# CSE 410: Assignment 2 (Jan 2022) Raster Based Graphics Pipeline

#### Overview:

In this assignment, you will develop the raster based graphics pipeline used in OpenGL. The pipeline can be thought of as a series of six stages. You will implement roughly 4 stages of the pipeline.

- 1. Stage 1: modeling transformation
- 2. Stage 2: view transformation
- 3. Stage 3: projection transformation
- 4. Stage 4: clipping & scan conversion using Z-buffer algorithm

Your program will output five files: stage1.txt, stage2.txt, stage3.txt and z-buffer.txt, out.bmp. The first three files will contain the output of the first three stages, respectively. The fourth file will contain Z-buffer values (only those which are less than the max value). And the fifth file will be a bmp image generated by the pipeline.

Three will be two input files: scene.txt and config.txt

The first file will contain the scene description and second file will contain the necessary information for the Z-buffer algorithm.

## Scene description:

You will be given a text file named "scene.txt". This will contain the following lines:

Line 1: eyeX eyeY eyeZ Line 2: lookX lookY lookZ Line 3: upX upY upZ Line 4: fovY aspectRatio near far

Lines 1-3 of scene.txt state the parameters of the <code>gluLookAt</code> function and Line 4 provides the <code>gluPerspective</code> parameters.

The display code contains 7 commands as follows:

1. triangle command – this command is followed by three lines specifying the coordinates of the three points of the triangle to be drawn. The points being p1, p2, and p3, 9 double values, i.e., p1.x, p1.y, p1.z, p2.x, p2.y, p2.z, p3.x, p3.y, and p3.z indicate the coordinates.

This is equivalent to the following in OpenGL code.

```
glBegin(GL_TRIANGLE);{
          glVertex3f(p1.x, p1.y, p1.z);
          glVertex3f(p2.x, p2.y, p2.z);
          glVertex3f(p3.x, p3.y, p3.z);
}glEnd();
```

- 2.  $\frac{\text{translate command}}{\text{translation command is followed by 3 double values } (tx, ty, and tz) in the next line indicating translation amounts along X, Y, and Z axes. This is equivalent to <math>\frac{1}{2} \text{glTranslatef}(tx, ty, tz)$  in OpenGL.
- 3. scale command this command is followed by 3 double values (sx, sy, and sz) in the next line indicating scaling factors along X, Y, and Z axes. This is equivalent to glScalef(sx, sy, sz) in OpenGL.
- 4. rotate command this command is followed by 4 double values in the next line indicating the rotation angle in degree (angle) and the components of the vector defining the axis of rotation (ax, ay, and az). This is equivalent to glRotatef (angle, ax, ay, az) in OpenGL.
- 5. push command This is equivalent to glPushMatrix in OpenGL.
- 6. pop command This is equivalent to glPopMatrix in OpenGL.
- 7. end command This indicates the end of the display code.

In this assignment, you will generate the output of the first three stages of the raster based graphics pipeline according to the scene description provided in the scene.txt file. The output of the stages should be put in stage1.txt, stage2.txt, and stage3.txt file. The input of the fourth stage will be stage3.txt and config.txt and the corresponding output should be put in z-buffer.txt and out.bmp (elaborated later).

Please check the scene.txt carefully to have a more comfortable understanding of the input.

## Stage 1: Modeling Transformation

In the Modeling transformation phase, the display code in scene.txt is parsed, the transformed positions of the points that follow each triangle command are determined, and the transformed coordinates of the points are written in stage1.txt file. We maintain a stack S of transformation matrices which is manipulated according to the commands given in the display code. Consider that the display code contains the following commands.

