

# Package ‘NNS’

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**Type** Package

**Title** Nonlinear Nonparametric Statistics

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**Description** Nonlinear nonparametric statistics using partial moments. Partial moments are the elements of variance and asymptotically approximate the area of  $f(x)$ . These robust statistics provide the basis for nonlinear analysis while retaining linear equivalences. NNS offers: Numerical integration, Numerical differentiation, Clustering, Correlation, Dependence, Causal analysis, ANOVA, Regression, Classification, Seasonality, Autoregressive modeling, Normalization and Stochastic dominance. All routines based on: Viole, F. and Nawrocki, D. (2013), Nonlinear Nonparametric Statistics: Using Partial Moments (ISBN: 1490523995).

**License** GPL-3

**BugReports** <https://github.com/OVVO-Financial/NNS/issues>

**RoxygenNote** 7.1.1

**Depends** R (>= 3.3.0), doParallel

**Imports** caret, data.table, dtw, dynlm, meboot, plyr, Rfast, rgl, stringr, tdigest

**Suggests** knitr, rmarkdown

**VignetteBuilder** knitr

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Co.LPM

*Co-Lower Partial Moment (Lower Left Quadrant 4)*

---

## Description

This function generates a co-lower partial moment for between two equal length variables for any degree or target.

## Usage

```
Co.LPM(degree.x, degree.y, x, y, target.x = mean(x), target.y = mean(y))
```

## Arguments

degree.x	integer; Degree for variable X. (degree.x = 0) is frequency, (degree.x = 1) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
x	a numeric vector.
y	a numeric vector of equal length to x.

target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

**Value**

Co-LPM of two variables

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
Co.LPM(0, 0, x, y, mean(x), mean(y))
```

---

Co.UPM

---

*Co-Upper Partial Moment (Upper Right Quadrant 1)*


---

**Description**

This function generates a co-upper partial moment between two equal length variables for any degree or target.

**Usage**

```
Co.UPM(degree.x, degree.y, x, y, target.x = mean(x), target.y = mean(y))
```

**Arguments**

degree.x	integer; Degree for variable X. (degree.x = 0) is frequency, (degree.x = 1) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
x	a numeric vector.
y	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

**Value**

Co-UPM of two variables

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
Co.UPM(0, 0, x, y, mean(x), mean(y))
```

---

D.LPM

---

*Divergent-Lower Partial Moment (Lower Right Quadrant 3)*


---

**Description**

This function generates a divergent lower partial moment between two equal length variables for any degree or target.

**Usage**

```
D.LPM(degree.x, degree.y, x, y, target.x = mean(x), target.y = mean(y))
```

**Arguments**

degree.x	integer; Degree for variable X. (degree.x = 0) is frequency, (degree.x = 1) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
x	a numeric vector.
y	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

**Value**

Divergent LPM of two variables

**Author(s)**

Fred Viole, OVVO Financial Systems

## References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

## Examples

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
D.LPM(0, 0, x, y, mean(x), mean(y))
```

---

D.UPM	<i>Divergent-Upper Partial Moment (Upper Left Quadrant 2)</i>
-------	---

---

## Description

This function generates a divergent upper partial moment between two equal length variables for any degree or target.

## Usage

```
D.UPM(degree.x, degree.y, x, y, target.x = mean(x), target.y = mean(y))
```

## Arguments

degree.x	integer; Degree for variable X. (degree.x = 0) is frequency, (degree.x = 1) is area.
degree.y	integer; Degree for variable Y. (degree.y = 0) is frequency, (degree.y = 1) is area.
x	a numeric vector.
y	a numeric vector of equal length to x.
target.x	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized)
target.y	numeric; Typically the mean of Variable Y for classical statistics equivalences, but does not have to be. (Vectorized)

## Value

Divergent UPM of two variables

## Author(s)

Fred Viole, OVVO Financial Systems

## References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

## Examples

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
D.UPM(0, 0, x, y, mean(x), mean(y))
```

---

dy.dx	<i>Partial Derivative dy/dx</i>
-------	---------------------------------

---

## Description

Returns the numerical partial derivate of y wrt x for a point of interest.

## Usage

```
dy.dx(x, y, eval.point = median(x), deriv.method = "FD")
```

## Arguments

x	a numeric vector.
y	a numeric vector.
eval.point	numeric or ("overall"); x point to be evaluated. Defaults to (eval.point = median(x)). Set to (eval.point = "overall") to find an overall partial derivative estimate (1st derivative only).
deriv.method	method of derivative estimation, options: ("NNS", "FD"); Determines the partial derivative from the coefficient of the <a href="#">NNS.reg</a> output when (deriv.method = "NNS") or generates a partial derivative using the finite difference method (deriv.method = "FD") (Default).

## Value

Returns a list of both 1st and 2nd derivative:

- `dy.dx(...)$First` the 1st derivative.
- `dy.dx(...)$Second` the 2nd derivative.

## Note

If a vector of derivatives is required, ensure (deriv.method = "FD").

## Author(s)

Fred Violen, OVVO Financial Systems

## References

- Violen, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)
- Vinod, H. and Violen, F. (2017) "Nonparametric Regression Using Clusters" <https://link.springer.com/article/10.1007/s10614-017-9713-5>

## Examples

```
## Not run:
x <- seq(0, 2 * pi, pi / 100) ; y <- sin(x)
dy.dx(x, y, eval.point = 1.75)

# Vector of derivatives
dy.dx(x, y, eval.point = c(1.75, 2.5), deriv.method = "FD")
## End(Not run)
```

---

dy.d_	<i>Partial Derivative <math>dy/d_{[wrt]}</math></i>
-------	---

---

## Description

Returns the numerical partial derivative of y with respect to [wrt] any regressor for a point of interest. Finite difference method is used with [NNS.reg](#) estimates as  $f(x + h)$  and  $f(x - h)$  values.

## Usage

```
dy.d_(x, y, wrt, eval.points = "obs", mixed = FALSE, messages = TRUE)
```

## Arguments

x	a numeric matrix or data frame.
y	a numeric vector with compatible dimensions to x.
wrt	integer; Selects the regressor to differentiate with respect to (vectorized).
eval.points	numeric or options: ("obs", "apd", "mean", "median", "last"); Regressor points to be evaluated. <ul style="list-style-type: none"> <li>Numeric values must be in matrix or data.frame form to be evaluated for each regressor, otherwise, a vector of points will evaluate only at the wrt regressor. See examples for use cases.</li> <li>Set to (eval.points = "obs") (default) to find the average partial derivative at every observation of the variable with respect to <i>for specific tuples of given observations</i>.</li> <li>Set to (eval.points = "apd") to find the average partial derivative at every observation of the variable with respect to <i>over the entire distribution of other regressors</i>.</li> <li>Set to (eval.points = "mean") to find the partial derivative at the mean of value of every variable.</li> <li>Set to (eval.points = "median") to find the partial derivative at the median value of every variable.</li> <li>Set to (eval.points = "last") to find the partial derivative at the last observation of every value (relevant for time-series data).</li> </ul>
mixed	logical; FALSE (default) If mixed derivative is to be evaluated, set (mixed = TRUE).
messages	logical; TRUE (default) Prints status messages.

**Value**

Returns column-wise matrix of wrt regressors:

- `dy.d(...)[,wrt]$First` the 1st derivative
- `dy.d(...)[,wrt]$Second` the 2nd derivative
- `dy.d(...)[,wrt]$Mixed` the mixed derivative (for two independent variables only).

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

Vinod, H. and Viole, F. (2020) "Comparing Old and New Partial Derivative Estimates from Nonlinear Nonparametric Regressions" <https://www.ssrn.com/abstract=3681104>

**Examples**

```
## Not run:
set.seed(123) ; x_1 <- runif(1000) ; x_2 <- runif(1000) ; y <- x_1 ^ 2 * x_2 ^ 2
B <- cbind(x_1, x_2)

## To find derivatives of y wrt 1st regressor for specific points of both regressors
dy.d(B, y, wrt = c(1, 2), eval.points = t(c(.5, .5)))

## To find average partial derivative of y wrt 1st regressor,
only supply 1 value in [eval.points], or a vector of [eval.points]:
dy.d(B, y, wrt = 1, eval.points = .5)

dy.d(B, y, wrt = 1, eval.points = fivenum(B[,1]))

## To find average partial derivative of y wrt 1st regressor,
for every observation of 1st regressor:
apd <- dy.d(B, y, wrt = 1, eval.points = "apd")
plot(B[,1], apd[,1]$First)

## 95% Confidence Interval to test if 0 is within
### Lower CI
LPM.VaR(.025, 0, apd[,1]$First)

### Upper CI
UPM.VaR(.025, 0, apd[,1]$First)

## End(Not run)
```



LPM

*Lower Partial Moment***Description**

This function generates a univariate lower partial moment for any degree or target.

**Usage**

```
LPM(degree, target, variable)
```

**Arguments**

degree	integer; (degree = 0) is frequency, (degree = 1) is area.
target	numeric; Typically set to mean, but does not have to be. (Vectorized)
variable	a numeric vector.

