

# Newton's Method Calculation

A quadratic equation with one variable (一元二次方程) is a equation that can be rearranged in standard form as  $ax^2 + bx + c = 0$ , where  $a$  ( $a \neq 0$ ),  $b$ , and  $c$  are constants.

The Newton's method is an iterative method that can be used to find the roots of a function. It involves choosing an initial guess and then repeatedly refining it until the solution is found.

In this problem, we are going to use the Newton' method to solve a quadratic equation with one variable. The inputs correspond to values **a, b, and c respectively** and the output are the solutions  $x_1$  and  $x_2$  in **increasing order**.

## Hint:

1. All the numbers in the calculation are taken as **double-precision**.
2. We make sure there must be **two different solutions** to this equation.
3. We make sure  $a$ ,  $b$  and  $c$  are **non-zero**.
4. When you substitute your solution  $x_n$  into the equation, the absolute value of the result  $|f(x_n)|$  should be less than **1e-6**. Once a result satisfying to this precision, it is considered to be a correct result, and iteration cannot be continued.
5. You can use `abs.d` to get the absolute value.
6. About the output, there is only **one newline** between the smaller value and the bigger value.

## The process is like this:

After reading  $a$ ,  $b$  and  $c$ , first calculate  $-\frac{b}{2a}$ , then minus  $1e-6$  as the first guess

$x_{fSmaller}$  for smaller  $x_n$ , and add  $1e-6$  as the first guess  $x_{fBigger}$  for bigger  $x_n$ .

Let's calculate smaller  $x_n$  as an example. The equation is like  $f(x) = ax^2 + bx + c$ , and calculate  $|f(x_n)|$  with our first guess  $x_{fSmaller}$ , and check whether  $|f(x_n)|$  is less than **1e-6**. If it satisfies, then this  $x_n$  is one of the results, but if not, calculate  $x_{n+1}$

like this  $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)} = x_n - \frac{ax_n^2 + bx_n + c}{2ax_n + b}$  as the next iteration's input.

## Standard:

To make sure the **precision**, please use data like this:

```
1  .data
2      precision: .double 0.000001
3      newline: .asciiz "\n"
```

And in text: You can use `ldc1 $f20, precision` for loading the precision, when calculating whether the result is less than the precision, you can use `c.lt.d $f8, $f20`.

When reading a, b and c it can be like this:

```
1  .text
2      li $v0, 7
3      syscall
4      mov.d $f14, $f0
5      syscall
6      mov.d $f16, $f0
7      syscall
8      mov.d $f18, $f0
```

## Sample inputs and outputs:

### Sample Input1:

```
1  1
2  4
3  1
```

### Sample Output1:

```
1  -3.732050820939485
2  -0.2679491790605153
```

### Sample Input2:

```
1  1
2  -5
3  6
```

### Sample Output2:

```
1  1.99999994826938
2  3.000000051730621
```

**Sample Input3:**

```
1  1.5
2  9.3
3  -4.7
```

**Sample Output3:**

```
1  -6.669780621053905
2  0.46978062105390345
```

**Sample Input4:**

```
1  5.2232
2  17.3754
3  3.2523
```

**Sample Output4:**

```
1  -3.127487307501963
2  -0.19909409853265192
```