



Optimization Techniques for Multi Cooperative Systems MCTR 1021
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Optimization Based Merging for Connected Vehicles

By

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This is to certify that:

- (i) the report comprises only my original work toward the course project,
- (ii) due acknowledgment has been made in the text to all other material used

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November 25, 2023

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List of Abbreviations

CAVs	Connected and Automated Vehicles
MS	Merging Sequence
CACC	Cooperative Adaptive Cruise Control
AVS	Autonomous vehicles

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Chapter 1

Introduction

1.1 Smart transportation and autonomous vehicles

A new era of urban development known as "smart cities" is being ushered in by the use of cutting-edge technology to improve resident quality of life while also advancing efficiency and sustainability. The idea of smart transport, a dynamic and networked system intended to completely transform the movement of people and products inside and between these cutting-edge urban environments, is at the core of this urban evolution. In this sense, smart transport represents a major change in the conception, planning, and operation of cities, offering safer, more convenient, and environmentally friendly mobility options for all. It goes beyond simply streamlining routes and easing traffic congestion. Autonomous vehicles (AVS) have become a game-changer in smart cities, offering revolutionary answers to persistent urban transportation problems. Their exceptional coordination and communication skills have been important in helping to reduce traffic congestion. Autonomously navigating highways, AVS may merge and manoeuvre with efficiency, interacting with infrastructure and other cars to maximise traffic flow. By doing this, bottlenecks are lessened and safety is improved. Because AVS can anticipate and adjust to traffic patterns, intersection management—which is frequently a cause of congestion and accidents—has improved. Wait times are shortened and traffic flow is improved as a result. Overall, by drastically lowering traffic, enhancing intersection management, and expediting highway merging and ramp operations, autonomous cars have transformed transportation in smart cities and, in the process, raised the prospect of a safer, more effective, and sustainable urban lifestyle. The way we travel on the roads of the world is changing due to connected vehicles, which are sometimes referred to as the keystone of the transportation industry to come. These sophisticated cars and other forms of transportation are outfitted with state-of-the-art technology that enables real-time communication between them and the traffic infrastructure. The data that linked cars exchange opens up a world of amazing opportunities. They can enhance safety by alerting drivers of accidents and traffic bottlenecks, allowing for

speedier route adjustments. They give traffic management systems vital information that helps to improve traffic flow and lessen congestion. Furthermore, because they can share data to manage challenging road conditions and enhance overall road safety, linked vehicles open the door for the development of autonomous driving.

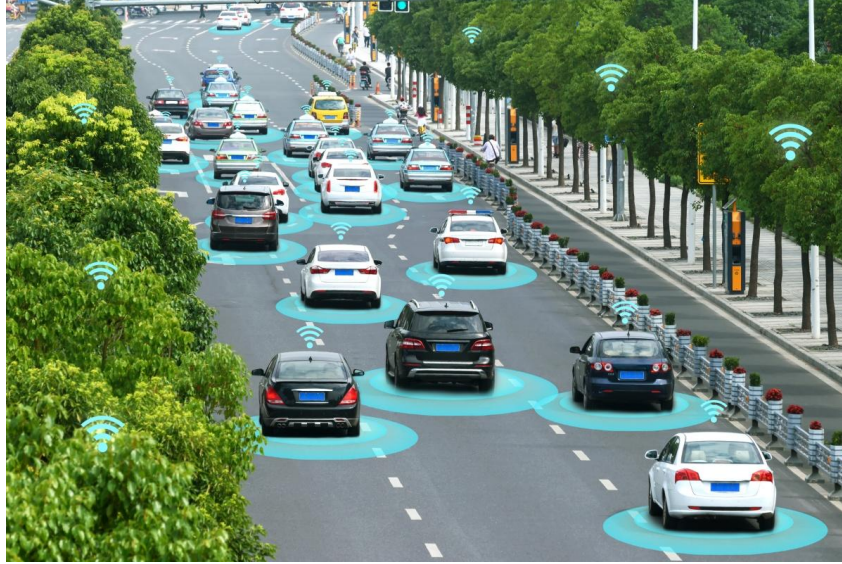


Figure 1.1: Autonomous vehicles

1.2 Merging vehicles in Highways on Ramps

Merging control of vehicles at highway on-ramps is a critical element in optimizing traffic flow and enhancing overall transportation efficiency. This process entails the seamless integration of vehicles entering the highway from an on-ramp with the existing traffic. Efficient merging is vital for reducing congestion, minimizing the potential for accidents, and ensuring the uninterrupted movement of vehicles on the highway. Advanced technologies, such as connected vehicles and autonomous driving systems, are poised to revolutionize this aspect of highway operations. Connected vehicles can communicate with each other and with the highway infrastructure in real-time, sharing information about their positions, speeds, and intentions. This enables a level of coordination and synchronization previously unattainable with traditional human drivers. AVS equipped with precise sensors, artificial intelligence, and instant communication capabilities, can anticipate traffic patterns and identify suitable gaps for merging onto the highway. These vehicles adjust their speed and trajectory in real-time, negotiating entry onto the highway with unparalleled precision. By removing human error and hesitation from the equation, these technologies not only make merging smoother but also enhance safety by reducing the risk of collisions and bottlenecks at on-ramps. Moreover, they enable a more efficient use of highway space and a more predictable traffic flow, ultimately improving the overall driving experience. As smart cities continue to evolve, the integration of merging control sys-