**Value**

LPM of variable

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
set.seed(123)
x <- rnorm(100)
LPM(0, mean(x), x)
```

LPM.ratio

*Lower Partial Moment RATIO***Description**

This function generates a standardized univariate lower partial moment for any degree or target.

**Usage**

```
LPM.ratio(degree, target, variable)
```

**Arguments**

degree	integer; (degree = 0) is frequency, (degree = 1) is area.
target	numeric; Typically set to mean, but does not have to be. (Vectorized)
variable	a numeric vector.

**Value**

Standardized LPM of variable

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

Viole, F. (2017) "Continuous CDFs and ANOVA with NNS" <https://www.ssrn.com/abstract=3007373>

**Examples**

```
set.seed(123)
x <- rnorm(100)
LPM.ratio(0, mean(x), x)

## Not run:
## Empirical CDF (degree = 0)
lpm_cdf <- LPM.ratio(0, sort(x), x)
plot(sort(x), lpm_cdf)

## Continuous CDF (degree = 1)
lpm_cdf_1 <- LPM.ratio(1, sort(x), x)
plot(sort(x), lpm_cdf_1)

## Joint CDF
x <- rnorm(5000) ; y <- rnorm(5000)
plot3d(x, y, Co.LPM(0, 0, sort(x), sort(y), x, y), col = "blue", xlab = "X", ylab = "Y",
zlab = "Probability", box = FALSE)

## End(Not run)
```

---

LPM.VaR

---

*LPM VaR*


---

**Description**

Generates a value at risk (VaR) quantile based on the Lower Partial Moment ratio.

**Usage**

```
LPM.VaR(percentile, degree, x)
```

**Arguments**

percentile	numeric [0, 1]; The percentile for left-tail VaR (vectorized).
degree	integer; (degree = 0) for discrete distributions, (degree = 1) for continuous distributions.
x	a numeric vector.

**Value**

Returns a numeric value representing the point at which "percentile" of the area of x is below.

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
set.seed(123)
x <- rnorm(100)

## For 5th percentile, left-tail
LPM.VaR(0.05, 0, x)
```

---

NNS.ANOVA

---

*NNS ANOVA*


---

**Description**

Analysis of variance (ANOVA) based on lower partial moment CDFs for multiple variables. Returns a degree of certainty the difference in sample means is zero, not a p-value.

**Usage**

```
NNS.ANOVA(
  control,
  treatment,
  confidence.interval = 0.95,
  tails = "Both",
  pairwise = FALSE,
  plot = TRUE
)
```

## Arguments

<code>control</code>	a numeric vector, matrix or data frame.
<code>treatment</code>	NULL (default) a numeric vector, matrix or data frame.
<code>confidence.interval</code>	numeric [0, 1]; The confidence interval surrounding the control mean, defaults to ( <code>confidence.interval</code> = 0.95).
<code>tails</code>	options: ("Left", "Right", "Both"). <code>tails</code> = "Both" (Default) Selects the tail of the distribution to determine effect size.
<code>pairwise</code>	logical; FALSE (default) Returns pairwise certainty tests when set to <code>pairwise</code> = TRUE.
<code>plot</code>	logical; TRUE (default) Returns the boxplot of all variables along with grand mean identification and confidence interval thereof.

## Value

Returns the following:

- "Control Mean" control mean.
- "Treatment Mean" treatment mean.
- "Grand Mean" mean of means.
- "Control CDF" CDF of the control from the grand mean.
- "Treatment CDF" CDF of the treatment from the grand mean.
- "Certainty" the certainty of the same population statistic.
- "Lower Bound Effect" and "Upper Bound Effect" the effect size of the treatment for the specified confidence interval.

## Author(s)

Fred Viole, OVVO Financial Systems

## References

- Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)
- Viole, F. (2017) "Continuous CDFs and ANOVA with NNS" <https://www.ssrn.com/abstract=3007373>

## Examples

```
### Binary analysis and effect size
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.ANOVA(control = x, treatment = y)

### Two variable analysis with no control variable
A <- cbind(x, y)
NNS.ANOVA(A)

### Multiple variable analysis with no control variable
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100) ; z <- rnorm(100)
```

```
A <- cbind(x, y, z)
NNS.ANOVA(A)
```

NNS.ARMA

*NNS ARMA*

## Description

Autoregressive model incorporating nonlinear regressions of component series.

## Usage

```
NNS.ARMA(
  variable,
  h = 1,
  training.set = NULL,
  seasonal.factor = TRUE,
  weights = NULL,
  best.periods = 2,
  modulo = NULL,
  mod.only = TRUE,
  negative.values = FALSE,
  method = "nonlin",
  dynamic = FALSE,
  plot = TRUE,
  seasonal.plot = TRUE,
  conf.intervals = NULL,
  ncores = NULL
)
```

## Arguments

<code>variable</code>	a numeric vector.
<code>h</code>	integer; 1 (default) Number of periods to forecast.
<code>training.set</code>	numeric; NULL (default) Sets the number of variable observations ( <code>variable[1 : training.set]</code> ) to monitor performance of forecast over in-sample range.
<code>seasonal.factor</code>	logical or integer(s); TRUE (default) Automatically selects the best seasonal lag from the seasonality test. To use weighted average of all seasonal lags set to ( <code>seasonal.factor = FALSE</code> ). Otherwise, directly input known frequency integer lag to use, i.e. ( <code>seasonal.factor = 12</code> ) for monthly data. Multiple frequency integers can also be used, i.e. ( <code>seasonal.factor = c(12, 24, 36)</code> )
<code>weights</code>	numeric or "equal"; NULL (default) sets the weights of the <code>seasonal.factor</code> vector when specified as integers. If ( <code>weights = NULL</code> ) each <code>seasonal.factor</code> is weighted on its <a href="#">NNS.seas</a> result and number of observations it contains, else an "equal" weight is used.
<code>best.periods</code>	integer; [2] (default) used in conjunction with ( <code>seasonal.factor = FALSE</code> ), uses the <code>best.periods</code> number of detected seasonal lags instead of ALL lags when ( <code>seasonal.factor = FALSE, best.periods = NULL</code> ).

<code>modulo</code>	integer(s); NULL (default) Used to find the nearest multiple(s) in the reported seasonal period.
<code>mod.only</code>	logical; code TRUE (default) Limits the number of seasonal periods returned to the specified <code>modulo</code> .
<code>negative.values</code>	logical; FALSE (default) If the variable can be negative, set to ( <code>negative.values = TRUE</code> ). If there are negative values within the variable, <code>negative.values</code> will automatically be detected.
<code>method</code>	options: ("lin", "nonlin", "both"); "nonlin" (default) To select the regression type of the component series, select ( <code>method = "both"</code> ) where both linear and nonlinear estimates are generated. To use a nonlinear regression, set to ( <code>method = "nonlin"</code> ); to use a linear regression set to ( <code>method = "lin"</code> ).
<code>dynamic</code>	logical; FALSE (default) To update the seasonal factor with each forecast point, set to ( <code>dynamic = TRUE</code> ). The default is ( <code>dynamic = FALSE</code> ) to retain the original seasonal factor from the inputted variable for all ensuing <code>h</code> .
<code>plot</code>	logical; TRUE (default) Returns the plot of all periods exhibiting seasonality and the variable level reference in upper panel. Lower panel returns original data and forecast.
<code>seasonal.plot</code>	logical; TRUE (default) Adds the seasonality plot above the forecast. Will be set to FALSE if no seasonality is detected or <code>seasonal.factor</code> is set to an integer value.
<code>conf.intervals</code>	numeric [0, 1]; NULL (default) Plots and returns the associated confidence intervals for the final estimate. Constructed using the maximum entropy bootstrap <a href="#">meboot</a> on the final estimates.
<code>ncores</code>	integer; value specifying the number of cores to be used in the parallelized procedure. If NULL (default), the number of cores to be used is equal to half the number of cores of the machine - 1.

### Value

Returns a vector of forecasts of length (`h`) if no `conf.intervals` specified. Else, returns a [data.table](#) with the forecasts as well as lower and upper confidence intervals per forecast point.

### Note

For monthly data series, increased accuracy may be realized from forcing seasonal factors to multiples of 12. For example, if the best periods reported are: {37, 47, 71, 73} use (`seasonal.factor = c(36, 48, 72)`).

(`seasonal.factor = FALSE`) can be a very computationally expensive exercise due to the number of seasonal periods detected.

If error encountered when (`seasonal.factor = TRUE`):

```
"NaNs produced Error in seq.default(length(variable)+1,1,-lag[i]) : wrong sign in 'by' argument"
```

use the combination of (`seasonal.factor = FALSE, best.periods = 1`).

### Author(s)

Fred Viole, OVVO Financial Systems

## References

- Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)
- Viole, F. (2019) "Forecasting Using NNS" <https://www.ssrn.com/abstract=3382300>

## Examples

```
## Nonlinear NNS.ARMA using AirPassengers monthly data and 12 period lag
## Not run:
NNS.ARMA(AirPassengers, h = 45, training.set = 100, seasonal.factor = 12, method = "nonlin")

## Linear NNS.ARMA using AirPassengers monthly data and 12, 24, and 36 period lags
NNS.ARMA(AirPassengers, h = 45, training.set = 120, seasonal.factor = c(12, 24, 36), method = "lin")

## Nonlinear NNS.ARMA using AirPassengers monthly data and 2 best periods lag
NNS.ARMA(AirPassengers, h = 45, training.set = 120, seasonal.factor = FALSE, best.periods = 2)
## End(Not run)
```

---

NNS.ARMA.optim

*NNS ARMA Optimizer*


---

## Description

Wrapper function for optimizing any combination of a given seasonal.factor vector in [NNS.ARMA](#). Minimum sum of squared errors (forecast-actual) is used to determine optimum across all [NNS.ARMA](#) methods.

