Modeling Second-Language Learning from a Psychological Perspective

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Abstract

Psychological research on learning and memory has tended to emphasize small-scale laboratory studies. However, large datasets of people using educational software provide opportunities to explore these issues from a new perspective. In this paper we describe our approach to the Duolingo Second Language Acquisition Modeling (SLAM) competition which was run in early 2018. After detailing our modeling approach and a number of supplementary simulations, we reflect on which aspects of our reasonably successful model are substantively informed by findings and theories from the psychological literature.

1 Introduction

Educational software that aims to teach people new skills, languages, and academic subjects have become increasingly popular. The wide-spread deployment of these tools has created interesting opportunities to study the process of language acquisition in extremely large samples of learners in naturalistic situations. The Duolingo shared task on Second Lanugage Acquisition Modeling (SLAM) was a competitive modeling challenge run in early 2018 (Settles et al., 2018). The challenge, organized by Duolingo[1], a popular second language learning app, was to use log data from thousands of users completing millions of exercises to predict patterns of future translation mistakes in held-out data. The data was divided into three sets covering Spanish speakers learning English (`en_es`), English speakers learning Spanish (`es_en`), and English speakers learning French (`fr_en`). This paper reports the approach used by our team which ended in third place for the `en_es` data set, second place for `es_en`, and third place for `fr_en`.

[1] http://duolingo.com

Learning and memory has been a core focus of psychological science for over 100 years. Most of this work has sought to build explanatory theories of human learning and memory using relatively small-scale laboratory studies. Such studies have identified a number of important and apparently robust phenomena in memory including the nature of the retention curve (Rubin and Wenzel, 1996), the advantage for spaced over massed practice (Ruth, 1928; Cepeda et al., 2006; Mozer et al., 2009), the testing effect (Henry L. Roediger and Karpicke, 2006), and retrieval-induced forgetting (Anderson et al., 1994). The advent of large datasets such as the one provided in the Duolingo SLAM challenge may offer a new perspective and approach which may prove complementary to laboratory scale science (Griffiths, 2015; Goldstone and Lupyan, 2016). First, the much larger sample sizes may help to better identify parameters of psychological models. Second, datasets covering more naturalistic learning situations may allow us to test the predictive accuracy of psychological theories in a more generalizable fashion (Yarkoni and Westfall, 2017).

Despite these promising opportunities, it remains unclear how much of current psychological theory might be important for tasks such as the Duolingo SLAM challenge. As one example, the field of education data mining which has attempted to build predictive models of student learning have found excellent results using deep neural networks (so called "deep knowledge tracing", Piech et al., 2015) as opposed to more traditional, and interpretable, models and approaches that are rooted in cognitive science (e.g., Atkinson, 1972b,a; Corbett and Anderson, 1995; Pavlik and Anderson, 2008; Tubridy et al., in review). Recently, Khajah, Lindsey, & Mozer (2016) compared deep knowledge tracing (DKT) to a more standard "Bayesian knowledge tracing" (BKT)

models and showed that it was possible to equate the performance of the the BKT model by additional features and parameters that represent core aspects of the psychology of learning and memory such as forgetting (Khajah et al., 2016).

Our entry to SLAM borrowed conceptually from the Khajah et al. (2016) approach. Specifically we started with a relatively well known and powerful classification algorithm (gradient boosting decision trees, GBDT, Ke et al., 2017). This algorithm has some advantages over deep learning approach including the fact that the inferred decision rules are interpretable after the model is fit while still being able to model relatively complex decision criteria. We then created a number of new features for the SLAM the dataset covering aspect such as user perseverance, learning processes, contextual factors, and cognate similarity. After finding a model which provided the best held-out performance on the test data set, we conducted a number of "lesioning" studies where we selectively removed features from the model and re-estimated the parameters in order to assess the contribution of particular types of features. We being by describing our overall modeling approach, and then discuss some fo the lessons learned from our analysis.

2 Task Approach

We approached the task as a binary classification problem over instances (i.e., single words within an exercise). Our solution can be divided into two components—constructing a set of features that is highly informative about whether the user will answer an instance correctly, and designing a model that can achieve high performance using this feature set.

2.1 Feature Engineering

We used a variety of features, including features directly present in the training data, features constructed using the training data, and features that use information external to the training data. Except where otherwise specified, categorical variables were one-hot encoded.

2.1.1 Exercise features

We encoded the exercise number, client, session, format, and duration (i.e., number of seconds to complete the exercise), as well as the time since the user started using Duolingo for the first time.

2.1.2 Word features

Using spaCy[2], we lemmatized each word to produce a root word. Both the root word token and the original token were used as categorical features. Due to their high cardinality, these features were not one-hot encoded but were preserved in single columns and handled in this form by the model (as described below).

