

#### You

Explain how ChatGPT works as if I was a 5 years old child.



#### **ChatGPT**

Alright, imagine you have a really smart friend who knows a lot of things. That friend is like a big, magical library with lots and lots of books. Now, this friend is called ChatGPT. When you ask ChatGPT a question or tell it something, it looks into all those books in its library (which are actually a huge amount of information it learned) and tries to give you the best answer or response it can find.

So, you can think of ChatGPT as a helpful buddy who loves to chat and share what it knows with you!



#### How does it really work?

# What is Language Modeling?

#### **Definition**

- A sequence of tokens  $(w_1, w_2, \ldots, w_n)$
- ullet For a position i, a language model (LM) predicts

$$P(w_i \mid (w_j)_{j 
eq i}) \in \Delta^V$$

• In words: a LM predicts the probability of a token given its context

### **Example**

I went to the ??? yesterday

P(park | I went to the ??? yesterday) = 0.1

P(zoo | I went to the ??? yesterday) = 0.07

• • •

P(under | I went to the ??? yesterday) = 0

### Why is it hard?

- Large vocabularies: 170,000 English words
- Lots of possible contexts:
  - $\circ$  For V possible tokens, there are  $V^L$  contexts of size L (in theory)
- Inherent uncertainty: not obvious even for humans

#### **Basic approach - Unigram**

• Learn the *non-contextual* probability (=frequency) of each token:

$$P(w_i \mid (w_j)_{j 
eq i}) = f$$

#### **Example**

chart against operations at influence the surface plays crown a inaro the three @ but the court lewis on hand american of seamen mu role due roger executives

### **Include context - Bigram**

Predict based on the last token only:

$$P(w_i \mid (w_j)_{j 
eq i}) = P_{ heta}(w_i \mid w_{i-1})$$

• (MLE): Measure next token frequency

#### **Example**

the antiquamen lost to dios nominated former is carved stone oak were problematic, 1910. his willingness to receive this may have been seen anything

### Include more context - n-gram

• Predict based on the *n* last tokens only:

$$P(w_i \mid (w_j)_{j 
eq i}) = P_{ heta}(w_i \mid w_{i-n} \dots w_{i-1})$$

• (MLE): Measure occurrences of tokens after  $w_{i-n} \dots w_{i-1}$ 

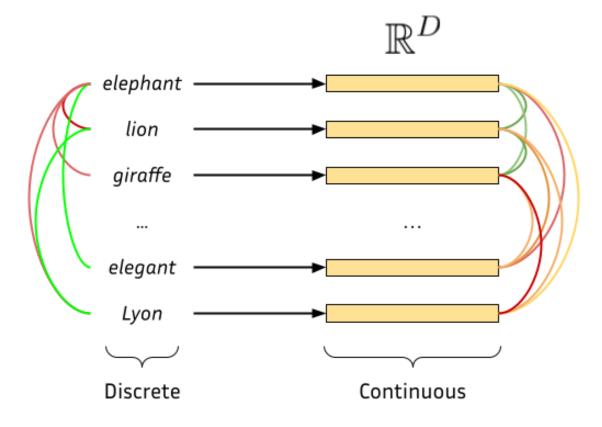
#### Example (n=4)

eva gauthier performed large amounts of contemporary french music across the united states marshals service traveled to frankfurt, germany and took custody of the matthews

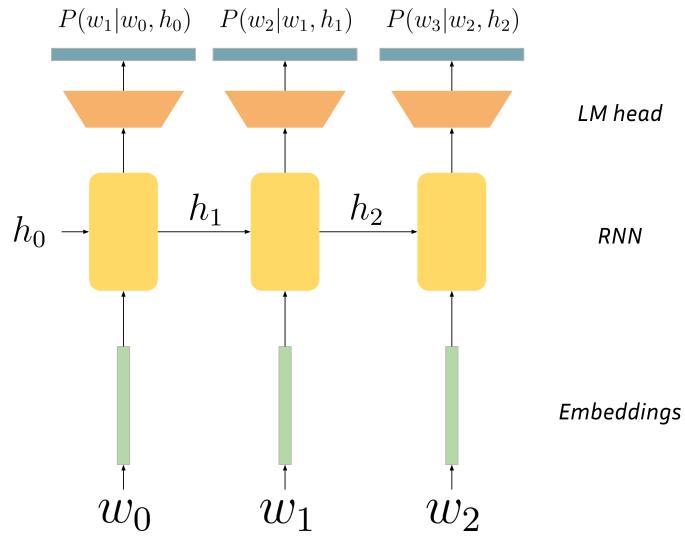
### Statistical n-grams: pro/cons

- Strenghts:
  - Easy to train
  - Easy to interpret
  - Fast inference
- Limitations:
  - Very limited context
  - Unable to extrapolate: can only model what it has seen