tems for vehicles at highway on-ramps holds great promise in reducing urban congestion and enhancing transportation sustainability. This technological advancement represents a critical step toward the realization of safer, more efficient, and more environmentally friendly mobility solutions in our increasingly interconnected and intelligent transportation networks.

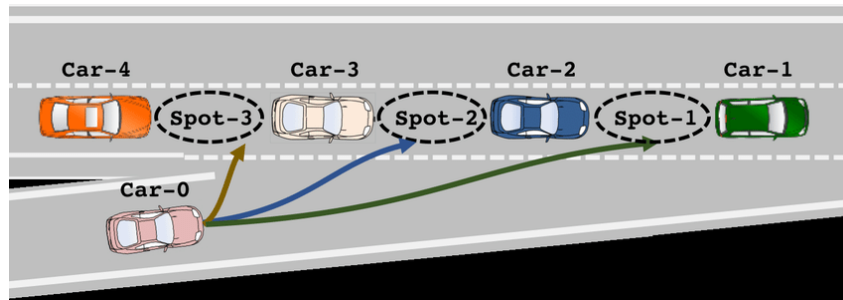


Figure 1.2: Merging vehicles

Chapter 2

Literature Review

There have been multiple research on the optimization of merging for connected vehicles. the study in [1] proposes a cooperative merging strategy for connected vehicles that uses a genetic algorithm to optimize traffic flow and minimize travel time. The strategy takes into account the inflow from on-ramps and uses wireless communication to improve traffic efficiency and fuel consumption. The paper presents simulation scenarios to verify the effectiveness of the proposed strategy and concludes with areas for future work.

There has been another study in [2] that proposes an optimization framework and analytical solution for coordinating connected and automated vehicles Connected and Automated Vehicles (CAVs) at merging roadways to achieve smooth traffic flow without stop-and-go driving. The effectiveness of the proposed solution is validated through simulation, showing significant reductions in fuel consumption and travel time. The majority of research efforts in this area have focused on intersections and merging highways.

Also the study in [3] presents an optimization framework for cooperative merging of platoons of connected and automated vehicles at highway on-ramps. The problem is modeled as a job-shop scheduling problem, and an optimal scheduling algorithm is presented to derive the sequence and time for each platoon to enter the highway safely. An optimal control problem is also formulated to derive the optimal control input (acceleration/deceleration) in terms of fuel consumption of the platoons at the highway. Simulation results show that the proposed framework significantly reduces crossing time and fuel consumption of platoons at highway on-ramps. The paper contributes to the literature on scheduling theory-based control algorithms for optimizing vehicle coordination in various transportation scenarios.

Another study in [4] discusses a rule-based cooperative merging strategy for connected and automated vehicles at highway on-ramps. The authors derive a near-optimal merging sequence using a rule-based adjusting algorithm and an energy-efficient motion planning method. Simulation-based case studies are conducted to compare the effectiveness and robustness of their method with other control strategies. The proposed strategy consistently outperforms the

other methods in terms of throughput and delay under unbalanced vehicle arrival rates. The paper provides a comprehensive review of related works on cooperative merging and identifies the differences of their work from the existing works. Overall, the paper presents an efficient and safe method for coordinating two strings of vehicles at highway on-ramps.

Finally, the paper in [5] presents a game-based approach to optimize merging behavior for connected and automated vehicles. The proposed approach improves traffic flow and fuel economy while reducing collision risks. The main contributions of the study are the mixed-strategy Nash equilibrium of the complete information static game for Merging Sequence (MS) allocation, the varying-scale grid search algorithm to numerically search for acceptable parameters in the cost function of the bi-objective optimization problem, and the adoption of a modified quick-sort algorithm to find the Pareto front. The paper also applies Pontryagin's minimum principle to calculate the optimal control law for the bi-objective optimization problem.

Ramp metering is an important concept for traffic management strategy used on highways and freeway systems to regulate the flow of vehicles entering the mainline traffic from on-ramps. It involves the use of traffic signals or control devices at the on-ramps to control the rate at which vehicles merge onto the mainline.

