

Bias Adjustment of ESPO-G6 v1.0

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This description of the ESPO-G6 v1.0 bias adjustment method is adapted from the description of the ESPO-R5 v1.0 method as both dataset were adjusted in the same way. The workflow for bias adjustment of ESPO-G6 was built with xscen. Temperature and precipitation data from the simulations were first extracted over an area covering North America.

The ESPO-G6 v1.0 bias adjustment procedure uses algorithms provided by xclim to adjust simulation bias following a quantile mapping procedure. In particular, the algorithm used is inspired by the "Detrended Quantile Mapping" method described by [2]. The procedure is univariate, bipartite, acts differently on the trends and the anomalies, and is applied iteratively on each day of the year (grouping) as well as on each grid point.

1 Variables

Adjustments were applied separately for each of the three (3) variables. Adjusting `tasmax` and `tasmin` independently can lead to physical inconsistencies in the final data (i.e., cases with `tasmin > tasmax`; [4], [1]). To ensure a physically consistent dataset (for this aspect at least), we computed the daily temperature range (or amplitude; `dtr = tasmax - tasmin`) and adjusted this variable, in addition to the `tasmax` and `pr` variables. `tasmin` is reconstructed after the bias-adjustment and this is the variable we store.

While `tasmax` has no physical bounds in practice, this is not the case for `pr` and `dtr` where a lower bound, at zero (0), exists. Because of this, the adjustment process explained below exists in two flavours: additive and multiplicative. In the latter, it is mathematically impossible for adjusted data to descend below zero (0).

2 Regridding

All the extracted simulation data was interpolated to the ERA5-Land grid. Because of the large difference in resolution between the simulations and ERA5-Land, the regridding is made in cascades, passing through a 1°grid and a 0.5°grid before the final 9 km resolution ERA5-Land grid. Each step used the bilinear method. This is the main difference between ESPO-R5 v1.0 and ESPO-G6 v1.0 methods.

3 Bias-adjustment

The bias adjustment acts independently on each day of the year as well as each grid point. To render the procedure more robust, a window of 31 days around the current day of the year was included in the inputs of the calibration (training step). For example, the adjustment for February 1 (day 32) was calibrated using data from January 15 to February 15, over the 30 years of the reference period; For leap years, this would mean that there are four (4) times fewer data points for the 366th day of the year. To circumvent this issue, we converted all inputs to a "no leap" calendar by dropping data on the 29th of February, except for simulations using the "360.day" calendar. In the latter case, the simulations were untouched but the reference data was converted to that calendar by dropping extra days taken at regular intervals.¹

3.1 Detrending

For each day of the year and each grid points, we first computed the averages and "anomalies" of the reference data and the simulations over the 1991-2020 reference period. Depending on the variable, anomalies are either taken

¹In a normal year, February 6th, April 20th, July 2nd, September 13th and November 25th are dropped. For a leap year, it is January 31st, April 1st, June 1st, August 1st, September 31st and December 1st.

additively or multiplicatively:

$$Y_r = \begin{cases} \overline{Y_r} + Y'_r & \text{tasmax} \\ \overline{Y_r} \cdot Y'_r & \text{dtr, pr} \end{cases} \quad (1)$$

and similarly for X_c , $\overline{X_c}$ and X'_c .

Instead of a simple moving mean, X_s was detrended with a locally weighted regression (LOESS; [3]). We chose this method for its slightly heavier weights given at the centre of the moving window, reducing impacts of abrupt interannual changes on the trend and anomalies. It also has a more robust handling of the extremities of the timeseries. The LOESS window had a 30-year width and a tricube shape, the local regression was of degree 0 and only one iteration was performed. The detrending was applied on each day of the year but after averaging over the 31-day window, it yielded the trend $\overline{X_s}$ and the residuals X'_s . Here again, the process can be additive or multiplicative.

3.2 Adjustment of the residuals

With $F_{Y'_r}$ and $F_{X'_c}$ the empirical cumulative distribution functions (CDF) of Y'_r and X'_c respectively, an adjustment factor function was first computed:

$$A_+(q) := F_{Y'_r}^{-1}(q) - F_{X'_c}^{-1}(q) \quad A_\times(q) := \frac{F_{Y'_r}^{-1}(q)}{F_{X'_c}^{-1}(q)} \quad (2)$$

Where q is a quantile (in range $[0, 1]$), $A_+(q)$ is the additive function used with **tasmax** and $A_\times(q)$ the multiplicative one, used with **pr** and **dtr**. The CDFs were then estimated from the 30 31-day windows. In the implementation, maps of A were saved to disk by sampling q with 50 values, going from 0.01 to 0.99 by steps of 0.02. The adjustment was then as follows:

$$X'_{ba} = X'_s + A_+(F_{X'_c}(X'_s)) \quad X'_{ba} = X'_s \cdot A_\times(F_{X'_c}(X'_s)) \quad (3)$$

Nearest neighbour interpolation was used to map $F_{X'_c}(X'_s)$ to the 50 values of q . Constant extrapolation was used for values of X'_s outside the range of X'_c .

3.3 Adjustment of the trend

In the training step, a simple scaling or offset factor was computed from the averages:

$$C_+ = \overline{Y_r} - \overline{X_c} \quad C_\times = \frac{\overline{Y_r}}{\overline{X_c}} \quad (4)$$

This factor was then applied to the trend in the adjustment step:

$$\overline{X_{ba}} = \overline{X_s} + C_+ \quad \overline{X_{ba}} = \overline{X_s} \cdot C_\times \quad (5)$$

3.4 Final scenario

Finally, the bias-adjusted timeseries for this day of the year, grid point, and variable was as follows:

$$X_{ba} = \overline{X_{ba}} + X'_{ba} \quad (6)$$

4 Pre-processing of precipitation

It should be noted that the multiplicative mode is prone to division by zero, especially with precipitation where values of zero are quite common. This problem was avoided by modifying the inputs of the calibration step where the zeros of precipitation were replaced by random values between zero (excluded) and 0.01 mm/d.

As observed by [5], when the model has a higher dry-day frequency than the reference, the calibration step of the quantile mapping adjustment will incorrectly map all dry days to precipitation days, resulting in a wet bias. The frequency adaptation method finds the fraction of "extra" dry days:

$$\Delta P_{dry} = \frac{F_{X_c}(D) - F_{Y_r}(D)}{F_{X_c}} \quad (7)$$

Where D is the dry-day threshold, taken here to be 1 mm/d. This fraction of dry days was transformed into wet days by injecting random values taken in the interval $[D, F_{Y_r}^{-1}(F_{X_c}(D))]$.

Both pre-processing functions were applied only on the calibration step inputs (Y_r and X_c) before the division between average and anomalies. As such, only the adjustment factors were impacted while there were no explicitly injected precipitation values in the final scenarios.

5 Pre- and post-processing of daily temperature range

As `dtr` uses the multiplicative mode, like `pr`, divisions by 0 should also be avoided for this variable. Even though `dtr` values close to 0K are rare, the `dtr` timeseries was modified for values under 0.0001 K with random values above 0 K.

As CMIP6 models have very large grid cells, regions that are considered land on the ERA5-Land grid might be completely on an ocean grid cell in the model. In regions with ice, this can lead to issues with `dtr` being very small over water and larger over ice. These variations do not play well with the quantile mapping which can lead to very large `dtr` and be translated into non-physical `tasmin`. This problem has only been seen in Alaska and Greenland for the model BCC-CSM2-MR and GFDL-ESM4. Instances of `tasmin` smaller than 100 K have been replaced by NaNs.

References

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