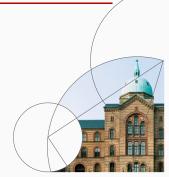


Introduction

Mini-Course: Heterogenous Agent Macro

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Plan

1. Introduction

2. Programming principles

3. Coding

4. Consumption-Saving

Introduction

Introduction

Central economic topics:

- 1. Consumption-saving behavior under risk and constraints
- 2. Heterogeneous agents in general equilibrium models
 - 2.1 Long-run effects on aggregate outcomes
 - 2.2 Short-run effects on aggregate outcomes
 - 2.3 Drivers of inequality

History:

- Heathcote et al. (2009), »Quantitative Macroeconomics with Heterogeneous Households«
- Kaplan and Violante (2018), »Microeconomic Heterogeneity and Macroeconomic Shocks«
- Cherrier et al. (2023), »Household Heterogeneity in Macroeconomic Models: A Historical Perspective«
- Central technical method: Programming in Python

Macroeconomic Models with Heterogeneous Agents

Model components:

- 1. Optimizing individual agents (households + firms)
- 2. Idiosyncratic and aggregate risk
- 3. Information flows (who knows what when \Rightarrow often everything)
- 4. Market clearing (Walras vs. search-and-match)

Insurance/markets:

 $Complete
ightarrow idiosyncratic risk insured away \sim representative agent Incomplete
ightarrow agents need to self-insure$

Heterogeneity:

Ex ante in preferences, abilities etc.
Ex post after realization of idiosyncratic shocks

- HANC: Heterogeneous Agent Neo-Classical model (Aiyagari-Bewley-Hugget-Imrohoroglu or Standard Incomplete Market model)
- HANK: Heterogeneous Agent New Keynesian model (i.e. include price and wage setting frictions)

Lectures

Topics:

- 1. Consumption-saving
- 2. Stationary equilibrium
- 3. Transitional dynamics
- 4. HANK models

• Teaching philosophy:

- 1. Go in depth from theory to implementation
- 2. Not a literature review key entrances to literature

Exam

- Format: 36 hours take-home
- **Baseline:** One of the models from the course
- Questions:
 - 1. Implement an extension (in Python code)
 - 2. Analyze the economic dynamics

Python

- Assumed knowledge: Similar to my undergraduate course Introduction to Programming and Numerical Analysis
 - 1.1 Python
 - 1.2 VSCode
 - 1.3 git

Preparation: video playlist (~10 hours at normal speed)

- 2. Updated Python: Install (or re-install) newest Anaconda
- 3. Packages: pip install quantecon, EconModel, consav
- 4. GEMoodel tools:
 - 4.1 Clone the GEModelTools repository
 - 4.2 Locate repository in command prompt
 - $4.3 \ {\rm Run \ pip \ install \ -e}$.

Programming principles

References (pointers)

- Variables are references to an instance of an object
- A class defines the type of an object
 - .attribute, state
 - .method(), action (incl. changing self)
- Arithmetic operators (e.g. +,*,/,//,**,%) combine objects
- = assigns a reference (not a copy!)

Question: What does a end up as? What if a = [1,2,3]?

```
1  a = np.array([1,2,3])
2  b = a
3  c = a[1:] # slicing
4  b[0] = 3 # indexing
5  c[0] = 3
```

Containers and inheritance

- Atomic types: int, float, str, bool, etc.
- Containers list, tuple, dict, set, np.array, etc.
- Inheritance (build from def. of »parent«, class Child(Parent))

e.g. integer
$$\subset$$
 scalar \subset number \subset

- Mutables (e.g. list, np.array) can change in-place
 - 1. Augmentation operators (+=, -= etc.)
 - 2. Slicing: x[:] = x + y
- Immutables (e.g. atomic types and tuples) can never change

Questions: What does y end up as?

```
1 x = np.array([1,2,3])

2 y = x

3 x += 1

4 x[:] = x + 1

5 x = x + 1
```

Functions

- Functions are objects (can e.g. be arguments in functions)
 Unlike in math:
 - 1. Can change its arguments (side-effects)
 - 2. Can call itself (recursion)
- Decorators change function behavior (e.g. @numba.njit)
- Variables can both be local scope (good) or global scope (bad)

Questions: What is the output?

```
1  a = 1
2  def f(x):
3    return x+a
4  print(f(1))
5  a = 2
6  print(f(1))
```

Computational tree and branches

- **Comparison** (==, !=, <, <=, not, and, or etc.)
- Conditionals (if, elif, else)
- Loops (for, while, continue, break)
- Convergence (tolerance in optimizer or root-finder/equation-solver)

Questions: How could this be implemented with a while loop?

```
1  x = x0
2  for i in range(n):
3     y = evaluate(x)
4     if check(y): break
5     x = update(x,y)
6  else:
7     raise ValueError('did not converge')
```

