# Course Plan: Heterogeneous Agent Macro

## Jeppe Druedahl

Course page: sites.google.com/view/numeconcph-het-agent-macro

#### **Preparation:**

- 1. Install Python and VSCode as explained here.
- 2. Watch the lecture videos on Python (~ 10 hours) here.
- 3. Go through the associated lecture notebooks here.

## Lectures

#### • Lecture 0. Introduction

Overview: Heathcote et al. (2009); Kaplan and Violante (2018); Cherrier et al. (2023).

## • Lecture 1. Consumption-saving

Central: Carroll (1997); Druedahl (2021)

More economics: Modigliani and Brumburg (1954); Friedman (1957); Deaton (1991); Carroll (1992, 2006); Kaplan and Violante (2014); Kaplan et al. (2014); Jørgensen (2017); Carroll et al. (2021); Guvenen et al. (2021); Fagereng et al. (2021); Harmenberg and Oberg (2021); Druedahl et al. (2021); Druedahl and Martinello (2022). More computational: Carroll (2006); Iskhakov et al. (2017); Druedahl and Jørgensen (2017); Harmenberg (2021); Rendahl (2022). Deep learning: Maliar et al. (2021); Azinovic et al. (2022); Kase et al. (2022); Han et al. (2021).

### • Lecture 2. Stationary equilibrium

Central: Aiyagari (1994); Hubmer et al. (2021) GEModelTools: Druedahl (2024a,f,c). Histogram simulation: Young (2010); Tan (2020); Ocampo and Robinson (2022).

#### • Lecture 3. Transitional dynamics

Central: Boppart et al. (2018); Auclert et al. (2021a). GEModelTools: Druedahl (2024a,f,c). More on policy: McKay and Wolf (2023); Dávila and Schaab (2023).

#### • Lecture 4. HANK

Central: Werning (2015); Kaplan et al. (2018); Auclert et al. (2023); Broer et al. (2023a). GEModelTools: Druedahl (2024d,e,b,g,h). More HANK: Bayer et al. (2019); Hagedorn et al. (2019); Auclert et al. (2020, 2021b); Druedahl et al. (2022). More zero-liquidity: McKay et al. (2017); Acharya and Dogra (2020); Broer et al. (2020); Bilbiie (2021); Ravn and Sterk (2021); Broer et al. (2023b).

## Plan

**Monday:** Lecture 0+1: 9:00 - 13:00

**Tuesday:** Lecture 2: 10:00 - 13:00

**Wednesday:** Lecture 3: 10:00 - 13:00

**Thursday:** Lecture 4: 10:00 - 13:00

## 1. EconModel:

Code-packages

github.com/NumEconCopenhagen/EconModel github.com/NumEconCopenhagen/EconModelNotebooks

#### 2. ConSav:

 $github.com/NumEconCopenhagen/ConsumptionSaving\\github.com/NumEconCopenhagen/ConsumptionSavingNotebooks$ 

## 3. **GEModelTools:**

github.com/NumEconCopenhagen/GEModelTools github.com/NumEconCopenhagen/GEModelToolsNotebooks