## Usage

```
NNS.ARMA.optim(
  variable,
  training.set,
  seasonal.factor,
  negative.values = FALSE,
  obj.fn = expression(sum((predicted - actual)^2)),
  objective = "min",
  linear.approximation = TRUE,
  lin.only = FALSE,
  print.trace = TRUE,
  ncores = NULL
)
```

## Arguments

- |                 |   |
|-----------------|---|
| variable        | a numeric vector.   |
| training.set    | integer; Sets the number of variable observations as the training set. See Note below for recommended uses.                 |
| seasonal.factor | integers; Multiple frequency integers considered for <a href="#">NNS.ARMA</a> model, i.e. (seasonal.factor = c(12, 24, 36)) |

<code>negative.values</code>	logical; FALSE (default) If the variable can be negative, set to ( <code>negative.values = TRUE</code> ).
<code>obj.fn</code>	expression; <code>expression(sum((predicted - actual)^2))</code> (default) Sum of squared errors is the default objective function. Any <code>expression()</code> using the specific terms predicted and actual can be used.
<code>objective</code>	options: ("min", "max") "min" (default) Select whether to minimize or maximize the objective function <code>obj.fn</code> .
<code>linear.approximation</code>	logical; TRUE (default) Uses the best linear output from <code>NNS.reg</code> to generate a nonlinear and mixture regression for comparison. FALSE is a more exhaustive search over the objective space.
<code>lin.only</code>	logical; FALSE (default) Restricts the optimization to linear methods only.
<code>print.trace</code>	logical; TRUE (default) Prints current iteration information. Suggested as backup in case of error, best parameters to that point still known and copyable!
<code>ncores</code>	integer; value specifying the number of cores to be used in the parallelized procedure. If NULL (default), the number of cores to be used is equal to half the number of cores of the machine.

### Value

Returns a list containing:

- `$period` a vector of optimal seasonal periods
- `$weights` the optimal weights of each seasonal period between an equal weight or NULL weighting
- `$obj.fn` the objective function value
- `$method` the method identifying which [NNS.ARMA](#) method was used.
- `$bias.shift` a numerical result of the overall bias of the optimum objective function result. To be added to the final result when using the [NNS.ARMA](#) with the derived parameters.

### Note

- Typically, (`training.set = length(variable) - 2 * length(forecast horizon)`) is used for optimization. Smaller samples would use (`training.set = length(variable) - length(forecast horizon)`) in order to preserve information.
- The number of combinations will grow prohibitively large, they should be kept as small as possible. `seasonal.factor` containing an element too large will result in an error. Please reduce the maximum `seasonal.factor`.
- If variable cannot logically assume negative values, then the `$bias.shift` must be limited to 0 via a `pmax(0, ...)` call.

### Author(s)

Fred Viøle, OVVO Financial Systems

### References

Viøle, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)



## Examples

```
## Nonlinear NNS.ARMA period optimization using 2 yearly lags on AirPassengers monthly data
## Not run:
nns.optims <- NNS.ARMA.optim(AirPassengers[1:132], training.set = 120,
seasonal.factor = seq(12, 24, 6))

## Then use optimal parameters in NNS.ARMA to predict 12 periods in-sample.
## Note the {$bias.shift} usage in the {NNS.ARMA} function:
nns.estimates <- NNS.ARMA(AirPassengers, h = 12, training.set = 132,
seasonal.factor = nns.optims$periods, method = nns.optims$method) + nns.optims$bias.shift

## If variable cannot logically assume negative values
nns.estimates <- pmax(0, nns.estimates)

## End(Not run)
```

---

NNS.boost	<i>NNS Boost</i>
-----------	------------------

---

## Description

Ensemble method for classification using the predictions of the NNS multivariate regression [NNS.reg](#) collected from uncorrelated feature combinations.

## Usage

```
NNS.boost(
  IVs.train,
  DV.train,
  IVs.test = NULL,
  type = NULL,
  representative.sample = FALSE,
  depth = NULL,
  learner.trials = 100,
  epochs = NULL,
  CV.size = 0.25,
  balance = FALSE,
  ts.test = NULL,
  folds = 5,
  threshold = NULL,
  obj.fn = expression(sum((predicted - actual)^2)),
  objective = "min",
  extreme = FALSE,
  features.only = FALSE,
  feature.importance = TRUE,
  status = TRUE
)
```

**Arguments**

<code>IVs.train</code>	a matrix or data frame of variables of numeric or factor data types.
<code>DV.train</code>	a numeric or factor vector with compatible dimensions to ( <code>IVs.train</code> ).
<code>IVs.test</code>	a matrix or data frame of variables of numeric or factor data types with compatible dimensions to ( <code>IVs.train</code> ). If NULL, will use ( <code>IVs.train</code> ) as default.
<code>type</code>	NULL (default). To perform a classification of discrete integer classes from factor target variable ( <code>DV.train</code> ) with a base category of 1, set to ( <code>type = "CLASS"</code> ), else for continuous ( <code>DV.train</code> ) set to ( <code>type = NULL</code> ).
<code>representative.sample</code>	logical; FALSE (default) Reduces observations of <code>IVs.train</code> to a set of representative observations per regressor.
<code>depth</code>	options: (integer, NULL, "max"); ( <code>depth = NULL</code> )(default) Specifies the order parameter in the <a href="#">NNS.reg</a> routine, assigning a number of splits in the regressors, analogous to tree depth.
<code>learner.trials</code>	integer; 100 (default) Sets the number of trials to obtain an accuracy threshold level. If the number of all possible feature combinations is less than selected value, the minimum of the two values will be used.
<code>epochs</code>	integer; $2 \times \text{length}(\text{DV.train})$ (default) Total number of feature combinations to run.
<code>CV.size</code>	numeric [0, 1]; ( <code>CV.size = .25</code> ) (default) Sets the cross-validation size. Defaults to 0.25 for a 25 percent random sampling of the training set.
<code>balance</code>	logical; FALSE (default) Uses both up and down sampling from <code>caret</code> to balance the classes. <code>type="CLASS"</code> required.
<code>ts.test</code>	integer; NULL (default) Sets the length of the test set for time-series data; typically $2 \times h$ parameter value from <a href="#">NNS.ARMA</a> or double known periods to forecast.
<code>folds</code>	integer; 5 (default) Sets the number of folds in the <a href="#">NNS.stack</a> procedure for optimal <code>n.best</code> parameter.
<code>threshold</code>	numeric; NULL (default) Sets the <code>obj.fn</code> threshold to keep feature combinations.
<code>obj.fn</code>	expression; <code>expression( sum((predicted - actual)^2) )</code> (default) Sum of squared errors is the default objective function. Any <code>expression()</code> using the specific terms <code>predicted</code> and <code>actual</code> can be used. Automatically selects an accuracy measure when ( <code>type = "CLASS"</code> ).
<code>objective</code>	options: ("min", "max") "max" (default) Select whether to minimize or maximize the objective function <code>obj.fn</code> .
<code>extreme</code>	logical; FALSE (default) Uses the maximum (minimum) threshold obtained from the <code>learner.trials</code> , rather than the upper (lower) quintile level for maximization (minimization) objective.
<code>features.only</code>	logical; FALSE (default) Returns only the final feature loadings along with the final feature frequencies.
<code>feature.importance</code>	logical; TRUE (default) Plots the frequency of features used in the final estimate.
<code>status</code>	logical; TRUE (default) Prints status update message in console.

**Value**

Returns a vector of fitted values for the dependent variable test set `$results`, and the final feature loadings `$feature.weights`, along with final feature frequencies `$feature.frequency`.

**Note**

Like a logistic regression, the (type = "CLASS") setting is not necessary for target variable of two classes e.g. [0, 1]. The response variable base category should be 1 for classification problems.

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. (2016) "Classification Using NNS Clustering Analysis" <https://www.ssrn.com/abstract=2864711>

**Examples**

```
## Using 'iris' dataset where test set [IVs.test] is 'iris' rows 141:150.
## Not run:
a <- NNS.boost(iris[1:140, 1:4], iris[1:140, 5],
IVs.test = iris[141:150, 1:4],
epochs = 100, learner.trials = 100,
type = "CLASS", depth = NULL)

## Test accuracy
mean(a$results == as.numeric(iris[141:150, 5]))

## End(Not run)
```

---

NNS.caus

*NNS Causation*


---

**Description**

Returns the causality from observational data between two variables.

**Usage**

```
NNS.caus(x, y = NULL, factor.2.dummy = FALSE, tau = 0, plot = FALSE)
```

**Arguments**

x	a numeric vector, matrix or data frame.
y	NULL (default) or a numeric vector with compatible dimensions to x.
factor.2.dummy	logical; FALSE (default) Automatically augments variable matrix with numerical dummy variables based on the levels of factors. Includes dependent variable y.
tau	options: ("cs", "ts", integer); 0 (default) Number of lagged observations to consider (for time series data). Otherwise, set (tau = "cs") for cross-sectional data. (tau = "ts") automatically selects the lag of the time series data, while (tau = [integer]) specifies a time series lag.
plot	logical; FALSE (default) Plots the raw variables, tau normalized, and cross-normalized variables.

**Value**

Returns the directional causation ( $x \longrightarrow y$ ) or ( $y \longrightarrow x$ ) and net quantity of association. For causal matrix, directional causation is returned as ([column variable]  $\longrightarrow$  [row variable]). Negative numbers represent causal direction attributed to [row variable].