Everything is discrete

- Never use exactness for decimal numbers
 - Order of computation matter
 - Best with numbers are around 1 (underflow and overflow)
- Division, exp, log etc. (costly) approximations
- Function approximation and interpolation often needed

Questions: Which are True and which are False?

```
print(0.1 + 0.2 == 0.3)
print(0.5 + 0.5 == 1.0)
print(np.isclose(0.1+0.2,0.3))
print(np.isclose(1e-200*1e200*1e200*1e-200,1.0))
print(np.isinf(1e-200*(1e200*1e200)*1e-200))
print(np.isclose(1e200*(1e-200*1e-200)*1e200,0.0))
```

Pseudo random numbers

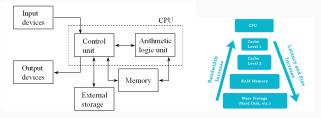
- Only one seed (randomness not assured across seeds)
- State of random number generator can be reset
- Monte Carlo simulation and integration
 - 1. Static alternative: Use quadrature rules
 - 2. Dynamic alternative: Discretize and derive transition matrix

Questions: What is z equal to?

```
rng = np.random.default_rng(123)
s = rng.bit_generator.state
x = rng.normal(size=10)
y = rng.normal(size=10)
rng.bit_generator.state = s
z = rng.normal(size=10)
```

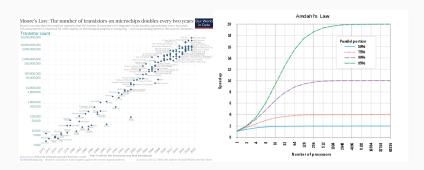
CPUs are complex

- Instruction set (assembly) is not just add, subtract, etc.
 - 1. Work on vectors (SIMD) \Rightarrow homogeneity is good
 - 2. Out-of-order execution \Rightarrow predictability is good
 - 3. Caching \Rightarrow latest read memory can be accessed quickly



- Compilers can optimize a lot ⇒ use existing libraries
- Parallelisation: Start up costs
 - 1. Hardware: Cores vs. CPUs vs. sockets vs, computers
 - 2. Software: Shared memory (e.g. OpenMP) or not (e.g. MPI)

Moore vs. Amdahl



- 1. Moore's law: Exponential growth in computational power
 - 1.1 Originally: Faster CPUs (calculations per time unit)
 - 1.2 Now: More cores per CPU
- 2. Amdahl's law: Sequential code becomes the bottleneck

Need for speed

- Computation time vs programmer time
 Use not-too-model-specific insights ⇒ better algorithm
- Premature optimization is the root of all evil! Use line-profiler!
 - 1. Use available code: Stand on the shoulder of giants
 - 2. In numpy: Use vectorization
 - 3. Else: Use numba
- Automatic differentiation? Use JAX (or PyTorch)
- Faster still? Implement bottleneck in C++ and call from Python

Documentation and debugging

- No code is self-explanatory (for others, incl. future you)
- Write documentation (use github-copilot)
 - 1. The comments explain humans what the code does.
 - 2. The code makes the computer do what the comments say
- Important design patterns:
 - 1. Use namespaces (be aware of scope) and meaningful names
 - 2. No repetition of code-lines \Rightarrow single-purpose functions/methods
 - 3. Use assert (also print and plot intermediate results)
 - 4. Use try-except
- Run from top to bottom (make <u>shortcut</u>)

Replication: datacodestandard.org

- Debugging
 - 1. Errors are (almost) always simple
 - 2. Go through code step-by-step (manually or debugger)

Other languages

High level languages:

- 1. MATLAB: Costly and not better.
- 2. R: Better at statistics and data work, but not pure numerical work.
- Julia: Faster than Python (incl. numba), slower than C++.
 Smallish community.

Low level languages:

- 1. **C++**: State-of-the-art for fastest code.
- 2. **Fortran**: No benefits relative to C++ (only legacy...).

Hardware:

- 1. CPU: Most complex cores.
- 2. GPU: More cores, but more specialized at linear algebra.
- 3. TPU: Even more specialized at AI (incl. machine learning)

Coding

Coding: Fractions

- Notebook: 01. Fractions.ipynb
- Task 1: Implement a class defining a fraction and allowing for a+b
- Task 2: Implement a class for defining a list of fractions, which you can loop through

Coding: Debugging

• Notebook: 02. Debugging.ipynb

Coding: Speed

• Notebook: 03. NeedForSpeed.ipynb

Coding: EconModelClass

Code: EconModel

Notebook:
 EconModelNotebooks\01. Using the EconModelClass.ipynb (not the C++ part)

Video: Youtube - EconModel

Consumption-Saving

Consumption-Saving

Next slide set