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1 function res = RK43D(f1, f2, f3, X0, h, t)
2 % RK4 method in 3d case;
3 % fi: component in each dimension
4 % X0 = (x0, y0, z0): initial values
5 % h: step size
6 % t = (t0, t1): time period
7 t0 = t(1)-h; t1 = t(2);
8 nstep = (t1-t0)/h;
9 res = zeros(nstep, 3);
10 x0 = X0(1); y0 = X0(2); z0 = X0(3);
11 for i = 1:nstep
12     t0 = t0+h;
13     res(i, 1) = x0; res(i, 2) = y0; res(i, 3) = z0;
14     X1 = x0; Y1 = y0; Z1 = z0;
15     X2 = x0+h/2*f1(t0, X1, Y1, Z1);
16     Y2 = y0+h/2*f2(t0, X1, Y1, Z1);
17     Z2 = z0+h/2*f3(t0, X1, Y1, Z1);
18     X3 = x0+h/2*f1(t0+h/2, X2, Y2, Z2);
19     Y3 = y0+h/2*f2(t0+h/2, X2, Y2, Z2);
20     Z3 = z0+h/2*f3(t0+h/2, X2, Y2, Z2);
21     X4 = x0+h*f1(t0+h/2, X3, Y3, Z3);
22     Y4 = y0+h*f2(t0+h/2, X3, Y3, Z3);
23     Z4 = z0+h*f3(t0+h/2, X3, Y3, Z3);
24     x0 = x0+h/6*(f1(t0, X1, Y1, Z1)+2*f1(t0+h/2, X2, Y2, Z2)...
25         +2*f1(t0+h/2, X3, Y3, Z3)+f1(t0+h, X4, Y4, Z4));
26     y0 = y0+h/6*(f2(t0, X1, Y1, Z1)+2*f2(t0+h/2, X2, Y2, Z2)...
27         +2*f2(t0+h/2, X3, Y3, Z3)+f2(t0+h, X4, Y4, Z4));
28     z0 = z0+h/6*(f3(t0, X1, Y1, Z1)+2*f3(t0+h/2, X2, Y2, Z2)...
29         +2*f3(t0+h/2, X3, Y3, Z3)+f3(t0+h, X4, Y4, Z4));
30 end

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1 f1 = @(t, x, y, z) 10*(y-x);
2 f3 = @(t, x, y, z) -8/3*z+x*y;
3 t = [0, 120];
4 h = 0.004;
5 R = [1, 14, 24, 24.2, 28, 100, 102, 400];
6 for i = 1:length(R)
7     r = R(i);
8     figure(i);
9     f2 = @(t, x, y, z) r*x-y-x*z;
10    X0 = [-8, 8, r-1];
11    res = RK43D(f1, f2, f3, X0, h, t);
12    plot3(res(:,1), res(:,2), res(:,3));
13    grid on;
14    xlabel('x');
15    ylabel('y');
16    zlabel('z');
17    title(strcat('r = ', num2str(r)));
18 end

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