# Package 'NNS'

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Type Package

Title Nonlinear Nonparametric Statistics

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Author Fred Viole
Maintainer Fred Viole <ovvo.financial.systems@gmail.com></ovvo.financial.systems@gmail.com>
<b>Description</b> Nonlinear nonparametric statistics using partial moments. Partial moments are the elements of variance and asymptotically approximate the area of f(x). These robust statistics provide the basis for nonlinear analysis while retaining linear equivalences. NNS offers: Numerical integration, Numerical differentiation, Clustering, Correlation, Dependence, Causal analysis, ANOVA, Regression, Classification, Seasonality, Autoregressive modeling, Normalization and Stochastic dominance. All routines based on: Viole, F. and Nawrocki, D. (2013), Nonlinear Nonparametric Statistics: Using Partial Moments (ISBN: 1490523995).
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Co.LPM         Co.UPM         D.LPM         D.UPM         dy.dx         dy.d_         LPM         LPM.ratio         LPM.VaR         NNS.ANOVA         NNS.ARMA
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Co.LPM

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Co.LPM

Co-Lower Partial Moment (Lower Left Quadrant 4)

# Description

This function generates a co-lower partial moment for between two equal length variables for any degree or target.

# Usage

```
Co.LPM(degree.x, degree.y, x, y, target.x = mean(x), target.y = mean(y))
```

# Arguments

```
degree.x integer; Degree for variable X. (degree.x = 0) is frequency, (degree.x = 1) is area.

degree.y integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
```

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x	a numeric vector.
У	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

# Value

Co-LPM of two variables

# Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

# **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
Co.LPM(0, 0, x, y, mean(x), mean(y))</pre>
```

Co.UPM

Co-Upper Partial Moment (Upper Right Quadrant 1)

# Description

This function generates a co-upper partial moment between two equal length variables for any degree or target.

# Usage

```
Co.UPM(degree.x, degree.y, x, y, target.x = mean(x), target.y = mean(y))
```

# Arguments

degree.x	integer; Degree for variable X. (degree. $x = 0$ ) is frequency, (degree. $x = 1$ ) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
x	a numeric vector.
У	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

D.LPM

#### Value

Co-UPM of two variables

#### Author(s)

Fred Viole, OVVO Financial Systems

# References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

# **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
Co.UPM(0,0,x,y,mean(x),mean(y))</pre>
```

D.LPM

Divergent-Lower Partial Moment (Lower Right Quadrant 3)

# Description

This function generates a divergent lower partial moment between two equal length variables for any degree or target.

# Usage

```
D.LPM(degree.x, degree.y, x, y, target.x = mean(x), target.y = mean(y))
```

# **Arguments**

degree.x	integer; Degree for variable X. (degree $. x = 0$ ) is frequency, (degree $. x = 1$ ) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
x	a numeric vector.
у	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

# Value

Divergent LPM of two variables

# Author(s)

Fred Viole, OVVO Financial Systems

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#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

# **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
D.LPM(0, 0, x, y, mean(x), mean(y))</pre>
```

D.UPM

Divergent-Upper Partial Moment (Upper Left Quadrant 2)

# **Description**

This function generates a divergent upper partial moment between two equal length variables for any degree or target.

# Usage

```
D.UPM(degree.x, degree.y, x, y, target.x = mean(x), target.y = mean(y))
```

#### **Arguments**

degree.x	integer; Degree for variable X. (degree $.x = 0$ ) is frequency, (degree $.x = 1$ ) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
X	a numeric vector.
У	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

# Value

Divergent UPM of two variables

# Author(s)

Fred Viole, OVVO Financial Systems

# References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
D.UPM(0, 0, x, y, mean(x), mean(y))</pre>
```

dy.dx

dy.dx

Partial Derivative dy/dx

# Description

Returns the numerical partial derivate of y wrt x for a point of interest.

# Usage

```
dy.dx(
    x,
    y,
    eval.point = median(x),
    deriv.order = 1,
    h = 0.05,
    deriv.method = "FS"
)
```

# **Arguments**

X	a numeric vector.
У	a numeric vector.
eval.point	numeric; x point to be evaluated. Defaults to (eval.point = median(x)). Set to (eval.point = "overall") to find an overall partial derivative estimate.
deriv.order	numeric options: $(1, 2)$ ; 1 (default) for first derivative. For second derivative estimate of $f(x)$ , set (deriv.order = 2).
h	numeric [0,]; Percentage step used for finite step method. Defaults to h = .05 representing a 5 percent step from the value of the independent variable.
deriv.method	method of derivative estimation, options: ("NNS", "FS"); Determines the partial derivative from the coefficient of the NNS.reg output when (deriv.method = "NNS") or generates a partial derivative using the finite step method (deriv.method = "FS") (Defualt).

#### Value

Returns the value of the partial derivative estimate for the given order.

# Note

If a vector of derivatives is required, ensure (deriv.method = "FS").

# Author(s)

Fred Viole, OVVO Financial Systems

#### References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

Vinod, H. and Viole, F. (2017) "Nonparametric Regression Using Clusters" https://link.springer.
```

com/article/10.1007/s10614-017-9713-5

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# **Examples**

```
## Not run:
x <- seq(0, 2 * pi, pi / 100) ; y <-sin(x)
dy.dx(x, y, eval.point = 1.75)

# Vector of derivatives
dy.dx(x, y, eval.point = c(1.75, 2.5), deriv.method = "FS")
## End(Not run)</pre>
```

dy.d\_

Partial Derivative dy/d\_[wrt]

# Description

Returns the numerical partial derivate of y with respect to [wrt] any regressor for a point of interest. Finite difference method is used with NNS.reg estimates as f(x + h) and f(x - h) values.

# Usage

```
dy.d_(
    x,
    y,
    wrt,
    eval.points = "median",
    folds = 5,
    mixed = FALSE,
    plot = FALSE,
    ncores = NULL,
    messages = TRUE
)
```

# Arguments

X	a numeric matrix or data frame.
У	a numeric vector with compatible dimsensions to x.
wrt	integer; Selects the regressor to differentiate with respect to (vectorized).
eval.points	numeric or options: ("mean", median", "last", "all"); Regressor points to be evaluated. (eval.points = "median") (default) to find the average partial derivative at the median of the variable with respect to. Set to (eval.points = "last") to find the average partial derivative at the last observation of the variable with respect to (relevant for time-series data). Set to (eval.points="mean") to find the average partial derivative at the mean of the variable with respect to. Set to (eval.points = "all") to find the average partial derivative at every observation of the variable with respect to.
folds	integer; 5 (default) Sets the number of folds in the NNS.stack procedure for optimal n.best parameter.
mixed	logical; FALSE (default) If mixed derivative is to be evaluated, set (mixed = TRUE).
plot	logical; FALSE (default) Set to (plot = TRUE) to view plot. Default setting is

(noise.reduction = "mean").

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ncores integer; value specifying the number of cores to be used in the parallelized procedure. If NULL (default), the number of cores to be used is equal to the number

of cores of the machine - 1.

messages logical; TRUE (default) Prints status messages of cross-validation on n. best pa-

rameter for NNS.reg.

#### Value

#### Returns:

- dy.d\_(...)\$"First" the 1st derivative
- dy.d\_(...)\$"Second" the 2nd derivative
- dy.d\_(...)\$"Mixed" the mixed derivative (for two independent variables only).

#### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
## Not run:
set.seed(123) ; x_1 \leftarrow runif(100) ; x_2 \leftarrow runif(100) ; y \leftarrow x_1 ^2 \times x_2 ^2
B \leftarrow cbind(x_1, x_2)
## To find average partial derivative of y wrt 1st regressor,
only supply 1 value in [eval.points]:
dy.d_{B}, y, wrt = 1, eval.points = c(.5)
dy.d_{B}, y, wrt = 1, eval.points = mean(B[, 1]))
## To find average partial derivative of y wrt 1st regressor,
for every oberservation of 1st regressor:
apd <- dy.d_(B, y, wrt = 1, eval.points = "all")
plot(B[,1], apd[[1]])
## 95% Confidence Interval to test if 0 is within
### Lower CI
LPM.VaR(.025, 0, apd)
### Upper CI
UPM.VaR(.025, 0, apd)
## To find derivatives of y wrt 1st regressor and specified 2nd regressor points
dy.d_{B}, y, wrt = 1, eval.points = c(.5, .5))
## Known function analysis: [y = a ^2 * b ^2]
x_1 \leftarrow seq(0, 1, .1); x_2 \leftarrow seq(0, 1, .1)
B \leftarrow expand.grid(x_1, x_2) ; y \leftarrow B[, 1]^2 * B[, 2]^2
```

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```
dy.d_(B, y, wrt = 1, eval.points = c(.5, .5))
## End(Not run)
```

LPM

Lower Partial Moment

# Description

This function generates a univariate lower partial moment for any degree or target.

# Usage

```
LPM(degree, target, variable)
```

# **Arguments**

degree integer; (degree = 0) is frequency, (degree = 1) is area.

target numeric; Typically set to mean, but does not have to be. (Vectorized)

variable a numeric vector.

# Value

LPM of variable

# Author(s)

Fred Viole, OVVO Financial Systems

### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
set.seed(123)
x <- rnorm(100)
LPM(0, mean(x), x)</pre>
```

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LPM.ratio

Lower Partial Moment RATIO

# **Description**

This function generates a standardized univariate lower partial moment for any degree or target.

