Package 'NNS'

June 20, 2017

Type Package

Version 0.3.4 **Date** 2017-06-20

Title Nonlinear Nonparametric Statistics

Author Fred Viole
Maintainer Fred Viole <ovvo.financial.systems@gmail.com></ovvo.financial.systems@gmail.com>
Description Nonlinear nonparametric statistics using partial moments. Partial moments are the elements of variance and asymptotically approximate the area of f(x). These robust statistics provide the basis for nonlinear analysis while retaining linear equivalences. NNS offers: Numerical integration, Numerical differentiation, Clustering, Correlation, Dependence, Causal analysis, ANOVA, Regression, Classification, Seasonality, Autoregressive modelling, Normalization and Stochastic dominance. All routines based on: Viole, F. and Nawrocki, D. (2013), Nonlinear Nonparametric Statistics: Using Partial Moments (ISBN: 1490523995).
License GPL-3
LazyData TRUE
RoxygenNote 6.0.1
Depends R (>= 3.3.0), data.table, rgl, stringr
Suggests knitr, rmarkdown
VignetteBuilder knitr
R topics documented:
Co.LPM Co.UPM D.LPM D.UPM dy.dx dy.d_ LPM LPM LPM. LPM.VaR NNS.ANOVA

Co.LPM

Index		34
	UPM.VaR	32
	01112	31
	1110.102.001	31
	NNS.TSD	30
	NNS.term.matrix	29
	111 Olduck	27
	NNS.SSD.uni	27
	NNS.SSD	26
	NNS.seas	25
	NNS.SD.Efficient.Set	24
	Tribines	21
	NNS.part	20
	NNS.norm	19
	NNS.FSD.uni	18
	NNS.FSD	18
	NNS.diff	17

Description

This function generates a co-lower partial moment for between two equal length variables for any degree or target.

Usage

```
Co.LPM(degree.x, degree.y, x, y, target.x, target.y)
```

Arguments

degree.x	integer; Degree for variable X. (degree.x = 0) is frequency, (degree.x = 1) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
X	a numeric vector.
У	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

Value

Co-LPM of two variables

Author(s)

Fred Viole, OVVO Financial Systems

Co.UPM 3

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
Co.LPM(0,0,x,y,mean(x),mean(y))</pre>
```

Co.UPM

Co-Upper Partial Moment (Upper Right Quadrant 1)

Description

This function generates a co-upper partial moment between two equal length variables for any degree or target.

Usage

```
Co.UPM(degree.x, degree.y, x, y, target.x, target.y)
```

Arguments

degree.x	integer; Degree for variable X. (degree.x = \emptyset) is frequency, (degree.x = 1) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
X	a numeric vector.
у	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

Value

Co-UPM of two variables

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
Co.UPM(0,0,x,y,mean(x),mean(y))</pre>
```

D.LPM

D.LPM

Divergent-Lower Partial Moment (Lower Right Quadrant 3)

Description

This function generates a divergent lower partial moment between two equal length variables for any degree or target.

Usage

```
D.LPM(degree.x, degree.y, x, y, target.x, target.y)
```

Arguments

degree.x	integer; Degree for variable X. (degree.x = 0) is frequency, (degree.x = 1) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
x	a numeric vector.
у	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

Value

Divergent LPM of two variables

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
D.LPM(0,0,x,y,mean(x),mean(y))</pre>
```

D.UPM 5

D.UPM	Divergent-Upper Partial Moment (Upper Left Quadrant 2)

Description

This function generates a divergent upper partial moment between two equal length variables for any degree or target.

Usage

```
D.UPM(degree.x, degree.y, x, y, target.x, target.y)
```

Arguments

degree.x	integer; Degree for variable X. (degree.x = 0) is frequency, (degree.x = 1) is area.
degree.y	integer; Degree for variable Y. (degree.y = \emptyset) is frequency, (degree.y = 1) is area.
x	a numeric vector.
У	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

Value

Divergent UPM of two variables

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
D.UPM(0,0,x,y,mean(x),mean(y))</pre>
```

6 dy.dx

Description

Returns the numerical partial derivate of y wrt x for a point of interest.

Usage

```
dy.dx(x, y, order = NULL, stn = 0.99, eval.point = median(x),
 deriv.order = 1, h = 0.01, noise.reduction = "mean",
 deriv.method = "FS")
```

Arguments

X	a numeric vector.
У	a numeric vector.
order	integer; Controls the number of partial moment quadrant means. Defaults to (order=NULL) which generates a more accurate derivative for well specified cases.
stn	numeric [0,1]; Signal to noise parameter, sets the threshold of NNS.dep which reduces "order" when (order=NULL). Defaults to 0.99 to ensure high dependence for higher "order" and endpoint determination.
eval.point	numeric; x point to be evaluated. Defaults to (eval.point=median(x)). Set to (eval.points="overall") to find an overall partial derivative estimate.
deriv.order	numeric options: $(1,2)$; 1 (default) For second derivative estimate of $f(x)$, set (deriv.order=2).
h	numeric [0,]; Percentage step used for finite step method. Defaults to h=.01 representing a 1 percent step from the value of the independent variable.
noise.reduction	n

the method of determing regression points options: ("mean", "median", "mode", "off"); In low signal to noise situations, (noise.reduction="median") uses medians instead of means for partitions, while (noise.reduction="mode") uses modes instead of means for partitions. (noise.reduction="off") allows for maximum possible fit in NNS.reg. Default setting is (noise.reduction="mean").

deriv.method

method of derivative estimation, options:("NNS","FS"); Determines the partial derivative from the coefficient of the NNS.reg output when (deriv.method="NNS") or generates a partial derivative using the finite step method (deriv.method="FS") (Defualt).