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
## Not run:
## x causes y...
set.seed(123)
x <- rnorm(1000) ; y <- x ^ 2
NNS.caus(x, y, tau = "cs")

## Causal matrix without per factor causation
NNS.caus(iris, tau = 0)

## Causal matrix with per factor causation
NNS.caus(iris, factor.2.dummy = TRUE, tau = 0)

## End(Not run)
```

---

NNS.CDF

---

*NNS CDF*


---

**Description**

This function generates an empirical CDF using partial moment ratios [LPM.ratio](#), and resulting survival, hazard and cumulative hazard functions.

**Usage**

```
NNS.CDF(variable, degree = 0, target = NULL, type = "CDF", plot = TRUE)
```

**Arguments**

variable	a numeric vector or data.frame of 2 variables for joint CDF.
degree	integer; (degree = 0) (default) is frequency, (degree = 1) is area.
target	numeric; NULL (default) Must lie within support of each variable.
type	options("CDF", "survival", "hazard", "cumulative hazard"); "CDF" (default) Selects type of function to return for bi-variate analysis. Multivariate analysis is restricted to "CDF".
plot	logical; plots CDF.

**Value**

Returns:

- "Function" a data.table containing the observations and resulting CDF of the variable.
- "target.value" value from the target argument.

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

Viole, F. (2017) "Continuous CDFs and ANOVA with NNS" <https://www.ssrn.com/abstract=3007373>

**Examples**

```
set.seed(123)
x <- rnorm(100)
NNS.CDF(x)

## Not run:
## Empirical CDF (degree = 0)
NNS.CDF(x)

## Continuous CDF (degree = 1)
NNS.CDF(x, 1)

## Joint CDF
x <- rnorm(5000) ; y <- rnorm(5000)
A <- cbind(x,y)

NNS.CDF(A, 0)

## Joint CDF with target
NNS.CDF(A, 0, target = c(0,0))

## End(Not run)
```

---

NNS.copula

*NNS Co-Partial Moments Higher Dimension Dependence*

---

**Description**

Determines higher dimension dependence coefficients based on co-partial moment matrices ratios.

**Usage**

```
NNS.copula(x, continuous = TRUE, plot = FALSE, independence.overlay = FALSE)
```

**Arguments**

<code>x</code>	a numeric matrix or data frame.
<code>continuous</code>	logical; TRUE (default) Generates a continuous measure using degree 1 <a href="#">PM.matrix</a> , while discrete FALSE uses degree 0 <a href="#">PM.matrix</a> .
<code>plot</code>	logical; FALSE (default) Generates a 3d scatter plot with regression points using <a href="#">plot3d</a> .
<code>independence.overlay</code>	logical; FALSE (default) Creates and overlays independent <a href="#">Co.LPM</a> and <a href="#">Co.UPM</a> regions to visually reference the difference in dependence from the data.frame of variables being analyzed. Under independence, the light green and red shaded areas would be occupied by green and red data points respectively.

**Value**

Returns a multivariate dependence value [0,1].

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. (2016) "Beyond Correlation: Using the Elements of Variance for Conditional Means and Probabilities" <https://www.ssrn.com/abstract=2745308>.

**Examples**

```
set.seed(123)
x <- rnorm(1000) ; y <- rnorm(1000) ; z <- rnorm(1000)
A <- data.frame(x, y, z)
NNS.copula(A, plot = TRUE, independence.overlay = TRUE)
```

---

NNS.dep

---

*NNS Dependence*


---

**Description**

Returns the dependence and nonlinear correlation between two variables based on higher order partial moment matrices measured by frequency or area.

**Usage**

```
NNS.dep(x, y = NULL, asym = FALSE, p.value = FALSE, print.map = FALSE)
```

**Arguments**

<code>x</code>	a numeric vector, matrix or data frame.
<code>y</code>	NULL (default) or a numeric vector with compatible dimensions to x.
<code>asym</code>	logical; FALSE (default) Allows for asymmetrical dependencies.
<code>p.value</code>	logical; FALSE (default) Generates 100 independent random permutations to test results against and plots 95 percent confidence intervals along with all results.
<code>print.map</code>	logical; FALSE (default) Plots quadrant means, or p-value replicates.

**Value**

Returns the bi-variate "Correlation" and "Dependence" or correlation / dependence matrix for matrix input.

**Note**

NNS.cor has been deprecated (NNS >= 0.5.4) and can be called via NNS.dep.

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
## Not run:
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.dep(x, y)

## Correlation / Dependence Matrix
x <- rnorm(100) ; y <- rnorm(100) ; z <- rnorm(100)
B <- cbind(x, y, z)
NNS.dep(B)

## End(Not run)
```

---

NNS.diff

---

*NNS Numerical Differentiation*


---

**Description**

Determines numerical derivative of a given univariate function using projected secant lines on the y-axis. These projected points infer finite steps h, in the finite step method.

**Usage**

```
NNS.diff(f, point, h = 0.1, tol = 1e-10, digits = 12, print.trace = FALSE)
```

**Arguments**

f	an expression or call or a formula with no lhs.
point	numeric; Point to be evaluated for derivative of a given function f.
h	numeric [0, ...]; Initial step for secant projection. Defaults to (h = 0.1).
tol	numeric; Sets the tolerance for the stopping condition of the inferred h. Defaults to (tol = 1e-10).

<code>digits</code>	numeric; Sets the number of digits specification of the output. Defaults to ( <code>digits = 12</code> ).
<code>print.trace</code>	logical; FALSE (default) Displays each iteration, lower y-intercept, upper y-intercept and inferred h.

**Value**

Returns a matrix of values, intercepts, derivatives, inferred step sizes for multiple methods of estimation.

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
f <- function(x) sin(x) / x
NNS.diff(f, 4.1)
```

---

NNS.distance	<i>NNS Distance</i>
--------------	---------------------

---

**Description**

Internal kernel function for NNS multivariate regression [NNS.reg](#) parallel instances.

**Usage**

```
NNS.distance(rpm, rpm_class, dist.estimate, type, k, n)
```

**Arguments**

<code>rpm</code>	REGRESSION.POINT.MATRIX from <a href="#">NNS.reg</a>
<code>rpm_class</code>	integer rpm.
<code>dist.estimate</code>	Vector to generate distances from.
<code>type</code>	"L1", "L2", "DTW" or "FACTOR"
<code>k</code>	n.best from <a href="#">NNS.reg</a>
<code>n</code>	number of observations.

**Value**

Returns sum of weighted distances.



---

NNS.FSD	<i>NNS FSD Test</i>
---------	---------------------

---

**Description**

Bi-directional test of first degree stochastic dominance using lower partial moments.

**Usage**

```
NNS.FSD(x, y, type = "discrete")
```

**Arguments**

x	a numeric vector.
y	a numeric vector.
type	options: ("discrete", "continuous"); "discrete" (default) selects the type of CDF.

**Value**

Returns one of the following FSD results: "X FSD Y", "Y FSD X", or "NO FSD EXISTS".

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. <https://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817>.

Viole, F. (2017) "A Note on Stochastic Dominance." <https://www.ssrn.com/abstract=3002675>.

**Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.FSD(x, y)
```

---

NNS.FSD.uni

*NNS FSD Test uni-directional*


---

### Description

Uni-directional test of first degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

### Usage

```
NNS.FSD.uni(x, y, type = "discrete")
```

### Arguments

x	a numeric vector.
y	a numeric vector.
type	options: ("discrete", "continuous"); "discrete" (default) selects the type of CDF.

### Value

Returns (1) if "X FSD Y", else (0).

### Author(s)

Fred Viole, OVVO Financial Systems

### References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. <https://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817>.

Viole, F. (2017) "A Note on Stochastic Dominance." <https://www.ssrn.com/abstract=3002675>.

### Examples

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.FSD.uni(x, y)
```

---

NNS.meboot	<i>NNS meboot</i>
------------	-------------------

---

## Description

Adapted maximum entropy bootstrap routine from meboot <https://cran.r-project.org/package=meboot>.

## Usage

```
NNS.meboot(
  x,
  reps = 999,
  rho = NULL,
  type = "spearman",
  drift = TRUE,
  trim = 0.1,
  xmin = NULL,
  xmax = NULL,
  reachbnd = TRUE,
  expand.sd = TRUE,
  force.clt = TRUE,
  scl.adjustment = FALSE,
  sym = FALSE,
  elaps = FALSE,
  colsubj,
  coldata,
  coltimes,
  ...
)
```

## Arguments

<code>x</code>	vector of data.
<code>reps</code>	numeric; number of replicates to generate.
<code>rho</code>	numeric [0,1]; The default setting <code>rho = NULL</code> assumes that the user does not want to generate replicates that are perfectly dependent on original time series, <code>rho=1</code> recovers the original meboot(...) settings. <code>rho &lt; 1</code> admits less perfect (more realistic for some purposes) dependence.
<code>type</code>	options("spearman", "pearson", "NNScor", "NNSdep"); <code>type = "spearman"</code> (default) dependence metric desired.
<code>drift</code>	logical; TRUE default preserves the drift of the original series.
<code>trim</code>	numeric [0,1]; The mean trimming proportion, defaults to <code>trim=0.1</code> .
<code>xmin</code>	numeric; the lower limit for the left tail.
<code>xmax</code>	numeric; the upper limit for the right tail.
<code>reachbnd</code>	logical; If TRUE potentially reached bounds ( <code>xmin = smallest value - trimmed mean</code> and <code>xmax = largest value + trimmed mean</code> ) are given when the random draw happens to be equal to 0 and 1, respectively.

<code>expand.sd</code>	logical; If TRUE the standard deviation in the ensemble is expanded. See <code>expand.sd</code> in <code>meboot::meboot</code> .
<code>force.clt</code>	logical; If TRUE the ensemble is forced to satisfy the central limit theorem. See <code>force.clt</code> in <code>meboot::meboot</code> .
<code>scl.adjustment</code>	logical; If TRUE scale adjustment is performed to ensure that the population variance of the transformed series equals the variance of the data.
<code>sym</code>	logical; If TRUE an adjustment is performed to ensure that the ME density is symmetric.
<code>elaps</code>	logical; If TRUE elapsed time during computations is displayed.
<code>colsubj</code>	numeric; the column in <code>x</code> that contains the individual index. It is ignored if the input data <code>x</code> is not a <code>pdata.frame</code> object.
<code>coldata</code>	numeric; the column in <code>x</code> that contains the data of the variable to create the ensemble. It is ignored if the input data <code>x</code> is not a <code>pdata.frame</code> object.
<code>coltimes</code>	numeric; an optional argument indicating the column that contains the times at which the observations for each individual are observed. It is ignored if the input data <code>x</code> is not a <code>pdata.frame</code> object.
<code>...</code>	possible argument <code>fiv</code> to be passed to <code>expand.sd</code> .

### Value

- `x` original data provided as input.
- replicates maximum entropy bootstrap replicates.
- ensemble average observation over all replicates.
- `xx` sorted order stats (`xx[1]` is minimum value).
- `z` class intervals limits.
- `dv` deviations of consecutive data values.
- `dvtrim` trimmed mean of `dv`.
- `xmin` data minimum for `ensemble=xx[1]-dvtrim`.
- `xmax` data `x` maximum for `ensemble=xx[n]+dvtrim`.
- `desintxb` desired interval means.
- `ordxx` ordered `x` values.
- kappa scale adjustment to the variance of ME density.
- `elaps` elapsed time.

### References

- Vinod, H.D. and Viole, F. (2020) Arbitrary Spearman's Rank Correlations in Maximum Entropy Bootstrap and Improved Monte Carlo Simulations <https://www.ssrn.com/abstract=3621614>
- Vinod, H.D. (2013), Maximum Entropy Bootstrap Algorithm Enhancements. <https://www.ssrn.com/abstract=22850>
- Vinod, H.D. (2006), Maximum Entropy Ensembles for Time Series Inference in Economics, *Journal of Asian Economics*, **17**(6), pp. 955-978.
- Vinod, H.D. (2004), Ranking mutual funds using unconventional utility theory and stochastic dominance, *Journal of Empirical Finance*, **11**(3), pp. 353-377.

**Examples**