The metrics used to evaluate the performance of the proposed approach are average travel time, number of cars crossing the merging zone and average vehicle speed.

Chapter 3

Methodology

3.1 Problem Formulation

3.1.1 Objective Function

Given m number of vehicles traveling on the main road in a platoon formation and r number of vehicles traveling on the ramp towards the merging point, The aim is to discover the optimal merging sequence between vehicles from the on-ramp and those already on the main highway that maximizes the total number of vehicles successfully merging from the ramp 3.1, while minimizing the overall delay for vehicles already on the main road eq:3.2, where r_1 is the number of vehicles that are left for the next merging decision.

$$f_1 = \frac{r - r_1}{r} \quad (3.1)$$

$$f_2 = \frac{-\sum_{i=1}^m t_i + \sum_{i=1}^m \frac{l_i}{v_{\min}}}{-\sum_{i=1}^m \frac{l_i}{v_{\max}} + \sum_{i=1}^m \frac{l_i}{v_{\min}}} \quad (3.2)$$

The final objective function is:

$$\max F = w_1 * f_1 + w_2 * f_2 \quad (3.3)$$

3.1.2 Constraints

The objective function in 3.3 is subject to the following constraints:

$$\begin{aligned}
 0 &\leq w_1 \leq 1 \\
 0 &\leq w_2 \leq 1 \\
 w_1 + w_2 &= 1 \\
 a_{\min} &\leq a_i \leq a_{\max} \quad \text{for } i = 1, 2, \dots, m \\
 a_{\min} &\leq a_j \leq a_{\max} \quad \text{for } j = 1, 2, \dots, r \\
 v_{\min} &\leq v_i \leq v_{\max} \quad \text{for } i = 1, 2, \dots, m \\
 v_{\min} &\leq v_j \leq v_{\max} \quad \text{for } j = 1, 2, \dots, r
 \end{aligned}$$

When a vehicle enters the control zone, all the data regarding the vehicle motion is transmitted to a central unit having all the data for all the vehicles inside the control zone. For the main road vehicles. once a vehicle enters the control zone, its initial acceleration is maintained constant until it reaches the decision point. The optimization problem is solved before the decision point is reached. After passing the decision point and the optimal sequence is obtained, Cooperative Adaptive Cruise Control (CACC) law 3.4 is applied to generate the trajectory for all vehicles in the solution on the array, when an on-ramp is scheduled to merge, the following vehicles in the sequence create a space for the vehicle to be merged in the future as the on-ramp vehicle is virtually moving with the main line vehicle until it merges at the merging point.

$$a_f = \alpha \cdot a_l + \beta \cdot (v_f - v_l) + \gamma \cdot (s - s_d) \quad (3.4)$$

where s_d is the distance between the following vehicle and the preceding vehicle.

3.1.3 Decision variable

The decision variable of this problem is the merging sequence between the on-ramp and main road vehicles, the sequence matrix represented in binary, where the main road cars are represented as 1, and the ramp cars will be represented as 0, an example of the solution array is shown in Fig.3.2.

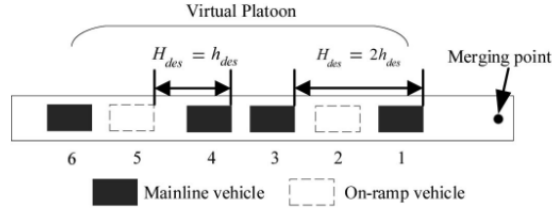


Figure 3.1: virtual platooning

	1	2	3	4	5	...	m-1	m
Mainline vehicles	1	1	1	1	1	...	1	1
	1	2	3	4	5	...	r-1	r
On-ramp vehicles	0	0	0	0	0	...	0	0
	1	2	3	4	5	...	m+r-1	m+r
Merging sequence	1	0	1	0	1	...	1	0

Figure 3.2: Solution Array

3.1.4 Assumptions

Several key assumptions are made to streamline the complexities of vehicle merging in a controlled environment. Firstly, the merging point of vehicles is assumed to be fixed upstream of the exit, ensuring a consistent location for merging. Lane-changing maneuvers are prohibited within the control zone, simplifying the scenario to include only the rightmost lane of the main road and a single lane on the on-ramp. Additionally, the focus is placed on longitudinal control of vehicles, disregarding lateral control, such as lane changes. The assumption of Cooperative Adaptive Cruise Control (CACC) vehicles, equipped with Vehicle-to-Vehicle (V2V) and Vehicle-to-Infrastructure (V2I) communication, enables the exchange of state information and real-time merging instructions. The merging process is divided into short time intervals, with constant acceleration assumed within each interval, facilitating the modeling and analysis of vehicle behavior. These assumptions collectively provide a controlled and predictable merging environment, essential for the development and optimization of cooperative merging strategies.