Value

Returns the value of the partial derivative estimate for the given order.

Author(s)

Fred Viole, OVVO Financial Systems

dy.d_ 7

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

Examples

```
x<-seq(0,2*pi,pi/100); y<-sin(x)
dy.dx(x,y,eval.point=1.75)</pre>
```

dy.d_

Partial Derivative dy/d[wrt]

Description

Returns the numerical partial derivate of y with respect to [wrt] any regressor for a point of interest. Finite difference method is used with NNS.reg estimates as f(x+h) and f(x-h) values.

Usage

```
dy.d_(x, y, wrt, eval.points = "median", order = NULL, stn = 0.9,
h = 0.1, n.best = 2, mixed = FALSE, plot = FALSE,
noise.reduction = "mean")
```

Arguments

x a numeric matrix or data frame.

y a numeric vector with compatible dimsensions to x.

wrt integer; Selects the regressor to differentiate with respect to.

eval.points numeric or options: ("median","last"); Regressor points to be evaluated. Set

to eval.points="median" to find partial derivatives at the median of every variable. Set to eval.points="last" to find partial derivatives at the last value

of every variable.

order integer; NNS.reg "order", defaults to NULL.

stn numeric [0,1]; Signal to noise parameter, sets the threshold of NNS.dep which

reduces "order" when (order=NULL). Defaults to 0.9 to ensure high depen-

dence for higher "order" and endpoint determination.

h numeric [0,...]; Percentage step used for finite step method. Defaults to h=.1

representing a 10 percent step from the value of the regressor.

n.best integer; Sets the number of closest regression points to use in weighting. De-

faults to 2.

mixed logical; FALSE (default) If mixed derivative is to be evaluated, set (mixed=TRUE).

plot logical; FALSE (default) Set to (plot=TRUE) to view plot.

noise.reduction

the method of determing regression points options: ("mean", "median", "mode", "off"); In low signal to noise situations, noise.reduction="median" uses medians instead of means for partitions, while noise.reduction="mode" uses modes instead of means for partitions. noise.reduction="off" allows for maximum possible fit in NNS.reg. Default setting is noise.reduction="mean".

8 LPM

Value

Returns the 1st derivative "First Derivative", 2nd derivative "Second Derivative", and mixed derivative "Mixed Derivative" (for two independent variables only).

Note

For known function testing and analysis, regressors should be transformed via expand.grid to fill the dimensions with (order="max"). Example provided below.

Author(s)

Fred Viole, OVVO Financial Systems

References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" 
http://amzn.com/1490523995
```

Examples

```
set.seed(123);x_1<-runif(100);x_2<-runif(100); y<-x_1^2*x_2^2
B=cbind(x_1,x_2)
## To find derivatives of y wrt 1st regressor
dy.d_(B,y,wrt=1,eval.points=c(.5,.5))
## Known function analysis
x_1<-seq(0,1,.1);x_2<-seq(0,1,.1)
B=expand.grid(x_1,x_2); y<-B[,1]^2*B[,2]^2
dy.d_(B,y,wrt=1,eval.points=c(.5,.5),order="max")</pre>
```

LPM

Lower Partial Moment

Description

This function generates a univariate lower partial moment for any degree or target.

Usage

```
LPM(degree, target, variable)
```

Arguments

```
degree integer; (degree = \emptyset) is frequency, (degree = 1) is area.
```

target numeric; Typically set to mean, but does not have to be. (Vectorized)

variable a numeric vector.

Value

LPM of variable

LPM.VaR

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

Examples

```
set.seed(123)
x<-rnorm(100)
LPM(0,mean(x),x)</pre>
```

LPM.VaR

LPM VaR

Description

Generates a VaR based on the Lower Partial Moment ratio

Usage

```
LPM.VaR(percentile, degree, x, extend = NULL)
```

Arguments

percentile numeric [0,1]; The percentile for left-tail VaR.

degree integer; (degree=0) for discrete distributions, (degree=1) for continuous dis-

tributions.

x a numeric vector.

extend options: ("yes", NULL); NULL (default) Sets the "extendInt" argument from

uniroot.

Value

Returns a numeric value representing the point at which "percentile" of the area of x is above.

Note

If endpoint error is generated, set (extend="yes").

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995 10 NNS.ANOVA

Examples

```
set.seed(123)
x<-rnorm(100)
## For 95th percentile VaR (left-tail)
LPM.VaR(0.95,0,x)</pre>
```

NNS. ANOVA

NNS ANOVA

Description

Analysis of variance (ANOVA) based on lower partial moment CDFs for multiple variables. Returns a degree of certainty the difference in sample means is zero, not a p-value.

Usage