```
## Not run:
# To generate an orthogonal rank correlated time-series to AirPassengers
boots <- NNS.meboot(AirPassengers, reps=100, rho = 0, xmin = 0)

# Verify correlation of replicates ensemble to original
cor(boots$ensemble, AirPassengers, method = "spearman")

# Plot all replicates
matplot(boots$replicates, type = 'l')

# Plot ensemble
lines(boots$ensemble, lwd = 3)

## End(Not run)
```

NNS.norm

*NNS Normalization***Description**

Normalizes a matrix of variables based on nonlinear scaling normalization method.

**Usage**

```
NNS.norm(A, linear = FALSE, chart.type = NULL, location = "topleft")
```

**Arguments**

<code>A</code>	a numeric matrix or data frame.
<code>linear</code>	logical; FALSE (default) Performs a linear scaling normalization, resulting in equal means for all variables.
<code>chart.type</code>	options: ("l", "b"); NULL (default). Set ( <code>chart.type = "l"</code> ) for line, ( <code>chart.type = "b"</code> ) for boxplot.
<code>location</code>	Sets the legend location within the plot, per the x and y co-ordinates used in base graphics <a href="#">legend</a> .

**Value**

Returns a [data.frame](#) of normalized values.

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

## Examples

```
set.seed(123)
x <- rnorm(100) ; y<-rnorm(100)
A <- cbind(x, y)
NNS.norm(A)
```

---

NNS.part

*NNS Partition Map*


---

## Description

Creates partitions based on partial moment quadrant centroids, iteratively assigning identifications to observations based on those quadrants (unsupervised partitional and hierarchial clustering method). Basis for correlation, dependence [NNS.dep](#), regression [NNS.reg](#) routines.

## Usage

```
NNS.part(
  x,
  y,
  Voronoi = FALSE,
  type = NULL,
  order = NULL,
  obs.req = 8,
  min.obs.stop = TRUE,
  noise.reduction = "off"
)
```

## Arguments

x	a numeric vector.
y	a numeric vector with compatible dimensions to x.
Voronoi	logical; FALSE (default) Displays a Voronoi type diagram using partial moment quadrants.
type	NULL (default) Controls the partitioning basis. Set to (type = "XONLY") for X-axis based partitioning. Defaults to NULL for both X and Y-axis partitioning.
order	integer; Number of partial moment quadrants to be generated. (order = "max") will institute a perfect fit.
obs.req	integer; (8 default) Required observations per cluster where quadrants will not be further partitioned if observations are not greater than the entered value. Reduces minimum number of necessary observations in a quadrant to 1 when (obs.req = 1).
min.obs.stop	logical; TRUE (default) Stopping condition where quadrants will not be further partitioned if a single cluster contains less than the entered value of obs.req.
noise.reduction	the method of determining regression points options for the dependent variable y: ("mean", "median", "mode", "off"); (noise.reduction = "mean") uses means for partitions. (noise.reduction = "median") uses medians instead

of means for partitions, while (noise.reduction = "mode") uses modes instead of means for partitions. Defaults to (noise.reduction = "off") where an overall central tendency measure is used, which is the default for the independent variable x.

## Value

Returns:

- "dt" a [data.table](#) of x and y observations with their partition assignment "quadrant" in the 3rd column and their prior partition assignment "prior.quadrant" in the 4th column.
- "regression.points" the [data.table](#) of regression points for that given (order = ...).
- "order" the order of the final partition given "min.obs.stop" stopping condition.

## Note

min.obs.stop = FALSE will not generate regression points due to possible unequal partitioning of quadrants from individual cluster observations.

## Author(s)

Fred Violen, OVVO Financial Systems

## References

Violen, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

## Examples

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.part(x, y)

## Data.table of observations and partitions
NNS.part(x, y, order = 1)$dt

## Regression points
NNS.part(x, y, order = 1)$regression.points

## Voronoi style plot
NNS.part(x, y, Voronoi = TRUE)

## Examine final counts by quadrant
DT <- NNS.part(x, y)$dt
DT[, counts := .N, by = quadrant]
DT
```

---

`NNS.PDF`*NNS PDF*

---

## Description

This function generates an empirical PDF using `dy.dx` on `NNS.CDF`.

## Usage

```
NNS.PDF(variable, degree = 1, target = NULL, bins = NULL, plot = TRUE)
```

## Arguments

<code>variable</code>	a numeric vector.
<code>degree</code>	integer; (degree = 0) is frequency, (degree = 1) (default) is area.
<code>target</code>	a numeric range of values [a,b] where a < b. NULL (default) uses the variable min and max observations respectively.
<code>bins</code>	integer; NULL Selects number of bins. Bin width defaults to <code>density(x)\$bw</code> .
<code>plot</code>	logical; plots PDF.

## Value

Returns a `data.table` containing the intervals used and resulting PDF of the variable.

## Author(s)

Fred Viole, OVVO Financial Systems

## References

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

## Examples

```
set.seed(123)
x <- rnorm(100)
NNS.PDF(x)

## Custom target range
NNS.PDF(x, target = c(-5, 5))
```



NNS.reg

*NNS Regression***Description**

Generates a nonlinear regression based on partial moment quadrant means.

**Usage**

```
NNS.reg(
  x,
  y,
  factor.2.dummy = TRUE,
  order = NULL,
  stn = 0.95,
  dim.red.method = NULL,
  tau = NULL,
  type = NULL,
  point.est = NULL,
  location = "top",
  return.values = TRUE,
  plot = TRUE,
  plot.regions = FALSE,
  residual.plot = TRUE,
  std.errors = FALSE,
  confidence.interval = NULL,
  threshold = 0,
  n.best = NULL,
  noise.reduction = "off",
  dist = "L2",
  ncores = NULL,
  point.only = FALSE,
  multivariate.call = FALSE
)
```

**Arguments**

<code>x</code>	a vector, matrix or data frame of variables of numeric or factor data types.
<code>y</code>	a numeric or factor vector with compatible dimensions to <code>x</code> .
<code>factor.2.dummy</code>	logical; TRUE (default) Automatically augments variable matrix with numerical dummy variables based on the levels of factors.
<code>order</code>	integer; Controls the number of partial moment quadrant means. Users are encouraged to try different ( <code>order = ...</code> ) integer settings with ( <code>noise.reduction = "off"</code> ). ( <code>order = "max"</code> ) will force a limit condition perfect fit.
<code>stn</code>	numeric [0, 1]; Signal to noise parameter, sets the threshold of ( <code>NNS.dep</code> ) which reduces (" <code>order</code> ") when ( <code>order = NULL</code> ). Defaults to 0.95 to ensure high dependence for higher (" <code>order</code> ") and endpoint determination.
<code>dim.red.method</code>	options: (" <code>cor</code> ", " <code>NNS.dep</code> ", " <code>NNS.caus</code> ", " <code>all</code> ", numeric vector, <code>NULL</code> ) method for determining synthetic $X^*$ coefficients. Selection of a method automatically engages the dimension reduction regression. The default is <code>NULL</code> for full