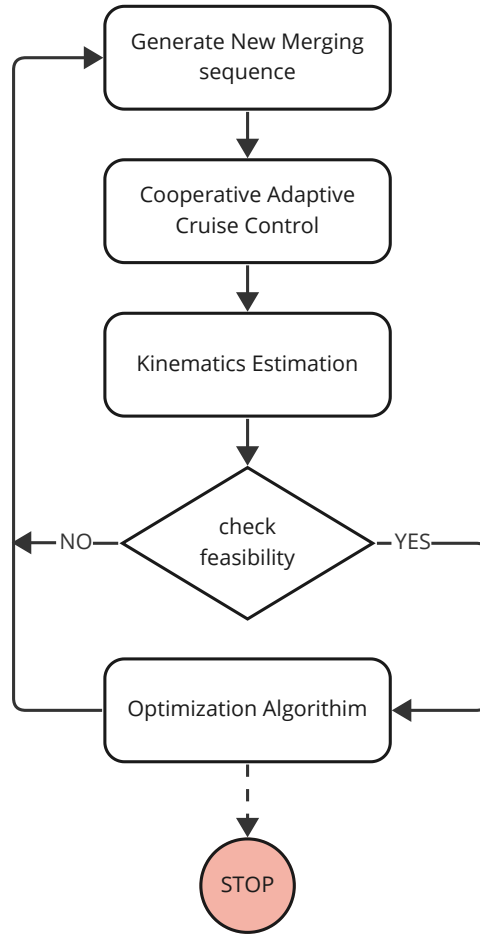


Figure 3.3: Proposed merging framework

3.2 Simulated annealing

Simulated Annealing (SA) is a heuristic optimization algorithm inspired by the annealing process in metallurgy, designed to find near-optimal solutions in complex search spaces. Starting with an initial solution, SA iteratively explores neighboring solutions, with its key feature being the ability to accept worse solutions with a decreasing probability as it cools down according to a predefined temperature schedule. This stochastic acceptance criterion allows the algorithm to escape local optima and converge towards global or near-optimal solutions. SA has been widely applied to various optimization problems, offering a versatile approach to challenges with intricate solution landscapes, making it a valuable tool for finding high-quality solutions in diverse domains, such as the traveling salesman problem, job scheduling, and parameter tuning in machine learning.

3.2.1 Procedure

1. Initialization: Begin with an initial solution to the optimization problem.
2. Temperature Initialization: Set an initial temperature parameter, which dictates the probability of accepting solutions with higher objective function values.
3. Iteration: Iterate through the following steps until a stopping criterion is met:
4. Generate Neighbor Solution: Generate a neighboring solution by perturbing the current solution, introducing randomness to the search process.
5. Objective Function Comparison: Compare the objective function values of the current and neighboring solutions.
6. Acceptance Probability: Calculate the probability of accepting the new solution based on the temperature and the difference in objective function values.
7. Update Solution: Accept the new solution with the calculated probability or, in some cases, with certainty if it improves the objective function value.
8. Temperature Update: Update the temperature according to a cooling schedule, gradually reducing it over iterations.
9. Stopping Criterion Check: Check whether a stopping criterion, such as a maximum number of iterations or a target temperature, has been reached.
10. Convergence: Conclude the algorithm when the stopping criterion is met, and the final solution is considered the optimized or near-optimal solution.

3.2.2 Pros and Cons

Simulated annealing (SA) possesses notable strengths in optimization. It excels in global searches, making it effective for problems with multiple solutions. SA is adaptable and can handle various problem types without relying on function differentiability. Furthermore, its ability to escape local optima enhances its efficacy. In terms of cons, SA doesn't guarantee optimality as it is a heuristic method that explores the solution space probabilistically. Parameter tuning is crucial, and suboptimal choices may impact performance. While SA is computationally less expensive than some alternatives, it may still face challenges with large-scale problems. Additionally, handling constraints in SA can be intricate, and its convergence rate might be slower compared to other optimization techniques. Despite these drawbacks, SA remains a versatile optimization tool with applications across diverse problem domains.