## The embedding paradigm



#### **LM with RNNs**



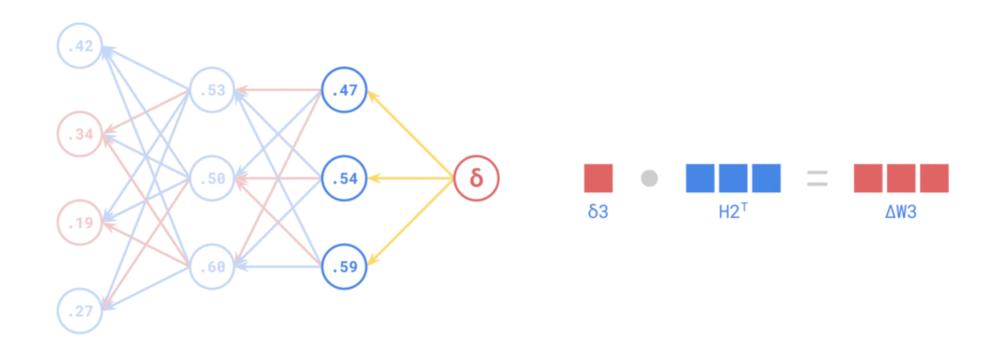
### **LM with RNNs - Training**

- $\theta$ : parameters of the RNN
- $(w_1,\ldots,w_n)$ : training sequence
- Cross-entropy loss  $\mathcal{L}_{ce}$ :

$$\mathcal{L}_{ce}(w, heta) = -\sum_{i=2}^n \mathbb{1}_{w_i} \cdot \log P_{ heta}(w_i|w_{i-1},h_{i-1})$$

Train via back-propagation + SGD

### **Reminder - Back-propagation**



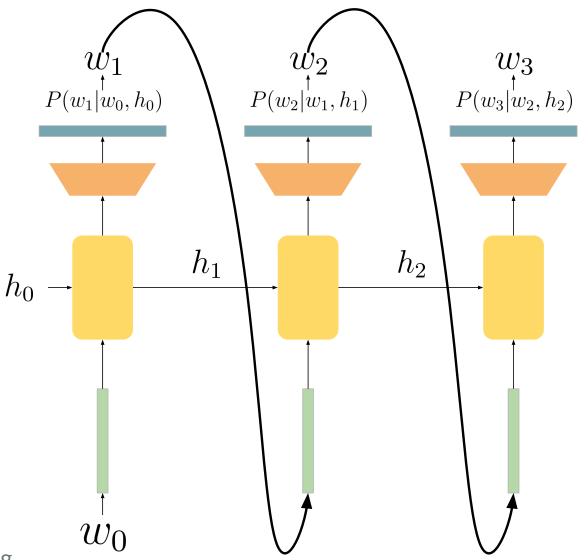
#### Reminder - Stochastic Gradient Descent

• Goal : Minimize a loss function  $\mathcal{L}(X,\theta)$  for given data X with respect to model parameters  $\theta$ 

#### Method:

- $\circ$  Split X in smaller parts  $x^i$  (called mini-batches)
- $\circ$  Compute  $\mathcal{L}(x^i, heta)$  (forward) and  $abla_{ heta} \mathcal{L}(x^i, heta)$  (back-prop)
- $\circ$  Update:  $heta \leftarrow heta \eta 
  abla_{ heta} \mathcal{L}(x^i, heta)$  ( $\eta \ll 1$ , learning rate)

#### LM with RNNs: Generation

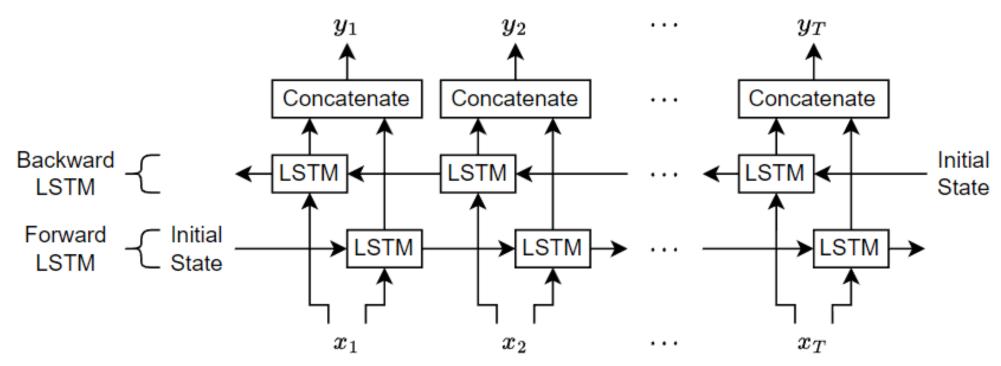


### RNNs: pro/cons

- Strenghts
  - Still relatively fast to train
  - $\circ$  ... and for inference (O(L))
  - Can extrapolate (works with continuous features)
- Limitations
  - Context dilution when information is far away

### **Extending RNNs: BiLSTMs**

- LSTM: improves context capacity
- Read the sequence in both directions



## **Transformers**

#### **Information flow - RNN**

How many steps between source of info and current position?

- What is the previous word? => O(L)
- What is the subject of verb X? => O(L)
- What are the other occurrences of current word? =>  $O(L^2)$

•

#### **Information flow - Transformers**

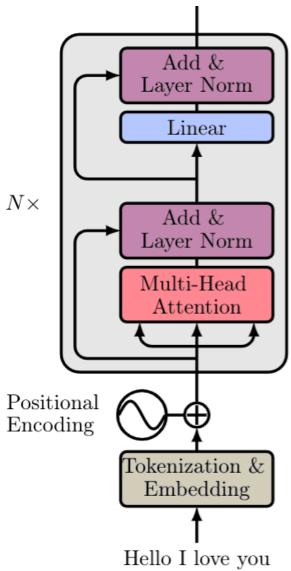
How many steps between source of info and current position?

