms

Term	Meaning
Increasing	Function increases on subset of domain
Decreasing	Function decreases on subset of domain
Strictly increasing	Function always increases on subset of domain
Strictly decreasing	Function always decreases on subset of domain
Weakly increasing	Function does not decrease on subset of domain
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(Strict) monotonicity	Order preservation; function (strictly) increasing or
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Table 3.2 from book (pg 51)

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Table 3.2 from book (pg 51)

This is useful for math land but also for theory building: how are x and y related? Does more x ALWAYS mean more y (function is monotonically increasing, etc)?

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We have the **intercept** (where the line crosses the y axis) and the **slope** (unit increase in iv related to dv). This is the 'plain vanilla' version.

The **linear function** is much more expansive: includes multiple variables, exponents, and logs (logarithms).

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## Exponents<sup>1</sup>

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**Try**: 
$$xz^2(x^3z^{-2})^3 = (xz^2(x^9z^{-6})) = x^{10}z^{-4}$$

# Exponents, Exponentials, Exponential functions

#### Exponents

Exponents are where you take a variable to some power - e.g.  $x^a$  where x is a variable and a is a constant. Typically, we focus on the numerical portion of the exponent–calling it 'the exponent'.

#### Exponential

An exponential is the reverse of the exponent – here it is a number to the power of a variable, e.g.  $a^x$ . To get the x 'down', we need to use logarithms (aka logs).

#### **Exponential Function**

The exponential function has a particular base, e, (where e is Euler's e and is approx 2.72.)

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We care because we might see these as utility functions or use higher order values as a way to represent the relationship between two variables in a linear regression Know what these concepts are—will be relevant later.

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Logarithms (typically base 10 (log(x)) or base e (ln(e)), but any base is possible, e.g.  $log_{8675309}x$  (Bases aside from e and 10 will be specified).

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Exponents in log are different from what you might expect:

- $\log(x^2) = 2(\log(x))$
- $\triangleright log(x/y) = log(x) log(y)$  provided (x, y > 0)

Logs help weigh smaller values more heavily; adding units not linear–less meaningful for larger values (log(100) - 2 log(1000) - 3)

# Logs Practice

#### Simplify the following

- $\triangleright log(x^4)$
- ▶ log(xy)
- ►  $ln(e^3)$
- ► In(1)
- $\triangleright$  log(3) + log(7)

$$\log(x^4) = 4\log(x)$$

▶ 
$$log(xy)$$

► 
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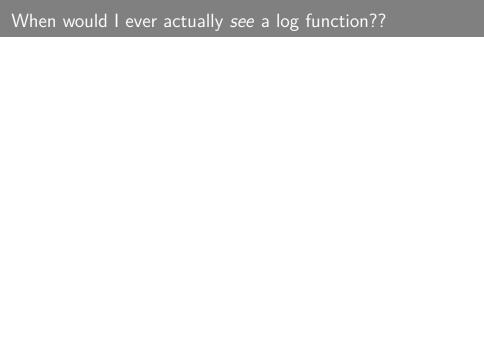
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$$ln(e^3) = 3$$

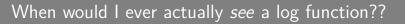
► 
$$ln(1) = 0$$

$$\log(3) + \log(7) = \log(21)$$

#### More Practice

► 
$$2e^{6x} = 18$$
  
►  $e^{x^2} = 1$   
►  $2^x = e^5$   
►  $2^{x-2} = 5$   
►  $ln(x^2) = 5$   
►  $ln(x^3) - ln(x) = ln(16)$ 





https://the society pages.org/graphic sociology/2010/12/07/1247/

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