## References

- Acharya, S. and Dogra, K. (2020). Understanding HANK: Insights From a PRANK. *Econometrica*, 88(3):1113–1158.
- Aiyagari, S. R. (1994). Uninsured Idiosyncratic Risk and Aggregate Saving. *The Quarterly Journal of Economics*, 109(3):659–684.
- Auclert, A., Bardóczy, B., Rognlie, M., and Straub, L. (2021a). Using the Sequence-Space Jacobian to Solve and Estimate Heterogeneous-Agent Models. *Econometrica*, 89(5):2375–2408.
- Auclert, A., Rognlie, M., Souchier, M., and Straub, L. (2021b). Exchange Rates and Monetary Policy with Heterogeneous Agents: Sizing up the Real Income Channel. NBER Working Paper 28872.
- Auclert, A., Rognlie, M., and Straub, L. (2020). Micro Jumps, Macro Humps: Monetary Policy and Business Cycles in an Estimated HANK Model. NBER Working Paper 26647.
- Auclert, A., Rognlie, M., and Straub, L. (2023). The Intertemporal Keynesian Cross. NBER Working Paper 25020, National Bureau of Economic Research.
- Azinovic, M., Gaegauf, L., and Scheidegger, S. (2022). Deep Equilibrium Nets. *International Economic Review*, 63(4):1471–1525.
- Bayer, C., Luetticke, R., Pham-Dao, L., and Tjaden, V. (2019). Precautionary Savings, Illiquid Assets, and the Aggregate Consequences of Shocks to Household Income Risk. *Econometrica*, 87(1):255–290.
- Bilbiie, F. O. (2021). Monetary Policy and Heterogeneity: An Analytical Framework. Working Paper.
- Boppart, T., Krusell, P., and Mitman, K. (2018). Exploiting MIT shocks in heterogeneous-agent economies: the impulse response as a numerical derivative. *Journal of Economic Dynamics and Control*, 89:68–92.
- Broer, T., Druedahl, J., Harmenberg, K., and Öberg, E. (2023a). Fiscal stimulus policies according to HANK-SAM. Working Paper.
- Broer, T., Druedahl, J., Harmenberg, K., and Öberg, E. (2023b). The Unemployment-Risk Channel in Business-Cycle Fluctuations. CEPR Discussion Paper 16639.
- Broer, T., Harbo Hansen, N.-J., Krusell, P., and Oberg, E. (2020). The New Keynesian Transmission Mechanism: A Heterogeneous-Agent Perspective. *The Review of Economic Studies*, 87(1):77–101.

- Carroll, C. D. (1992). The buffer-stock theory of saving: Some macroeconomic evidence. *Brookings Papers on Economic Activity*, 2:61–156.
- Carroll, C. D. (1997). Buffer-Stock Saving and the Life Cycle/Permanent Income Hypothesis. *The Quarterly Journal of Economics*, 112(1):1–55.
- Carroll, C. D. (2006). The Method of Endogenous Gridpoints for Solving Dynamic Stochastic Optimization Problems. *Economics Letters*, 91(3):312–320.
- Carroll, C. D., Holm, M. B., and Kimball, M. S. (2021). Liquidity constraints and precautionary saving. *Journal of Economic Theory*, 195:105276.
- Cherrier, B., Duarte, P., and Saïdi, A. (2023). Household heterogeneity in macroeconomic models: a historical perspective. *European Economic Review*, page 104497.
- Deaton, A. (1991). Saving and liquidity constraints. *Econometrica*, 59(5):1221–1248.
- Druedahl, J. (2021). A Guide on Solving Non-Convex Consumption-Saving Models. *Computational Economics*, 58(3):747–775.
- Druedahl, J. (2024a). Documentation for GEModelTools. Technical report.
- Druedahl, J. (2024b). GEModelTools: A HANK-SAM model. Technical report.
- Druedahl, J. (2024c). GEModelTools: HANC with Government. Technical report.
- Druedahl, J. (2024d). GEModelTools: HANK with Sticky Prices. Technical report.
- Druedahl, J. (2024e). GEModelTools: HANK with Sticky Wages. Technical report.
- Druedahl, J. (2024f). GEModelTools: Heterogenous Agent NeoClassical Model (HANC). Technical report.
- Druedahl, J. (2024g). GEModelTools: Two-Asset Model with Capital. Technical report.
- Druedahl, J. (2024h). GEModelTools: Two-Sector I-HANK model. Technical report.
- Druedahl, J., Graber, M., and Jørgensen, T. H. (2021). High Frequency Income Dynamics. CEBI Working Paper 08/21.
- Druedahl, J. and Jørgensen, T. H. (2017). A general endogenous grid method for multi-dimensional models with non-convexities and constraints. *Journal of Economic Dynamics and Control*, 74:87–107.
- Druedahl, J. and Martinello, A. (2022). Long-Run Saving Dynamics: Evidence from Unexpected Inheritances. *The Review of Economics and Statistics*, 104(5):1079–1095.