3.3 Genetic Algorithm (GA)

A genetic algorithm (GA) is a search heuristic inspired by the process of natural selection and genetics. It belongs to the broader class of evolutionary algorithms, which are optimization algorithms inspired by the principles of biological evolution. GAs are commonly used to find approximate solutions to optimization and search problems. Here's an overview of the key components and procedures of a genetic algorithm:

3.3.1 Procedure

1. **Initialization:** Generate a population of potential solutions (individuals or chromosomes). The solutions are typically represented as strings of parameters, where each parameter represents a potential solution to the problem.
2. **Fitness Evaluation:** Evaluate the fitness of each individual in the population. The fitness function quantifies how well an individual solves the problem at hand. The fitness function is problem-specific and defines the objective or goal of the optimization.
3. **Selection:** Select individuals from the current population to be parents based on their fitness. Individuals with higher fitness are more likely to be selected, mimicking the natural selection process.
4. **Crossover (Recombination):** Pair selected individuals and create new offspring by combining their genetic information. This is typically done by exchanging portions of the parents' chromosomes.
5. **Mutation:** Introduce random changes in the offspring's genetic information to maintain genetic diversity. Mutation helps explore new regions of the solution space.
6. **Replacement:** Replace the old population with the new population of parents and offspring.
7. **Termination:** Repeat the process for a certain number of generations or until a termination condition is met (e.g., reaching a satisfactory solution).

3.3.2 Pros and Cons

Genetic algorithms (GAs) offer several advantages, including their proficiency in conducting global searches across entire solution spaces, rendering them suitable for problems with multiple solutions. Their adaptability is evident in their capability to handle diverse problem types without relying on the differentiability of the objective function. Furthermore, GAs can exploit parallelism, allowing for the efficient utilization of parallel computing resources. However, GAs come with inherent limitations. They do not guarantee optimality, functioning as heuristic methods that may not always find the optimal solution. The performance of GAs is sensitive to

parameter choices, necessitating careful tuning for different problem instances. Additionally, GAs can incur computational costs, especially for intricate problems and large populations. Another challenge lies in their limited ability to handle constraints, with some genetic algorithms struggling in problems involving constraints, often requiring supplemental techniques for improved performance.

Chapter 4

Results

4.1 Initial Scenario

We implemented a code that initializes two lists of car objects one for the main road and one for the ramp cars, in order to use in the simulation of our algorithm, the car class takes values like seen in Tab.4.1.

Parameter	Value
random_pos_lower	5m
random_pos_upper	8m
cars_main_num	$rand(5, 10)$
cars_ramp_num	$rand(5, 20)$
solution_size	10
initial_main_p	$decision_position$
initial_ramp_p	$decision_position_random.randint(10, 30)$
initial_main_v	16.67m/s
initial_ramp_v	13.888m/s
initial_main_a	$3m/s^2$
initial_ramp_a	$0m/s^2$

Table 4.1: Parameters for Initializing Cars Info

Furthermore, we implemented a code that can generate different solutions, for each solution we need to check if it is feasible and follows the constraints or not, this check should be done at each time step the car spends in the acceleration zone, where our algorithm will be implemented in real life. We achieved that by implementing a cruise control algorithm for the generated car sequence, it evaluates the position and velocity and acceleration at each time step, the sampling period is referred as 'delta_time' in Tab.4.3. the constraints used is shown in 4.2, and the parameters for cruise control is shown in Tab.4.3.

Constraint	Minimum Value	Maximum Value
v_main	$2.777m/s$	$33.33m/s$
v_ramp	$1.388m/s$	$33.33m/s$
a_main	$-20m/s^2$	$20m/s$
a_ramp	$-20m/s^2$	$20m/s^2$

Table 4.2: Constraints

Parameter	Value
alpha	1
beta	1.2
gamma	0.5
desired_distance_bet_cars	6 m
decision_position	40 m
merging_position	140 m
delta_time	0.01 seconds

Table 4.3: Parameters for Cruise Control

4.1.1 Scalability and dynamic code

In our code, we can change the number of cars on the main road and the number of ramp cars, and we also can change the number of cars in the solution array, in addition, the initial positions of all cars are semi-random, where we generate a random number for the position added to the previous position of the previous cars.

You can change a lot of the parameters mentioned before and get new results.

4.2 Implementation of Simulated Annealing

We implemented this Python script to address the optimization of vehicle merging behavior on a highway ramp using a Simulated Annealing (SA) approach. The script begins by importing the necessary modules and setting critical constraints that define the problem, including speed and acceleration limits for both main and ramp vehicles.

To generate a suitable sequence of vehicles for merging, we implemented the 'generate_solution' function, which not only returns the sequence itself but also calculates distances to the merging point, aiding in the evaluation process. The 'check_feasibility' function is crucial for verifying that the generated solution complies with the predefined constraints.

The core of the optimization process lies in the Simulated Annealing (SA) loop, where we applied the SA algorithm iteratively. We fine-tuned parameters such as the initial temperature, cooling rate, number of iterations, and the final temperature. Each iteration involves initializ-

ing car configurations, generating new solutions, and conducting feasibility checks. The SA algorithm determines whether the new solution is accepted based on objective function values, temperature, and a probabilistic criterion. The best solution is consistently updated, and the optimization process concludes when the temperature reaches the specified final value or other defined stopping criteria are met.