Along with the tokens themselves we encoded each instance word's part of speech, morphological features, and dependency edge label. (We noticed that some words in the original dataset were paired with the wrong morphological features, particularly near where punctuation had been removed from the sentence. To fix this, we reprocessed the data using Google SyntaxNet[3].)

We also encoded word length and several word characteristics gleaned from external data sources. The word frequency effect suggests that uncommon words are harder to process than common words; readers will look longer at low-frequency words and perform worse in word-identification tasks for these than for high-frequency words (Rayner, 1998). We therefore included a feature that encoded the frequency of each word in the language being acquired, calculated from Speer et al. (2017). A number of studies have also shown that age-of-acquisition (i.e., the age a which children typically exhibit this word in their vocabulary) is another strong predictor of word processing and lexical retrieval difficulty that is somewhat independent of word frequency (Brysbaert and Cortese, 2011; Ferrand et al., 2011). We therefore included mean age-of-acquisition (in English) as a feature, derived from published age-of-acquisition norms for 30,000 English words from (Kuperman et al., 2012) which covered many of the words present in the dataset. Additionally, cognates, or words sharing a common linguistic derivation, are easier to learn than words with dissimilar translations (De Groot and Keijzer, 2000). As an approximate measure of linguistic similarity, we used the Levenshtein edit distance between the word tokens and their translations scaled by the length of the longer word. We found translations using Google Translate[4] and calculated the Levenshtein distance to reflect the letter-by-letter similarity of the word and its translation (Hyyrö,

[2]https://spacy.io/
[3]https://github.com/ljm625/syntaxnet-rest-api
[4]https://cloud.google.com/translate/

2001).

2.1.3 User features

Just as we did for word tokens, we encoded the user ID as a single-column, high-cardinality feature. We also calculated several other user-level features that related to the "learning type" of a user. In particular, we encoded features to estimate the long-term motivation and diligence of a user. These features could help predict how users interact with old and novel words they encounter.

To estimate users' motivation we grouped their exercises into "bursts." Bursts were separated by at least 24 hours todd says: did you change my code because bursts were separate by 1 hour in my imementation. We used three concrete features about these bursts, namely the mean and median number of exercises within bursts as well as the total number of bursts of a given user. Users that were more motivated had potentially bursts with more exercises. Simultaneously, a larger total number of bursts indicated that the burst length estimate was more trustworthy.

To estimate users' diligence we speculated that a very diligent user might be using the app regularly at the same time of day, perhaps following a study schedule, compared to a less diligent user whose schedule might vary more. The data set did not provide a variable with the time of day, which would have been an interesting feature on its own. Instead, we were able to extract for each exercise the time of day relative to the first time a user had used the app, ranging from 0 to 1 (with 0 indicating the same time, 0.25 indicating a relative shift by 6 hours, etc.). We then discretized this variable into 20-minute bins and computed the entropy of the empirical frequency distribution over these bins. A lower entropy score indicated less variability in the times of day a user started their exercises.

2.1.4 Positional features

To account for the effects of surrounding words on the difficulty of an instance, we created several features related to the instance word's context in the exercise. These included the token of the previous word, the next word, and the instance word's root in the dependency tree, all stored in single columns as with the instance token itself. We also included the part of speech of each of these context words as additional features. When there was no previous word, next word, or dependency-tree root word, a special `None` token or `None` part of speech was used.

2.1.5 Temporal features

A user's probability of succeeding on an instance is likely related to their prior experience with that instance. To capture this, we calculated several features related to past experience.

First, we encoded the number of times the current exercise's exact sentence had been seen before by the user. This is informed by psychological research showing memory and perceptual processing improvement for repeated contexts or chunks (e.g., Chun and Phelps, 1999)

We also encoded a set of features recording past experience with the particular instance word. These features were encoded separately for the instance token and for the instance root word created by lemmatization. For each token (and root) we tracked user performance through four weighted error averages. At the user's first encounter of the token, each error term E starts at zero. After an encounter with an instance of the token with label L, it is updated according to the equation

$$E \leftarrow E + \alpha(L - E)$$

where α determines the speed of error updating. The four feature weighted error terms use $\alpha = \{.3, .1, .03, .01\}$, allowing both short-run and long-run changes in a user's error rate with a token to be tracked. Note that in cases where a token appears multiple times in an exercise, a single update of the error features is conducted using the mean of the token labels. Along with the error tracking features, for each token we calculated the number of labeled, unlabeled, and total encounters; time since last labeled encounter and last encounter; and whether the instance is the first encounter with the token.