### Usage

```
LPM.ratio(degree, target, variable)
```

#### **Arguments**

```
degree integer; (degree = 0) is frequency, (degree = 1) is area.
```

target numeric; Typically set to mean, but does not have to be. (Vectorized)

variable a numeric vector.

#### Value

Standardized LPM of variable

#### Author(s)

Fred Viole, OVVO Financial Systems

# References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995
```

Viole, F. (2017) "Continuous CDFs and ANOVA with NNS" https://ssrn.com/abstract=3007373

```
set.seed(123)
x <- rnorm(100)
LPM.ratio(0, mean(x), x)

## Not run:
## Empirical CDF (degree = 0)
lpm_cdf <- LPM.ratio(0, sort(x), x)
plot(sort(x), lpm_cdf)

## Continuous CDF (degree = 1)
lpm_cdf_1 <- LPM.ratio(1, sort(x), x)
plot(sort(x), lpm_cdf_1)

## Joint CDF
x <- rnorm(5000) ; y <- rnorm(5000)
plot3d(x, y, Co.LPM(0, 0, sort(x), sort(y), x, y), col = "blue", xlab = "X", ylab = "Y", zlab = "Probability", box = FALSE)

## End(Not run)</pre>
```

LPM.VaR

LPM.VaR LPM VaR

## **Description**

Generates a value at risk (VaR) quantile based on the Lower Partial Moment ratio.

# Usage

```
LPM.VaR(percentile, degree, x)
```

# Arguments

percentile numeric [0, 1]; The percentile for left-tail VaR (vectorized).

degree integer; (degree = 0) for discrete distributions, (degree = 1) for continuous

distributions.

x a numeric vector.

#### Value

Returns a numeric value representing the point at which "percentile" of the area of x is below.

# Author(s)

Fred Viole, OVVO Financial Systems

# References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

# **Examples**

```
set.seed(123)
x <- rnorm(100)
## For 5% quantile, left-tail
LPM.VaR(0.05, 0, x)</pre>
```

NNS.ANOVA

NNS ANOVA

# Description

Analysis of variance (ANOVA) based on lower partial moment CDFs for multiple variables. Returns a degree of certainty the difference in sample means is zero, not a p-value.

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#### Usage

```
NNS.ANOVA(
  control,
  treatment,
  confidence.interval = 0.95,
  tails = "Both",
  pairwise = FALSE,
  plot = TRUE,
  binary = TRUE
)
```

#### **Arguments**

control a numeric vector, matrix or data frame.

treatment NULL (default) a numeric vector, matrix or data frame.

confidence.interval

numeric [0, 1]; The confidence interval surrounding the control mean when

(binary = TRUE). Defaults to (confidence.interval = 0.95).

tails options: ("Left", "Right", "Both"). tails = "Both"(Default) Selects the tail of

the distribution to determine effect size.

pairwise logical; FALSE (defualt) Returns pairwise certainty tests when set to pairwise

= TRUE.

plot logical; TRUE (default) Returns the boxplot of all variables along with grand

mean identification. When (binary = TRUE), returns the boxplot of both variables along with grand mean identification and confidence interval thereof.

binary logical; TRUE (default) Selects binary analysis between a control and treatment

variable.

# Value

For (binary = FALSE) returns the degree certainty the difference in sample means is zero [0, 1]. For (binary = TRUE) returns:

- "Control Mean"
- "Treatment Mean"
- "Grand Mean"
- "Control CDF"
- "Treatment CDF"
- "Certainty" the certainty of the same population statistic
- "Lower Bound Effect" and "Upper Bound Effect" the effect size of the treatment for the specified confidence interval

### Author(s)

Fred Viole, OVVO Financial Systems

### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

NNS.ARMA

### **Examples**

```
### Binary analysis and effect size
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.ANOVA(control = x, treatment = y)

### Two variable analysis with no control variable
A <- cbind(x, y)
NNS.ANOVA(A)

### Multiple variable analysis with no control variable
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100) ; z <- rnorm(100)
A <- cbind(x, y, z)
NNS.ANOVA(A)</pre>
```

NNS.ARMA

NNS ARMA

# **Description**

Autoregressive model incorporating nonlinear regressions of component series.

# Usage

```
NNS.ARMA(
  variable,
  h = 1,
  training.set = NULL,
  seasonal.factor = TRUE,
  weights = NULL,
  best.periods = 2,
  negative.values = FALSE,
  method = "nonlin",
  dynamic = FALSE,
  plot = TRUE,
  seasonal.plot = TRUE,
  conf.intervals = NULL,
  ncores = NULL
)
```

### **Arguments**

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seasonal.factor

logical or integer(s); TRUE (default) Automatically selects the best seasonal lag from the seasonality test. To use weighted average of all seasonal lags set to (seasonal.factor = FALSE). Otherwise, directly input known frequency integer lag to use, i.e. (seasonal.factor = 12) for monthly data. Multiple frequency integers can also be used, i.e. (seasonal.factor = c(12, 24, 36))

weights

numeric; NULL (default) sets the weights of the seasonal.factor vector when specified as integers. If (weights = NULL) each seasonal.factor is weighted on its NNS.seas result and number of observations it contains.

best.periods

integer; [2] (default) used in conjuction with (seasonal.factor = FALSE), uses the best.periods number of detected seasonal lags instead of ALL lags when (seasonal.factor = FALSE).

negative.values

logical; FALSE (default) If the variable can be negative, set to (negative.values = TRUE). If there are negative values within the variable, negative.values will automatically be detected.

method

options: ("lin", "nonlin", "both"); "nonlin" (default) To select the regression type of the component series, select (method = "both") where both linear and nonlinear estimates are generated. To use a nonlineaer regression, set to (method = "nonlin"); to use a linear regression set to (method = "lin").

dynamic

logical; FALSE (default) To update the seasonal factor with each forecast point, set to (dynamic = TRUE). The default is (dynamic = FALSE) to retain the original seasonal factor from the inputted variable for all ensuing h.

plot

logical; TRUE (default) Returns the plot of all periods exhibiting seasonality and the variable level reference in upper panel. Lower panel returns original data and forecast.

seasonal.plot

logical; TRUE (default) Adds the seasonality plot above the forecast. Will be set to FALSE if no seasonality is detected or seasonal. factor is set to an integer value.

conf.intervals numeric [0, 1]; NULL (default) Plots and returns the associated confidence intervals for the final estimate. Constructed using the maximum entropy bootstap meboot on the final estimates.

ncores

integer; value specifying the number of cores to be used in the parallelized procedure. If NULL (default), the number of cores to be used is equal to half the number of cores of the machine - 1.

# Value

Returns a vector of forecasts of length (h) if no conf. intervals specified. Else, returns a data.table with the forecasts as well as lower and upper confidence intervals per forecast point.

### Note

For monthly data series, increased accuracy may be realized from forcing seasonal factors to multiples of 12. For example, if the best periods reported are: {37, 47, 71, 73} use (seasonal.factor = c(36, 48, 72).

(seasonal.factor = FALSE) can be a very comutationally expensive exercise due to the number of seasonal periods detected.

If error encountered when (seasonal.factor = TRUE):

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```
"NaNs produced Error in seq.default(length(variable)+1,1,-lag[i]): wrong sign in 'by' argument"
use the combination of (seasonal.factor = FALSE,best.periods = 1).
```

#### Author(s)

Fred Viole, OVVO Financial Systems

#### References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

Viole, F. (2019) "Forecasting Using NNS" https://ssrn.com/abstract=3382300
```

### **Examples**

```
## Nonlinear NNS.ARMA using AirPassengers monthly data and 12 period lag
## Not run:
NNS.ARMA(AirPassengers, h = 45, training.set = 100, seasonal.factor = 12, method = "nonlin")
## Linear NNS.ARMA using AirPassengers monthly data and 12, 24, and 36 period lags
NNS.ARMA(AirPassengers, h = 45, training.set = 120, seasonal.factor = c(12, 24, 36), method = "lin")
## Nonlinear NNS.ARMA using AirPassengers monthly data and 2 best periods lag
NNS.ARMA(AirPassengers, h = 45, training.set = 120, seasonal.factor = FALSE, best.periods = 2)
## End(Not run)
```

NNS.ARMA.optim

NNS ARMA Optimizer

# Description

Wrapper function for optimizing any combination of a given seasonal.factor vector in NNS.ARMA. Minimum sum of squared errors (forecast-actual) is used to determine optimum across all NNS.ARMA methods.

### Usage

