

NORMAL DISTRIBUTION

NORMAL DISTRIBUTION

THE NORMAL DISTRIBUTION HOLDS
A SPECIAL ROLE IN STATISTICS

IT TURNS OUT THAT MANY, MANY
PHENOMENA IN REAL LIFE FOLLOW
THE NORMAL CURVE

NORMAL DISTRIBUTION

WEIGHTS OF A TEAM
OF FOOTBALL PLAYERS

NORMAL DISTRIBUTION

HEIGHTS OF A GROUP
OF FOOTBALL PLAYERS

THE **SIZES OF HOUSES** IN A
NEIGHBORHOOD

NORMAL DISTRIBUTION

HEIGHTS OF A GROUP
OF FOOTBALL PLAYERS

THE SIZES OF HOUSES
IN A NEIGHBORHOOD

THE **NUMBER OF DEFECTS** IN
A LOT AT A FACTORY

NORMAL DISTRIBUTION

HEIGHTS OF A GROUP
OF FOOTBALL PLAYERS

THE SIZES OF HOUSES
IN A NEIGHBORHOOD

THE NUMBER OF
DEFECTS IN A LOT
AT A FACTORY

THE **IQs** OF A GROUP OF
STUDENTS

NORMAL DISTRIBUTION

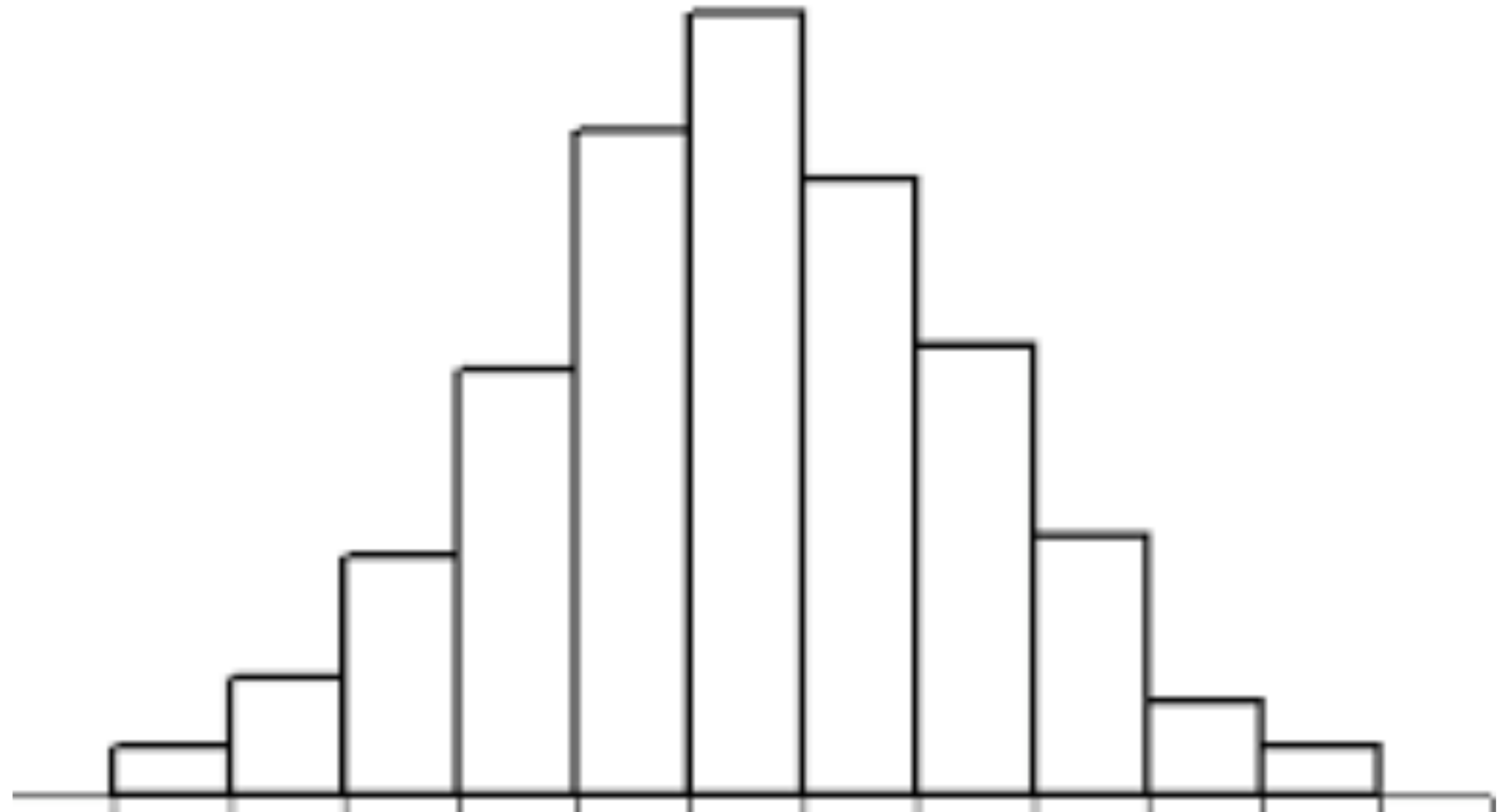
IF YOU TAKE **ANY OF THESE** AND PLOT A
HISTOGRAM OF THE VALUES