Triangle
Translate
Triangle
Rotate
Scale
Triangle
Rotate
Triangle
Triangle

The pseudo-code for the modeling transformation phase is as follows:

```
initialize empty stack S
S.push(identity matrix)
while true
     input command
     if command = "triangle"
           input three points
           for each three point P
                P' <- transformPoint(S.top,P)
                output P'
     else if command = "translate"
           input translation amounts
           generate the corresponding translation matrix T
           S.push(product(S.top,T))
     else if command = "scale"
           //do it yourself
     else if command = "rotate"
           //do it yourself
     else if command = "push"
           //do it yourself
      else if command =
                  "pop"
      //do it yourself
     else if command =
                  "end"
           break
```

#### **Transformation matrix for Translation**

```
translate
tx ty tz
```

The transformation matrix for the above translation is as follows:

```
1 0 0 tx
0 1 0 ty
0 0 1 tz
0 0 0 1
```

#### **Transformation matrix for Scaling**

```
scale
sx sy sz
```

The transformation matrix for the above scaling is as follows:

#### **Transformation matrix for Rotation**

Remember that the columns of the rotation matrix indicate where the unit vectors along the principal axes (namely, i, j, and k) are transformed. We will use the vector form of Rodrigues formula to determine where i, j, and k are transformed and use those to generate the rotation matrix. The vector form of Rodrigues formula is as follows:

$$R(\vec{x}) = \cos\theta \vec{x} + (1 - \cos\theta)(\vec{a} \cdot \vec{x})\vec{a} + \sin\theta(\vec{a} \times \vec{x})$$

In the above formula,  $\underline{\mathbf{x}}$  is a unit vector defining the axis of rotation,  $\theta$  is the angle of rotation, and  $\underline{\mathbf{a}}$  is the vector to be rotated.

Now we outline the process of generating transformation matrix for the following rotation:

```
rotate
angle ax ay az

We denote the vector (ax, ay, az) by a. The steps to generate the rotation matrix are as follows:
a.normalize()
c1=R(i,a,angle)
c2=R(j,a,angle)
c3=R(k,a,angle)
```

The corresponding rotation matrix is given below:

#### **Managing Push and Pop**

The following table demonstrates how <code>push</code> and <code>pop</code> works. The state of the transformation matrix stack after execution of each line of the code in the left is shown in the right. Design a data structure that manages <code>push</code> and <code>pop</code> operations on the transformation matrix stack accordingly.

|                          | Stack State after Lines |   |                |    |                |                |                |                |                |                |             |    |
|--------------------------|-------------------------|---|----------------|----|----------------|----------------|----------------|----------------|----------------|----------------|-------------|----|
| Code                     | 0                       | 1 | 2              | 3  | 4              | 5              | 6              | 7              | 8              | 9              | 10          | 11 |
| 1.Push                   |                         |   |                |    |                |                |                |                |                |                |             |    |
| 2.Translate <sub>1</sub> |                         |   |                |    |                |                |                |                |                |                |             |    |
| 3.Push                   |                         |   |                |    |                |                |                |                |                |                |             |    |
| 4.Rotate <sub>1</sub>    |                         |   |                |    |                |                |                |                |                |                |             |    |
| 5.Pop                    |                         |   |                |    |                |                |                |                |                |                |             |    |
| 6.Scale <sub>1</sub>     |                         |   |                |    |                |                |                |                |                |                |             |    |
| 7.Push                   |                         |   |                |    |                |                |                |                |                |                |             |    |
| 8.Rotate <sub>2</sub>    |                         |   |                |    |                |                |                |                | $T_1S_1R_2$    |                | $T_1S_1S_2$ |    |
| 9.Pop                    |                         |   |                |    | T1R1           |                | T1S1           | T1S1           | T1S1           | T1S1           | T1S1        |    |
| 10.Scale <sub>2</sub>    |                         |   | T <sub>1</sub> | Т1 | T <sub>1</sub> | T <sub>1</sub> | T <sub>1</sub> | T <sub>1</sub> | $\mathtt{T}_1$ | T <sub>1</sub> | $T_1$       |    |
| 11.Pop                   | I                       | I | I              | I  | I              | I              | I              | I              | I              | I              | I           | I  |

## Stage 2: View Transformation

In the view transformation phase, the gluLookAt parameters in scene.txt is used to generate the view transformation matrix V, and the points in stage1.txt are transformed by V and written in stage2.txt. The process of generating V is given below.

