$$\lim_{n \to \infty} \sup_{x \in \mathbb{R}} f_n(x^2) < n \Big(\sum_{x \in \mathbb{R}, n \in \mathbb{N}} \big| f_n(x^2) \big| \Big)$$