```
> utility\_left := (1-r) \cdot H \cdot (s \cdot (1-r) + (1-s) \cdot ((thetar - 1) \cdot r + 1))^{-alpha} - RI \cdot (1-r)^{-beta} - (1-r) \cdot F \cdot (1-r \cdot s)^{-gamma}
\textit{utility\_left} \coloneqq (1-r) \; H \left( s \; (1-r) + (1-s) \; \left( \left( \textit{thetar} - 1 \right) \; r + 1 \right) \right)^{-\alpha} - RI \; (1-r)^{-\beta} - \left( 1 \; r \right)^{-\beta} + \left( 1 \; r \right)^
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   (1)
> utility\_right := ((thetar - 1) \cdot r + 1) \cdot H \cdot (s \cdot (1 - r) + (1 - s) \cdot ((thetar - 1) \cdot r + 1))^{-alpha} - R2 \cdot (1 - r)^{-beta} - F \cdot (1 - r \cdot s)^{-gamma}
utility\_right := ((thetar - 1) r + 1) H(s(1 - r) + (1 - s) ((thetar - 1) r + 1))^{-\alpha} - (1 - s)^{-\alpha}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (2)
                              (-r)^{-\beta}R^2 - F(-rs+1)^{-\gamma}
> utility := s \cdot utility left + (1-s) \cdot utility right
utility := s \left( (1-r) H(s(1-r) + (1-s) ((thetar - 1) r + 1) \right)^{-\alpha} - RI (1-r)^{-\beta} - (1-r)^{-\beta} + (1-r)^{-\beta} - (1-r)^{-\beta} + (1-r)^{-
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (3)
                              -r) F(-rs+1)^{-\gamma} + (1-s) ((thetar-1) r+1) H(s(1-r) + (1-r) 
                              -s) ((thetar-1) r+1)^{-\alpha} - (1-r)^{-\beta} R^2 - F(-rs+1)^{-\gamma}
> simplify(utility)
 -H(-1+r(sthetar-thetar+1))(-r(s-1)thetar-r+1)^{-\alpha}+F(rs-1)(-rs+1)^{-\gamma}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (4)
                             -((R1-R2) s + R2) (1-r)^{-\beta}
\rightarrow DS := simplify(diff(utility, s))
DS \coloneqq -H\alpha r \left(-1 + \left(1 + \left(s - 1\right) \text{ thetar}\right) r\right) \text{ thetar } \left(-r \left(s - 1\right) \text{ thetar} - r + 1\right)^{-\alpha - 1} - H\left(-r \left(s - 1\right) \right) r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (5)
                          -r(s-1) thetar -r+1) ^{-\alpha}r thetar +Fr\gamma(rs-1)(-rs+1)^{-\gamma-1}+F(-rs+1)^{-\gamma}r
                            -(1-r)^{-\beta}(R1-R2)
\rightarrow maximize (utility, s = 0..1)
maximize(s((1-r)H(s(1-r)+(1-s)((thetar-1)r+1))^{-\alpha}-RI((1-r)^{-\beta}-(1-r)^{-\beta}))^{-\alpha}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (6)
                              -r) F(-rs+1)^{-\gamma}) + (1-s) (((thetar-1) r+1) H(s(1-r)+(1-r))
                              -s) ((thetar - 1) r + 1))^{-\alpha} - R2 (1 - r)^{-\beta} - F (-rs + 1)^{-\gamma}), s = 0...1)
> utility test := H \cdot (s \cdot (1-r) + (1-s) \cdot ((thetar - 1) \cdot r + 1))^{-alpha} \cdot (thetar \cdot r \cdot (s+1) - 2 \cdot r \cdot s)
                                               -r+1) - (1-r)^{-\text{beta}} \cdot (s \cdot RI + (1-s) \cdot R2) - F \cdot (1-rs)^{-\text{gamma}} \cdot (1-rs)
utility test := H(s(1-r) + (1-s)((thetar - 1)r + 1))^{-\alpha}(thetar r(s+1) - 2rs - r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (7)
                             +1) -(1-r)^{-\beta}(sR1+(1-s)R2)-F(1-rs)^{-\gamma}(1-rs)
> simplify(utility test)
(-r(s-1) thetar - r + 1)^{-\alpha} H(1 + ((thetar - 2) s + thetar - 1) r) - F(1 - rs)^{-\gamma + 1} - (1 - rs)^{-\gamma
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (8)
                              (-r)^{-\beta} ((R1 - R2) s + R2)
simplify(utility test — utility)
2 Hrs (thetar - 1) (-r(s-1) thetar - r + 1)^{-\alpha} - ((1-rs)^{-\gamma+1} + (-rs+1)^{-\gamma} (rs+1)^{-\gamma})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (9)
                               -1))F
> utility left2 := H \cdot (1-r) \cdot A^{-\text{alpha}} - RI \cdot (1-r)^{-\text{beta}} - F \cdot (1-r) \cdot (1-r \cdot s)^{-\text{gamma}}
                                                                        utility left2 := H(1-r) A^{-\alpha} - RI(1-r)^{-\beta} - (1-r) F(-rs+1)^{-\gamma}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (10)
```

>
$$utility_right2 := H \cdot ((thetar - 1) \cdot r + 1) \cdot A^{-alpha} - R2 \cdot (1 - r)^{-beta} - F \cdot (1 - r \cdot s)^{-gamma}$$

 $utility_right2 := H \cdot ((thetar - 1) r + 1) A^{-\alpha} - (1 - r)^{-\beta} R2 - F \cdot (-rs + 1)^{-\gamma}$ (11)
> $utility2 := simplify(s \cdot utility_left2 + (1 - s) \cdot utility_right2)$
 $utility2 := F \cdot (rs - 1) \cdot (-rs + 1)^{-\gamma} + ((-R1 + R2) \cdot s - R2) \cdot (1 - r)^{-\beta} - A^{-\alpha} \cdot (-1 + r \cdot (s \cdot thetar - thetar + 1)) H$