HEIGHTS OF A GROUP
OF FOOTBALL PLAYERS

THE SIZES OF HOUSES
IN A NEIGHBORHOOD

THE NUMBER OF
DEFECTS IN A LOT
AT A FACTORY

THE IQs OF A
GROUP OF
STUDENTS



NORMAL DISTRIBUTION

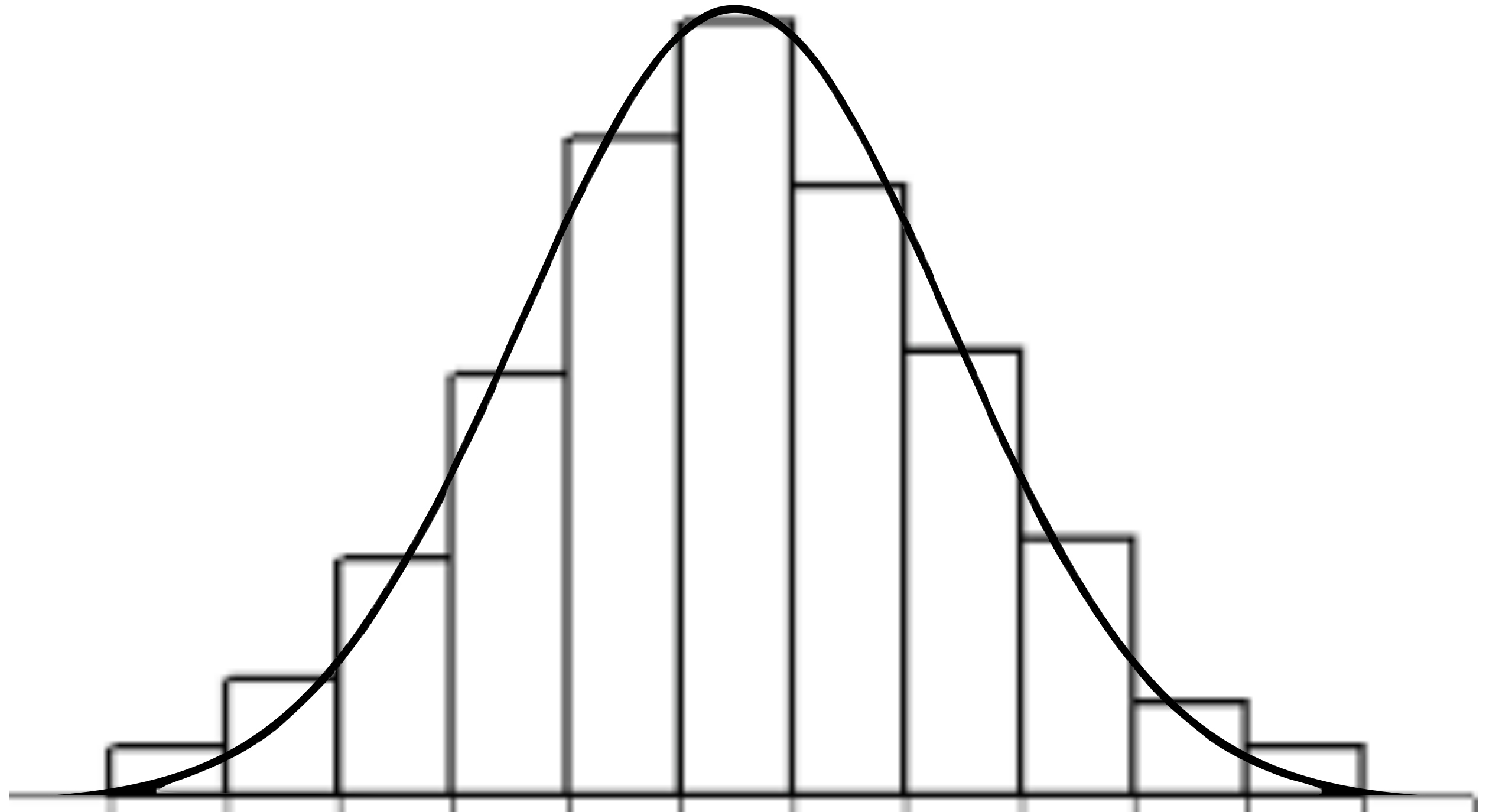
THE **RESULT** WILL BE VERY CLOSE THE
NORMAL DISTRIBUTION CURVE

HEIGHTS OF A GROUP
OF FOOTBALL PLAYERS

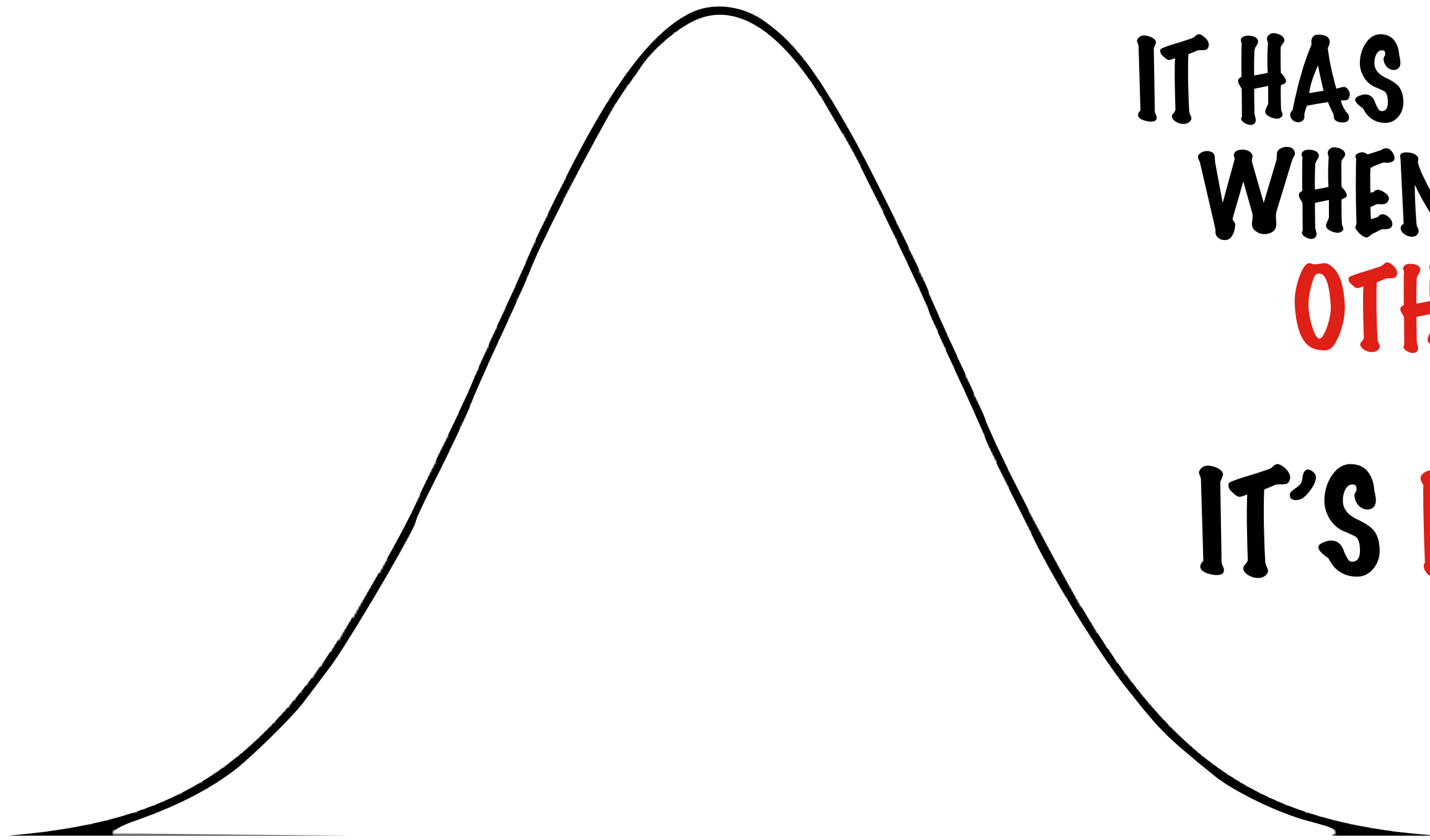
THE SIZES OF HOUSES
IN A NEIGHBORHOOD

THE NUMBER OF
DEFECTS IN A LOT
AT A FACTORY

THE IQs OF A
GROUP OF
STUDENTS