```
NNS.ANOVA(control, treatment, confidence.interval = 0.95, pairwise = FALSE, plot = TRUE, binary = TRUE, extend = NULL)
```

Arguments

control a numeric vector, matrix or data frame.

treatment NULL (default) a numeric vector, matrix or data frame.

confidence.interval

numeric [0,1]; The confidence interval surrounding the control mean when (binary=TRUE).

Defaults to (confidence.interval=0.95).

pairwise logical; FALSE (defualt) Returns pairwise certainty tests when set to pairwise=TRUE.

plot logical; TRUE (default) Returns the boxplot of all variables along with grand

mean identification. When (binary=TRUE), returns the boxplot of both variables along with grand mean identification and confidence interval thereof

ables along with grand mean identification and confidence interval thereof.

binary logical; TRUE (default) Selects binary analysis between a control and treatment

variable.

extend options: ("yes", NULL): NULL (default) Sets the "extendInt" argument from

uniroot.

Value

For (binary=FALSE) returns the degree certainty the difference in sample means is zero [0,1].

For (binary=TRUE) returns "Control Mean", "Treatment Mean", "Grand Mean", "Control CDF", "Treatment CDF", the certainty of the same population statistic "Certainty", the effect size of the treatment for a specified confidence interval with "Lower Bound Effect" and "Upper Bound Effect".

Note

If endpoint error is generated, set (extend="yes").

Author(s)

Fred Viole, OVVO Financial Systems

NNS.ARMA 11

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

Examples

```
### Binary analysis and effect size
set.seed(123)
x<- rnorm(100); y<- rnorm(100)</pre>
NNS.ANOVA(control=x,treatment=y)
### Two variable analysis with no control variable
A<- cbind(x,y)
NNS.ANOVA(A)
### Multiple variable analysis with no control variable
set.seed(123)
x<- rnorm(100); y<- rnorm(100); z<- rnorm(100)
A < - cbind(x,y,z)
NNS.ANOVA(A)
```

NNS.ARMA

NNS ARMA

Description

Autoregressive model incorporating nonlinear regressions of component series.

Usage

```
NNS.ARMA(variable, h = 1, training.set = NULL, seasonal.factor = TRUE,
 best.periods = NULL, negative.values = FALSE, method = "nonlin",
  dynamic = FALSE, plot = TRUE, seasonal.plot = TRUE, intervals = FALSE)
```

Arguments

variable a numeric vector.

h integer; 1 (default) Number of periods to forecast.

NULL (defualt) numeric; Sets the number of variable observations (variable[1:training.set]) training.set

to monitor performance of forecast over in-sample range.

seasonal.factor

logical or integer(s); TRUE (default) Automatically selects the best seasonal lag from the seasonality test. To use weighted average of all seasonal lags set to (seasonal.factor=FALSE). Otherwise, directly input known frequency integer lag to use, i.e. (seasonal.factor=12) for monthly data. Multiple frequency integers can also be used, i.e. (seasonal.factor=c(12,24,36))

integer; to be used in conjuction with (seasonal.factor=FALSE), uses the best.periods

best.periods number of detected seasonal lags instead of ALL lags when (seasonal.factor=FALSE

negative.values

logical; FALSE (default) If the variable can be negative, set to (negative.values=TRUE).

12 NNS.ARMA

method options:("lin","nonlin","both"); "nonlin" (default) To select the regression type of the component series, select (method="both") where both linear and nonlin-

ear estimates are generated. To use a nonlineaer regression, set to (method="nonlin");

to use a linear regression set to (method="lin").

dynamic logical; FALSE (default) To update the seasonal factor with each forecast point,

set to (dynamic=TRUE). The default is (dynamic=FALSE) to retain the original

seasonal factor from the inputted variable for all ensuing h.

plot logical; TRUE (default) Returns the plot of all periods exhibiting seasonality and

the variable level reference in upper panel. Lower panel returns original data

and forecast.

seasonal.plot logical; TRUE (default) Adds the seasonality plot above the forecast. Will be set

to FALSE if no seasonality is detected or seasonal. factor is set to an integer

value.

intervals logical; FALSE (default) Plots the surrounding forecasts around the final estimate

when (intervals=TRUE) and (seasonal.factor=FALSE). There are no other

forecasts to plot when a single seasonal. factor is selected.

Value

Returns a vector of forecasts of length (h).

Note

(seasonal.factor=FALSE) can be a very comutationally expensive exercise due to the number of seasonal periods detected.

If error encountered:

"NaNs produced Error in seq.default(length(variable)+1, 1, -lag[i]): wrong sign in 'by' argument" when (seasonal.factor=TRUE), try the combination of (seasonal.factor=FALSE) and (best.periods=1) as those two settings are equivalent.

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

```
## Nonlinear NNS.ARMA using AirPassengers monthly data and 12 period lag
## Not run:
NNS.ARMA(AirPassengers,h=45,training.set=100,seasonal.factor=12,method='nonlin')
## End(Not run)

## Nonlinear NNS.ARMA using AirPassengers monthly data and 12, 24, and 36 period lags
## Not run:
NNS.ARMA(AirPassengers,h=45,training.set=100,seasonal.factor=c(12,24,36),method='nonlin')
## End(Not run)
```

NNS.caus 13

```
## Nonlinear NNS.ARMA using AirPassengers monthly data and 2 best periods lag
## Not run:
NNS.ARMA(AirPassengers,h=45,training.set=100,seasonal.factor=FALSE,best.periods=2,method='nonlin')
## End(Not run)
```

NNS.caus

NNS Causation

Description

Returns the causality from observational data between two variables

Usage

```
NNS.caus(x, y, tau, plot = FALSE)
```

Arguments

x a numeric vector, matrix or data frame.

y NULL (default) or a numeric vector with compatible dimsensions to x.

tau integer; Number of lagged observations to consider.

plot logical; FALSE (default) Plots the raw variables, tau normalized, and cross-

normalized variables.

Value

Returns the directional causation $(x \longrightarrow y)$ or $(y \longrightarrow x)$ and net quantity of association. For causal matrix, gross quantity of association is returned as $(x[column] \longrightarrow y[row])$.

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