```
NNS.ARMA.optim(
  variable,
  training.set,
  seasonal.factor,
  negative.values = FALSE,
  obj.fn = expression(sum((predicted - actual)^2)),
  objective = "min",
  linear.approximation = TRUE,
  print.trace = TRUE,
  ncores = NULL
)
```

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#### **Arguments**

variable a numeric vector.

training.set numeric; Sets the number of variable observations as the training set. See Note

below for recommended uses.

seasonal.factor

integers; Multiple frequency integers considered for NNS.ARMA model, i.e.

(seasonal.factor = c(12, 24, 36))

negative.values

logical; FALSE (default) If the variable can be negative, set to (negative.values

= TRUE).

obj.fn expression; expression(sum((predicted -actual)^2)) (default) Sum of squared

errors is the default objective function. Any expression() using the specific

terms predicted and actual can be used.

objective options: ("min", "max") "min" (default) Select whether to minimize or maxi-

mize the objective function obj.fn.

linear.approximation

logical; TRUE (default) Uses the best linear output from NNS. reg to generate a

nonlinear and mixture regression for comparison. FALSE is a more exhaustive

search over the objective space.

print.trace logical; TRUE (defualt) Prints current iteration information. Suggested as backup

in case of error, best parameters to that point still known and copyable!

ncores integer; value specifying the number of cores to be used in the parallelized pro-

cedure. If NULL (default), the number of cores to be used is equal to half the

number of cores of the machine.

#### Value

Returns a list containing:

- \$period a vector of optimal seasonal periods
- \$weights the optimal weights of each seasonal period between an equal weight or NULL weighting
- \$obj. fn the objective function value
- \$method the method identifying which NNS.ARMA method was used.
- \$bias.shift a numerical result of the overall bias of the optimum objective function result. To be added to the final result when using the NNS.ARMA with the derived parameters.

#### Note

- Typically, (training.set = length(variable) -2 \* length(forecast horizon)) is used for optimization. Smaller samples would use (training.set = length(variable) -length(forecast horizon)) in order to preserve information.
- The number of combinations will grow prohibitively large, they should be kept as small as possible. seasonal.factor containing an element too large will result in an error. Please reduce the maximum seasonal.factor.
- If variable cannot logically assume negative values, then the \$bias.shift must be limited to 0 via a pmax(0,...) call.

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#### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

### **Examples**

```
## Nonlinear NNS.ARMA period optimization using 2 yearly lags on AirPassengers monthly data
## Not run:
nns.optims <- NNS.ARMA.optim(AirPassengers[1:132], training.set = 120,
seasonal.factor = seq(12, 24, 6))

## Then use optimal parameters in NNS.ARMA to predict 12 periods in-sample.
## Note the {$bias.shift} usage in the {NNS.ARMA} function:
nns.estimates <- NNS.ARMA(AirPassengers, h = 12, training.set = 132,
seasonal.factor = nns.optims$periods, method = nns.optims$method) + nns.optims$bias.shift

## If variable cannot logically assume negative values
nns.estimates <- pmax(0, nns.estimates)

## End(Not run)</pre>
```

 ${\tt NNS.boost}$ 

NNS Boost

# **Description**

Ensemble method for classification using the predictions of the NNS multivariate regression NNS.reg collected from uncorrelated feature combinations.

# Usage

```
NNS.boost(
  IVs.train,
  DV.train,
  IVs.test = NULL,
  type = NULL,
  representative.sample = FALSE,
  depth = "max",
  n.best = NULL,
  learner.trials = 100,
  epochs = NULL,
  CV.size = 0.25,
  ts.test = NULL,
  folds = 5,
  threshold = NULL,
  obj.fn = expression(sum((predicted - actual)^2)),
  objective = "min",
```

NNS.boost

```
extreme = FALSE,
  feature.importance = TRUE,
  status = TRUE,
  ncores = NULL
)
```

# **Arguments**

IVs. train a matrix or data frame of variables of numeric or factor data types.

DV. train a numeric or factor vector with compatible dimsensions to (IVs. train).

IVs. test a matrix or data frame of variables of numeric or factor data types with compat-

ible dimsensions to (IVs.train). If NULL, will use (IVs.train) as default.

type NULL (default). To perform a classification of disrete integer classes from fac-

tor target variable (DV.train), set to (type = "CLASS"), else for continuous

(DV. train) set to (type = NULL).

representative.sample

logical; FALSE (default) Reduces observations of IVs. train to a set of repre-

sentative observations per regressor.

depth options: (integer, NULL, "max"); Specifies the order parameter in the NNS.reg

routine, assigning a number of splits in the regressors. (depth = "max")(default) will be significantly faster, but increase the variance of results, which is sug-

gested for mixed continuous and discrete (unordered, ordered) data.

 $\hbox{n.best} \qquad \qquad \hbox{integer; NULL (default) Sets the number of nearest regression points to use in} \\$ 

weighting for multivariate regression at sqrt(# of regressors). Analogous to k in a k Nearest Neighbors algorithm. If NULL, determines the optimal clusters

via the NNS.stack procedure.

 $learner.\,trials\ \ integer; NULL\,(default)\,Sets\,the\,number\,of\,trials\,to\,obtain\,an\,accuracy\,threshold$ 

level. (learner.trials = 100) is the default setting.

epochs integer; 2\*length(DV.train) (default) Total number of feature combinations

to run.

CV. size numeric [0, 1]; (CV. size = .25) (default) Sets the cross-validation size. De-

faults to 0.25 for a 25 percent random sampling of the training set.

ts. test integer; NULL (default) Sets the length of the test set for time-series data; typ-

ically 2\*h parameter value from NNS.ARMA or double known periods to fore-

cast.

folds integer; 5 (default) Sets the number of folds in the NNS.stack procedure for

optimal n.best parameter.

threshold numeric; NULL (default) Sets the obj. fn threshold to keep feature combinations.

obj.fn expression; expression( sum((predicted -actual)^2) ) (default) Sum of squared

errors is the default objective function. Any expression() using the specific terms predicted and actual can be used. Automatically selects an accuracy

measure when (type = "CLASS").

objective options: ("min", "max") "max" (default) Select whether to minimize or maxi-

mize the objective function obj.fn.

extreme logical; FALSE (default) Uses the maximum (minimum) threshold obtained

from the learner  $.\,trials,$  rather than the upper (lower) quintile level for max-

imization (minimization) objective.

feature.importance

logical; TRUE (default) Plots the frequency of features used in the final estimate.

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status logical; TRUE (default) Prints status update message in console.

ncores integer; value specifying the number of cores to be used in the parallelized pro-

cedure. If NULL (default), the number of cores to be used is equal to the number

of cores of the machine - 1.

#### Value

Returns a vector of fitted values for the dependent variable test set \$results, and the final feature loadings \$feature.weights.

#### Note

Like a logistic regression, the (type = "CLASS") setting is not necessary for target variable of two classes e.g. [0, 1].

# Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. (2016) "Classification Using NNS Clustering Analysis" https://ssrn.com/abstract=2864711

# **Examples**

```
## Using 'iris' dataset where test set [IVs.test] is 'iris' rows 141:150.
## Not run:
a <- NNS.boost(iris[1:140, 1:4], iris[1:140, 5],
IVs.test = iris[141:150, 1:4],
epochs = 100, learner.trials = 100,
type = "CLASS")

## Test accuracy
mean( a$results == as.numeric(iris[141:150, 5]))
## End(Not run)</pre>
```

NNS.caus

NNS Causation

# **Description**

Returns the causality from observational data between two variables.

# Usage

```
NNS.caus(x, y, factor.2.dummy = FALSE, tau = 0, plot = FALSE)
```

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# **Arguments**

X	a numeric vector, matrix or data frame.
У	NULL (default) or a numeric vector with compatible dimsensions to x.
factor.2.dummy	$logical; {\it FALSE} \ (default) \ Automatically \ augments \ variable \ matrix \ with \ numerical \ dummy \ variables \ based \ on \ the \ levels \ of \ factors. \ Includes \ dependent \ variable \ y.$
tau	options: ("cs", "ts", integer); 0 (default) Number of lagged observations to consider (for time series data). Otherwise, set (tau = "cs") for cross-sectional data. (tau = "ts") automatically selects the lag of the time series data, while (tau = [integer]) specifies a time series lag.
plot	logical; FALSE (default) Plots the raw variables, tau normalized, and cross-normalized variables.

#### Value

Returns the directional causation  $(x \longrightarrow y)$  or  $(y \longrightarrow x)$  and net quantity of association. For causal matrix, directional causation is returned as ([column variable]  $\longrightarrow$  [row variable]). Negative numbers represent causal direction attributed to [row variable].

# Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

# **Examples**

```
## Not run:
## x causes y...
set.seed(123)
x <- rnorm(1000) ; y <- x ^ 2
NNS.caus(x, y, tau = "cs")

## Causal matrix without per factor causation
NNS.caus(iris, tau = 0)

## Causal matrix with per factor causation
NNS.caus(iris, factor.2.dummy = TRUE, tau = 0)

## End(Not run)</pre>
```

NNS.CDF

NNS CDF

# **Description**

This function generates an empirical CDF using partial moment ratios LPM.ratio, and resulting survival, hazard and cumulative hazard functions.

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#### Usage