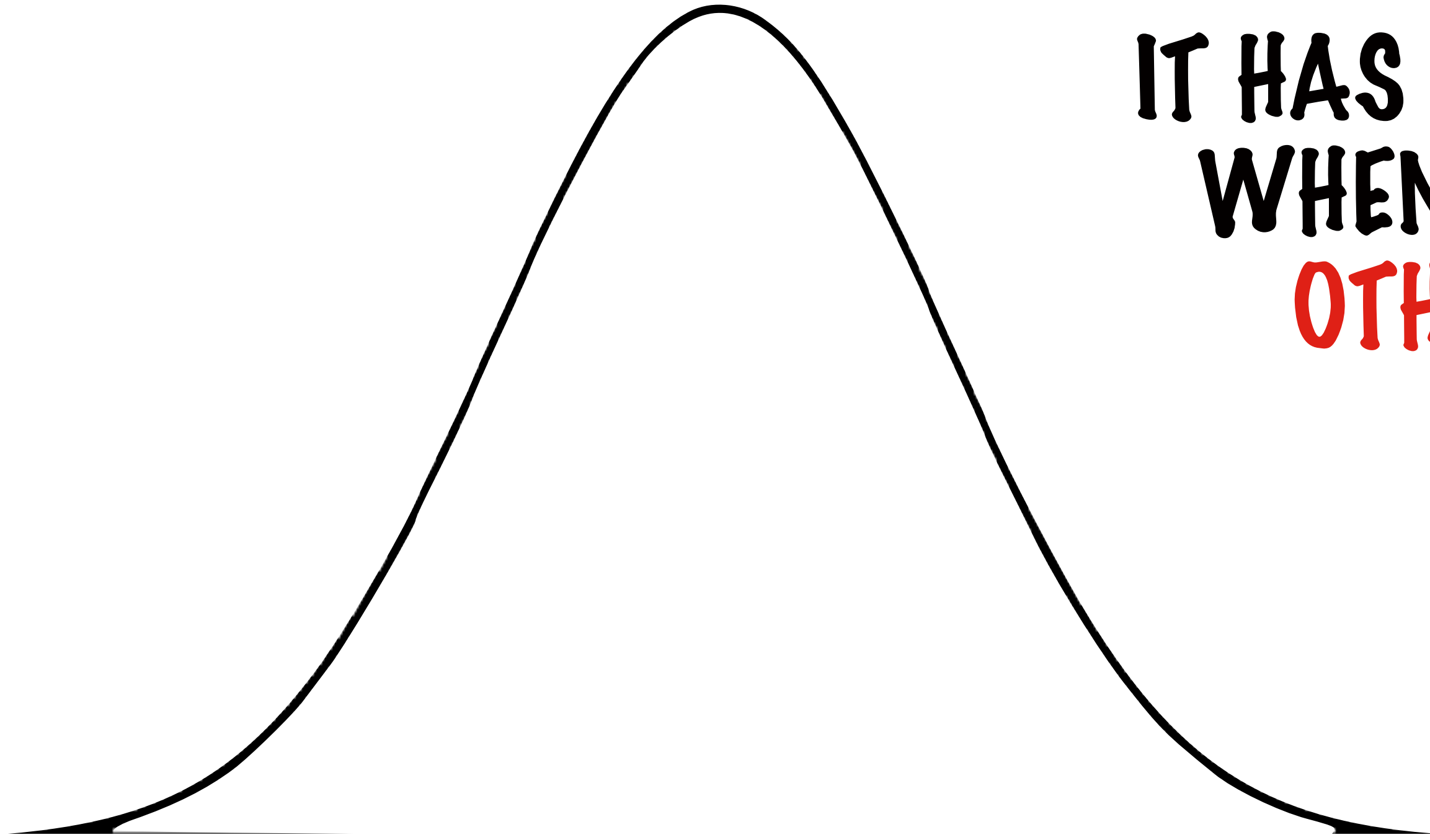
NORMAL DISTRIBUTION



IT HAS BEEN **MATHEMATICALLY PROVED** THAT
WHEN **ANYTHING** IS THE RESULT OF **MANY**
OTHER INDEPENDENT RANDOM THINGS

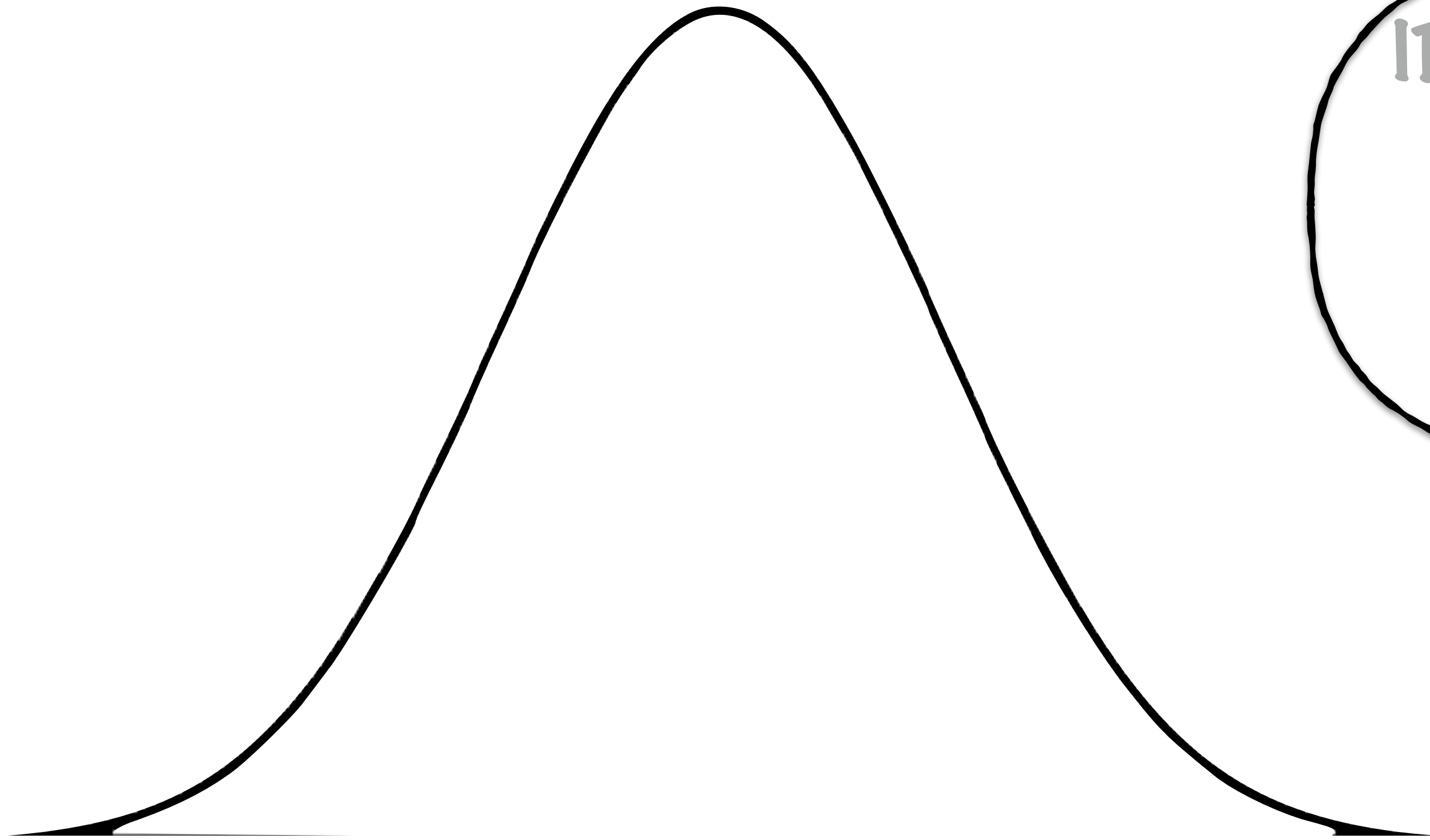
IT'S **DISTRIBUTION** WILL FOLLOW
THE **NORMAL CURVE**

NORMAL DISTRIBUTION



IT HAS BEEN **MATHEMATICALLY PROVED** THAT
WHEN **ANYTHING** IS THE RESULT OF **MANY**
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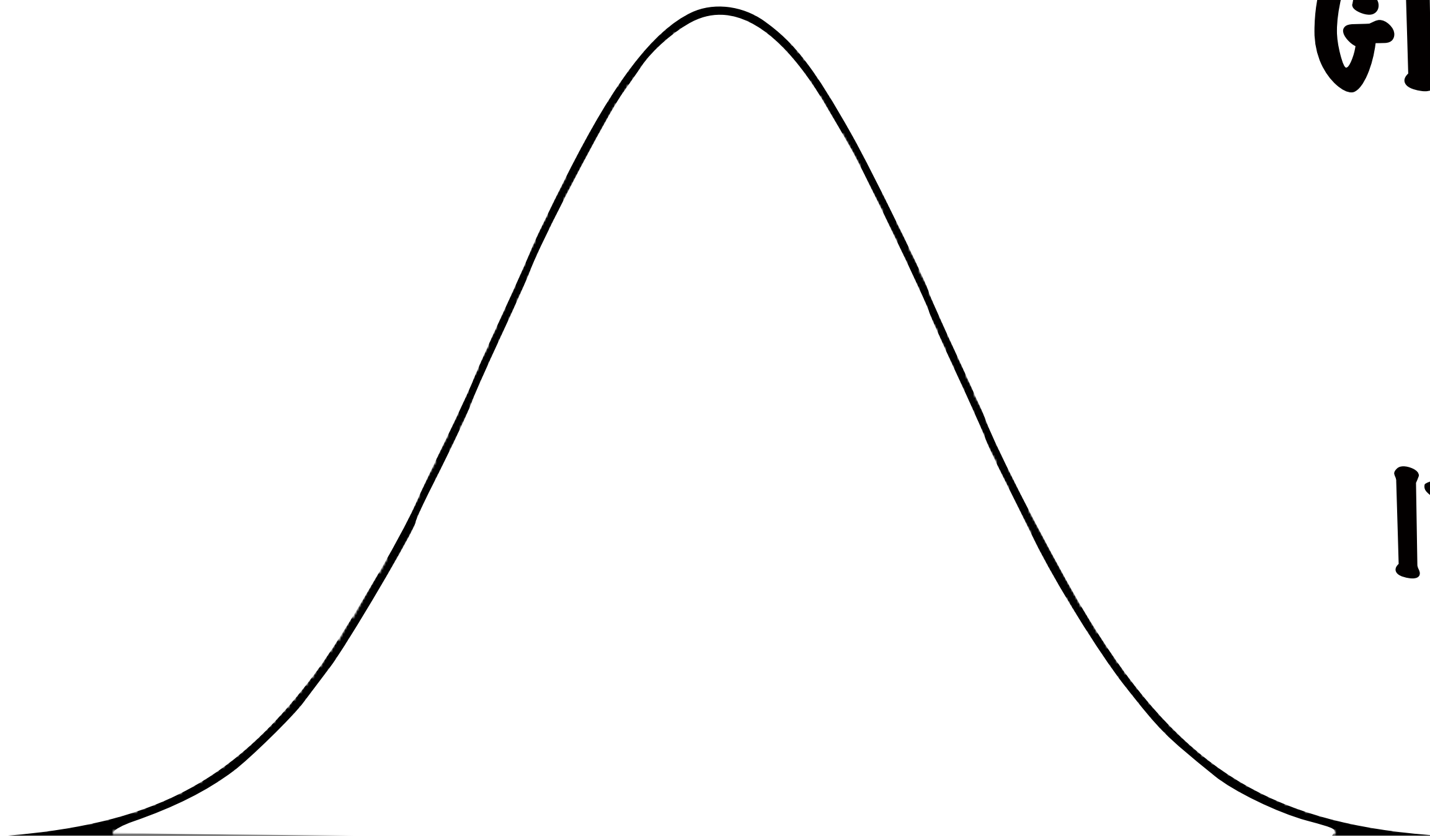
NORMAL DISTRIBUTION