	multivariate regression. ( <code>dim.red.method = "NNS.dep"</code> ) uses <a href="#">NNS.dep</a> for nonlinear dependence weights, while ( <code>dim.red.method = "NNS.caus"</code> ) uses <a href="#">NNS.caus</a> for causal weights. ( <code>dim.red.method = "cor"</code> ) uses standard linear correlation for weights. ( <code>dim.red.method = "all"</code> ) averages all methods for further feature engineering. Alternatively, user can specify a numeric vector of coefficients.
<code>tau</code>	<code>options("ts", NULL); NULL (default)</code> To be used in conjunction with ( <code>dim.red.method = "NNS.caus"</code> ) or ( <code>dim.red.method = "all"</code> ). If the regression is using time-series data, set ( <code>tau = "ts"</code> ) for more accurate causal analysis.
<code>type</code>	<code>NULL (default)</code> . To perform a classification, set to ( <code>type = "CLASS"</code> ). Like a logistic regression, it is not necessary for target variable of two classes e.g. [0, 1].
<code>point.est</code>	a numeric or factor vector with compatible dimensions to <code>x</code> . Returns the fitted value $\hat{y}$ for any value of <code>x</code> .
<code>location</code>	Sets the legend location within the plot, per the <code>x</code> and <code>y</code> co-ordinates used in base graphics <a href="#">legend</a> .
<code>return.values</code>	logical; <code>TRUE (default)</code> , set to <code>FALSE</code> in order to only display a regression plot and call values as needed.
<code>plot</code>	logical; <code>TRUE (default)</code> To plot regression.
<code>plot.regions</code>	logical; <code>FALSE (default)</code> . Generates 3d regions associated with each regression point for multivariate regressions. Note, adds significant time to routine.
<code>residual.plot</code>	logical; <code>TRUE (default)</code> To plot $\hat{y}$ and $Y$ .
<code>std.errors</code>	logical; <code>FALSE (default)</code> To provide standard errors of each linear segment in the "Fitted.xy" output.
<code>confidence.interval</code>	numeric [0, 1]; <code>NULL (default)</code> Plots the associated confidence interval with the estimate and reports the standard error for each individual segment.
<code>threshold</code>	numeric [0, 1]; ( <code>threshold = 0</code> ) ( <code>default</code> ) Sets the threshold for dimension reduction of independent variables when ( <code>dim.red.method</code> ) is not <code>NULL</code> .
<code>n.best</code>	integer; <code>NULL (default)</code> Sets the number of nearest regression points to use in weighting for multivariate regression at $\sqrt{\text{\# of regressors}}$ . ( <code>n.best = "all"</code> ) will select and weight all generated regression points. Analogous to <code>k</code> in a <code>k</code> Nearest Neighbors algorithm. Different values of <code>n.best</code> are tested using cross-validation in <a href="#">NNS.stack</a> .
<code>noise.reduction</code>	the method of determining regression points options: ("mean", "median", "mode", "off"); In low signal:noise situations, ( <code>noise.reduction = "mean"</code> ) uses means for <a href="#">NNS.dep</a> restricted partitions, ( <code>noise.reduction = "median"</code> ) uses medians instead of means for <a href="#">NNS.dep</a> restricted partitions, while ( <code>noise.reduction = "mode"</code> ) uses modes instead of means for <a href="#">NNS.dep</a> restricted partitions. ( <code>noise.reduction = "off"</code> ) uses an overall central tendency measure for partitions.
<code>dist</code>	options:("L1", "L2", "DTW", "FACTOR") the method of distance calculation; Selects the distance calculation used. <code>dist = "L2"</code> ( <code>default</code> ) selects the Euclidean distance and ( <code>dist = "L1"</code> ) selects the Manhattan distance; ( <code>dist = "DTW"</code> ) selects the dynamic time warping distance; ( <code>dist = "FACTOR"</code> ) uses a frequency.
<code>ncores</code>	integer; value specifying the number of cores to be used in the parallelized procedure. If <code>NULL (default)</code> , the number of cores to be used is equal to the number of cores of the machine - 1.

`point.only` Internal argument for abbreviated output.  
`multivariate.call` Internal argument for multivariate regressions.

### Value

UNIVARIATE REGRESSION RETURNS THE FOLLOWING VALUES:

- "R2" provides the goodness of fit;
- "SE" returns the overall standard error of the estimate between  $y$  and  $\hat{y}$ ;
- "Prediction.Accuracy" returns the correct rounded "Point.est" used in classifications versus the categorical  $y$ ;
- "derivative" for the coefficient of the  $x$  and its applicable range;
- "Point.est" for the predicted value generated;
- "regression.points" provides the points used in the regression equation for the given order of partitions;
- "Fitted.xy" returns a [data.table](#) of  $x$ ,  $y$ ,  $\hat{y}$ , resid, NNS.ID, gradient;

MULTIVARIATE REGRESSION RETURNS THE FOLLOWING VALUES:

- "R2" provides the goodness of fit;
- "equation" returns the numerator of the synthetic  $X^*$  dimension reduction equation as a [data.table](#) consisting of regressor and its coefficient. Denominator is simply the length of all coefficients  $> 0$ , returned in last row of equation [data.table](#).
- " $x.star$ " returns the synthetic  $X^*$  as a vector;
- "rhs.partitions" returns the partition points for each regressor  $x$ ;
- "RPM" provides the Regression Point Matrix, the points for each  $x$  used in the regression equation for the given order of partitions;
- "Point.est" returns the predicted value generated;
- "Fitted.xy" returns a [data.table](#) of  $x, y, \hat{y}$ , gradient, and NNS.ID.

### Note

- Please ensure `point.est` is of compatible dimensions to  $x$ , error message will ensue if not compatible.
- Like a logistic regression, the (`type = "CLASS"`) setting is not necessary for target variable of two classes e.g.  $[0, 1]$ . The response variable base category should be 1 for classification problems.

### Author(s)

Fred Violen, OVVO Financial Systems

### References

- Violen, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)
- Vinod, H. and Violen, F. (2017) "Nonparametric Regression Using Clusters" <https://link.springer.com/article/10.1007/s10614-017-9713-5>
- Vinod, H. and Violen, F. (2018) "Clustering and Curve Fitting by Line Segments" <https://www.preprints.org/manuscript/201801.0090/v1>

## Examples

```
## Not run:
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.reg(x, y)

## Manual {order} selection
NNS.reg(x, y, order = 2)

## Maximum {order} selection
NNS.reg(x, y, order = "max")

## x-only partitioning (Univariate only)
NNS.reg(x, y, type = "XONLY")

## For Multiple Regression:
x <- cbind(rnorm(100), rnorm(100), rnorm(100)) ; y <- rnorm(100)
NNS.reg(x, y, point.est = c(.25, .5, .75))

## For Multiple Regression based on Synthetic X* (Dimension Reduction):
x <- cbind(rnorm(100), rnorm(100), rnorm(100)) ; y <- rnorm(100)
NNS.reg(x, y, point.est = c(.25, .5, .75), dim.red.method = "cor")

## IRIS dataset examples:
# Dimension Reduction:
NNS.reg(iris[,1:4], iris[,5], dim.red.method = "cor", order = 5)

# Dimension Reduction using causal weights:
NNS.reg(iris[,1:4], iris[,5], dim.red.method = "NNS.caus", order = 5)

# Multiple Regression:
NNS.reg(iris[,1:4], iris[,5], order = 2, noise.reduction = "off")

# Classification:
NNS.reg(iris[,1:4], iris[,5], point.est = iris[1:10, 1:4], type = "CLASS")$Point.est

## To call fitted values:
x <- rnorm(100) ; y <- rnorm(100)
NNS.reg(x, y)$Fitted

## To call partial derivative (univariate regression only):
NNS.reg(x, y)$derivative
## End(Not run)
```

---

NNS.SD.efficient.set    *NNS SD Efficient Set*

---

## Description

Determines the set of stochastic dominant variables for various degrees.

## Usage

```
NNS.SD.efficient.set(x, degree, type = "discrete", status = TRUE)
```

**Arguments**

x	a numeric matrix or data frame.
degree	numeric options: (1, 2, 3); Degree of stochastic dominance test from (1, 2 or 3).
type	options: ("discrete", "continuous"); "discrete" (default) selects the type of CDF.
status	logical; TRUE (default) Prints status update message in console.

**Value**

Returns set of stochastic dominant variable names.

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

- Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. <https://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817>.
- Viole, F. (2017) "A Note on Stochastic Dominance." <https://www.ssrn.com/abstract=3002675>.

**Examples**

```
set.seed(123)
x <- rnorm(100) ; y<-rnorm(100) ; z<-rnorm(100)
A <- cbind(x, y, z)
NNS.SD.efficient.set(A, 1)
```

---

NNS.seas

---

*NNS Seasonality Test*


---

**Description**

Seasonality test based on the coefficient of variation for the variable and lagged component series. A result of 1 signifies no seasonality present.

**Usage**

```
NNS.seas(variable, modulo = NULL, mod.only = TRUE, plot = TRUE)
```

**Arguments**

variable	a numeric vector.
modulo	integer(s); NULL (default) Used to find the nearest multiple(s) in the reported seasonal period.
mod.only	logical; code TRUE (default) Limits the number of seasonal periods returned to the specified modulo.
plot	logical; TRUE (default) Returns the plot of all periods exhibiting seasonality and the variable level reference.

**Value**

Returns a matrix of all periods exhibiting less coefficient of variation than the variable with "all.periods"; and the single period exhibiting the least coefficient of variation versus the variable with "best.period"; as well as a vector of "periods" for easy call into [NNS.ARMA.optim](#). If no seasonality is detected, NNS.seas will return ("No Seasonality Detected").

**Author(s)**

Fred Violo, OVVO Financial Systems

**References**

Violo, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
set.seed(123)
x <- rnorm(100)

## To call strongest period based on coefficient of variation:
NNS.seas(x, plot = FALSE)$best.period

## Using modulus for logical seasonal inference:
NNS.seas(x, modulo = c(2,3,5,7), plot = FALSE)
```

---

NNS.SSD	<i>NNS SSD Test</i>
---------	---------------------

---

**Description**

Bi-directional test of second degree stochastic dominance using lower partial moments.

**Usage**

```
NNS.SSD(x, y)
```

**Arguments**

x	a numeric vector.
y	a numeric vector.

**Value**

Returns one of the following SSD results: "X SSD Y", "Y SSD X", or "NO SSD EXISTS".

**Author(s)**

Fred Violo, OVVO Financial Systems

## References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. <https://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817>.

## Examples

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.SSD(x, y)
```

---

NNS.SSD.uni

*NNS SSD Test uni-directional*

---

## Description

Uni-directional test of second degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

## Usage

```
NNS.SSD.uni(x, y)
```

## Arguments

x	a numeric vector.
y	a numeric vector.

## Value

Returns (1) if "X SSD Y", else (0).

## Author(s)

Fred Viole, OVVO Financial Systems

## References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. <https://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817>.