```
NNS.CDF(variable, degree = 0, target = NULL, type = "CDF", plot = TRUE)
```

#### **Arguments**

variable a numeric vector or data.frame of 2 variables for joint CDF.

degree integer; (degree = 0) (default) is frequency, (degree = 1) is area.

target numeric; NULL (default) Must lie within support of each variable.

type options("CDF", "survival", "hazard", "cumulative hazard"); "CDF" (default) Se-

lects type of function to return for bi-variate analysis. Multivariate analysis is

restricted to "CDF".

plot logical; plots CDF.

#### Value

### Returns:

- "Function" a data.table containing the observations and resulting CDF of the variable.
- "target.value" value from the target argument.

### Author(s)

Fred Viole, OVVO Financial Systems

#### References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995
```

Viole, F. (2017) "Continuous CDFs and ANOVA with NNS" https://ssrn.com/abstract=3007373

```
set.seed(123)
x <- rnorm(100)
NNS.CDF(x)

## Not run:
## Empirical CDF (degree = 0)
NNS.CDF(x)

## Continuous CDF (degree = 1)
NNS.CDF(x, 1)

## Joint CDF
x <- rnorm(5000) ; y <- rnorm(5000)
A <- cbind(x,y)

NNS.CDF(A, 0)

## Joint CDF with target
NNS.CDF(A, 0, target = c(0,0))

## End(Not run)</pre>
```

NNS.cor

N	NS	•	cor	-

NNS Correlation

# **Description**

Returns the nonlinear correlation between two variables based on higher order partial moment matrices measured by frequency or area.

#### Usage

```
NNS.cor(x, y = NULL, order = NULL, degree = NULL)
```

# **Arguments**

x a numeric vector, matrix or data frame.

y NULL (default) or a numeric vector with compatible dimsensions to x.

order integer; Controls the level of quadrant partitioning. Defualts to (order = NULL).

Errors can generally be rectified by setting (order = 1).

degree integer; (degree = 0) is frequency based correlations, while (degree = 1) is

for area based correlations. Defaults to (degree = 0) for smaller number of

observations.

#### Value

Returns nonlinear correlation coefficient between two variables, or nonlinear correlation matrix for matrix input.

### Note

p-values and confidence intervals can be obtained from sampling random permutations of  $y_p$  and running NNS.  $dep(x,y_p)$  to compare against a null hypothesis of 0 correlation or independence between x,y.

See NNS.dep for examples.

#### Author(s)

Fred Viole, OVVO Financial Systems

# References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
## Not run:
set.seed(123)
## Pairwise Correlation
x <- rnorm(100) ; y <- rnorm(100)
NNS.cor(x, y)</pre>
```

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```
## Correlation Matrix
x <- rnorm(100) ; y <- rnorm(100) ; z<-rnorm(100)
B <- cbind(x, y, z)
NNS.cor(B)
## End(Not run)</pre>
```

NNS.dep

NNS Dependence

### **Description**

Returns the dependence and nonlinear correlation between two variables based on higher order partial moment matrices measured by frequency or area.

# Usage

```
NNS.dep(
   x,
   y = NULL,
   order = 3,
   degree = NULL,
   asym = FALSE,
   print.map = FALSE,
   ncores = NULL
)
```

# **Arguments**

x a numeric vector, matrix or data frame.

y NULL (default) or a numeric vector with compatible dimsensions to x.

order integer; Controls the level of quadrant partitioning. Defaults to (order = 3).

Errors can generally be rectified by setting (order = 1).

degree integer; Defaults to NULL to allow number of observations to be "degree" determinant.

asym logical; FALSE (default) Allows for asymmetrical dependencies.

print.map logical; FALSE (default) Plots quadrant means.

integer; value specifying the number of cores to be used in the parallelized pro-

cedure. If NULL (default), the number of cores to be used is equal to the number

of cores of the machine - 1.

#### Value

ncores

Returns the bi-variate "Correlation" and "Dependence" or correlation / dependence matrix for matrix input.

# Note

p-values and confidence intervals can be obtained from sampling random permutations of  $y_p$  and running NNS.  $dep(x,y_p)$  to compare against a null hypothesis of 0 correlation or independence between x,y.

NNS.dep

#### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
## Not run:
set.seed(123)
x <- rnorm(100); y <- rnorm(100)
NNS.dep(x, y)
## Correlation / Dependence Matrix
x \leftarrow rnorm(100); y \leftarrow rnorm(100); z \leftarrow rnorm(100)
B \leftarrow cbind(x, y, z)
NNS.dep(B)
## p-values for [NNS.dep]
x \leftarrow seq(-5, 5, .1); y \leftarrow x^2 + rnorm(length(x))
nns\_cor\_dep \leftarrow NNS.dep(x, y, print.map = TRUE)
nns_cor_dep
\#\# Create permutations of y
y_p <- replicate(1000, sample.int(length(y)))</pre>
## Generate new correlation and dependence measures on each new permutation of y
nns.mc \leftarrow apply(y_p, 2, function(g) NNS.dep(x, y[g]))
## Store results
cors <- unlist(lapply(nns.mc, "[[", 1))</pre>
deps <- unlist(lapply(nns.mc, "[[", 2))</pre>
## View results
hist(cors)
hist(deps)
## Left tailed correlation p-value
cor_p_value <- LPM(0, nns_cor_dep$Correlation, cors)</pre>
cor_p_value
## Right tailed correlation p-value
cor_p_value <- UPM(0, nns_cor_dep$Correlation, cors)</pre>
cor_p_value
## Confidence Intervals
## For 95th percentile VaR (both-tails) see [LPM.VaR] and [UPM.VaR]
## Lower CI
LPM.VaR(.025, 0, cors)
## Upper CI
UPM.VaR(.025, 0, cors)
```

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```
## Left tailed dependence p-value
dep_p_value <- LPM(0, nns_cor_dep$Dependence, deps)
dep_p_value

## Right tailed dependence p-value
dep_p_value <- UPM(0, nns_cor_dep$Dependence, deps)
dep_p_value

## End(Not run)</pre>
```

NNS.dep.base

NNS Dependence Base

# Description

Internal function for NNS dependence NNS.dep parallel instances.

# Usage

```
NNS.dep.base(
    x,
    y = NULL,
    order = NULL,
    degree = NULL,
    type = NULL,
    print.map = FALSE,
    asym = FALSE
)
```

# Arguments

```
x from NNS.part
y from NNS.part
order from NNS.part
degree from NNS.part
type from NNS.part
print.map from NNS.part
```

asym for asymmetrical dependecies

### Value

Returns NNS dependence.

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NNS.dep.hd

NNS Co-Partial Moments Higher Dimension Dependence

# Description

Determines higher dimension dependence coefficients based on degree 0 co-partial moments.

# Usage

```
NNS.dep.hd(x, plot = FALSE, independence.overlay = FALSE)
```

### **Arguments**

x a numeric matrix or data frame.

plot logical; FALSE (default) Generates a 3d scatter plot with regression points using

plot3d.

independence.overlay

logical; FALSE (default) Creates and overlays independent Co.LPM and Co.UPM regions to visually reference the difference in dependence from the data.frame of variables being analyzed. Under independence, the light green and red shaded areas would be occupied by green and red data points respectively.

# Value

- \$actual.observations Number of Co.LPM and Co.UPM observations.
- \$independent.null Expected number of Co.LPM and Co.UPM observations under the null hypothesis of independence.
- \$Dependence Multivariate nonlinear dependence coefficient [0,1]

# Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. (2016) "Beyond Correlation: Using the Elements of Variance for Conditional Means and Probabilities" http://ssrn.com/abstract=2745308.

```
set.seed(123)  x \leftarrow rnorm(1000) ; y \leftarrow rnorm(1000) ; z \leftarrow rnorm(1000) \\ A \leftarrow data.frame(x, y, z) \\ NNS.dep.hd(A, plot = TRUE, independence.overlay = TRUE)
```

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NNS.diff NNS Numerical Differentiation	NNS.diff	NNS Numerical Differentiation	
--	----------	-------------------------------	--

# Description

Determines numerical derivative of a given function using projected secant lines on the y-axis. These projected points infer finite steps h, in the finite step method.

# Usage

```
NNS.diff(f, point, h = 0.1, tol = 1e-10, print.trace = FALSE)
```

# Arguments

f	an expression or call or a formula with no lhs.
point	numeric; Point to be evaluated for derivative of a given function f.
h	numeric $[0,]$ ; Initial step for secant projection. Defaults to (h = 0.1).
tol	numeric; Sets the tolerance for the stopping condition of the inferred h. Defualts to $(tol = 1e-10)$ .
print.trace	logical; FALSE (default) Displays each iteration, lower y-intercept, upper y-intercept and inferred h.

### Value

Returns a matrix of values, intercepts, derivatives, inferred step sizes for multiple methods of estimation.