```
## x clearly causes y...
set.seed(123)
x<-rnorm(100); y<-x^2
NNS.caus(x,y,1)
## Causal matrix
## Not run:
NNS.caus(data.matrix(iris),tau = 0)
## End(Not run)</pre>
```

NNS.cor

NNS.cor

NNS Correlation

Description

Returns the nonlinear correlation between two variables based on higher order partial moment matrices measured by frequency or area.

Usage

```
NNS.cor(x, y = NULL, order = NULL, degree = NULL)
```

Arguments

x a numeric vector, matrix or data frame.

y NULL (default) or a numeric vector with compatible dimsensions to x.

order integer; Controls the level of quadrant partitioning. Defualts to (order=NULL).

Errors can generally be rectified by setting (order=1).

degree integer; (degree = 0) is frequency based correlations, while (degree = 1)

is for area based correlations. Defaults to (degree = 0) for smaller number of

observations.

Value

Returns nonlinear correlation coefficient between two variables, or nonlinear correlation matrix for matrix input.

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

```
set.seed(123)
## Pairwise Correlation
x<-rnorm(100); y<-rnorm(100)
NNS.cor(x,y)

## Correlation Matrix
x<-rnorm(100); y<-rnorm(100); z<-rnorm(100)
B<-cbind(x,y,z)
NNS.cor(B)</pre>
```

NNS.cor.hd 15

NNS.cor.hd

NNS Co-Partial Moments Higher Dimension Correlation

Description

Determines higher dimension correlation coefficients based on degree 0 co-partial moments.

Usage

```
NNS.cor.hd(x, plot = FALSE, independence.overlay = FALSE)
```

Arguments

a numeric matrix or data frame.

plot logical; FALSE (default) Generates a 3d scatter plot with regression points using

plot3d.

independence.overlay

logical; FALSE (default) Creates and overlays independent Co.LPM and Co.UPM regions to visually reference the difference in dependence from the data.frame of variables being analyzed. Under independence, the light green and red shaded areas would be occupied by green and red data points respectively.

Value

Returns multivariate nonlinear correlation coefficient

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. (2016) "Beyond Correlation: Using the Elements of Variance for Conditional Means and Probabilities" http://ssrn.com/abstract=2745308.

```
set.seed(123)
x<-rnorm(1000); y<-rnorm(1000); z<-rnorm(1000)
A<-data.frame(x,y,z)
NNS.cor.hd(A,plot=TRUE,independence.overlay=TRUE)</pre>
```

NNS.dep

N	N	S	d	e	c
I٧	I٧	0	u	е	L

NNS Dependence

Description

Returns the dependence and nonlinear correlation between two variables based on higher order partial moment matrices measured by frequency or area.

Usage

```
NNS.dep(x, y = NULL, order = NULL, degree = NULL, print.map = FALSE)
```

Arguments

x	a numeric vector, matrix or data frame.
У	NULL (default) or a numeric vector with compatible dimsensions to x.
order	integer; Controls the level of quadrant partitioning. Defaults to (order=NULL). Errors can generally be rectified by setting (order=1). Will not partition further if less than 4 observations exist in a quadrant.
degree	integer; Defaults to NULL to allow number of observations to be "degree" determinant.
print.map	logical; FALSE (default) Plots quadrant means.

Value

Returns the bi-variate "Correlation" and "Dependence" or correlation / dependence matrix for matrix input.

Author(s)

Fred Viole, OVVO Financial Systems

References

```
Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" 
http://amzn.com/1490523995
```

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
NNS.dep(x,y)
## Correlation / Dependence Matrix
x<-rnorm(100); y<-rnorm(100); z<-rnorm(100)
B<-cbind(x,y,z)
NNS.dep(B)</pre>
```

NNS.diff

Description

Determines numerical derivative of a given function using projected secant lines on the y-axis. These projected points infer finite steps h, in the finite step method.

Usage

```
NNS.diff(f, point, h = 0.1, tol = 1e-10, print.trace = FALSE)
```

Arguments

f	an expression or call or a formula with no lhs.
point	numeric; Point to be evaluated for derivative of a given function f.
h	numeric [0,]; Initial step for secant projection. Defaults to (h=0.1).
tol	numeric; Sets the tolerance for the stopping condition of the inferred h. Defualts to (tol=1e-10).
print.trace	logical; FALSE (default) Displays each iteration, lower y-intercept, upper y-intercept and inferred h.

Value

Returns a matrix of values, intercepts, derivatives, inferred step sizes for multiple methods of estimation.

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

```
f<- function(x) sin(x)/x
NNS.diff(f,4.1)

g<- function(x) sin(x)
NNS.diff(g,1)</pre>
```

18 NNS.FSD.uni

NNS.FSD

NNS FSD Test

Description

Bi-directional test of first degree stochastic dominance using lower partial moments.

Usage

```
NNS.FSD(x, y)
```

Arguments

x a numeric vector.y a numeric vector.

Value

Returns one of the following FSD results: "X FSD Y", "Y FSD X", or "NO FSD EXISTS".

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
NNS.FSD(x,y)</pre>
```

NNS.FSD.uni

NNS FSD Test uni-directional

Description

Uni-directional test of first degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

Usage

```
NNS.FSD.uni(x, y)
```

NNS.norm

Arguments

x a numeric vector.y a numeric vector.

Value

```
Returns (1) if "X FSD Y", else (0).
```

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
NNS.FSD.uni(x,y)</pre>
```

NNS.norm

NNS Normalization

Description

Normalizes a matrix of variables based on nonlinear scaling normalization method.

