$$K_{4} = \times_{n} =$$

$$2n \text{ crossing s}$$

$$A^{4} f(K_{+}) - A^{-4} f(K_{-}) = (A^{-2} - A^{2}) f(K_{0})$$

$$A^{4} f(X_{n}) - A^{-4} f(X_{n-1}) = (A^{-2} - A^{2}) f(H_{-}) = (A^{2} - A^{2}) (-A^{2} (1 + A^{8}))$$

$$= (A^{4} - 1) (A^{8} + 1)$$

$$f(X_{n}) = A^{-8} f(X_{n-1}) + (1 - A^{-4}) (A^{9} + 1)$$

$$f(X_{0}) = f(U_{1}) = 1$$

$$Claim : f(X_{n}) = \frac{A^{4} (A^{8} + 1)}{A^{4} + 1} (1 - A^{-8n}) + A^{-8n}$$