# Author(s)

Fred Viole, OVVO Financial Systems

# References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
f <- function(x) sin(x) / x
NNS.diff(f, 4.1)</pre>
```

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NNS.distance

NNS Distance

# **Description**

Internal kernel function for NNS multivariate regression NNS.reg parallel instances.

# Usage

```
NNS.distance(rpm, dist.estimate, type, k)
```

# Arguments

rpm REGRESSION.POINT.MATRIX from NNS.reg

dist.estimate Vector to generate distances from.

type "L1", "L2" or "DTW" k n.best from NNS.reg

#### Value

Returns sum of weighted distances.

NNS.FSD

NNS FSD Test

# Description

Bi-directional test of first degree stochastic dominance using lower partial moments.

# Usage

```
NNS.FSD(x, y, type = "discrete")
```

# **Arguments**

x a numeric vector.y a numeric vector.

type options: ("discrete", "continuous"); "discrete" (default) selects the type of

CDF.

### Value

Returns one of the following FSD results: "X FSD Y", "Y FSD X", or "NO FSD EXISTS".

# Author(s)

Fred Viole, OVVO Financial Systems

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#### References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

Viole, F. (2017) "A Note on Stochastic Dominance." https://ssrn.com/abstract=3002675.

# **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.FSD(x, y)</pre>
```

NNS.FSD.uni

NNS FSD Test uni-directional

# Description

Uni-directional test of first degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

# Usage

```
NNS.FSD.uni(x, y, type = "discrete")
```

### **Arguments**

```
    x a numeric vector.
    y a numeric vector.
    type options: ("discrete", "continuous"); "discrete" (default) selects the type of CDF.
```

### Value

```
Returns (1) if "X FSD Y", else (0).
```

#### Author(s)

Fred Viole, OVVO Financial Systems

### References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

Viole, F. (2017) "A Note on Stochastic Dominance." https://ssrn.com/abstract=3002675.

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.FSD.uni(x, y)</pre>
```

NNS.meboot

NNS.meboot NNS meboot

# Description

Adapted maximum entropy bootstrap routine from meboot https://cran.r-project.org/package=meboot.

# Usage

```
NNS.meboot(
  х,
  reps = 999,
  setSpearman = NULL,
  drift = TRUE,
  trim = 0.1,
  xmin = NULL,
  xmax = NULL,
  reachbnd = TRUE,
  expand.sd = TRUE,
  force.clt = TRUE,
  scl.adjustment = FALSE,
  sym = FALSE,
  elaps = FALSE,
  colsubj,
  coldata,
  coltimes,
)
```

# Arguments

x	vector of data, ts object or pdata. frame object.
reps	numeric; number of replicates to generate.
setSpearman	numeric [0,1]; The default setting setSpearman = NULL assumes that the user does not want to generate replicates that are perfectly dependent on original time series, setSpearman=1 recovers the original meboot() settings. setSpearman < 1 admits less perfect (more realistic for some purposes) dependence.
drift	logical; TRUE default preserves the drift of the original series.
trim	numeric [0,1]; The mean trimming proportion, defaults to trim=0.1.
xmin	numeric; the lower limit for the left tail.
xmax	numeric; the upper limit for the right tail.
reachbnd	logical; If TRUE potentially reached bounds (xmin = smallest value - trimmed mean and xmax = largest value + trimmed mean) are given when the random draw happens to be equal to 0 and 1, respectively.
expand.sd	logical; If TRUE the standard deviation in the ensemble is expanded. See expand. sd in $meboot: meboot$ .
force.clt	logical; If TRUE the ensemble is forced to satisfy the central limit theorem. See

force.clt in meboot::meboot.

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scl.adjustment	logical; If TRUE scale adjustment is performed to ensure that the population variance of the transformed series equals the variance of the data.
sym	logical; If TRUE an adjustment is performed to ensure that the ME density is symmetric.
elaps	logical; If TRUE elapsed time during computations is displayed.
colsubj	numeric; the column in $x$ that contains the individual index. It is ignored if the input data $x$ is not a pdata. frame object.
coldata	numeric; the column in x that contains the data of the variable to create the ensemble. It is ignored if the input data x is not a pdata. frame object.
coltimes	numeric; an optional argument indicating the column that contains the times at which the observations for each individual are observed. It is ignored if the input data x is not a pdata. frame object.
• • •	possible argument fiv to be passed to expand.sd.

#### Value

- x original data provided as input.
- replicates maximum entropy bootstrap replicates.
- ensemble average observation over all replicates.
- xx sorted order stats (xx[1] is minimum value).
- z class intervals limits.
- · dv deviations of consecutive data values.
- dvtrim trimmed mean of dv.
- xmin data minimum for ensemble=xx[1]-dvtrim.
- xmax data x maximum for ensemble=xx[n]+dvtrim.
- desintxb desired interval means.
- ordxx ordered x values.
- kappa scale adjustment to the variance of ME density.
- elaps elapsed time.

### References

- Vinod, H.D. (2013), Maximum Entropy Bootstrap Algorithm Enhancements. http://ssrn.com/abstract=2285041.
- Vinod, H.D. (2006), Maximum Entropy Ensembles for Time Series Inference in Economics, *Journal of Asian Economics*, **17**(6), pp. 955-978.
- Vinod, H.D. (2004), Ranking mutual funds using unconventional utility theory and stochastic dominance, *Journal of Empirical Finance*, **11**(3), pp. 353-377.

```
## Not run:

# To generate an orthogonal rank correlated time-series to AirPassengers boots <- NNS.meboot(AirPassengers, reps=100, setSpearman = 0, xmin = 0)

# Verify correlation of replicates ensemble to original cor(boots$ensemble, AirPassengers, method = "spearman")

# Plot all replicates
```

NNS.norm

```
matplot(boots$replicates, type = 'l')
# Plot ensemble
lines(boots$ensemble, lwd = 3)
## End(Not run)
```

NNS.norm

NNS Normalization

#### **Description**

Normalizes a matrix of variables based on nonlinear scaling normalization method.

# Usage

```
NNS.norm(A, linear = FALSE, chart.type = NULL, location = "topleft")
```

# **Arguments**

A a numeric matrix or data frame.

linear logical; FALSE (default) Performs a linear scaling normalization, resulting in

equal means for all variables.

chart.type options: ("1", "b"); NULL (default). Set (chart.type = "1") for line, (chart.type

= "b") for boxplot.

location Sets the legend location within the plot, per the x and y co-ordinates used in base

graphics legend.

# Value

Returns a data.frame of normalized values.

# Author(s)

Fred Viole, OVVO Financial Systems

# References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
set.seed(123)
x <- rnorm(100) ; y<-rnorm(100)
A <- cbind(x, y)
NNS.norm(A)</pre>
```

NNS.part 33

NNS Partition Map NNS.part

#### **Description**

Creates partitions based on partial moment quadrant means, iteratively assigning identifications to observations based on those quadrants (unsupervised partitional and hierarchial clustering method). Basis for correlation NNS.cor, dependence NNS.dep, regression NNS.reg routines.

### Usage

```
NNS.part(
  х,
  Voronoi = FALSE,
  type = NULL,
  order = NULL,
  obs.req = 10,
  min.obs.stop = TRUE,
  noise.reduction = "off"
)
```

#### **Arguments**

х a numeric vector. a numeric vector with compatible dimsensions to x. У Voronoi logical; FALSE (default) Displays a Voronoi type diagram using partial moment quadrants. type NULL (default) Controls the partitioning basis. Set to (type = "XONLY") for Xaxis based partitioning. Defaults to NULL for both X and Y-axis partitioning. integer; Number of partial moment quadrants to be generated. (order = "max") order will institute a perfect fit. obs.req integer; (10 default) Required observations per cluster where quadrants will not be further partitioned if observations are not greater than the entered value. Reduces minimum number of necessary observations in a quadrant to 1 when (obs.req = 1).min.obs.stop logical; TRUE (default) Stopping condition where quadrants will not be further

partitioned if a single cluster contains less than the entered value of obs. req.

noise.reduction

the method of determing regression points options: ("mean", "median", "mode", "off"); (noise.reduction = "mean") uses means for partitions. (noise.reduction = "median") uses medians instead of means for partitions, while (noise.reduction = "mode") uses modes instead of means for partitions. Defaults to (noise.reduction

= "off") where an overall central tendency measure is used.

# Value

Returns:

NNS.PDF

• "dt" a data.table of x and y observations with their partition assignment "quadrant" in the 3rd column and their prior partition assignment "prior.quadrant" in the 4th column.

- "regression.points" the data.table of regression points for that given (order = ...).
- "order" the order of the final partition given "min.obs.stop" stopping condition.

#### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

# **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.part(x, y)

## Data.table of observations and partitions
NNS.part(x, y, order = 1)$dt

## Regression points
NNS.part(x, y, order = 1)$regression.points

## Voronoi style plot
NNS.part(x, y, Voronoi = TRUE)

## Examine final counts by quadrant
DT <- NNS.part(x, y)$dt
DT[ , counts := .N, by = quadrant]
DT</pre>
```

NNS.PDF

NNS PDF

# Description

This function generates an empirical PDF using dy.dx on NNS.CDF.

# Usage

```
NNS.PDF(variable, degree = 1, target = NULL, bins = NULL, plot = TRUE)
```

# Arguments

variable	a numeric vector.
degree	integer; (degree = 0) is frequency, (degree = 1) (default) is area.
target	a numeric range of values $[a,b]$ where $a < b$ . NULL (default) uses the variable observations.
bins	numeric; NULL (default) Selects number of observations as default number of bins.
plot	logical; plots PDF.

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#### Value

Returns a data.table containing the intervals used and resulting PDF of the variable.

### Author(s)

Fred Viole, OVVO Financial Systems

#### References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995
```

# **Examples**

```
set.seed(123)
x <- rnorm(100)
NNS.PDF(x)
## Custom target range
NNS.PDF(x, target = c(-5, 5))</pre>
```

NNS.reg

NNS Regression

# **Description**

Generates a nonlinear regression based on partial moment quadrant means.

# Usage

```
NNS.reg(
  Х,
  у,
  factor.2.dummy = TRUE,
  order = NULL,
  stn = 0.95,
  dim.red.method = NULL,
  tau = NULL,
  type = NULL,
  point.est = NULL,
  location = "top",
  return.values = TRUE,
  plot = TRUE,
  plot.regions = FALSE,
  residual.plot = TRUE,
  std.errors = FALSE,
  confidence.interval = NULL,
  threshold = 0,
  n.best = NULL,
  noise.reduction = "off",
  dist = "L2",
```

NNS.reg

```
ncores = NULL,
multivariate.call = FALSE
)
```

# **Arguments**

x a vector, matrix or data frame of variables of numeric or factor data types.

y a numeric or factor vector with compatible dimsensions to x.

factor . 2 . dummy logical; TRUE (default) Automatically augments variable matrix with numerical

dummy variables based on the levels of factors.

order integer; Controls the number of partial moment quadrant means. Users are en-

couraged to try different (order = ...) integer settings with (noise.reduction

= "off"). (order = "max") will force a limit condition perfect fit.

stn numeric [0, 1]; Signal to noise parameter, sets the threshold of (NNS.dep) which

reduces ("order") when (order = NULL). Defaults to 0.95 to ensure high de-

pendence for higher ("order") and endpoint determination.

dim.red.method options: ("cor", "NNS.dep", "NNS.caus", "all", NULL) method for determin-

ing synthetic  $X^*$  coefficients. Selection of a method automatically engages the dimension reduction regression. The default is NULL for full multivariate regression. (dim.red.method = "NNS.dep") uses NNS.dep for nonlinear dependence weights, while (dim.red.method = "NNS.caus") uses NNS.caus for causal weights. (dim.red.method = "cor") uses standard linear correlation for weights. (dim.red.method = "all") averages all methods for further feature

engineering.

tau options("ts", NULL); NULL(default) To be used in conjuction with (dim.red.method

= "NNS.caus") or (dim.red.method = "all"). If the regression is using time-

series data, set (tau = "ts") for more accurate causal analysis.

type NULL (default). To perform a classification, set to (type = "CLASS"). Like a

logistic regression, it is not necessary for target variable of two classes e.g. [0,

1].

point.est a numeric or factor vector with compatible dimsensions to x. Returns the fitted

value y.hat for any value of x.

location Sets the legend location within the plot, per the x and y co-ordinates used in base

graphics legend.

return.values logical; TRUE (default), set to FALSE in order to only display a regression plot

and call values as needed.

plot logical; TRUE (default) To plot regression.

plot.regions logical; FALSE (default). Generates 3d regions associated with each regression

point for multivariate regressions. Note, adds significant time to routine.

residual.plot logical; TRUE (default) To plot y.hat and Y.

std.errors logical; FALSE (default) To provide standard errors of each linear segment in the

"Fitted.xy" output.

confidence.interval

numeric [0, 1]; NULL (default) Plots the associated confidence interval with the

estimate and reports the standard error for each individual segment.

threshold numeric [0, 1]; (threshold = 0) (default) Sets the threshold for dimension re-

duction of independent variables when (dim.red.method) is not NULL.

NNS.reg 37

n.best

integer; NULL (default) Sets the number of nearest regression points to use in weighting for multivariate regression at sqrt(# of regressors). (n.best = "all") will select and weight all generated regression points. Analogous to k in a k Nearest Neighbors algorithm. Different values of n.best are tested using cross-validation in NNS.stack.

noise.reduction

the method of determing regression points options: ("mean", "median", "mode", "off"); In low signal:noise situations, (noise.reduction = "mean") uses means for NNS.dep restricted partitions, (noise.reduction = "median") uses medians instead of means for NNS.dep restricted partitions, while (noise.reduction

= "mode") uses modes instead of means for NNS.dep restricted partitions. (noise.reduction

= "off") uses an overall central tendency measure for partitions.

dist

options:("L1", "L2", "DTW", "FACTOR") the method of distance calculation; Selects the distance calculation used. dist = "L2" (default) selects the Euclidean distance and (dist = "L1") seclects the Manhattan distance; (dist = "DTW") selects the dynamic time warping distance; (dist = "FACTOR") uses a frequency.

ncores

integer; value specifying the number of cores to be used in the parallelized procedure. If NULL (default), the number of cores to be used is equal to the number of cores of the machine - 1.

multivariate.call

Internal parameter for multivariate regressions.

#### Value

### UNIVARIATE REGRESSION RETURNS THE FOLLOWING VALUES:

- "R2" provides the goodness of fit;
- "SE" returns the overall standard error of the estimate between y and y.hat;
- "Prediction.Accuracy" returns the correct rounded "Point.est" used in classifications versus the categorical y;
- "derivative" for the coefficient of the x and its applicable range;
- "Point.est" for the predicted value generated;
- "regression.points" provides the points used in the regression equation for the given order of partitions;
- "Fitted.xy" returns a data.table of x, y, y.hat, resid, NNS.ID, gradient;

#### MULTIVARIATE REGRESSION RETURNS THE FOLLOWING VALUES:

- "R2" provides the goodness of fit;
- "equation" returns the numerator of the synthetic X\* dimension reduction equation as a data.table consisting of regressor and its coefficient. Denominator is simply the length of all coefficients > 0, returned in last row of equation data.table.
- "x.star" returns the synthetic  $X^*$  as a vector;
- "rhs.partitions" returns the partition points for each regressor x;
- "RPM" provides the Regression Point Matrix, the points for each x used in the regression equation for the given order of partitions;
- "Point.est" returns the predicted value generated;
- "Fitted.xy" returns a data.table of x,y, y.hat, gradient, and NNS.ID.

NNS.reg

#### Note

Please ensure point.est is of compatible dimensions to x, error message will ensue if not compatible.

### Author(s)

Fred Viole, OVVO Financial Systems

#### References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995
```

Vinod, H. and Viole, F. (2017) "Nonparametric Regression Using Clusters" https://link.springer.com/article/10.1007/s10614-017-9713-5

Vinod, H. and Viole, F. (2018) "Clustering and Curve Fitting by Line Segments" https://www.preprints.org/manuscript/201801.0090/v1

```
## Not run:
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.reg(x, y)
## Manual {order} selection
NNS.reg(x, y, order = 2)
## Maximum {order} selection
NNS.reg(x, y, order = "max")
## x-only paritioning (Univariate only)
NNS.reg(x, y, type = "XONLY")
## For Multiple Regression:
x \leftarrow cbind(rnorm(100), rnorm(100), rnorm(100)); y \leftarrow rnorm(100)
NNS.reg(x, y, point.est = c(.25, .5, .75))
## For Multiple Regression based on Synthetic X* (Dimension Reduction):
x \leftarrow cbind(rnorm(100), rnorm(100), rnorm(100)); y \leftarrow rnorm(100)
NNS.reg(x, y, point.est = c(.25, .5, .75), dim.red.method = "cor")
## IRIS dataset examples:
# Dimension Reduction:
NNS.reg(iris[,1:4], iris[,5], dim.red.method = "cor", order = 5)
# Dimension Reduction using causal weights:
NNS.reg(iris[,1:4], iris[,5], dim.red.method = "NNS.caus", order = 5)
# Multiple Regression:
NNS.reg(iris[,1:4], iris[,5], order = 2, noise.reduction = "off")
# Classification:
NNS.reg(iris[,1:4], iris[,5], point.est = iris[1:10, 1:4], type = "CLASS")$Point.est
## To call fitted values:
```

NNS.SD.efficient.set 39

```
x <- rnorm(100); y <- rnorm(100)
NNS.reg(x, y)$Fitted
## To call partial derivative (univariate regression only):
NNS.reg(x, y)$derivative
## End(Not run)</pre>
```

```
NNS.SD.efficient.set NNS SD Efficient Set
```

### **Description**

Determines the set of stochastic dominant variables for various degrees.

# Usage

```
NNS.SD.efficient.set(x, degree, type = "discrete")
```

## Arguments

```
x a numeric matrix or data frame.

degree numeric options: (1, 2, 3); Degree of stochastic dominance test from (1, 2 or 3).

type options: ("discrete", "continuous"); "discrete" (default) selects the type of CDF.
```

### Value

Returns set of stochastic dominant variable names.

#### Author(s)

Fred Viole, OVVO Financial Systems

### References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

Viole, F. (2017) "A Note on Stochastic Dominance." https://ssrn.com/abstract=3002675.