Usage

```
NNS.norm(A, chart.type = NULL, linear = FALSE)
```

Arguments

A a numeric matrix or data frame.

chart.type options: ("I","b"); NULL (default). Set (chart.type="l") for line, (chart.type="b")

for boxplot.

linear logical; FALSE (default) Performs a linear scaling normalization, resulting in

equal means for all variables.

Value

Returns a data.frame of normalized values.

Author(s)

Fred Viole, OVVO Financial Systems

20 NNS.part

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
A<-cbind(x,y)
NNS.norm(A)</pre>
```

NNS.part

NNS Partition Map

Description

Creates partitions based on partial moment quadrant means, iteratively assigning identifications to observations based on those quadrants (unsupervised partitional and hierarchial clustering method). Basis for correlation NNS.cor, dependence NNS.dep, regression NNS.reg routines.

Usage

```
NNS.part(x, y, Voronoi = FALSE, type = NULL, order = NULL, max.obs = 4,
min.obs.stop = FALSE, noise.reduction = "mean")
```

Arguments

x a numeric vector.

y a numeric vector with compatible dimsensions to x.

Voronoi logical; FALSE (default) Displays a Voronoi type diagram using partial moment

quadrants.

type NULL (default) Controls the partitioning basis. Set to (type="XONLY") for X-

axis based partitioning. Defaults to NULL for both X and Y-axis partitioning.

order integer; Number of partial moment quadrants to be generated. (order="max")

will institute a perfect fit.

max.obs integer; (4 default) Desired observations per cluster where quadrants will not

be further partitioned if observations are not greater than the entered value. Reduces minimum number of necessary observations in a quadrant to 1 when

 $(\max.obs=1).$

min.obs.stop logical; FALSE (default) Stopping condition where quadrants will not be further

partitioned if a single cluster contains less than the entered value of max.obs.

noise.reduction

the method of determing regression points options: ("mean", "median", "mode", "off"); (noise.reduction="median") uses medians instead of means for partitions, while (noise.reduction="mode") uses modes instead of means for partitions. Defaults to (noise.reduction="mean"), while (noise.reduction="off") will partition quadrant to a single observation for a given (order=...).

NNS.reg 21

Value

Returns:

• "dt" a data.table of x and y observations with their partition assignment "quadrant" in the 3rd column and their prior partition assignment "prior.quadrant" in the 4th column.

- "regression.points" the data.table of regression points for that given (order=...).
- "order" the order of the final partition given "min.obs.stop" stopping condition.

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
NNS.part(x,y)

## Data.table of observations and partitions
NNS.part(x,y,order=1)$dt

## Regression points
NNS.part(x,y,order=1)$regression.points

## Voronoi style plot
NNS.part(x,y,Voronoi=TRUE)

## Examine final counts by quadrant
DT=NNS.part(x,y)$dt
DT[,counts := .N,by=quadrant]
DT</pre>
```

NNS.reg

NNS Regression

Description

Generates a nonlinear regression based on partial moment quadrant means.

Usage

```
NNS.reg(x, y, order = NULL, stn = 0.99, dim.red = FALSE, type = NULL,
point.est = NULL, location = "top", return.values = TRUE, plot = TRUE,
plot.regions = FALSE, residual.plot = TRUE, threshold = 0,
n.best = NULL, noise.reduction = "mean", norm = NULL, dist = "L2",
multivariate.call = FALSE)
```

22 NNS.reg

Arguments

x a vector, matrix or data frame of variables of numeric or factor data types.

y a numeric or factor vector with compatible dimsensions to x.

order integer; Controls the number of partial moment quadrant means. Users are en-

couraged to try different (order=...) integer settings with (noise.reduction="off").

(order="max") will force a limit condition perfect fit.

stn numeric [0,1]; Signal to noise parameter, sets the threshold of (NNS.dep) which

reduces ("order") when (order=NULL). Defaults to 0.99 to ensure high dependence for higher ("order") and endpoint determination. (noise.reduction="off")

sets (stn=0) to allow for maximum fit.

dim.red logical; FALSE (default). Set to (dim.red=TRUE) for dimension reduction using

synthetic X*.

type NULL (default). To perform logistic regression, set to (type = "LOGIT"). To

perform a classification, set to (type = "CLASS").

point.est a numeric or factor vector with compatible dimsensions to x. Returns the fitted

value y. hat for any value of x.

location Sets the legend location within the plot, per the x and y co-ordinates used in base

graphics legend.

return.values logical; TRUE (default), set to FALSE in order to only display a regression plot

and call values as needed.

plot logical; TRUE (default) To plot regression.

plot.regions logical; FALSE (default). Generates 3d regions associated with each regression

point for multivariate regressions. Note, adds significant time to routine.

residual.plot logical; TRUE (default) To plot y.hat and Y.

threshold numeric [0,1]; threshold=0 (default) Sets the correlation threshold for inde-

pendent variables.

n.best integer; NULL (default) Sets the number of nearest regression points to use in

weighting for multivariate regression at 2*(# of regressors). (n.best="all")

will select and weight all generated regression points. Analogous to kink Nearest Neighbors

algorithm and different values are tested using cross-validation in NNS.stack.

noise.reduction

the method of determing regression points options: ("mean", "median", "mode", "off"); In low signal:noise situations, (noise.reduction="mean") uses means for NNS.dep restricted partitions, (noise.reduction="median") uses medians instead of means for NNS.dep restricted partitions, while (noise.reduction="mode")

uses modes instead of means for NNS.dep restricted partitions. (noise.reduction="off")

allows for maximum possible fit with a specific order.

norm NULL (default) the method of normalization options: ("NNS", "std", "off"); Nor-

malizes x between 0 and 1 for multivariate regression when set to (norm="std"), or normalizes x according to NNS.norm when set to (norm="NNS"). Uses raw

values when set to (norm="off").

dist options:("L1","L2") the method of distance calculation; Selects the distance cal-

culation used. $\mbox{dist="L2"}$ (default) selects the Euclidean distance and ($\mbox{dist="L1"}$)

seclects the Manhattan distance.

multivariate.call

Internal parameter for multivariate regressions.