- What is the previous word? => O(1)
- What is the subject of verb X? => O(1)
- What are the other occurrences of current word? => O(1)
- ... => O(1)

#### **Outside Transformers**

- ullet A Transformer network  $T_{ heta}$
- ullet Input: Sequence of vectors  $(e_1,\ldots,e_n)\in\mathbb{R}^D$
- ullet Output: Sequence of vectors  $(h_1,\ldots,h_n)\in\mathbb{R}^D$
- Each  $h_i$  may depend on the whole input sequence  $(e_1, \ldots, e_n)$

#### **Inside Transformers**



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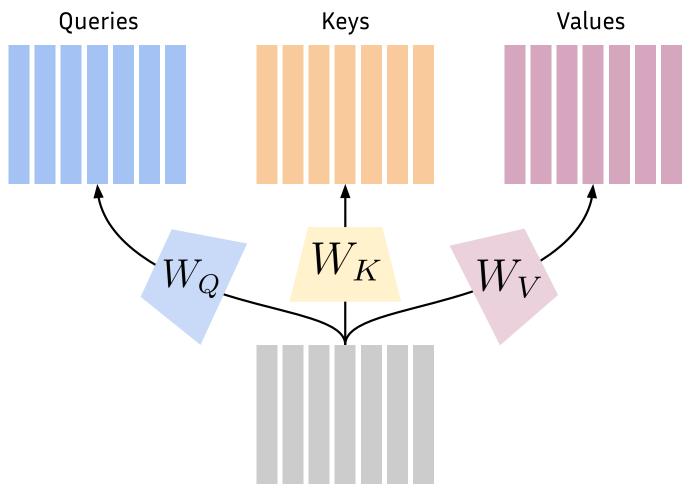
### **Inside Transformers: Embeddings**

Before going in the network:

- Given an input token sequence  $(w_1,\ldots,w_n)$
- ullet We retrieve token embeddings  $(e_w(w_1),\ldots,e_w(w_n))\in\mathbb{R}^D$
- ullet We retrieve position embeddings  $(e_p(1),\ldots,e_p(n))\in\mathbb{R}^D$
- ullet We compute input embeddings:  $e_i = e_w(w_i) + e_p(i)$

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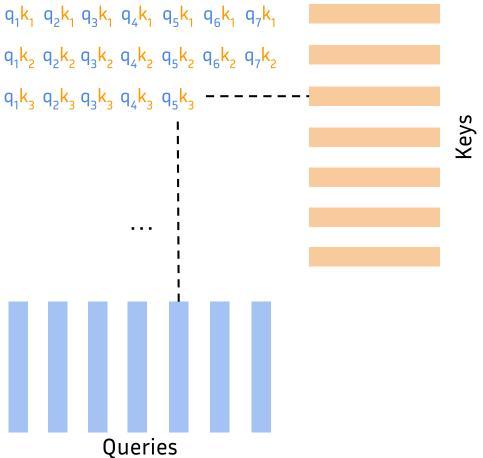
#### **Inside Transformers: Self-attention**



Inputs

### **Inside Transformers: Q and K**

=> Model interactions between tokens:

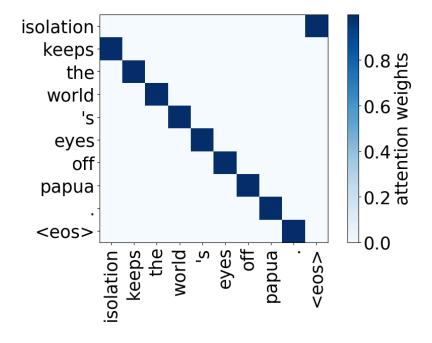


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### **Inside Transformers: Q and K**

- ullet Each row of  $QK^T$  is then normalized using softmax
- Interpretable patterns:



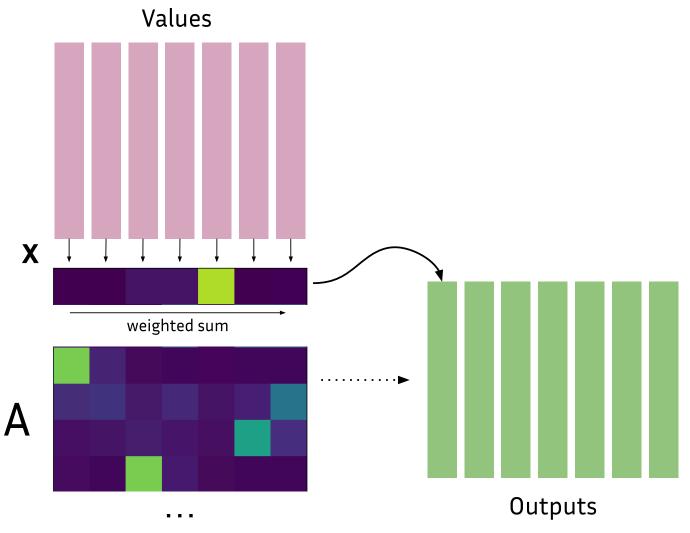
#### **Inside Transformers: Q and K**

• Formally:

$$A_{i,j} = rac{1}{\sqrt{d_h}} \cdot rac{e^{(QK^T)_{i,j}}}{\sum_k e^{(QK^T)_{i,k}}}$$

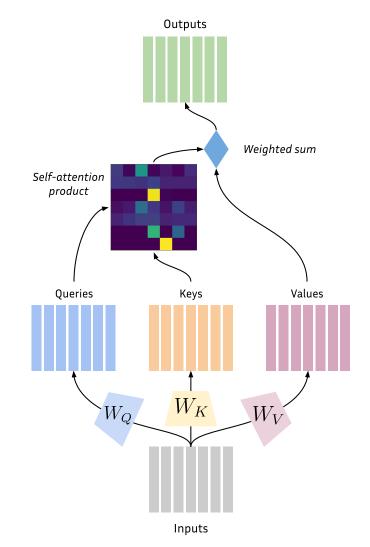
where  $d_h$  is the hidden dimension of the model