IT HAS BEEN MATHEMATICALLY PROVED THAT
WHEN ANYTHING IS THE RESULT OF MANY
OTHER INDEPENDENT RANDOM THINGS
IT'S DISTRIBUTION WILL FOLLOW THE
NORMAL CURVE

THE **CENTRAL LIMIT**
THEOREM

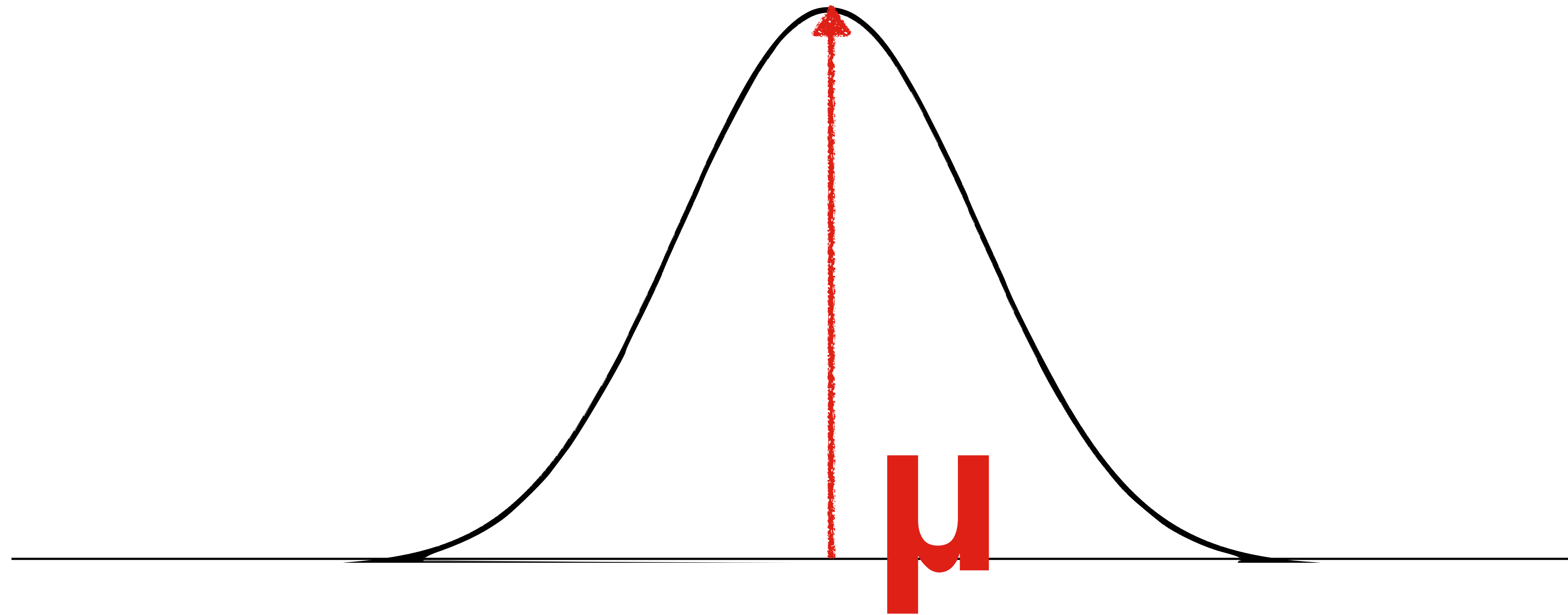
NORMAL DISTRIBUTION



GIVEN **HOW OFTEN** WE'LL
COME ACROSS IT

IT'S **WORTH SPENDING SOME
TIME** UNDERSTANDING IT'S
CHARACTERISTICS

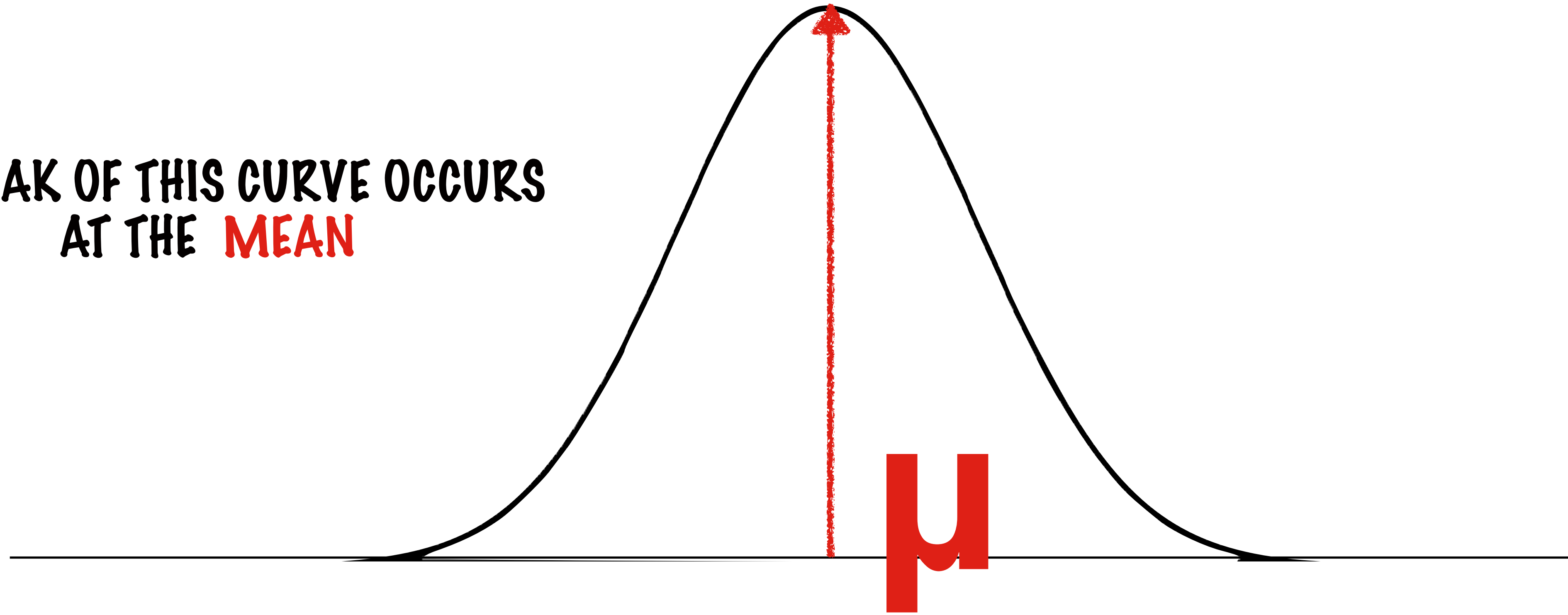
NORMAL DISTRIBUTION



THE PEAK OF THIS