NNS.reg 23

Value

UNIVARIATE REGRESSION RETURNS THE FOLLOWING VALUES:

- "R2" provides the goodness of fit;
- "MSE" returns the MSE between y and y.hat;
- "Prediction.Accuracy" returns the correct rounded "Point.est" used in classifications versus the categorical y;
- "derivative" for the coefficient of the x and its applicable range;
- "Point" returns the x point(s) being evaluated;
- "Point.est" for the predicted value generated;
- "regression.points" provides the points used in the regression equation for the given order of partitions;
- "Fitted" returns a vector containing only the fitted values, y.hat;
- "Fitted.xy" returns a data.table of x,y, y.hat, and NNS.ID;

MULTIVARIATE REGRESSION RETURNS THE FOLLOWING VALUES:

- "R2" provides the goodness of fit;
- "equation" returns the numerator of the synthetic X* dimension reduction equation as a data.table consisting of regressor and its coefficient. Denominator is simply the length of all coefficients > 0.
- "x.star" returns the synthetic X* as a vector;
- "rhs.partitions" returns the partition points for each regressor x;
- "RPM" provides the Regression Point Matrix, the points for each x used in the regression equation for the given order of partitions;
- "Point.est" returns the predicted value generated;
- "Fitted" returns a vector containing only the fitted values, y.hat;
- "Fitted.xy" returns a data.table of x,y, y.hat, and NNS.ID.

Note

Please ensure point.est is of compatible dimensions to x, error message will ensue if not compatible. Also, upon visual inspection of the data, if a highly periodic variable is observed set (stn=0) or (order="max") to ensure a proper fit.

Identical regressors can be used as long as they do not share the same name. For instance, NNS.reg(cbind(x,1*x), y) will work as NNS.reg is not affected by multicollinearity.

NNS (>= v.0.3.4) has repurposed parameter (type="CLASS"). (type="CLASS") is now restricted to signifying a classification analysis for NNS.reg while (dim.red=TRUE) enables dimension reduction regressions.

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995 24 NNS.SD.Efficient.Set

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)</pre>
NNS.reg(x,y)
## Manual {order} selection
NNS.reg(x,y,order=2)
## Maximum {order} selection
NNS.reg(x,y,order="max")
## x-only paritioning (Univariate only)
NNS.reg(x,y,type="XONLY")
## Logistic Regression (Univariate only)
NNS.reg(x,y,type="LOGIT")
## For Multiple Regression:
x<-cbind(rnorm(100),rnorm(100)); y<-rnorm(100)</pre>
NNS.reg(x,y,point.est=c(.25,.5,.75))
\#\# For Multiple Regression based on Synthetic X* (Dimension Reduction):
x<-cbind(rnorm(100),rnorm(100),rnorm(100)); y<-rnorm(100)</pre>
NNS.reg(x,y,point.est=c(.25,.5,.75),dim.red=TRUE)
## IRIS dataset example:
#Dimension Reduction:
NNS.reg(iris[,1:4],iris[,5],dim.red=TRUE,order=5)
#Multiple Regression:
NNS.reg(iris[,1:4],iris[,5],order=2,noise.reduction="off")
## To call fitted values:
x<-rnorm(100); y<-rnorm(100)</pre>
NNS.reg(x,y)$Fitted
## To call partial derivative (univariate regression only):
x<-rnorm(100); y<-rnorm(100)</pre>
NNS.reg(x,y)$derivative
```

NNS.SD.Efficient.Set NNS SD Efficient Set

Description

Determines the set of stochastic dominant variables for various degrees.

Usage

```
NNS.SD.Efficient.Set(x, degree)
```

Arguments

```
x a numeric matrix or data frame.

degree numeric options: (1,2,3); Degree of stochastic dominance test from (1,2 or 3).
```

NNS.seas 25

Value

Returns set of stochastic dominant variable names.

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100); z<-rnorm(100)
x<-data.frame(x,y,z)
NNS.SD.Efficient.Set(x,1)</pre>
```

NNS.seas

NNS Seasonality Test

Description

Seasonality test based on the coefficient of variance for the variable and lagged component series. A result of 1 signifies no seasonality present.

Usage

```
NNS.seas(variable, plot = TRUE)
```

Arguments

variable a numeric vector.

plot logical; TRUE (default) Returns the plot of all periods exhibiting seasonality and

the variable level reference.

Value

Returns a matrix of all periods exhibiting less coefficient of variance than the variable with "all.periods"; and the single period exhibiting the least coefficient of variance versus the variable with "best.period". If no seasonality is detected, NNS.seas will return ("No Seasonality Detected").

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995 26 NNS.SSD

Examples

```
set.seed(123)
x<-rnorm(100)
## To call strongest period based on coefficient of variance:
NNS.seas(x)$best.period</pre>
```

NNS.SSD

NNS SSD Test

Description

Bi-directional test of second degree stochastic dominance using lower partial moments.