#### **Inside Transformers: A and V**



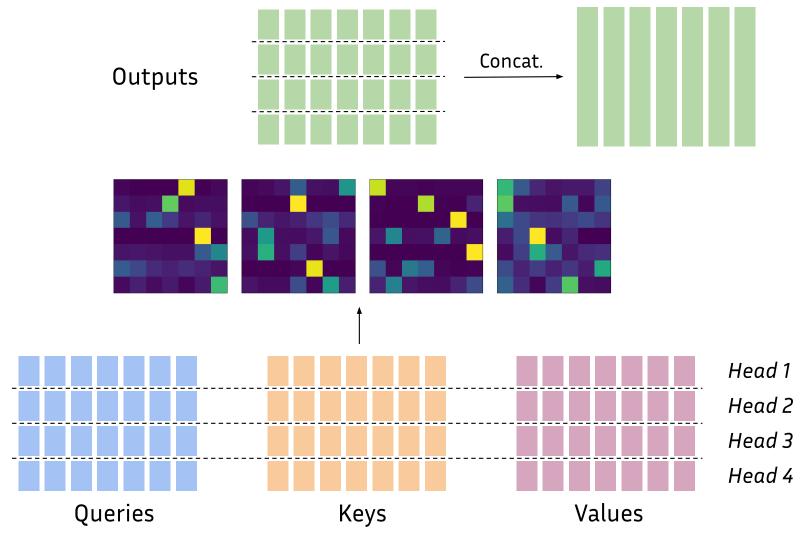
### **Inside Transformers: Self-attention summary**

- Inputs are mapped to Queries, Keys and Values
- Queries and Keys are used to measure interaction (A)
- Interaction weights are used to "select" relevant Values combinations
- Complexity: O(L^2)



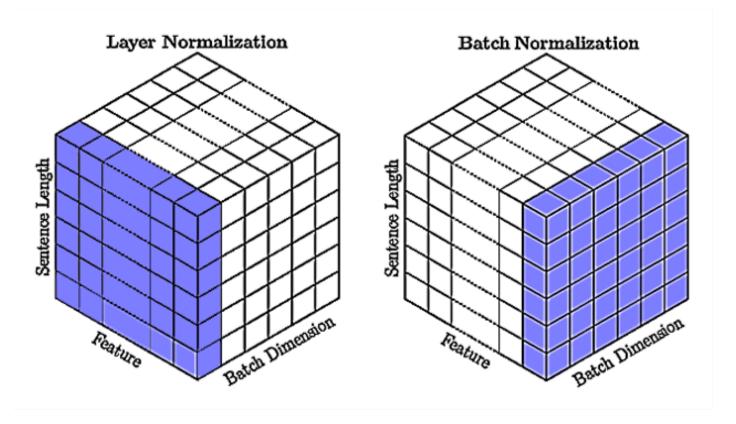
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#### **Inside Transformers: Multi-head attention**

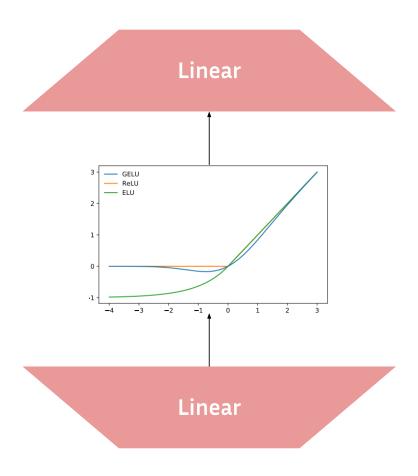


### **Inside Transformers: LayerNorm**

Avoids gradient explosion



## **Inside Transformers: Output layer**



### **Modern flavors: Relative Positional Embeddings**

• Encode position at attention-level:

$$(\Omega QK^T)_{i,j} = \langle \omega_i(Q_i), \omega_j(K_j) 
angle + eta_{i,j}$$

- Rotary Positional Embeddings (RoPE, Su et al. 2023)
  - $\circ \ \omega_i$  is a rotation of angle i heta; no eta
- Linear Biases (ALiBi, Press et al. 2022)
  - $egin{aligned} \circ \ eta_{i,j} = m \cdot (i-j) ext{ with } m \in \mathbb{R} \end{aligned}$

#### Modern flavors: RMSNorm

- Replaces LayerNorm
- Re-scaling is all you need

$$RMSNorm_g(a_i) = rac{a_i}{\sqrt{rac{1}{N}\sum_{j=1}^N a_j^2}}g_i$$

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### **Modern flavors: Grouped-Query Attention**