Lastly, we incorporated a visualization component, plotting temperature against the objective function value, to provide a clear representation of the SA optimization process. In essence, we developed this script to take on the complex challenge of optimizing vehicle merging on a highway ramp, with the primary goal of achieving a safe, efficient, and constraint-compliant merging process while leveraging advanced optimization techniques.

4.2.1 Testing different cases

Case 1: Linear change in temperature After running the simulated Annealing algorithm, with the parameters in 4.1 we get the following:

last solution: [0, 1, 1, 1, 1, 1, 0, 0, 0, 0]

last Objective function value (rounded): 0.949

Best solution : [0, 1, 1, 1, 1, 1, 0, 0, 0, 0]

Best Objective function value (rounded): 0.949.

The development of best solution of the SA algorithm versus temperature is shown in Fig.4.2.

The Objective function value is relatively high, Note that in our problem we want to maximize the total objective function and we have normalized the objective function so its highest value is 1.

Parameter	Value
initial_temperature	1000.0
cooling_rate	5
num_iterations	1000
final_temperature	0.05
w_1	0.5
linear	True

Figure 4.1: Simulated Annealing Parameters

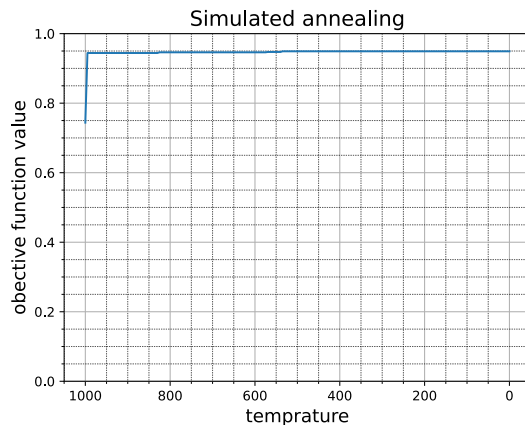


Figure 4.2: Objective function value vs temperature.

Case 2: Geometric change in temperature After running the simulated Annealing algorithm, with the parameters in 4.3 we get the following:

last solution: [0, 0, 1, 1, 0, 1, 1, 0, 0, 1]

last Objective function value (rounded): 0.942

Best solution : [1, 0, 0, 1, 0, 1, 0, 1, 0, 1]

Best Objective function value: 0.944.

The development of best solution of the SA algorithm versus temperature is shown in Fig.4.4.

Parameter	Value
initial_temperature	1000.0
cooling_rate	0.8
num_iterations	1000
final_temperature	0.05
w_1	0.2
linear	False

Figure 4.3: Simulated Annealing Parameters

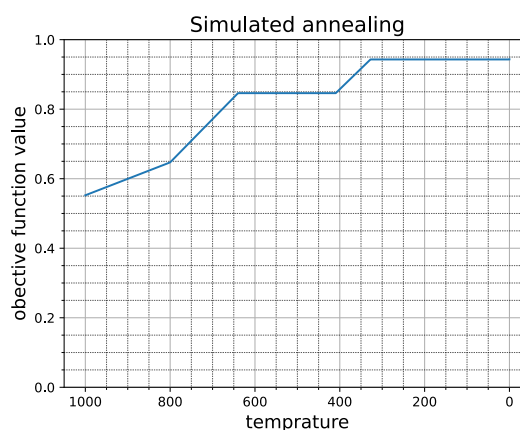


Figure 4.4: Objective function value vs temperature with simulated annealing.

Case 3: After running the simulated Annealing algorithm, with the parameters in 4.5 we get the following:

last solution: [0, 0, 1, 1, 0, 1, 1, 1, 0, 0]

last Objective function value (rounded): 0.936

Best solution : [1, 1, 1, 0, 1, 1, 0, 0, 0, 0]

Best Objective function value (rounded): 0.954.

The development of best solution of the SA algorithm versus temperature is shown in Fig.4.6.

For this case, we notice that in this solution, all the cars on the ramp are added later so in the next algorithms this will be taken into consideration and a penalty will be applied.

Parameter	Value
initial_temperature	500.0
cooling_rate	0.5
num_iterations	1000
final_temperature	0.05
w_1	0.5
linear	True

Figure 4.5: Simulated Annealing Parameters

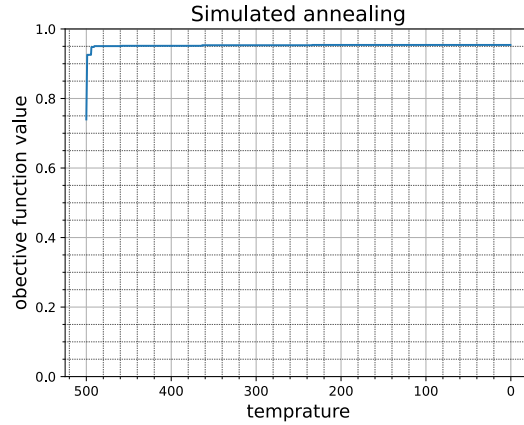


Figure 4.6: Objective function value vs temperature with simulated annealing.