CURVE OCCURS AT THE
MEAN

NORMAL DISTRIBUTION

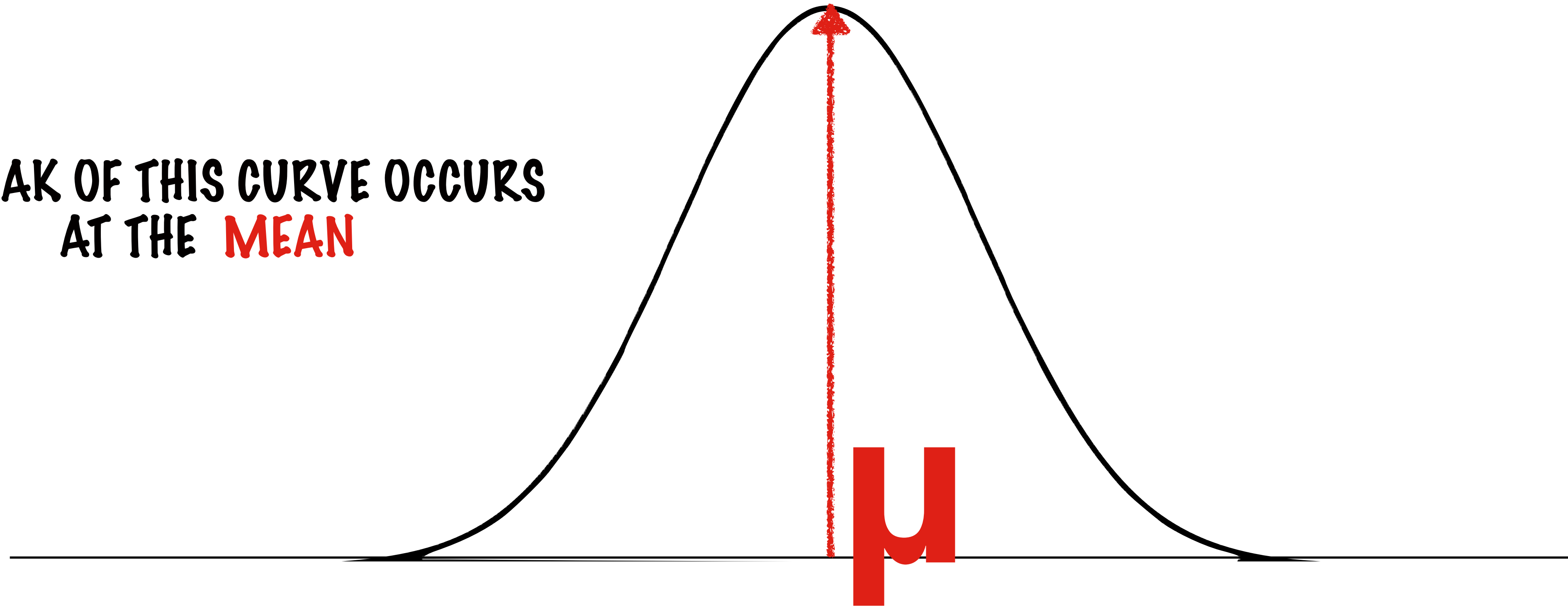
THE PEAK OF THIS CURVE OCCURS
AT THE **MEAN**



WHEN A VARIABLE IS NORMAL, IT'S **VALUE**
WILL "**MOST LIKELY**" BE CLOSE TO THE MEAN

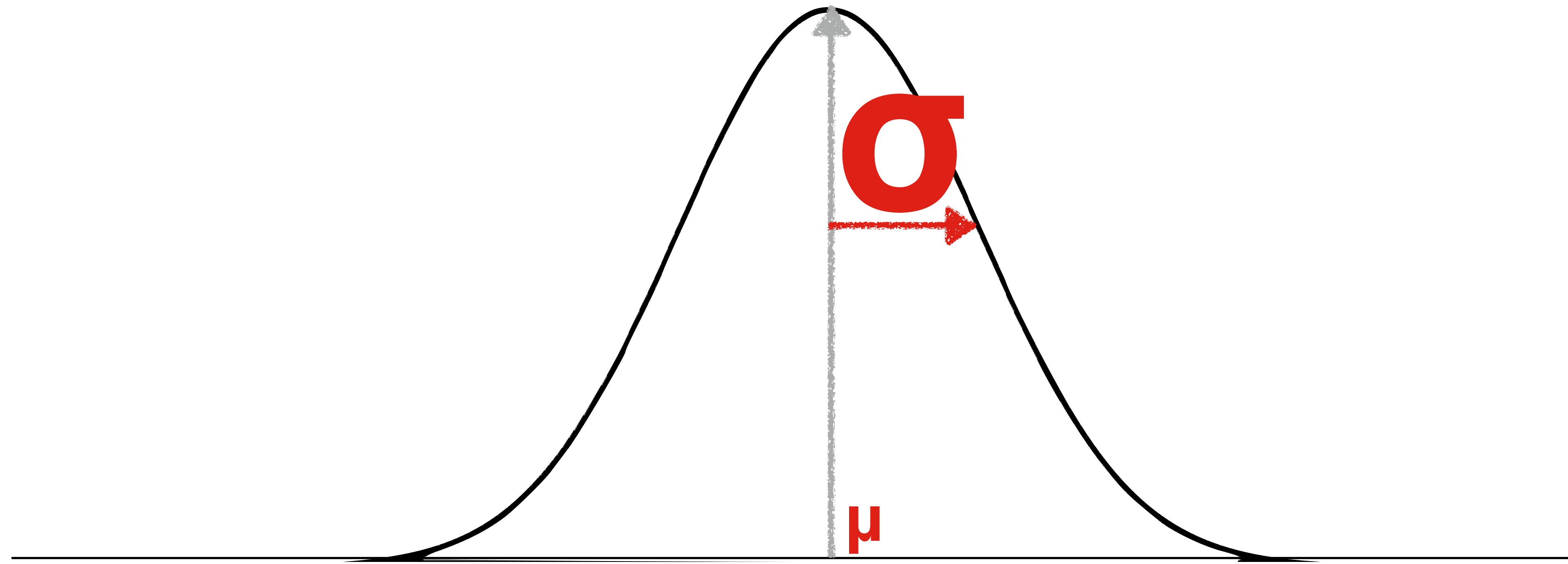
NORMAL DISTRIBUTION

THE PEAK OF THIS CURVE OCCURS
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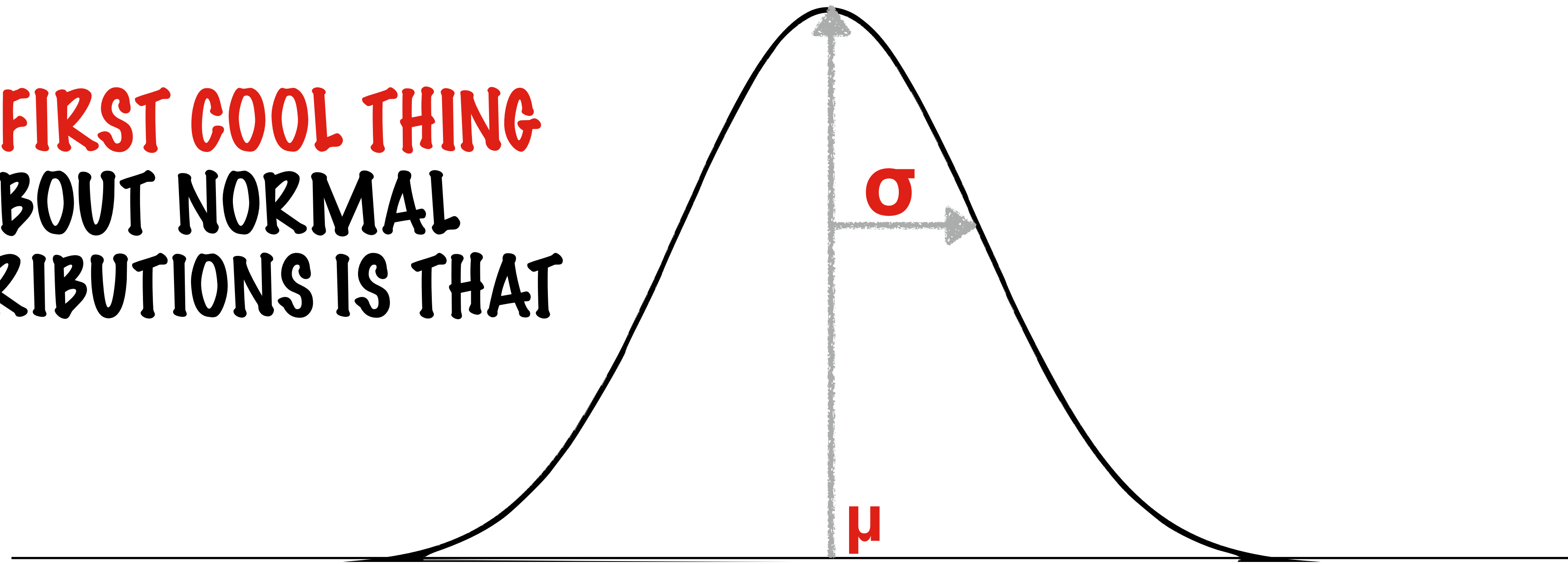
NORMAL DISTRIBUTION