First determine mutually perpendicular unit vectors 1, r, and u from the gluLookAt parameters.

```
l = look - eye
l.normalize()
r = l X up
r.normalize()
u = r X l
```

Apply the following translation T to move the eye/camera to origin.

Apply the following rotation R such that the 1 aligns with the -Z axis, r with X axis, and u with Y axis. Remember that, the rows of the rotation matrix contain the unit vectors that align with the unit vectors along the principal axes after transformation.

Thus the view transformation matrix V = RT.

## Stage 3: Projection Transformation

In the projection transformation phase, the gluPerspective parameters in scene.txt are used to generate the projection transformation matrix P, and the points in stage2.txt are transformed by P and written in stage3.txt. The process of generating P is as follows:

First compute the field of view along the X (fovX) axis and determine r and t.

```
fovX = fovY * aspectRatio
t = near * tan(fovY/2)
r = near * tan(fovX/2)
```

The projection matrix *P* is given below:

Refer to [1] for understanding the 3<sup>rd</sup> row of the above projection matrix. Image source: [2].

## Stage 4: Clipping & scan conversion using Z-buffer algorithm

In this stage, you have to implement a very simple Hidden Surface Removal algorithm for the objects within a bounding box. You have to work with triangles only, as specified in scene.txt. The output generated by your program after the third stage, stage3.txt and the given input file config.txt will work as the input for this stage. However, during implementation it is recommended to test with smaller cases so that you can debug easily.

## Config description:

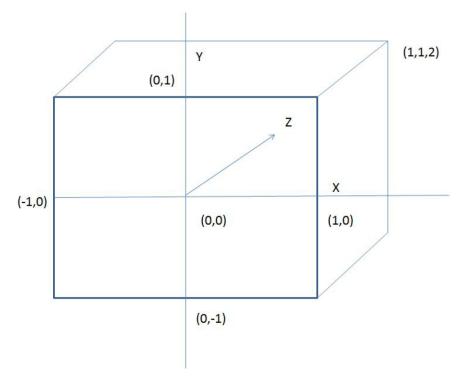
- 1. The first Line of file contains two integers, representing Screen\_Width and Screen\_Height respectively.
- 2. The second line contains a -ve number which specifies the left limit of X. You can get the right limit of X by negating this value.
- 3. The third line contains a -ve number which specifies the bottom limit of Y. You can get the top limit of Y by negating this value.
- 4. The fourth line contains two real numbers denoting front and rear limits of Z respectively.
- 5. Example:

500 -1.00

-1.00

0.00 2.00

6. Visual representation of the configuration according to the aforementioned example:



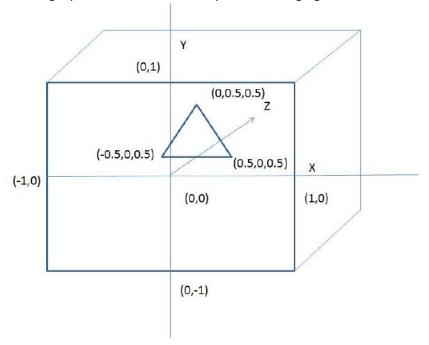
Your only viewing volume is bounded by the box shown above.

## Stage 3 description:

The stage3.txt file generated by your program will contain each triangle information as three lines specifying the coordinates of the three points of the triangle. Suppose, the there is only one triangle and the file contains the following:

```
0.50 0.00 0.50 
-0.50 0.00 0.50 
0.00 0.50 0.50
```

The triangle position can be shown by the following figure within the viewing volume.