Usage

```
NNS.SSD(x, y)
```

Arguments

x a numeric vector.y a numeric vector.

Value

Returns one of the following SSD results: "X SSD Y", "Y SSD X", or "NO SSD EXISTS".

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
NNS.SSD(x,y)</pre>
```

NNS.SSD.uni 27

NNS.SSD.uni

NNS SSD Test uni-directional

Description

Uni-directional test of second degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

Usage

```
NNS.SSD.uni(x, y)
```

Arguments

```
x a numeric vector.
y a numeric vector.
```

Value

```
Returns (1) if "X SSD Y", else (0).
```

Author(s)

Fred Viole, OVVO Financial Systems

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
NNS.SSD.uni(x,y)</pre>
```

NNS.stack

NNS stack

Description

Prediction model using the predictions of the NNS base models NNS.reg as features (i.e. meta-features) for the stacked model.

Usage

```
NNS.stack(IVs.train, DV.train, IVs.test = NULL, CV.size = 0.2,
weight = "MSE", precision = "LOW", method = c(1, 2), threshold = 0,
seed = 123)
```

28 NNS.stack

Arguments

IVs.train a vector, matrix or data frame of variables of numeric or factor data types. a numeric or factor vector with compatible dimsensions to (IVs.train). DV.train IVs.test a vector, matrix or data frame of variables of numeric or factor data types. CV.size numeric [0,1]; Sets the cross-validation size if (IVs.test=NULL). Defaults to 0.2 for a 20 percent random sampling of the training set. weight options: ("MSE", "Features") method for selecting model output weight; Set (weight="MSE") for optimum parameters and weighting based on each base model's "MSE". (weight="Feautures") uses a weighting based on the number of features present, whereby logistic NNS.reg receives higher relative weights for more regressors. Defaults to "MSE". precision options: ("LOW", "HIGH"); 2 settings offered: "LOW" (Default) and "HIGH". "HIGH" is the limit condition of every observation as a regression point and uses a (norm="NNS") while (precision="LOW") uses a (norm="std") in NNS.reg. Errors/warnings can generally be reconciled with (precision="LOW"). method numeric options: (1,2); Select the NNS method to include in stack. (method=1) selects NNS.reg; (method=2) selects NNS.reg dimension reduction regression. Defaults to method=c(1,2), including both NNS regression methods in the stack. threshold numeric [0,1]; Sets the correlation threshold for independent variables in NNS.reg. Defaults to (threshold=0). numeric; 123 (default) Sets seed for CV sampling. seed

Value

Returns a vector of fitted values for the dependent variable test set for all models.

- "NNS.reg.n.best" returns the optimum "n.best" paramater for the NNS.reg multivariate regression. "MSE.reg" returns the MSE for the NNS.reg multivariate regression.
- "NNS.dim.red.threshold" returns the optimum "threshold" from the NNS.reg dimension reduction regression.
- "MSE.dim.red" returns the MSE for the NNS.reg dimension reduction regression.
- "reg" returns NNS.reg output.
- "dim. red" returns NNS.reg dimension reduction regression output.
- "stack" returns the output of the stacked model.

Note

If character variables are used, transform them first to factors using as.factor, or data.matrix to ensure overall dataset is numeric. A multifunction sapply can also be applied to the overall dataset: $data <- sapply(data, function(x){as.factor(x);as.numeric(x)})$. Then run NNS.stack with transformed variables.

Author(s)

Fred Viole, OVVO Financial Systems

NNS.term.matrix 29

References

Viole, F. (2016) "Classification Using NNS Clustering Analyis" https://ssrn.com/abstract=2864711

Examples

```
## Using 'iris' dataset where test set [IVs.test] is 'iris' rows 141:150.
## Not run:
NNS.stack(iris[1:140,1:4],iris[1:140,5],IVs.test=iris[141:150,1:4])
## End(Not run)

## Using 'iris' dataset to determine [n.best] and [logistic.order] with no test set.
## Not run:
NNS.stack(iris[,1:4],iris[,5])
## End(Not run)

## Selecting NNS.reg and dimension reduction techniques.
## Not run:
NNS.stack(iris[1:140,1:4],iris[1:140,5],iris[141:150,1:4],method=c(1,2))
## End(Not run)
```

NNS.term.matrix

NNS Term Matrix

Description

Generates a term matrix for text classification use in NNS.reg.

Usage

```
NNS.term.matrix(x, oos = NULL, names = FALSE)
```

Arguments

X	Text A two column dataset should be used. Concatenate text from original sources to comply with format. Also note the possibility of factors in "DV",
	so "as.numeric(as.character())" is used to avoid issues.
00S	Out-of-sample text dataset to be classified.
names	Column names for "IV" and "oos". Defaults to FALSE.

Value

Returns the text as independent variables "IV" and the classification as the dependent variable "DV". Out-of-sample independent variables are returned with "OOS".

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995 NNS.TSD

Examples

NNS.TSD

NNS TSD Test

Description

Bi-directional test of third degree stochastic dominance using lower partial moments.

Usage

```
NNS.TSD(x, y)
```

Arguments

x a numeric vector.
y a numeric vector.

Value

Returns one of the following TSD results: "X TSD Y", "Y TSD X", or "NO TSD EXISTS".

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. http://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817.