THE **SPREAD** OF THIS CURVE IS
GIVEN BY THE **STANDARD DEVIATION**

NORMAL DISTRIBUTION

THE **FIRST COOL THING**
ABOUT NORMAL
DISTRIBUTIONS IS THAT

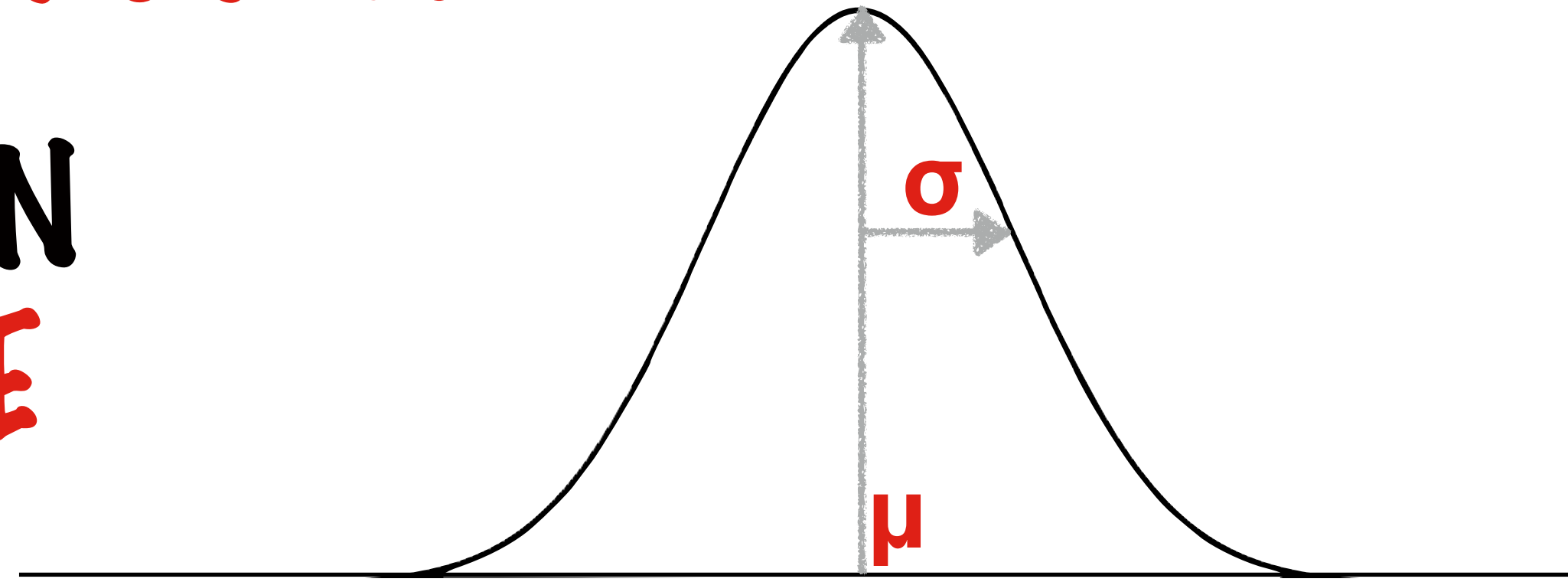


IF YOU KNOW **THE MEAN, SD**
YOU CAN TELL THE
PROBABILITY OF ANY VALUE

NORMAL DISTRIBUTION

IF YOU KNOW THE MEAN, SD YOU CAN
TELL THE PROBABILITY OF ANY VALUE

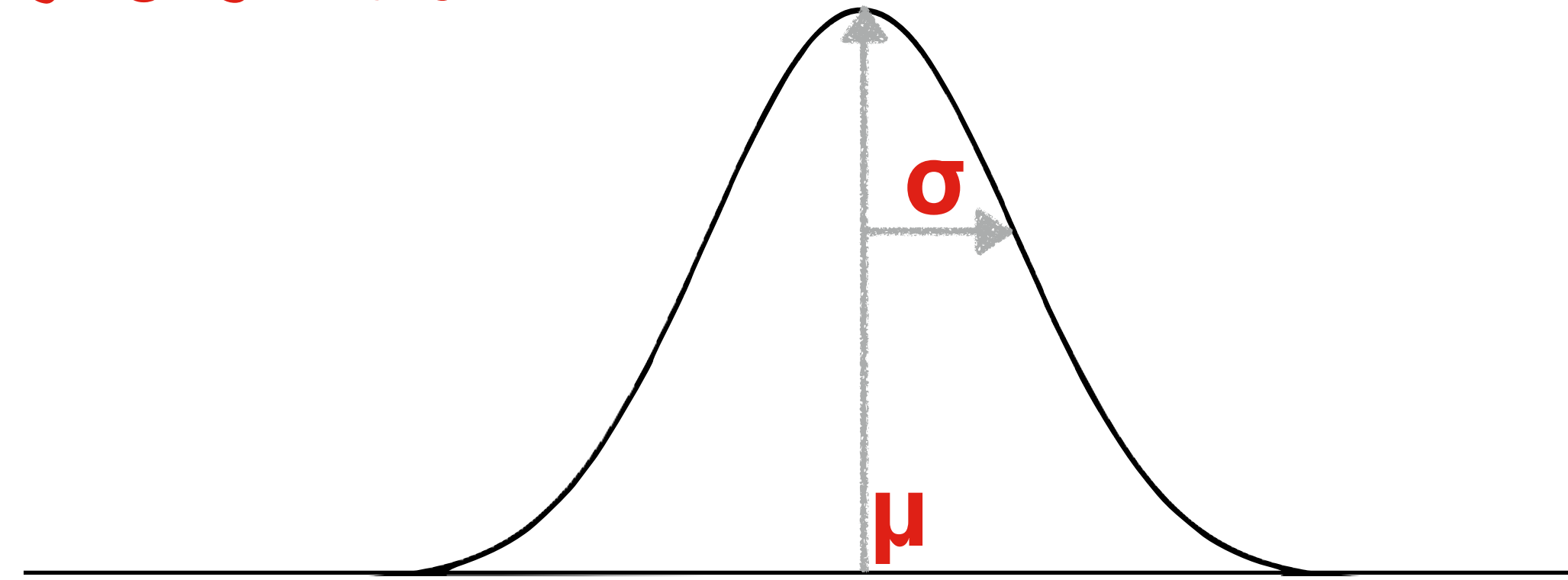
$$f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$



Ummm!! You lost
me there!