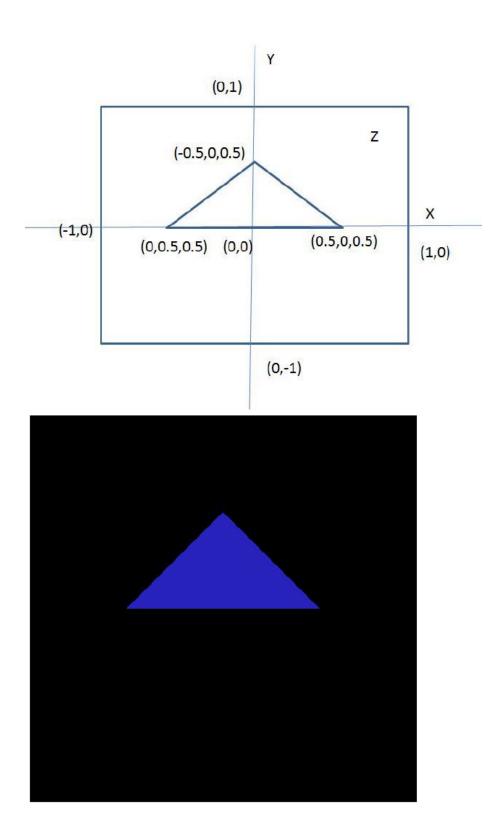
## Tasks:

- 1. Clip everything outside the viewing volume.
- 2. Considering yourself as a parallel viewer from the XY-plane, generate the image (dimension: Screen\_Width X Screen\_Height) that can be seen on the XY plane after computing the necessary clipping and depth information of objects (triangles) within this viewing volume.
- 3. Print Z-buffer values into a file named z-buffer.txt. (only those values where z\_buffer[row][col] < z\_max).

## Output:

The output from the viewing plane for the aforementioned configuration and triangle is shown by the following figures (the first one is for your understanding and the second one is the actual output).

<sup>\*</sup>Check "Procedures" for more details and further instructions.



You should save the output image in a file named out.bmp, and the Z-buffer values in a text file named z-buffer.txt.

## Another Sample:

Suppose. stage3.txt contains the following while the config.txt is the same as before.

1.5 0 0.5

-0.5 0 0.5

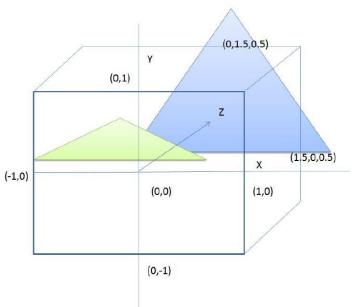
0 1.5 0.5

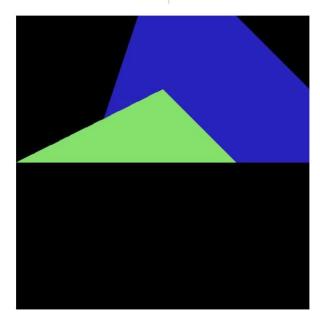
0.5 0 0.25

-1.0 0 0.25

0 0.5 0.25

In this case, the output will be as follows.





### Procedure:

The aforementioned tasks can be divided into the following sub-tasks inside your main function.

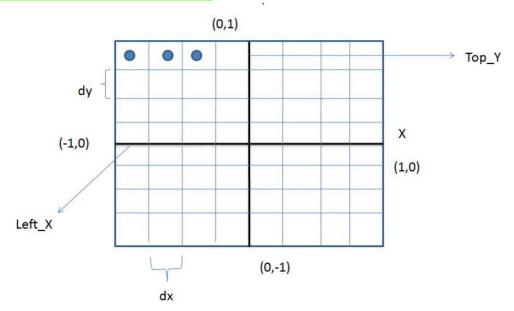
- 1. Read data
- 2. Initialize Z-buffer and Frame buffer
- 3. Apply procedure
- 4. Save
- 5. Free memory

The description of each of these sub-tasks is as follows.