NNS.TSD.uni 31

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
NNS.TSD(x,y)</pre>
```

NNS.TSD.uni

NNS TSD Test uni-directional

Description

Uni-directional test of third degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

Usage

```
NNS.TSD.uni(x, y)
```

Arguments

x a numeric vector. y a numeric vector.

Value

```
Returns (1) if "X TSD Y", else (0).
```

Author(s)

Fred Viole, OVVO Financial Systems

Examples

```
set.seed(123)
x<-rnorm(100); y<-rnorm(100)
NNS.TSD.uni(x,y)</pre>
```

UPM

Upper Partial Moment

Description

This function generates a univariate upper partial moment for any degree or target.

Usage

```
UPM(degree, target, variable)
```

32 UPM.VaR

Arguments

degree integer; (degree = 0) is frequency, (degree = 1) is area.

target numeric; Typically set to mean, but does not have to be. (Vectorized)

variable a numeric vector.

Value

UPM of variable

Author(s)

Fred Viole, OVVO Financial Systems

References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" http://amzn.com/1490523995

Examples

```
set.seed(123)
x<-rnorm(100)
UPM(0,mean(x),x)</pre>
```

UPM. VaR

UPM VaR

Description

Generates an upside VaR based on the Upper Partial Moment ratio

Usage

```
UPM.VaR(percentile, degree, x, extend = NULL)
```

Arguments

percentile numeric [0,1]; The percentile for right-tail VaR.

degree integer; (degree=0) for discrete distributions, (degree=1) for continuous dis-

tributions.

x a numeric vector.

extend options: ("yes",NULL); NULL (default) Sets the "extendInt" argument from

uniroot.

Value

Returns a numeric value representing the point at which "percentile" of the area of x is below.

UPM.VaR 33

```
set.seed(123)
x<-rnorm(100)
## For 95th percentile VaR (right-tail)
UPM.VaR(0.95,0,x)</pre>
```

Index

*Topic ANOVA,	NNS.ANOVA, 10
NNS.ANOVA, 10	*Topic matrix
*Topic Autoregressive	NNS.term.matrix, 29
NNS.ARMA, 11	*Topic mean ,
*Topic CDF	LPM, 8
LPM, 8	UPM, 31
UPM, 31	*Topic model
*Topic VaR	NNS.ARMA, 11
LPM. VaR, 9	*Topic moments,
UPM. VaR, 32	Co.LPM, 2
*Topic causation	Co.UPM, 3
NNS.caus, 13	D.LPM, 4
*Topic classifier	D. UPM, 5
NNS.reg, 21	LPM, 8
NNS.stack, 27	UPM, 31
*Topic cluster	*Topic multivaiate
NNS.part, 20	dy.d_, 7
*Topic correlation	*Topic nonlinear
NNS.cor, 14	NNS.cor, 14
NNS.cor.hd, 15	NNS.reg, 21
NNS.dep, 16	*Topic normalization
*Topic covariance	NNS.norm, 19
Co.LPM, 2	*Topic numerical
Co.UPM, 3	NNS.diff, 17
D.LPM, 4	*Topic partial
D. UPM, 5	Co.LPM, 2
*Topic dependence ,	Co.UPM, 3
NNS.cor.hd, 15	D.LPM, 4
NNS.dep, 16	D. UPM, 5
*Topic derivative	dy.d_, 7
dy.d_,7	dy.dx, 6
dy.dx, 6	LPM, 8
*Topic differentiation,	UPM, 31
NNS.diff, 17	*Topic partitioning,
*Topic document	NNS.part, 20
NNS.term.matrix, 29	*Topic regression,
*Topic dominance	NNS.reg, 21
NNS.FSD, 18	*Topic seasonality
NNS.FSD.uni, 18	NNS.seas, 25
NNS.SD.Efficient.Set, 24	*Topic secant
NNS.SSD, 26	NNS.diff, 17
NNS.TSD, 30	*Topic size
*Topic effect	NNS. ANOVA, 10

INDEX 35

*Topic stochastic	plot3d, <i>15</i>	
NNS.FSD, 18	sapply, 28	
NNS.FSD.uni, 18 NNS.SD.Efficient.Set, 24	3dpp1y, 20	
NNS.SSD, 26	uniroot, <i>9</i> , <i>10</i> , <i>32</i>	
NNS.TSD, 30	UPM, 31	
*Topic term	UPM. VaR, 32	
NNS.term.matrix, 29		
*Topic upper		
UPM, 31		
*Topic variance ,		
LPM, 8		
UPM, 31		
as.factor, 28		
Co.LPM, 2, 15		
Co. UPM, 3, 15		
D.LPM, 4		
D. UPM, 5		
data.frame, 19		
data.matrix, 28		
data.table, <i>21</i> , <i>23</i>		
dy.d_, 7		
dy.dx, 6		
expand.grid, 8		
legend, 22		
LPM, 8		
LPM. VaR, 9		
NNS.ANOVA, 10		
NNS.ARMA, 11		
NNS.caus, 13		
NNS.cor, 14, 20		
NNS.cor.hd, 15		
NNS.dep, 7, 16, 20, 22		
NNS.diff, 17		
NNS.FSD, 18		
NNS.FSD.uni, 18		
NNS.norm, 19, 22		
NNS.part, 20		
NNS.reg, 6, 7, 20, 21, 27–29		
NNS.SD.Efficient.Set, 24		
NNS.seas, 25		
NNS. SSD, 26		
NNS.SSD.uni, 27		
NNS. stack, 22, 27		
NNS.term.matrix, 29		
NNS.TSD, 30		
NNS.TSD.uni, 31		