- Druedahl, J., Ravn, S. H., Sunder-Plassmann, L., Sundram, J. M., and Waldstrøm, N. (2022). The Transmission of Foreign Demand Shocks. Working Paper.
- Dávila, E. and Schaab, A. (2023). Optimal Monetary Policy with Heterogeneous Agents: Discretion, Commitment, and Timeless Policy. Working Paper.
- Fagereng, A., Holm, M. B., and Natvik, G. J. (2021). MPC Heterogeneity and Household Balance Sheets. *American Economic Journal: Macroeconomics*, 13(4):1–54.
- Friedman, M. (1957). *A theory of the consumption function*. Princeton university Press for NBER.
- Guvenen, F., Karahan, F., Ozkan, S., and Song, J. (2021). What Do Data on Millions of U.S. Workers Reveal About Lifecycle Earnings Dynamics? *Econometrica*, 89(5):2303–2339.
- Hagedorn, M., Manovskii, I., and Mitman, K. (2019). The Fiscal Multiplier. NBER Working Paper 25571.
- Han, J., Yang, Y., and E, W. (2021). DeepHAM: A Global Solution Method for Heterogeneous Agent Models with Aggregate Shocks.
- Harmenberg, K. (2021). Aggregating heterogeneous-agent models with permanent income shocks. *Journal of Economic Dynamics and Control*, 129:104185.
- Harmenberg, K. and Oberg, E. (2021). Consumption dynamics under time-varying unemployment risk. *Journal of Monetary Economics*, 118:350–365.
- Heathcote, J., Storesletten, K., and Violante, G. L. (2009). Quantitative Macroeconomics with Heterogeneous Households. *Annual Review of Economics*, 1(1):319–354.
- Hubmer, J., Krusell, P., and Smith., A. A. (2021). Sources of US Wealth Inequality: Past, Present, and Future. *NBER Macroeconomics Annual*, 35:391–455. Publisher: The University of Chicago Press.
- Iskhakov, F., Jørgensen, T. H., Rust, J., and Schjerning, B. (2017). The endogenous grid method for discrete-continuous dynamic choice models with (or without) taste shocks. *Quantitative Economics*, 8(2):317–365.
- Jørgensen, T. H. (2017). Life-Cycle Consumption and Children: Evidence from a Structural Estimation. *Oxford Bulletin of Economics and Statistics*, 79(5):717–746.
- Kaplan, G., Moll, B., and Violante, G. L. (2018). Monetary Policy According to HANK. *American Economic Review*, 108(3):697–743.
- Kaplan, G., Violante, G., and Weidner, J. (2014). The Wealthy Hand-to-Mouth. *Brookings Papers on Economic Activity*, pages 77–138.

- Kaplan, G. and Violante, G. L. (2014). A Model of the Consumption Response to Fiscal Stimulus Payments. *Econometrica*, 82(4):1199–1239.
- Kaplan, G. and Violante, G. L. (2018). Microeconomic Heterogeneity and Macroeconomic Shocks. *Journal of Economic Perspectives*, 32(3):167–194.
- Kase, H., Melosi, L., and Rottner, M. (2022). Estimating Nonlinear Heterogeneous Agents Models with Neural Networks. Federal Reserve Bank of Chicago, WP 2022-26.
- Maliar, L., Maliar, S., and Winant, P. (2021). Deep learning for solving dynamic economic models. *Journal of Monetary Economics*, 122:76–101.
- McKay, A., Nakamura, E., and Steinsson, J. (2017). The Discounted Euler Equation: A Note. *Economica*, 84(336):820–831.
- McKay, A. and Wolf, C. K. (2023). Optimal Policy Rules in HANK. Technical report.
- Modigliani, F. and Brumburg, R. (1954). Utility Analysis and the Consumptio Function: An Interpretation of Cross-Section Data. In Kurihara, K. and Brunswick, N., editors, *Post-Keynesian Economics*, pages 338–436. Rutgers University Press.
- Ocampo, S. and Robinson, B. (2022). Computing Longitudinal Moments for Heterogeneous Agent Models. Working Paper.
- Ravn, M. O. and Sterk, V. (2021). Macroeconomic Fluctuations with HANK & SAM: an Analytical Approach. *Journal of the European Economic Association*, 19(2):1162–1202.
- Rendahl, P. (2022). Continuous vs. Discrete Time: Numerical Gains from Trade. Working Paper.
- Tan, E. (2020). A fast and low computational memory algorithm for non-stochastic simulations in heterogeneous agent models. *Economics Letters*, 193:109285.
- Werning, I. (2015). Incomplete Markets and Aggregate Demand. NBER Working Paper 21448.
- Young, E. R. (2010). Solving the incomplete markets model with aggregate uncertainty using the Krusell-Smith algorithm and non-stochastic simulations. *Journal of Economic Dynamics and Control*, 34(1):36–41.