In the training data, all instances are labeled as correct or incorrect, so the label for the previous encounter is always available. In the test data, labels are unavailable, so predictions must be made using a mix of labeled and unlabeled past encounters. To generate training-set features that are comparable to test-set features, we selectively ignored some labels when encoding temporal features on the training set. Specifically, for each user we first calculated the number of exercises n in the true test set. Then, when encoding the features for each instance, we selected a random integer r

Parameter	fr_en	en_es	es_en	all
num_leaves	256	512	512	1024
learning_rate	.05	.05	.05	.05
min_data_in_leaf	100	100	100	100
num_boost_rounds	750	650	600	750
cat_smooth	200	200	200	200
feature_fraction	.7	.7	.7	.7
max_cat_threshold	32	32	32	64

Table 1: Parameters of final LightGBM models. See LightGBM documentation for more information; all other parameters were left at their default values.

in the range $[1, n]$, and ignored labels in the prior r exercises. That is, we encode features for the current instance as though other instances in those prior exercises were unlabeled, and ignore updates to the error averages from those exercises. The result of this process is that each instance in the training set is encoded as though it were between one and n exercises into the test set.

2.2 Modeling

After featurizing the training data, we trained GBDT models to minimize log loss. GBDT works by iteratively building regression trees, each of which seeks to minimize the residual loss from prior trees. This allows it to capture non-linear effects and high-order interactions among features. We used the LightGBM[5] implementation of GBDT (Ke et al., 2017).

For continuous-valued features, GBDT can split a leaf at any point, creating different predicted values above and below that threshold. For categories that are one-hot encoded, it can split a leaf on any of the category's features. This means that for a category with thousands of values, potentially thousands of tree splits would be needed to capture its relation to the target. Fortunately, LightGBM implements an algorithm for partitioning the values of a categorical feature into two groups based on their relevence to the current loss, and create a single split to divide those groups (Fisher, 1958). Thus, as alluded to above, high-cardinality features like token and user were encoded as single columns and handled as categories by LightGBM.

We trained a model for each of the three language tracks of `en_es`, `es_en`, and `fr_en`, and also trained a model on the combined data from all three tracks, adding an additional "language" feature. Following model training, we averaged the predictions of each single-language model with that of the all-language model to form our final predictions.

To tune model hyper-parameters and evaluate the usefulness of features, we first trained the models on the "train" data set and evaluated them on the "dev" data set. Once the model structure was finalized, we trained on the combined "train" and "dev" data and produced predictions for the "test" data. The LightGBM hyperparameters used for each model are listed in Table 1.

2.3 Performance

The AUROC of our final predictions was .8585 on `en_es`, .8350 on `es_en`, and .8540 on `fr_en`. We did not attempt to optimize the model's F1 score, but the F1 score could likely be improved (at the cost of increased log loss) by finding the rescaling of the "dev" predicted probabilities that maximized the F1 score at the 0.5 threshold, and applying this rescaling to the "test" predicted probabilities.

3 Feature Removal Experiments

To better understand which features or groups of features were most important to our model's predictions, we conducted a set of experiments in which we lesioned (i.e., removed) a group of features and re-trained the model on the `train` set, evaluating performance on the `dev` set. For simplicity, we ran each of the lesioned models on all language data and report the average performance. We did not run individual-language models as we did for our primary model.

The results of the lesion experiments are shown in Figure 1. The models are as follows.

none: all features are included.

user: all user-level features, including the user ID and other calculated features like entropy and measures of exercise bursts, are removed.

userid & user other: only user ID or only the calculated features user features, respectively, are removed.

word: Token and token root IDs; previous, next, and dependency-tree root word IDs; and morphological, part of speech, and dependency tree features are removed.

word id & word other: only word IDs or only other word features, respectively, are removed.

[5] http://lightgbm.readthedocs.io/

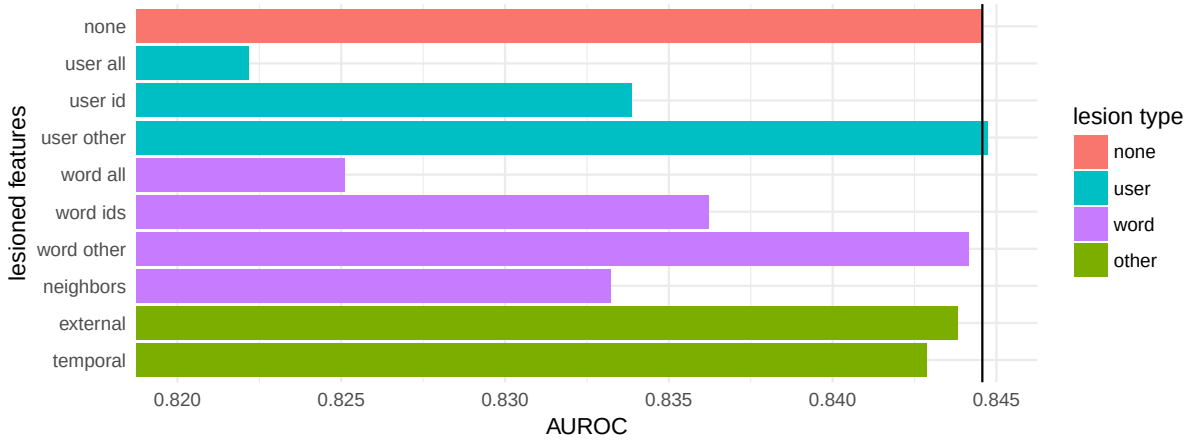

Figure 1: Performance on `dev` of models trained on all `train` data, with different groups of lesioned features. See main text for description of lesion groups