NORMAL DISTRIBUTION

IF YOU KNOW THE MEAN, SD YOU CAN TELL
THE PROBABILITY OF ANY VALUE

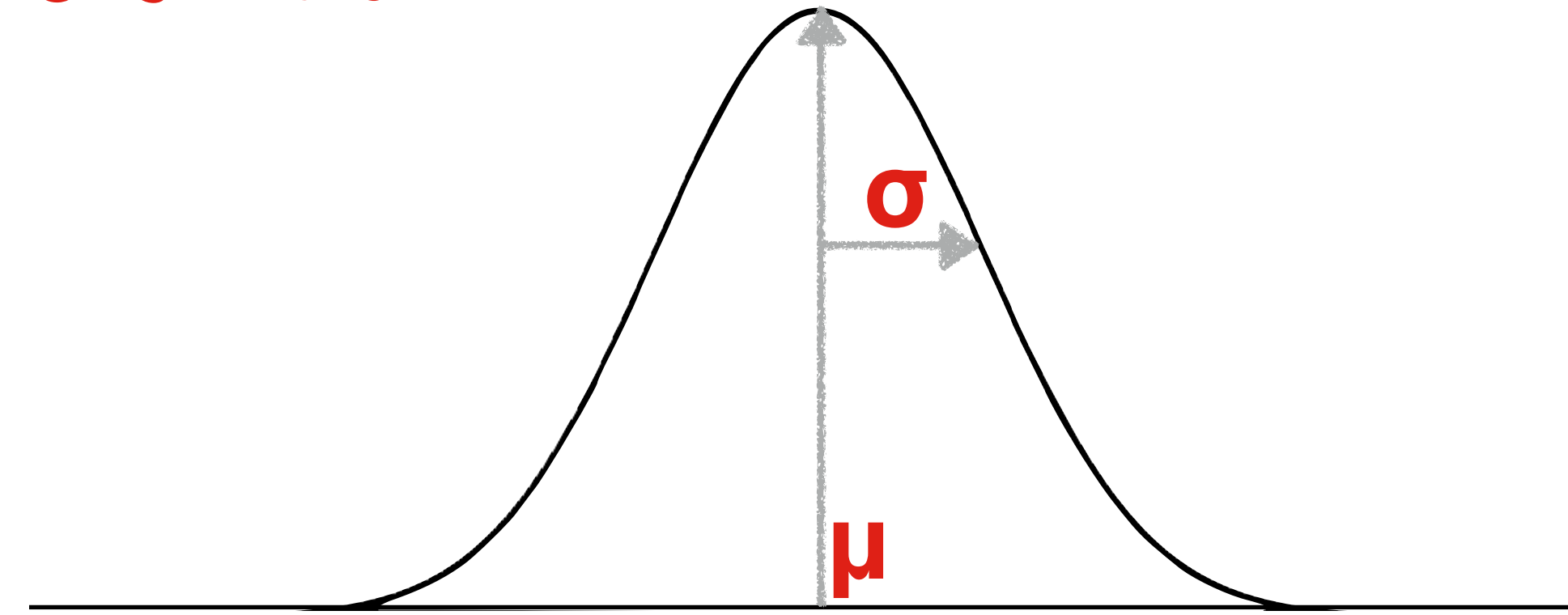


$$f(x) = F(x, \mu, \sigma)$$

IF YOU LOOK CLOSELY, YOU'LL SEE THAT
THIS FUNCTION HAS 2 PARAMETERS

NORMAL DISTRIBUTION

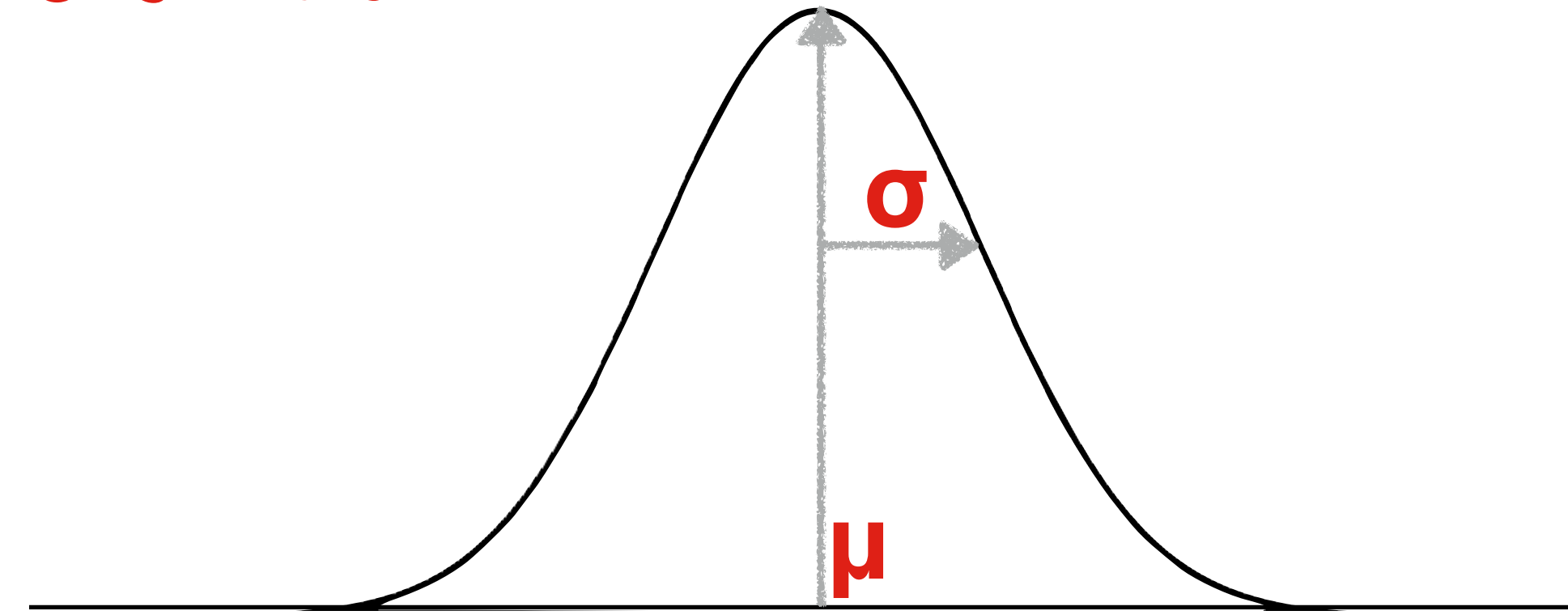
$$f(x) = F(x, \mu, \sigma)$$



IF YOU KNOW THE MEAN, SD YOU CAN
TELL THE PROBABILITY OF ANY VALUE

NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

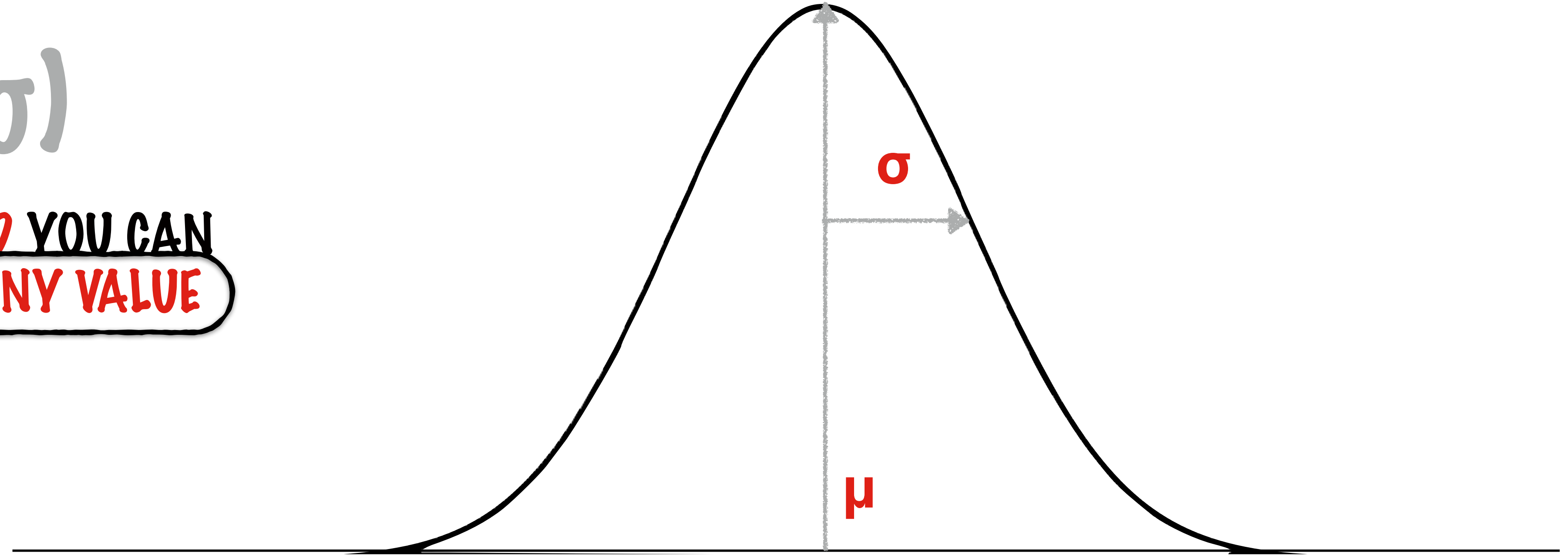


IF YOU KNOW THE MEAN, SD YOU CAN
TELL THE PROBABILITY OF ANY VALUE

NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

IF YOU KNOW THE MEAN, SD YOU CAN
TELL THE **PROBABILITY OF ANY VALUE**



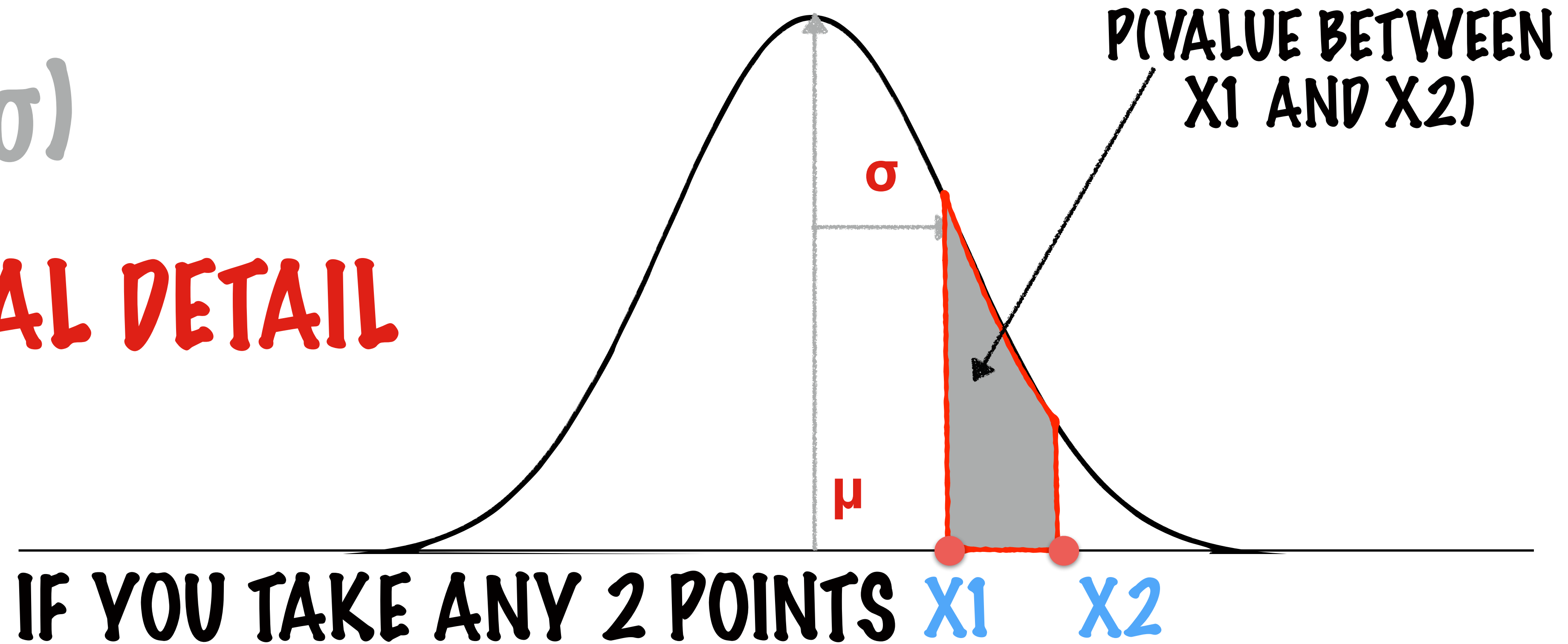