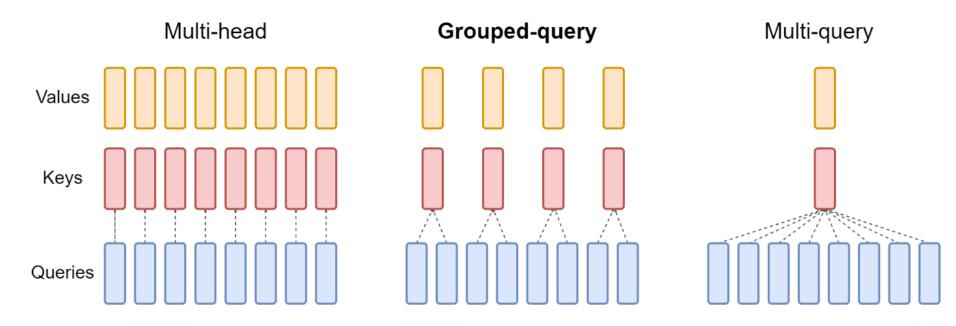
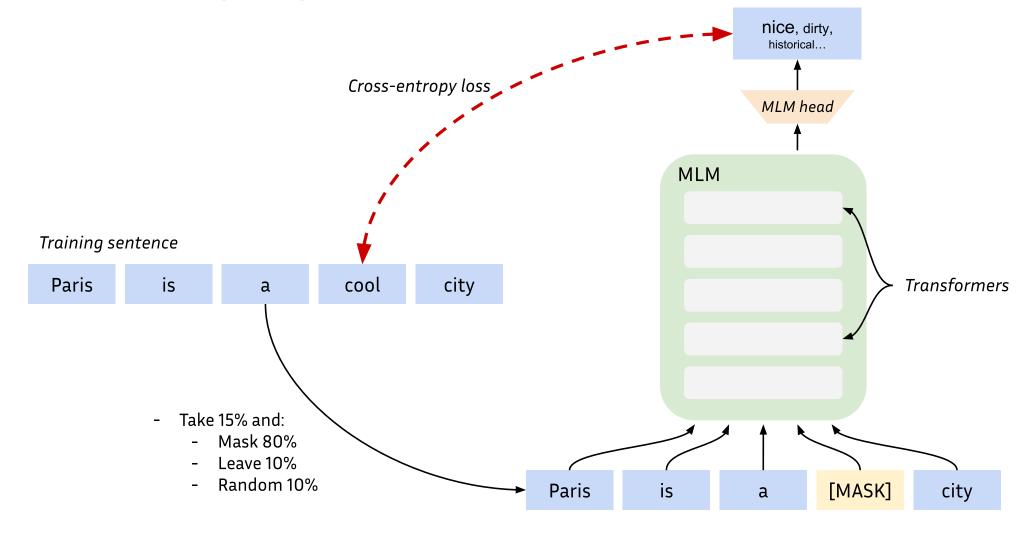


Figure 2: Overview of grouped-query method. Multi-head attention has H query, key, and value heads. Multi-query attention shares single key and value heads across all query heads. Grouped-query attention instead shares single key and value heads for each *group* of query heads, interpolating between multi-head and multi-query attention.

# **Encoder Models**

# **Masked Language Models**



# BERT (Devlin et al., 2018)

- Pre-trained on 128B tokens from Wikipedia + BooksCorpus
- Additional Next Sentence Prediction (NSP) loss
- Two versions:
  - BERT-base (110M parameters)
  - BERT-large (350M parameters)
- Cost: ~1000 GPU hours

## RoBERTa (Liu et al., 2019)

- Pre-trained on 128B 2T tokens from web data (BERT x10)
- No more Next Sentence Prediction (NSP) loss
- Two versions:
  - RoBERTa-base (110M parameters)
  - RoBERTa-large (350M parameters)
- Better results in downstream tasks
- Cost: ~25000 GPU hours

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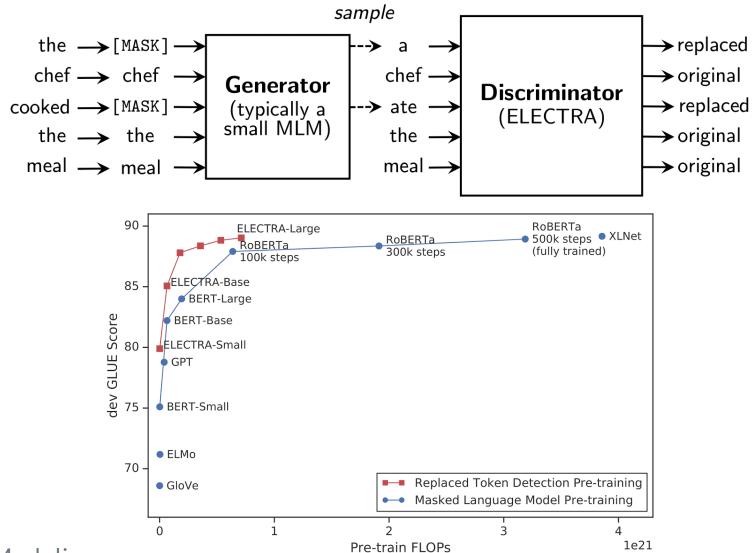
## Multilingual BERT (mBERT)

- Pre-trained on 128B tokens from multilingual Wikipedia
- 104 languages
- One version:
  - mBERT-base (179M parameters)
- Cost: unknown

# XLM-RoBERTa (Conneau et al., 2019)

- Pre-trained on 63T tokens from CommonCrawl
- 100 languages
- Two versions:
  - XLM-RoBERTa-base (279M parameters)
  - XLM-RoBERTa-large (561M parameters)
- Cost: ~75000 GPU hours