4.3 Implementation of Genetic algorithm

The implemented genetic algorithm functions are designed to address a combinatorial optimization problem associated with car sequencing. The primary genetic algorithm function serves as the orchestrator, guiding the evolution of potential solutions through a series of steps. This includes the initialization of a population with feasible solutions, iterative application of selection, crossover, and mutation operations, and the continual tracking of the best solution throughout generations. The incorporation of elitism ensures that the most promising individuals persist across iterations, contributing to the overall efficiency of the algorithm.

Supporting functions play crucial roles in this optimization process. The initialization function generates an initial population, emphasizing the importance of feasibility by incorporating checks to ensure that only valid solutions are considered. The fitness calculation function assesses the performance of each individual in the population based on a specified fitness function. Crossover and mutation functions handle the creation of new offspring and the introduction of random changes, respectively. Notably, the code demonstrates a keen awareness of the feasibility of solutions, underscoring the significance of valid solutions in the evolutionary process, the process of (GA) is illustrated in Fig.4.7.

Overall, the success of the genetic algorithm hinges on the effective collaboration of these functions, each tailored to address specific facets of the car sequencing problem. The algorithm's strength lies in its ability to balance exploration and exploitation through selection mechanisms, while the supporting functions contribute to the diversity and quality of the evolving population, ultimately working towards finding optimal or near-optimal solutions.

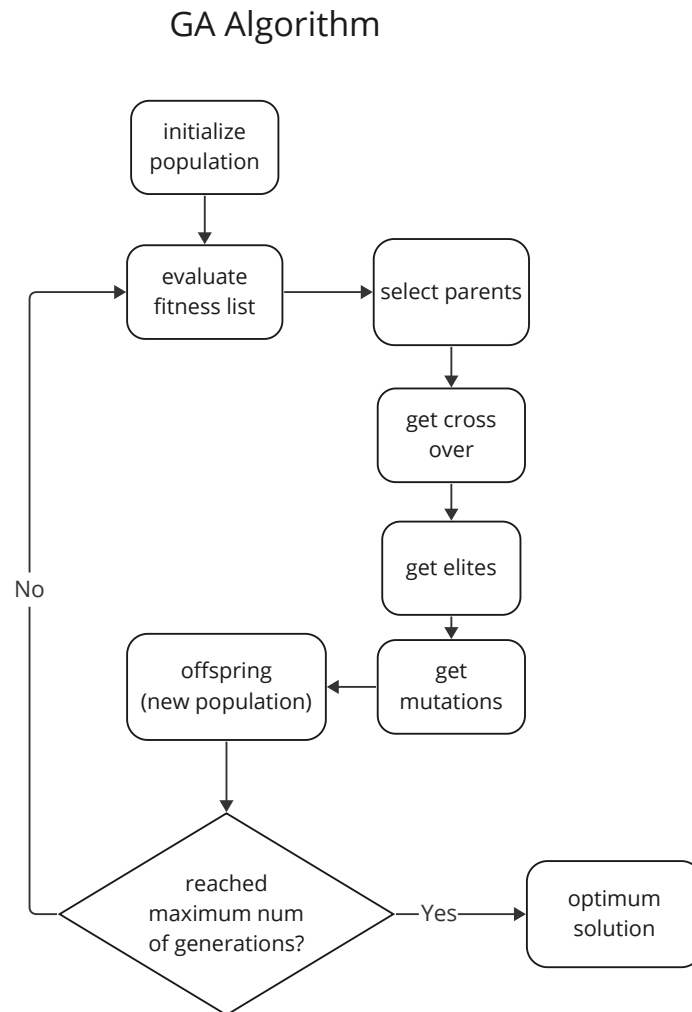


Figure 4.7: Flow of the Genetic algorithm

4.3.1 Values to Change for Different Cases

1. **Population Size:** The number of individuals in each generation. Larger populations may enhance exploration but also increase computation time.
2. **Crossover Rate:** The probability that crossover will be applied to a pair of individuals. Controls the balance between exploration and exploitation.
3. **Mutation Rate:** The probability that a gene in an individual will be mutated. Regulates the exploration of the solution space.

4.3.2 Testing different cases

Case 1: High elites ratio The algorithm is tested with the parameters in Tab.4.8, and the following were obtained:

Best GA solution: $[0, 0, 1, 0, 0, 0, 0, 0, 0, 0]$

Best GA fitness (rounded): 0.888

The best solution over generations is shown in Fig.4.9.