## Examples

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.SSD.uni(x, y)
```

NNS.stack

NNS Stack

## Description

Prediction model using the predictions of the NNS base models [NNS.reg](#) as features (i.e. meta-features) for the stacked model.

## Usage

```
NNS.stack(
  IVs.train,
  DV.train,
  IVs.test = NULL,
  type = NULL,
  obj.fn = expression(sum((predicted - actual)^2)),
  objective = "min",
  optimize.threshold = TRUE,
  dist = "L2",
  CV.size = NULL,
  balance = FALSE,
  ts.test = NULL,
  folds = 5,
  order = NULL,
  norm = NULL,
  method = c(1, 2),
  stack = TRUE,
  dim.red.method = "cor",
  status = TRUE,
  ncores = NULL
)
```

## Arguments

IVs.train	a vector, matrix or data frame of variables of numeric or factor data types.
DV.train	a numeric or factor vector with compatible dimensions to (IVs.train).
IVs.test	a vector, matrix or data frame of variables of numeric or factor data types with compatible dimensions to (IVs.train). If NULL, will use (IVs.train) as default.
type	NULL (default). To perform a classification of discrete integer classes from factor target variable (DV.train) with a base category of 1, set to (type = "CLASS"), else for continuous (DV.train) set to (type = NULL). Like a logistic regression, this setting is not necessary for target variable of two classes e.g. [0, 1].
obj.fn	expression; expression(sum((predicted - actual)^2)) (default) Sum of squared errors is the default objective function. Any expression() using the specific terms predicted and actual can be used.
objective	options: ("min", "max") "min" (default) Select whether to minimize or maximize the objective function obj.fn.



optimize.threshold	logical; TRUE (default) Will optimize the probability threshold value for rounding in classification problems. If FALSE, returns 0.5.
dist	options:("L1", "L2", "DTW", "FACTOR") the method of distance calculation; Selects the distance calculation used. <code>dist = "L2"</code> (default) selects the Euclidean distance and ( <code>dist = "L1"</code> ) selects the Manhattan distance; ( <code>dist = "DTW"</code> ) selects the dynamic time warping distance; ( <code>dist = "FACTOR"</code> ) uses a frequency.
CV.size	numeric [0, 1]; NULL (default) Sets the cross-validation size if ( <code>IVs.test = NULL</code> ). Defaults to 0.25 for a 25 percent random sampling of the training set under ( <code>CV.size = NULL</code> ).
balance	logical; FALSE (default) Uses both up and down sampling from <code>caret</code> to balance the classes. <code>type="CLASS"</code> required.
ts.test	integer; NULL (default) Sets the length of the test set for time-series data; typically $2 \times h$ parameter value from <a href="#">NNS.ARMA</a> or double known periods to forecast.
folds	integer; folds = 5 (default) Select the number of cross-validation folds.
order	options: (integer, "max", NULL); NULL (default) Sets the order for <a href="#">NNS.reg</a> , where ( <code>order = "max"</code> ) is the k-nearest neighbors equivalent, which is suggested for mixed continuous and discrete (unordered, ordered) data.
norm	options: ("std", "NNS", NULL); NULL (default) 3 settings offered: NULL, "std", and "NNS". Selects the norm parameter in <a href="#">NNS.reg</a> .
method	numeric options: (1, 2); Select the NNS method to include in stack. ( <code>method = 1</code> ) selects <a href="#">NNS.reg</a> ; ( <code>method = 2</code> ) selects <a href="#">NNS.reg</a> dimension reduction regression. Defaults to <code>method = c(1, 2)</code> , which will reduce the dimension first, then find the optimal <code>n.best</code> .
stack	logical; TRUE (default) Uses dimension reduction output in <code>n.best</code> optimization, otherwise performs both analyses independently.
dim.red.method	options: ("cor", "NNS.dep", "NNS.caus", "equal", "all") method for determining synthetic $X^*$ coefficients. ( <code>dim.red.method = "cor"</code> ) (default) uses standard linear correlation for weights. ( <code>dim.red.method = "NNS.dep"</code> ) uses <a href="#">NNS.dep</a> for nonlinear dependence weights, while ( <code>dim.red.method = "NNS.caus"</code> ) uses <a href="#">NNS.caus</a> for causal weights. ( <code>dim.red.method = "all"</code> ) averages all methods for further feature engineering.
status	logical; TRUE (default) Prints status update message in console.
ncores	integer; value specifying the number of cores to be used in the parallelized subroutine <a href="#">NNS.reg</a> . If NULL (default), the number of cores to be used is equal to the number of cores of the machine - 1.

## Value

Returns a vector of fitted values for the dependent variable test set for all models.

- "[NNS.reg.n.best](#)" returns the optimum "`n.best`" parameter for the [NNS.reg](#) multivariate regression. "[SSE.reg](#)" returns the SSE for the [NNS.reg](#) multivariate regression.
- "[OBJfn.reg](#)" returns the `obj.fn` for the [NNS.reg](#) regression.
- "[NNS.dim.red.threshold](#)" returns the optimum "`threshold`" from the [NNS.reg](#) dimension reduction regression.
- "[OBJfn.dim.red](#)" returns the `obj.fn` for the [NNS.reg](#) dimension reduction regression.

- "probability.threshold" returns the optimum probability threshold for classification, else 0.5 when set to FALSE.
- "reg" returns [NNS.reg](#) output.
- "dim.red" returns [NNS.reg](#) dimension reduction regression output.
- "stack" returns the output of the stacked model.

### Note

- Like a logistic regression, the (type = "CLASS") setting is not necessary for target variable of two classes e.g. [0, 1]. The response variable base category should be 1 for multiple class problems.
- Missing data should be handled prior as well using [na.omit](#) or [complete.cases](#) on the full dataset.

If error received:

"Error in is.data.frame(x) : object 'RP' not found"  
reduce the CV.size.

### Author(s)

Fred Viole, OVVO Financial Systems

### References

Viole, F. (2016) "Classification Using NNS Clustering Analysis" <https://www.ssrn.com/abstract=2864711>

### Examples

```
## Using 'iris' dataset where test set [IVs.test] is 'iris' rows 141:150.
## Not run:
NNS.stack(iris[1:140, 1:4], iris[1:140, 5], IVs.test = iris[141:150, 1:4], type = "CLASS")

## Using 'iris' dataset to determine [n.best] and [threshold] with no test set.
NNS.stack(iris[, 1:4], iris[, 5], type = "CLASS")

## Selecting NNS.reg and dimension reduction techniques.
NNS.stack(iris[1:140, 1:4], iris[1:140, 5], iris[141:150, 1:4], method = c(1, 2), type = "CLASS")
## End(Not run)
```

---

NNS.term.matrix

*NNS Term Matrix*

---

### Description

Generates a term matrix for text classification use in [NNS.reg](#).

### Usage

```
NNS.term.matrix(x, oos = NULL, names = FALSE)
```

**Arguments**

x	mixed data.frame; character/numeric; A two column dataset should be used. Concatenate text from original sources to comply with format. Also note the possibility of factors in "DV", so "as.numeric(as.character(...))" is used to avoid issues.
oos	mixed data.frame; character/numeric; Out-of-sample text dataset to be classified.
names	logical; Column names for "IV" and "oos". Defaults to FALSE.

**Value**

Returns the text as independent variables "IV" and the classification as the dependent variable "DV". Out-of-sample independent variables are returned with "OOS".

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
x <- data.frame(cbind(c("sunny", "rainy"), c(1, -1)))
NNS.term.matrix(x)

### Concatenate Text with space separator, cbind with "DV"
x <- data.frame(cbind(c("sunny", "rainy"), c("windy", "cloudy"), c(1, -1)))
x <- data.frame(cbind(paste(x[, 1], x[, 2], sep = " "), as.numeric(as.character(x[, 3]))))
NNS.term.matrix(x)

### NYT Example
## Not run:
require(RTextTools)
data(NYTimes)

### Concatenate Columns 3 and 4 containing text, with column 5 as DV
NYT <- data.frame(cbind(paste(NYTimes[, 3], NYT[, 4], sep = " "),
                           as.numeric(as.character(NYTimes[, 5]))))
NNS.term.matrix(NYT)
## End(Not run)
```

---

NNS.TSD

---

*NNS TSD Test*


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**Description**

Bi-directional test of third degree stochastic dominance using lower partial moments.

**Usage**

```
NNS.TSD(x, y)
```

**Arguments**

x                      a numeric vector.  
y                      a numeric vector.

**Value**

Returns one of the following TSD results: "X TSD Y", "Y TSD X", or "NO TSD EXISTS".

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." Journal of Mathematical Finance, 6, 105-126. <https://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817>.

**Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.TSD(x, y)
```

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NNS.TSD.uni

*NNS TSD Test uni-directional*


---

**Description**

Uni-directional test of third degree stochastic dominance using lower partial moments used in SD Efficient Set routine.

**Usage**

```
NNS.TSD.uni(x, y)
```

**Arguments**

x                      a numeric vector.  
y                      a numeric vector.

**Value**

Returns (1) if "X TSD Y", else (0).

**Author(s)**

Fred Viole, OVVO Financial Systems

## References

Viole, F. and Nawrocki, D. (2016) "LPM Density Functions for the Computation of the SD Efficient Set." *Journal of Mathematical Finance*, 6, 105-126. <https://www.scirp.org/Journal/PaperInformation.aspx?PaperID=63817>.

## Examples

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100)
NNS.TSD.uni(x, y)
```

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NNS.VAR	<i>NNS VAR</i>
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---

## Description

Nonparametric vector autoregressive model incorporating [NNS.ARMA](#) estimates of variables into [NNS.reg](#) for a multi-variate time-series forecast.