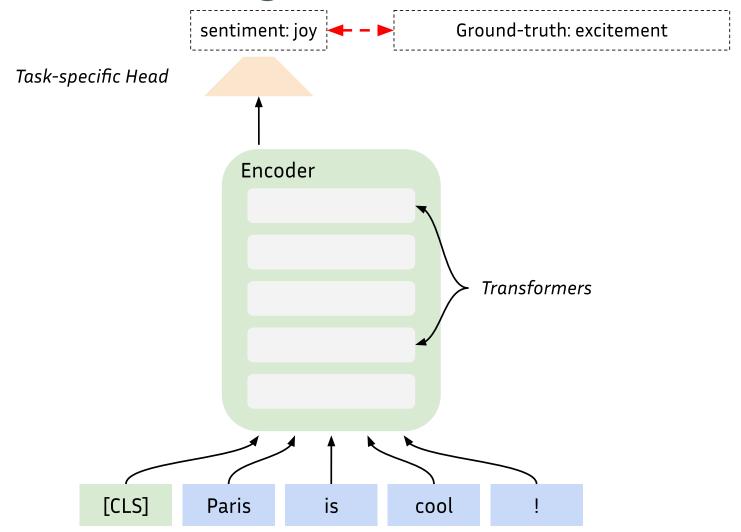
# ELECTRA (Clark et al., 2020)



## ELECTRA (Clark et al., 2020)

- Pre-trained on 63T tokens from CommonCrawl
- 100 languages
- Three versions:
  - ELECTRA-small (14M parameters)
  - ELECTRA-base (110M parameters)
  - ELECTRA-large (350M parameters)
- Really better than BERT/RoBERTa
- Cost: =BERT

# **Encoders: Fine-tuning**



## **Encoders: Classical applications**

- Natural Language Inference (NLI)
  - I like cake! / Cake is bad => same neutral opposite
- Text classification (+ clustering)
  - I'm so glad to be here! => joy
- Named Entity Recognition (NER)
  - I voted for Obama! => (Obama, pos:3, class:PER)
- and many others...

# **Decoders**

#### **Decoders - Motivation**

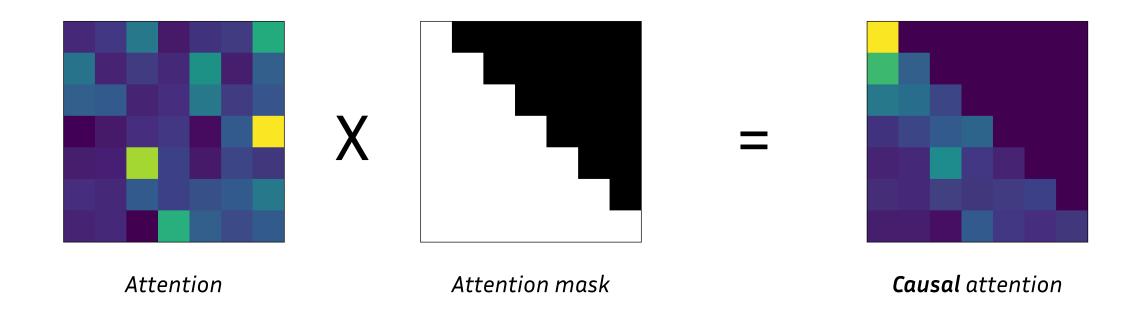
- Models that are designed to generate text
- Next-word predictors:

$$P(w_i \mid (w_j)_{j 
eq i}) = P_{ heta}(w_i \mid w_1 \ldots w_{i-1})$$

 Problem: How do we impede self-attention to consider future tokens?

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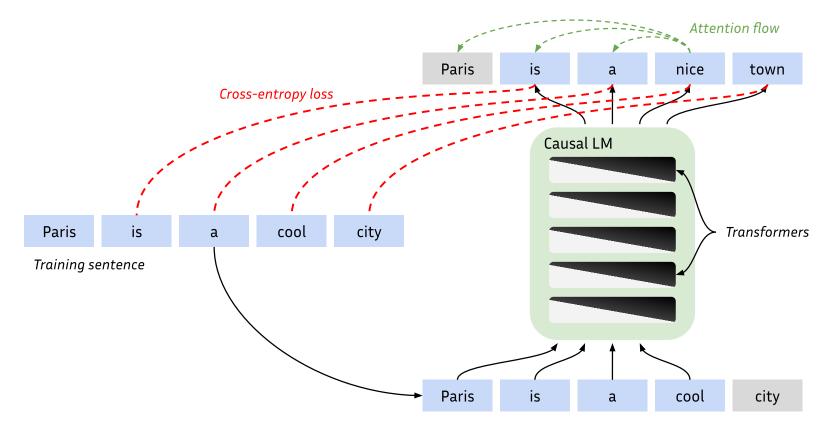
#### **Decoders - Attention mask**



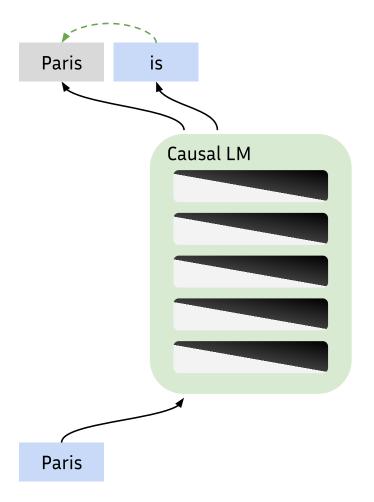
• Each attention input can only attend to previous positions