- 1. Read data
  - a. Read the config.txt file and store the values as Screen\_Width, Screen\_Height, limits along the X, Y, Z axes accordingly.
  - b. Read input information from the stage3.txt file. This file should contain each triangle information in three consecutive lines where each line contains three coordinate values x, y, z as real numbers.
  - c. Use a suitable data structure to hold this information. Also associate a random color value (R, G, B) with each object (no need to worry about the seed). RGB values are bounded by 0-255.
  - d. An example of a triangle object data structure can be as follows.

```
Triangle{
    Point points[3];
    Color colors[3]; // Color can be primitive/user-defined
}
```

- e. Print and check whether you have correctly read the information from the files (for debugging purposes).
- 2. Initialize Z-buffer and Frame buffer.



a. Create a pixel mapping between the x-y range values and the Screen\_Width X Screen\_Height range.

dx = (right limit - left limit along X-axis) / Screen\_Width
dy = (top limit - bottom limit along Y-axis) / Screen\_Height

Besides, specify Top\_Y and Left\_X values.

Top\_Y = top limit along Y-axis - dy/2Left X = left limit along X-axis + dx/2

- b. During scanning from top to bottom and left to right, check for the middle values of each cell. e.g. Top Y-row no\*dy, Left X+col no\*dx
- c. Create a Z-buffer, a two dimensional array of Screen\_Width X Screen\_Height dimension. Initialize all the values in Z-buffer with z\_max. In the aforementioned examples, z\_max = 2.0. The memory for Z-buffer should be dynamically allocated (using STL is allowed).
- d. Create a bitmap\_image object with Screen\_Width X Screen\_Height resolution and initialize its background color with black. You can follow the image\_drawing.cpp code sample for checking how to utilize the image library.

#### 3. Apply procedure

a. Pseudocode:

for each object : Triangles

Find top\_scanline and bottom\_scanline after necessary clipping

for row\_no from top\_scanline to bottom\_scanline

Find left\_intersecting\_column and right\_intersecting\_column after necessary clipping

for col no from left intersecting column to right intersecting column

Calculate z values

Compare with Z-buffer and z\_front\_limit and update if required Update pixel information if required

end

end

end

\* Note that you should not update a Z-buffer value if the point's z-coordinate < z\_front\_limit (invisible to the observer, but ignore its occlusion impact).

#### b. Clipping:

- i. Compute the max\_y for each triangle. If max\_y > Top\_Y, clip (i.e. ignore) the portion above Top\_Y and start scanning from Top\_Y. Otherwise find the suitable mapping of max\_y to a top\_scanline below Top\_Y. Do a similar checking for min\_y and Bottom\_Y.
- ii. Compute min\_x for each scan line for each triangle. If min\_x < Left\_X, clip (i.e. ignore) the portion to the left of Left\_X. Otherwise find the suitable mapping of min\_x to a column to the right of Left\_X (left\_intersecting\_column). Do a similar checking for max\_x and Right\_X

- 4. Save
  - a. Save the image as output.bmp
  - b. Save the Z-buffer values in <code>z\_buffer.txt</code>. Save only those values which are less than <code>z\_max</code> i.e. for each row and col, <code>z\_buffer[row][col] < z\_max</code>.

Check the sample output files for a better understanding.

- 5. Free memory
  - a. Free image memory
  - b. Free Z-buffer and Frame buffer memory

#### Do's and Dont's

- 1. Use homogeneous coordinates. The points should be represented by 4\*1 matrices and transformations by 4\*4 matrices.
- 2. While transforming a homogeneous point by multiplying it with a transformation matrix, don't forget to scale the resultant point such that the *w* coordinate of the point becomes 1.
- 3. Do not use the matrix form of Rodrigues formula directly to generate the rotation matrix. Use the procedure shown above that uses the vector form of Rodrigues formula.
- 4. Do not specify gluLookAt parameters in scene.txt such that the looking direction, i.e., look-eye, becomes parallel to the up direction.
- 5. Make sure that the model is situated entirely in front of the near plane.

#### Reference

- [1] http://www.songho.ca/opengl/gl\_projectionmatrix.html
- [2] http://www.opengl-tutorial.org/beginners-tutorials/tutorial-3-matrices/