## Usage

```
NNS.VAR(
  variables,
  h,
  tau = 1,
  dim.red.method = "cor",
  obj.fn = expression(sum((predicted - actual)^2)),
  objective = "min",
  status = TRUE,
  ncores = NULL
)
```

## Arguments

variables	a numeric matrix or data.frame of contemporaneous time-series to forecast.
h	integer; 1 (default) Number of periods to forecast. (h = 0) will return just the interpolated and extrapolated values.
tau	positive integer [ > 0]; 1 (default) Number of lagged observations to consider for the time-series data. Vector for single lag for each respective variable or list for multiple lags per each variable.
dim.red.method	options: ("cor", "NNS.dep", "NNS.caus", "all") method for reducing regressors via <a href="#">NNS.stack</a> . (dim.red.method = "cor") (default) uses standard linear correlation for dimension reduction in the lagged variable matrix. (dim.red.method = "NNS.dep") uses <a href="#">NNS.dep</a> for nonlinear dependence weights, while (dim.red.method = "NNS.caus") uses <a href="#">NNS.caus</a> for causal weights. (dim.red.method = "all") averages all methods for further feature engineering.
obj.fn	expression; expression(sum((predicted - actual)^2)) (default) Sum of squared errors is the default objective function. Any expression() using the specific terms predicted and actual can be used.

objective	options: ("min", "max") "min" (default) Select whether to minimize or maximize the objective function <code>obj.fn</code> .
status	logical; TRUE (default) Prints status update message in console.
ncores	integer; value specifying the number of cores to be used in the parallelized subroutine <a href="#">NNS.ARMA.optim</a> . If NULL (default), the number of cores to be used is equal to the number of cores of the machine - 1.

## Value

Returns the following matrices of forecasted variables:

- "interpolated\_and\_extrapolated" Returns a `data.frame` of the linear interpolated and [NNS.ARMA](#) extrapolated values to replace NA values in the original `variables` argument. This is required for working with variables containing different frequencies, e.g. where NA would be reported for intra-quarterly data when indexed with monthly periods.
- "relevant\_variables" Returns the relevant variables from the dimension reduction step.
- "univariate" Returns the univariate [NNS.ARMA](#) forecasts.
- "multivariate" Returns the multi-variate [NNS.reg](#) forecasts.
- "ensemble" Returns the ensemble of both "univariate" and "multivariate" forecasts.

## Note

- `dim.red.method = "cor"` is significantly faster than the other methods, but comes at the expense of ignoring possible nonlinear relationships between lagged variables.
- Not recommended for factor variables, even after transformed to numeric. [NNS.reg](#) is better suited for factor or binary regressor extrapolation.

## Author(s)

Fred Violen, OVVO Financial Systems

## References

- Violen, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)
- Violen, F. (2019) "Multi-variate Time-Series Forecasting: Nonparametric Vector Autoregression Using NNS" <https://www.ssrn.com/abstract=3489550>
- Violen, F. (2020) "NOWCASTING with NNS" <https://www.ssrn.com/abstract=3586658>
- Violen, F. (2019) "Forecasting Using NNS" <https://www.ssrn.com/abstract=3382300>
- Vinod, H. and Violen, F. (2017) "Nonparametric Regression Using Clusters" <https://link.springer.com/article/10.1007/s10614-017-9713-5>
- Vinod, H. and Violen, F. (2018) "Clustering and Curve Fitting by Line Segments" <https://www.preprints.org/manuscript/201801.0090/v1>

## Examples

```
## Not run:
#####
### Standard Nonparametric Vector Autoregression ###
#####
```

```

set.seed(123)
x <- rnorm(100) ; y <- rnorm(100) ; z <- rnorm(100)
A <- cbind(x = x, y = y, z = z)

### Using lags 1:4 for each variable
NNS.VAR(A, h = 12, tau = 4, status = TRUE)

### Using lag 1 for variable 1, lag 3 for variable 2 and lag 3 for variable 3
NNS.VAR(A, h = 12, tau = c(1,3,3), status = TRUE)

### Using lags c(1,2,3) for variables 1 and 3, while using lags c(4,5,6) for variable 2
NNS.VAR(A, h = 12, tau = list(c(1,2,3), c(4,5,6), c(1,2,3)), status = TRUE)

### CONFIDENCE INTERVALS FOR PREDICTIONS
# Store NNS.VAR output
nns_estimate <- NNS.VAR(A, h = 12, tau = 4, status = TRUE)

# Create bootstrap replicates using NNS.meboot
replicates <- NNS.meboot(nns_estimate$ensemble[,1])$replicates

# Apply UPM.VaR and LPM.VaR for desired confidence interval
# Tail percentage used in first argument per {LPM.VaR} and {UPM.VaR} functions
upper_CIs <- apply(replicates, 1, function(g) UPM.VaR(.025, 0, g))
lower_CIs <- apply(replicates, 1, function(g) LPM.VaR(.025, 0, g))

# View results
cbind(nns_estimate$ensemble[,1], lower_CIs, upper_CIs)

#####
### NOWCASTING with Mixed Frequencies ###
#####

library(Quandl)
econ_variables <- Quandl(c("FRED/GDPC1", "FRED/UNRATE", "FRED/CPIAUCSL"), type = 'ts',
                        order = "asc", collapse = "monthly", start_date = "2000-01-01")

### Note the missing values that need to be imputed
head(econ_variables)
tail(econ_variables)

NNS.VAR(econ_variables, h = 12, tau = 12, status = TRUE)

## End(Not run)

```

---

PM.matrix

---

*Partial Moment Matrix*


---

## Description

This function generates a co-partial moment matrix for the specified co-partial moment.

**Usage**

```
PM.matrix(LPM.degree, UPM.degree, target = NULL, variable, pop.adj = FALSE)
```

**Arguments**

LPM.degree	integer; Degree for variable below target deviations. (degree = 0) is frequency, (degree = 1) is area.
UPM.degree	integer; Degree for variable above target deviations. (degree = 0) is frequency, (degree = 1) is area.
target	numeric; Typically the mean of Variable X for classical statistics equivalences, but does not have to be. (Vectorized) (target = NULL) (default) will set the target as the mean of every variable.
variable	a numeric matrix or data.frame.
pop.adj	logical; FALSE (default) Adjusts the sample co-partial moment matrices for population statistics.

**Value**

Matrix of partial moment quadrant values (CUPM, DUPM, DLPM, CLPM), and overall covariance matrix. Uncalled quadrants will return a matrix of zeros.

**Note**

For divergent asymmetrical "D.LPM" and "D.UPM" matrices, matrix is D.LPM(column,row,...).

**Author(s)**

Fred Violen, OVVO Financial Systems

**References**

Violen, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments" [https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

Violen, F. (2017) "Bayes' Theorem From Partial Moments" <https://www.ssrn.com/abstract=3457377>

**Examples**

```
set.seed(123)
x <- rnorm(100) ; y <- rnorm(100) ; z <- rnorm(100)
A <- cbind(x,y,z)
PM.matrix(LPM.degree = 1, UPM.degree = 1, variable = A)

## Use of vectorized numeric targets (target_x, target_y, target_z)
PM.matrix(LPM.degree = 1, UPM.degree = 1, target = c(0, 0.15, .25), variable = A)

## Calling Individual Partial Moment Quadrants
cov.mtx <- PM.matrix(LPM.degree = 1, UPM.degree = 1, variable = A)
cov.mtx$cupm

## Full covariance matrix
cov.mtx$cov.matrix
```



UPM

*Upper Partial Moment***Description**

This function generates a univariate upper partial moment for any degree or target.

**Usage**

```
UPM(degree, target, variable)
```

**Arguments**

degree	integer; (degree = 0) is frequency, (degree = 1) is area.
target	numeric; Typically set to mean, but does not have to be. (Vectorized)
variable	a numeric vector.

**Value**

UPM of variable

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
set.seed(123)
x <- rnorm(100)
UPM(0, mean(x), x)
```

UPM.ratio

*Upper Partial Moment RATIO***Description**

This function generates a standardized univariate upper partial moment for any degree or target.

**Usage**

```
UPM.ratio(degree, target, variable)
```

**Arguments**

degree	integer; (degree = 0) is frequency, (degree = 1) is area.
target	numeric; Typically set to mean, but does not have to be. (Vectorized)
variable	a numeric vector.

**Value**

Standardized UPM of variable

**Author(s)**

Fred Viole, OVVO Financial Systems

**References**

Viole, F. and Nawrocki, D. (2013) "Nonlinear Nonparametric Statistics: Using Partial Moments"  
[https://www.amazon.com/dp/1490523995/ref=cm\\_sw\\_su\\_dp](https://www.amazon.com/dp/1490523995/ref=cm_sw_su_dp)

**Examples**

```
set.seed(123)
x <- rnorm(100)
UPM.ratio(0, mean(x), x)

## Joint Upper CDF
## Not run:
x <- rnorm(5000) ; y <- rnorm(5000)
plot3d(x, y, Co.UPM(0, 0, sort(x), sort(y), x, y), col = "blue", xlab = "X", ylab = "Y",
zlab = "Probability", box = FALSE)

## End(Not run)
```

---

UPM.VaR

---

*UPM VaR*


---

**Description**

Generates an upside value at risk (VaR) quantile based on the Upper Partial Moment ratio

**Usage**

```
UPM.VaR(percentile, degree, x)
```

**Arguments**

percentile	numeric [0, 1]; The percentile for right-tail VaR (vectorized).
degree	integer; (degree = 0) for discrete distributions, (degree = 1) for continuous distributions.
x	a numeric vector.

**Value**

Returns a numeric value representing the point at which "percentile" of the area of x is above.

**Examples**

```
set.seed(123)
x <- rnorm(100)

## For 5th percentile, right-tail
UPM.VaR(0.05, 0, x)
```

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