## **Decoders - Causal LM pre-training**

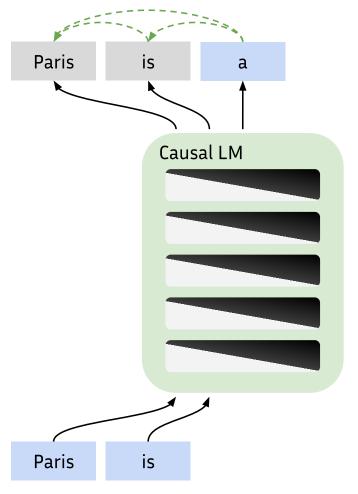
Teacher-forcing



# **Decoders - Causal LM inference (greedy)**



# **Decoders - Causal LM inference (greedy)**



## **Decoders - Refining inference**

- ullet What we have : a good model for  $P_{ heta}(w_i|w_1\dots w_{i-1})$
- What we want at inference:

$$W^* = ackslash ext{argmax}_{n, w_i \dots w_n} P_{ heta}(w_i \dots w_n | w_1 \dots w_{i-1})$$

- ullet For a given completion length n, there are  $|V|^n$  possibilities
  - $\circ$  e.g.: 19 new tokens with a vocab of 30000 tokens > #atoms in  $\Omega$
- We need approximations

### **Decoders - Greedy inference**

Keep best word at each step and start again:

$$W^* = ackslash ext{argmax}_{n,w_{i+1}...w_n} P_{ heta}(w_{i+1}...w_n|w_1...w_{i-1}w_i^*)$$

where 
$$w_i^* = \langle \mathop{\mathrm{argmax}}_{w_i} P_{ heta}(w_i|w_1...w_{i-1})$$

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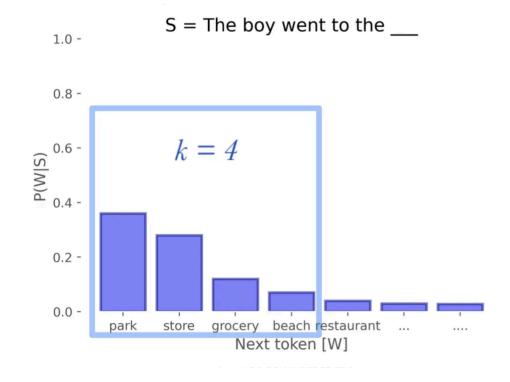
#### **Decoders - Beam search**

- Keep best k chains of tokens at each step:
  - $\circ$  Take k best  $w_i$  and compute  $P_{ heta}(w_{i+1}|\dots w_i)$  for each
  - $\circ$  Take k best  $w_{i+1}$  in each sub-case (now we have  $k imes k \ (w_i, w_{i+1})$  pairs to consider)
  - $\circ$  Consider only the k more likely  $(w_i,w_{i+1})$  pairs
  - $\circ$  Compute  $P_{ heta}(w_{i+2}|\dots w_iw_{i+1})$  for the k candidates
  - o and so on...

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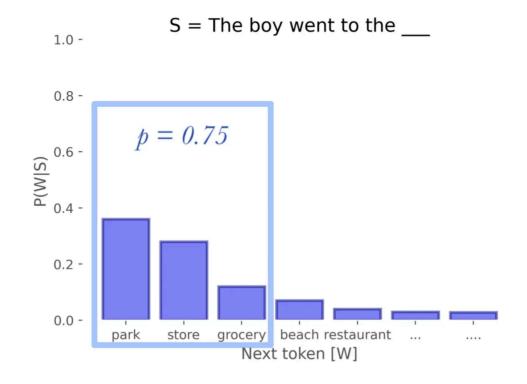
## **Decoders - Top-k sampling**

ullet Randomly sample among top-k tokens based on  $P_{ heta}$ 



# Decoders - Top-p (=Nucleus) sampling

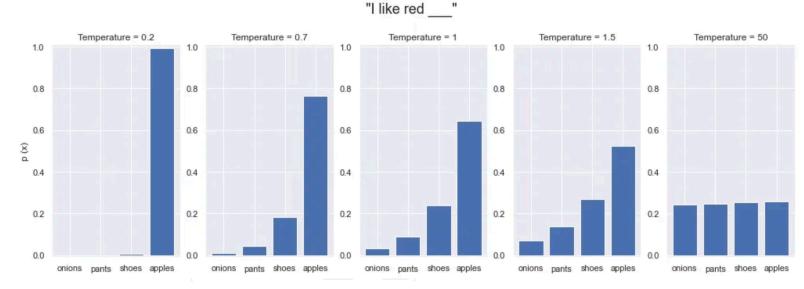
ullet Randomly sample based on  $P_{ heta}$  up to p%



### **Decoders - Generation Temperature**

Alter the softmax function:

$$softmax_{ au}(x) = rac{e^{rac{x_{i}}{ au}}}{\sum_{j} e^{rac{x_{j}}{ au}}}$$

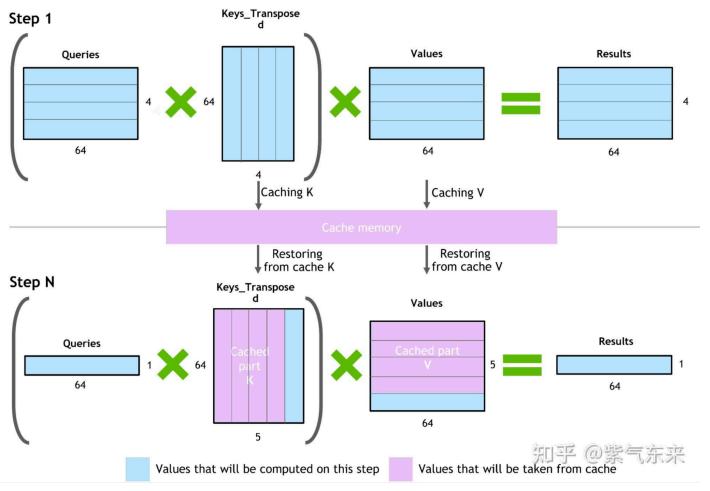


# **Decoders - Inference speed**

- For greedy decoding without prefix:
  - $\circ \,\, n$  passes with sequences of length  $1 \leq t \leq n$
  - $\circ$  Each pass is  $O(n^2)$
  - $\circ$  Complexity:  $O(n^3)$
- Other decoding are <u>more costly</u>
- Ways to go faster?