neighbors: Both word IDs and other word features are removed, but only for the previous, next, and dependency-tree root words. Information about the present word is maintained.

external: External information about the word, including corpus frequency, Levenshtein distance from translation, and age of acquisition, are removed.

temporal: Temporal information, including number and timing of past encounters with the word and error tracking information, is removed.

Interestingly, we found that for both user-level and word-level features, the bulk of the model's predictive power could be achieved using ID's alone, represented as high-cardinality categorical features. Removing other word features, such as morphological features and part of speech, created only a small degradation of performance. In the case of users, removing features such as entropy and average exercise burst length led to a tiny increase of performance. In the case of both users and words, though, we find that in the absence of ID features the other features are helpful and leads to better performance than removing all features. We also found that removing all information about neighboring words and the dependency-parse root word degraded performance. This confirms that word context matters, and suggests that users commonly make errors in word order, subject–verb matching and other grammatical rules.

Our external word features—Levenshtein distance to translation, frequency, and age of acquisition—provided a slight boost to model performance, showing the benefit of considering from a psychological and linguistic perspective what makes a word hard to learn. Adding temporal features about past encounters and errors helped the models, but not as much as we expected. While not included in the final model, we had also tried augmenting the temporal feature set with more features related to massing and spacing of encounters with a word, but found it did not improve performance. This is perhaps not surprising given how small the benefit of the existing temporal features are in our model.

While not plotted above, we also ran a model lesioning exercise-level features including client, session type, format, and exercise duration. This model achieved an AUROC of .787, far lower than any other lesion. This points to the importance of how a question is asked for user performance, reflecting insights from psychology such as the difference between recall and recognition memory (Yonelinas, 2002).

4 Discussion

When approaching the Duolingo SLAM task, we hoped to leverage psychological insights in building our model. We found that in some cases, such as the age of acquisition, this was helpful. In general, though, our model gained its power not from hand-crafted features but from applying a powerful inference technique (gradient boosted trees) to raw input about user and word IDs and exercise features.

There are multiple reasons for the limited applicability of psychology to this competition. First,

computational psychological models, while useful, are not well-suited to generating highly accurate predictions from large data sets. Because they are designed not for prediction but for explanation, they tend to use a small number of input variables and allow those variables to interact in limited ways. In contrast, gradient boosted trees, as well as other cutting-edge techniques like deep learning can extract high-level interactions among hundreds of features. Though they are highly opaque, require a lot of data, and are not amenable to explanation, these models excel at prediction.

Second, it is possible that our ability to use theories of learning, including ideas about massed and spaced practice, was disrupted by the fact that the data may have been adaptively created using these very principles (Settles and Meeder, 2016). If Duolingo adaptively sequenced the spacing of trials based on past errors, then the relationship between future errors and past spacing may have differed from that found in the psychological literature (Cepeda et al., 2006).

Finally, a task in which braoder generalization was required might have allowed psychologically inspired features to perform more competitively. In this task, there is a large amount of labeled training data for every user and for most words. This allow simple ID-based features to work because the past history of a user will likely influence their future performance. However, for a newly-encountered user or word, such an ID is useless because there will be not relevant parameter estimate. Theory-driven features, in contrast, can often generalize to new settings because they capture more generic aspects of the learning task. For example, if we were asked to generalize to a completely new language such as German, many parts of our model would falter but word frequency, age of acquisition, and Levenshtein distance to first-language translation would still likely prove to be features which have high predictive utility.

In sum, we believe that the Duolingo SLAM dataset and challenge provide interesting opportunities for cognitive science and psychology. One particularly useful paradigm is to use large-scale, predictive challenges like this one to identify the features or variables that are possibly important for learning. Then, complementary laboratory scale studies can be conducted which establish the causal status of such features through controlled experimentation. Or something more positive to end on?

5 Acknowledgments

This research was supported by NSF grant DRL-1631436 and BCS-1255538, and the John S. McDonnell Foundation Scholar Award to TMG. We thank Shannon Tubridy and Tal Yarkoni for helpful suggestions in the development of this work.

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