```
set.seed(123)
x <- rnorm(100) ; y<-rnorm(100) ; z<-rnorm(100)
A <- cbind(x, y, z)
NNS.SD.efficient.set(A, 1)</pre>
```

40 NNS.seas

NNS.seas	NNS Seasonality Test	

### **Description**

Seasonality test based on the coefficient of variation for the variable and lagged component series. A result of 1 signifies no seasonality present.

### Usage

```
NNS.seas(variable, modulo = NULL, mod.only = TRUE, plot = TRUE)
```

### Arguments

variable	a numeric vector.
modulo	integer(s); NULL (default) Used to find the nearest multiple(s) in the reported seasonal period.
mod.only	logical; codeTRUE (default) Limits the number of seasonal periods returned to the specified modulo.
plot	logical; TRUE (default) Returns the plot of all periods exhibiting seasonality and the variable level reference.

#### Value

Returns a matrix of all periods exhibiting less coefficient of variation than the variable with "all.periods"; and the single period exhibiting the least coefficient of variation versus the variable with "best.period"; as well as a vector of "periods" for easy call into NNS.ARMA.optim. If no seasonality is detected, NNS.seas will return ("No Seasonality Detected").

### Author(s)

Fred Viole, OVVO Financial Systems

### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
set.seed(123)
x <- rnorm(100)

## To call strongest period based on coefficient of variation:
NNS.seas(x, plot = FALSE)$best.period

## Using modulos for logical seasonal inference:
NNS.seas(x, modulo = c(2,3,5,7), plot = FALSE)</pre>
```

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NNS.SSD

NNS SSD Test

### **Description**

Bi-directional test of second degree stochastic dominance using lower partial moments.

### Usage

```
NNS.SSD(x, y)
```

# **Arguments**

```
x a numeric vector.y a numeric vector.
```

### Value

Returns one of the following SSD results: "X SSD Y", "Y SSD X", or "NO SSD EXISTS".

#### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

# **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.SSD(x, y)</pre>
```

NNS.SSD.uni

NNS SSD Test uni-directional

# Description

Uni-directional test of second degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

```
NNS.SSD.uni(x, y)
```

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#### **Arguments**

```
x a numeric vector.
y a numeric vector.
```

#### Value

```
Returns (1) if "X SSD Y", else (0).
```

#### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

# **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.SSD.uni(x, y)</pre>
```

NNS.stack

NNS Stack

# Description

Prediction model using the predictions of the NNS base models NNS.reg as features (i.e. meta-features) for the stacked model.

```
NNS.stack(
  IVs.train,
  DV.train,
  IVs.test = NULL,
  type = NULL,
  obj.fn = expression(sum((predicted - actual)^2)),
  objective = "min",
  dist = "L2",
  CV.size = NULL,
  ts.test = NULL,
  folds = 5,
  order = NULL,
  norm = NULL,
  method = c(1, 2),
  stack = TRUE,
  dim.red.method = "cor",
  status = TRUE,
  ncores = NULL
)
```

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#### **Arguments**

IVs.train a vector, matrix or data frame of variables of numeric or factor data types. DV.train a numeric or factor vector with compatible dimsensions to (IVs.train).

IVs.test a vector, matrix or data frame of variables of numeric or factor data types with compatible dimsensions to (IVs.train). If NULL, will use (IVs.train) as

default.

type NULL (default). To perform a classification of disrete integer classes from factor target variable (DV.train), set to (type = "CLASS"), else for continuous (DV. train) set to (type = NULL). Like a logistic regression, this setting is not

necessary for target variable of two classes e.g. [0, 1].

obj.fn expression; expression(sum((predicted -actual)^2)) (default) Sum of squared

errors is the default objective function. Any expression() using the specific

terms predicted and actual can be used.

objective options: ("min", "max") "min" (default) Select whether to minimize or maxi-

mize the objective function obj. fn.

dist options:("L1", "L2", "DTW", "FACTOR") the method of distance calculation;

> Selects the distance calculation used. dist = "L2" (default) selects the Euclidean distance and (dist = "L1") seclects the Manhattan distance; (dist = "DTW") selects the dynamic time warping distance; (dist = "FACTOR") uses a

frequency.

CV.size numeric [0, 1]; NULL (default) Sets the cross-validation size if (IVs.test =

NULL). Defaults to 0.25 for a 25 percent random sampling of the training set

under (CV.size = NULL).

integer; NULL (default) Sets the length of the test set for time-series data; typts.test

ically 2\*h parameter value from NNS.ARMA or double known periods to fore-

folds integer; folds = 5 (default) Select the number of cross-validation folds.

options: (integer, "max", NULL); NULL (default) Sets the order for NNS.reg, order

where (order = "max") is the k-nearest neighbors equivalent, which is sug-

gested for mixed continuous and discrete (unordered, ordered) data.

options: ("std", "NNS", NULL); NULL (default) 3 settings offered: NULL, "std", norm

and "NNS". Selects the norm parameter in NNS.reg.

method numeric options: (1, 2); Select the NNS method to include in stack. (method =

1) selects NNS.reg; (method = 2) selects NNS.reg dimension reduction regression. Defaults to method = c(1,2), which will reduce the dimension first, then

find the optimal n.best.

logical; TRUE (default) Uses dimension reduction output in n. best optimization, stack

otherwise performs both analyses independently.

options: ("cor", "NNS.dep", "NNS.caus", "all") method for determining syndim.red.method

> thetic  $X^*$  coefficients. (dim.red.method = "cor") (default) uses standard linear correlation for weights. (dim. red. method = "NNS. dep") uses NNS. dep for nonlinear dependence weights, while (dim.red.method = "NNS.caus") uses NNS.caus for causal weights. (dim.red.method = "all") averages all meth-

ods for further feature engineering.

status logical; TRUE (default) Prints status update message in console.

integer; value specifying the number of cores to be used in the parallelized subncores

routine NNS.reg. If NULL (default), the number of cores to be used is equal to

the number of cores of the machine - 1.

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#### Value

Returns a vector of fitted values for the dependent variable test set for all models.

- "NNS.reg.n.best" returns the optimum "n.best" paramater for the NNS.reg multivariate regression. "SSE.reg" returns the SSE for the NNS.reg multivariate regression.
- "OBJfn.reg" returns the obj.fn for the NNS.reg regression.
- "NNS.dim.red.threshold" returns the optimum "threshold" from the NNS.reg dimension reduction regression.
- "OBJfn.dim.red" returns the obj.fn for the NNS.reg dimension reduction regression.
- "reg" returns NNS.reg output.
- "dim. red" returns NNS.reg dimension reduction regression output.
- "stack" returns the output of the stacked model.

#### Note

- Like a logistic regression, the (type = "CLASS") setting is not necessary for target variable of two classes e.g. [0, 1].
- Missing data should be handled prior as well using na.omit or complete.cases on the full dataset.

If error received:

```
"Error in is.data.frame(x): object 'RP' not found" reduce the CV.size.
```

### Author(s)

Fred Viole, OVVO Financial Systems

### References

```
Viole, F. (2016) "Classification Using NNS Clustering Analysis" https://ssrn.com/abstract=2864711
```

```
## Using 'iris' dataset where test set [IVs.test] is 'iris' rows 141:150.
## Not run:
NNS.stack(iris[1:140, 1:4], iris[1:140, 5], IVs.test = iris[141:150, 1:4], type = "CLASS")

## Using 'iris' dataset to determine [n.best] and [threshold] with no test set.
NNS.stack(iris[ , 1:4], iris[ , 5], type = "CLASS")

## Selecting NNS.reg and dimension reduction techniques.
NNS.stack(iris[1:140, 1:4], iris[1:140, 5], iris[141:150, 1:4], method = c(1, 2), type = "CLASS")
## End(Not run)
```

NNS.term.matrix 45

NNS.term.matrix

NNS Term Matrix

### **Description**

Generates a term matrix for text classification use in NNS.reg.

#### Usage

```
NNS.term.matrix(x, oos = NULL, names = FALSE)
```

#### **Arguments**

x	Text A two column dataset should be used. Concatenate text from original sources to comply with format. Also note the possibility of factors in "DV", so "as.numeric(as.character())" is used to avoid issues.
oos	Out-of-sample text dataset to be classified.
names	Column names for "IV" and "oos". Defaults to FALSE.

#### Value

Returns the text as independent variables "IV" and the classification as the dependent variable "DV". Out-of-sample independent variables are returned with "OOS".

### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

46 NNS.TSD.uni

NNS.TSD

NNS TSD Test

### **Description**

Bi-directional test of third degree stochastic dominance using lower partial moments.

### Usage

```
NNS.TSD(x, y)
```

# **Arguments**

x a numeric vector.y a numeric vector.

### Value

Returns one of the following TSD results: "X TSD Y", "Y TSD X", or "NO TSD EXISTS".

#### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

# **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.TSD(x, y)</pre>
```

NNS.TSD.uni

NNS TSD Test uni-directional

### **Description**

Uni-directional test of third degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

```
NNS.TSD.uni(x, y)
```

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### **Arguments**

```
x a numeric vector.y a numeric vector.
```

#### Value

```
Returns (1) if "X TSD Y", else (0).
```

### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

### **Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.TSD.uni(x, y)</pre>
```

NNS.VAR

NNS VAR

# Description

Nonparametric vector autoregressive model incorporating NNS.ARMA estimates of variables into NNS.reg for a multi-variate time-series forecast.

```
NNS.VAR(
  variables,
  h,
  tau = 1,
  dim.red.method = "cor",
  obj.fn = expression(sum((predicted - actual)^2)),
  objective = "min",
  status = TRUE,
  ncores = NULL
)
```

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### **Arguments**

variables a numeric matrix or data.frame of contemporaneous time-series to forecast. h integer; 1 (default) Number of periods to forecast. positive integer [ > 0]; 1 (default) Number of lagged observations to consider tau for the time-series data. Vector for single lag for each respective variable or list for multiple lags per each variable. dim.red.method options: ("cor", "NNS.dep", "NNS.caus", "all") method for reducing regressors via NNS.stack. (dim.red.method = "cor") (default) uses standard linear correlation for dimension reduction in the lagged variable matrix. (dim.red.method = "NNS.dep") uses NNS.dep for nonlinear dependence weights, while (dim.red.method = "NNS.caus") uses NNS.caus for causal weights. (dim.red.method = "all") averages all methods for further feature engineering. obj.fn expression; expression(sum((predicted -actual)^2)) (default) Sum of squared errors is the default objective function. Any expression() using the specific terms predicted and actual can be used. options: ("min", "max") "min" (default) Select whether to minimize or maxiobjective mize the objective function obj.fn. status logical; TRUE (default) Prints status update message in console.

### Value

ncores

Returns the following matrices of forecasted variables:

"interpolated\_and\_extrapolated" Returns a data.table of the linear interpolated and NNS.ARMA
extrapolated values to replace NA values in the original variables argument. This is required
for working with variables containing different frequencies, e.g. where NA would be reported
for intra-quarterly data when indexed with monthly periods.

integer; value specifying the number of cores to be used in the parallelized sub-

routine NNS.ARMA.optim. If NULL (default), the number of cores to be used

"relevant\_variables" Returns the relevant variables from the dimension reduction step.

is equal to the number of cores of the machine - 1.

- "univariate" Returns the univariate NNS.ARMA forecasts.
- "multivariate" Returns the multi-variate NNS.reg forecasts.
- "ensemble" Returns the ensemble of both "univariate" and "multivariate" forecasts.

### Note

- dim.red.method = "cor" is significantly faster than the other methods, but comes at the expense of ignoring possible nonlinear relationships between lagged variables.
- Not recommended for factor variables, even after transformed to numeric. NNS.reg is better suited for factor or binary regressor extrapolation.

### Author(s)

Fred Viole, OVVO Financial Systems

NNS.VAR 49

#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

Viole, F. (2019) "Multi-variate Time-Series Forecasting: Nonparametric Vector Autoregression Using NNS" https://ssrn.com/abstract=3489550

Viole, F. (2020) "NOWCASTING with NNS" https://ssrn.com/abstract=3586658

Viole, F. (2019) "Forecasting Using NNS" https://ssrn.com/abstract=3382300

Vinod, H. and Viole, F. (2017) "Nonparametric Regression Using Clusters" https://link.springer.com/article/10.1007/s10614-017-9713-5

Vinod, H. and Viole, F. (2018) "Clustering and Curve Fitting by Line Segments" https://www.

### **Examples**

preprints.org/manuscript/201801.0090/v1

```
## Not run:
### Standard Nonparametric Vector Autoregression ###
set.seed(123)
x \leftarrow rnorm(100); y \leftarrow rnorm(100); z \leftarrow rnorm(100)
A \leftarrow cbind(x = x, y = y, z = z)
### Using lags 1:4 for each variable
NNS.VAR(A, h = 12, tau = 4, status = TRUE)
 ### Using lag 1 for variable 1, lag 3 for variable 2 and lag 3 for variable 3
NNS.VAR(A, h = 12, tau = c(1,3,3), status = TRUE)
### Using lags c(1,2,3) for variables 1 and 3, while using lags c(4,5,6) for variable 2
NNS.VAR(A, h = 12, tau = list(c(1,2,3), c(4,5,6), c(1,2,3)), status = TRUE)
### NOWCASTING with Mixed Frequencies ###
library(Quandl)
econ_variables <- Quandl(c("FRED/GDPC1", "FRED/UNRATE", "FRED/CPIAUCSL"),type = 'ts',</pre>
                      order = "asc", collapse = "monthly", start_date="2000-01-01")
 ### Note the missing values that need to be imputed
head(econ_variables)
tail(econ_variables)
NNS.VAR(econ_variables, h = 12, tau = 12, status = TRUE)
## End(Not run)
```

50 PM.matrix

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Partial Moment Matrix

### **Description**

This function generates a co-partial moment matrix for the specified co-partial moment.

### Usage

```
PM.matrix(LPM.degree, UPM.degree, target = "mean", variable, pop.adj = FALSE)
```

### Arguments

LPM.degree	integer; Degree for variable below target deviations. (degree = 0) is frequency, (degree = 1) is area.	
UPM.degree	integer; Degree for variable above target deviations. (degree = 0) is frequency, (degree = 1) is area.	
target	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized) (target = "mean") (default) will set the target as the mean of every variable.	
variable	a numeric matrix or data.frame.	
pop.adj	logical; FALSE (default) Adjusts the sample co-partial moment matrices for population statistics.	

#### Value

Matrix of partial moment quadrant values (CUPM, DUPM, DLPM, CLPM), and overall covariance matrix. Uncalled quadrants will return a matrix of zeros.

# Note

For divergent asymmetical "D.LPM" and "D.UPM" matrices, matrix is D.LPM(column, row, ...).

# Author(s)

Fred Viole, OVVO Financial Systems

#### References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995
```

Viole, F. (2017) "Bayes' Theorem From Partial Moments" https://ssrn.com/abstract=3457377

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100) ; z <- rnorm(100)
A <- cbind(x,y,z)
PM.matrix(LPM.degree = 1, UPM.degree = 1, target = "mean", variable = A)
## Use of vectorized numeric targets (target_x, target_y, target_z)</pre>
```

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```
PM.matrix(LPM.degree = 1, UPM.degree = 1, target = c(0, 0.15, .25), variable = A)
## Calling Individual Partial Moment Quadrants
cov.mtx <- PM.matrix(LPM.degree = 1, UPM.degree = 1, target = "mean", variable = A)
cov.mtx$cupm
## Full covariance matrix
cov.mtx$cov.matrix</pre>
```

UPM

Upper Partial Moment

# Description

This function generates a univariate upper partial moment for any degree or target.

#### Usage

```
UPM(degree, target, variable)
```

### **Arguments**

degree integer; (degree = 0) is frequency, (degree = 1) is area.

target numeric; Typically set to mean, but does not have to be. (Vectorized)

variable a numeric vector.

### Value

UPM of variable

### Author(s)

Fred Viole, OVVO Financial Systems

#### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
set.seed(123)
x <- rnorm(100)
UPM(0, mean(x), x)</pre>
```

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UPM.ratio

Upper Partial Moment RATIO

### **Description**

This function generates a standardized univariate upper partial moment for any degree or target.

### Usage

```
UPM.ratio(degree, target, variable)
```

### Arguments

```
degree integer; (degree = 0) is frequency, (degree = 1) is area.
```

target numeric; Typically set to mean, but does not have to be. (Vectorized)

variable a numeric vector.

#### Value

Standardized UPM of variable

# Author(s)

Fred Viole, OVVO Financial Systems

### References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" https://www.amazon.com/dp/1490523995

```
set.seed(123)
x <- rnorm(100)
UPM.ratio(0, mean(x), x)

## Joint Upper CDF
## Not run:
x <- rnorm(5000) ; y <- rnorm(5000)
plot3d(x, y, Co.UPM(0, 0, sort(x), sort(y), x, y), col = "blue", xlab = "X", ylab = "Y",
zlab = "Probability", box = FALSE)

## End(Not run)</pre>
```

UPM. VaR

# **Description**

Generates an upside value at risk (VaR) quantile based on the Upper Partial Moment ratio

### Usage

```
UPM.VaR(percentile, degree, x)
```

### **Arguments**

percentile numeric [0, 1]; The percentile for right-tail VaR (vectorized).

degree integer; (degree = 0) for discrete distributions, (degree = 1) for continuous

distributions.

x a numeric vector.

### Value

Returns a numeric value representing the point at which "percentile" of the area of x is above.

```
set.seed(123)
x <- rnorm(100)
## For 5% quantile, right-tail
UPM.VaR(0.05, 0, x)</pre>
```

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