### **Decoders - Query-Key caching**

(Q \* K^T) \* V computation process with caching

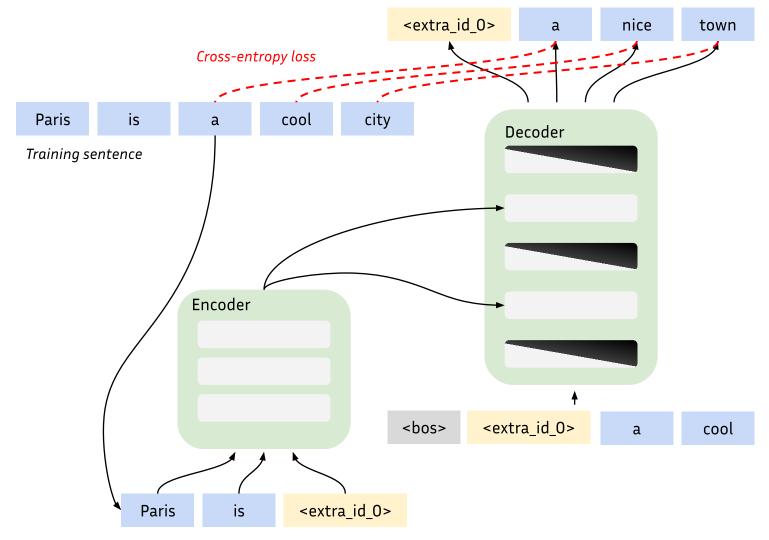


## **Decoders - Speculative decoding**

- ullet Generate  $\gamma$  tokens using  $P_\phi$  where  $|\phi|\ll | heta|$  (smaller model)
- ullet Forward  $w_i \ldots w_{i+\gamma}$  in teacher-forcing mode and predict  $w_{i+\gamma+1}$  with the bigger model
- ullet Compare  $P_{ heta}$  and  $P_{\phi}$  and only keep tokens where they don't differ too much

# **Encoder-Decoder models**

# T5 pre-training



# All models can do everything

- Encoders are mostly used to get contextual embeddings
  - $\circ$  They can also generate :  $T_{enc}$  ("I love [MASK]")
- Decoders are mostly used for language generation
  - $\circ$  They can also give contextual embeddings :  $T_{dec}$  ("I love music!")
  - Or solve any task using prompts:
    - "What is the emotion in this tweet? Tweet: '...' Answer:"
- Encoders-decoders are used for language in-filling

# **Evaluating models**

- A useful evaluation metric: *Perplexity*
- Defined as:

$$ppl(T_{ heta}; w_1 \ldots w_n) = \exp\left(-rac{1}{n} \sum_{t=1}^n \log P_{ heta}(w_t|w_{< t})
ight)$$

• Other metrics: accuracy, MAUVE, ...

#### **Zero-shot evaluation**

- Never-seen problems/data
- Example: "What is the capital of Italy? Answer:"
  - Open-ended: Let the model continue the sentence and check exact match
  - Ranking: Get next-word likelihood for "Rome", "Paris", "London", and check if "Rome" is best
  - Perplexity: Compute perplexity of "Rome" and compare with other models

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### Few-shot evaluation / In-context learning

- Never-seen problems/data
- Example: "Paris is the capital of France. London is the capital of the UK. Rome is the capital of"
- Chain-of-Thought (CoT) examples:
  - Normal: "(2+3)x5=25. What's (3+4)x2?"
  - CoT: "To solve (2+3)x5, we first compute (2+3) = 5 and then multiply (2+3)x5=5x5=25. What's (3+4)x2?"

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### **Open-sourced evaluation**

- Generative models are evaluated on benchmarks
- Example (LLM Leaderboard from HuggingFace):

Т	Model	Average 🚹 🔺	ARC 🔺	HellaSwag ▲	MMLU 🔺	TruthfulQA 🔺	Winogrande ▲	GSM8K ▲
	Owen/Owen-72B	73.6	65.19	85.94	77.37	60.19	82.48	70.43
	chargoddard/Yi-34B-Llama	70.95	64.59	85.63	76.31	55.6	82.79	60.8
	01-ai/Yi-34B-200K	70.81	65.36	85.58	76.06	53.64	82.56	61.64
	01-ai/Yi-34B	69.42	64.59	85.69	76.35	56.23	83.03	50.64
	deepseek-ai/deepseek-llm-67b-base	69.38	65.44	87.1	71.78	51.08	84.14	56.71
	mistralai/Mixtral-8x7B-v0.1	68.42	66.04	86.49	71.82	46.78	81.93	57.47
	meta-llama/Llama-2-70b-hf	67.87	67.32	87.33	69.83	44.92	83.74	54.06
	tiiuae/falcon-180B	67.85	69.45	88.86	70.5	45.47	86.9	45.94

# Lab session