Parameter	Value
population_size	10
generation_size	100
elites_ratio	0.7
crossover_ratio	0.2
mutation_ratio	0.1
w_1	0.2

Figure 4.8: Genetic Algorithm parameters

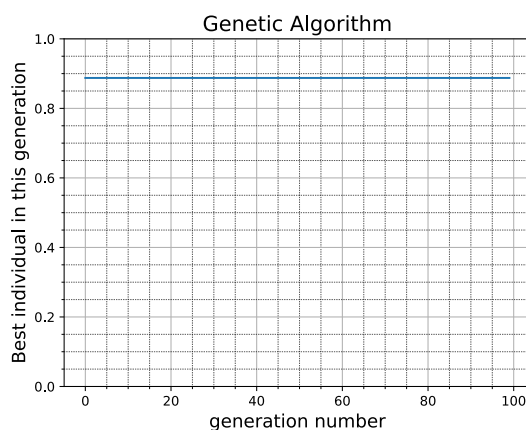


Figure 4.9: Best chromosome vs generation.

Case 2: High cross-over ratio The algorithm is tested with the parameters in Tab.4.10, and the following were obtained:

Best GA solution: $[0, 1, 0, 0, 0, 0, 0, 0, 0, 0]$

Best GA fitness (rounded): 0.908

The best solution over generations is shown in Fig.4.11.

Parameter	Value
population_size	10
generation_size	100
elites_ratio	0.1
crossover_ratio	0.8
mutation_ratio	0.1
w_1	0.2

Figure 4.10: Genetic Algorithm parameters

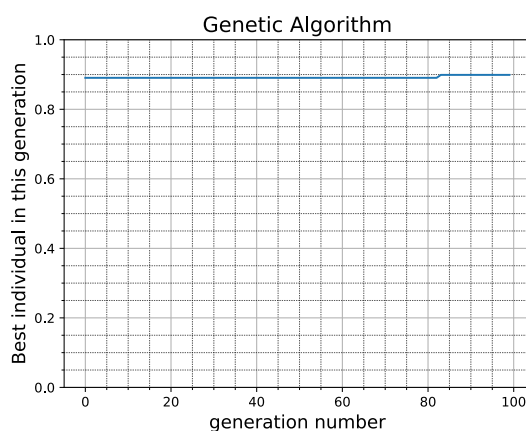


Figure 4.11: Best chromosome vs generation.

Case 3: High mutation ratio The algorithm is tested with the parameters in Tab.4.10, and the following were obtained:

Best GA solution: [0, 1, 0, 0, 0, 0, 0, 0, 0]

Best GA fitness (rounded): 0.910

The best solution over generations is shown in Fig.4.11.

Parameter	Value
population_size	10
generation_size	100
elites_ratio	0.1
crossover_ratio	0.4
mutation_ratio	0.5
w_1	0.2

Figure 4.12: Genetic Algorithm parameters

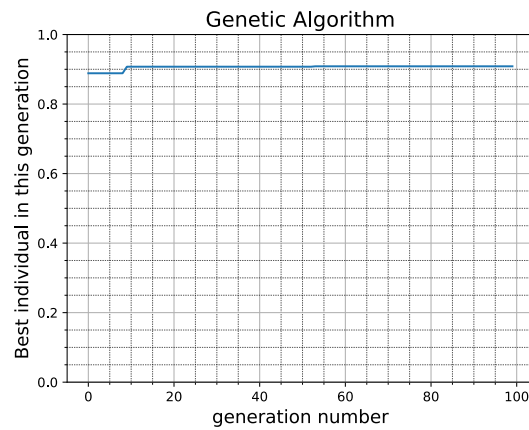


Figure 4.13: Best chromosome vs generation.

4.4 Comparison between optimization algorithms

Comparing two optimization algorithms involves assessing their performance based on various criteria. it's often a good idea to perform multiple experiments on a diverse set of test problems to get a comprehensive understanding of their strengths and weaknesses.

4.4.1 SA and GA

The simulated annealing and genetic algorithm are compared with the same initial scenario which has the same parameters as mentioned in 4.1 but with $w_1 = 0.2$ and parameters in 4.2 and in 4.3 as well. SA and GA will be compared in Tab.4.4, according to the chosen criteria, the values obtained in Tab.4.4 are averaged over 100 runs, while the (GA) showed different solution in each run, the (SA) algorithm almost reached the same exact solution in each run.

Criteria / Algorithm	SA	GA
Best solution fitness (normalized)	0.911	0.907
Average execution time (seconds)	6.96	28.61

Table 4.4: Comparison between SA and GA

It is concluded that for the presented problem, the performance of the SA is better overall.

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