ONE TECHNICAL DETAIL

**THIS CURVE DOESN'T
REALLY REPRESENT THE
PROBABILITY OF A VALUE**

NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

ONE TECHNICAL DETAIL

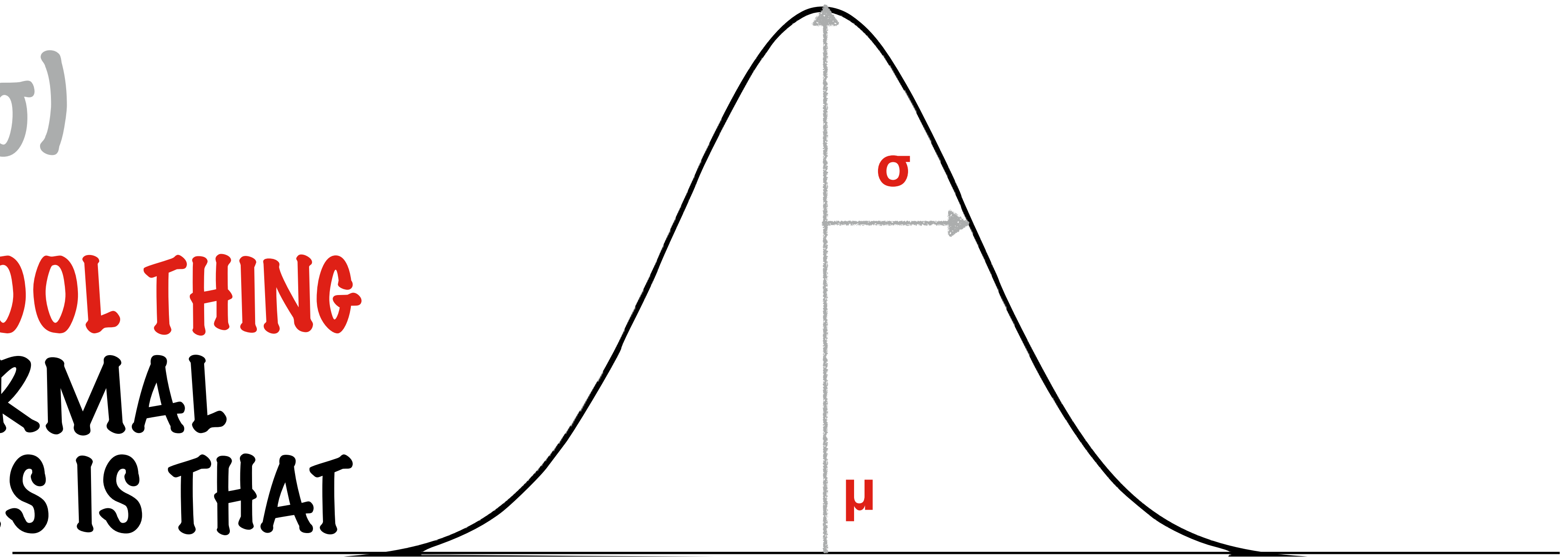


THE **AREA** UNDER THE **CURVE** = **P** (THE VARIABLE IS BETWEEN THE 2 POINTS)

NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

THE **SECOND COOL THING**
ABOUT NORMAL
DISTRIBUTIONS IS THAT

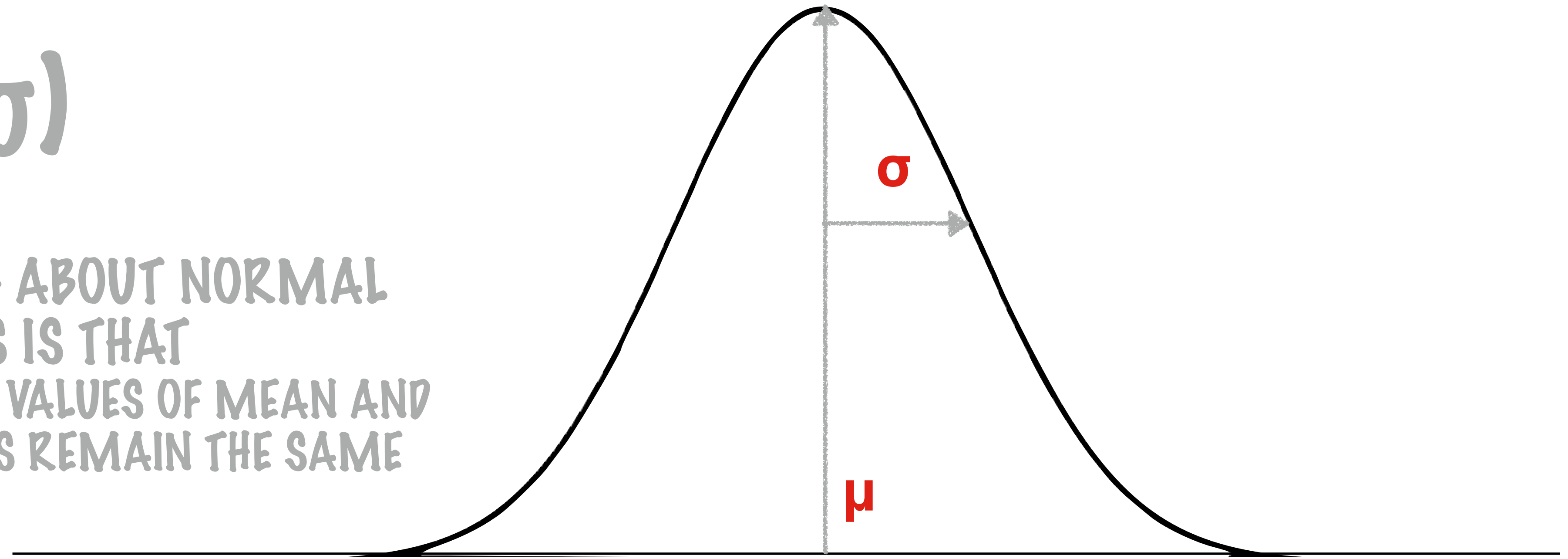


REGARDLESS OF THE ACTUAL **VALUES**
OF MEAN AND SD SOME
CHARACTERISTICS **REMAIN THE SAME**

NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

THE SECOND COOL THING ABOUT NORMAL DISTRIBUTIONS IS THAT REGARDLESS OF THE ACTUAL VALUES OF MEAN AND SD SOME CHARACTERISTICS REMAIN THE SAME



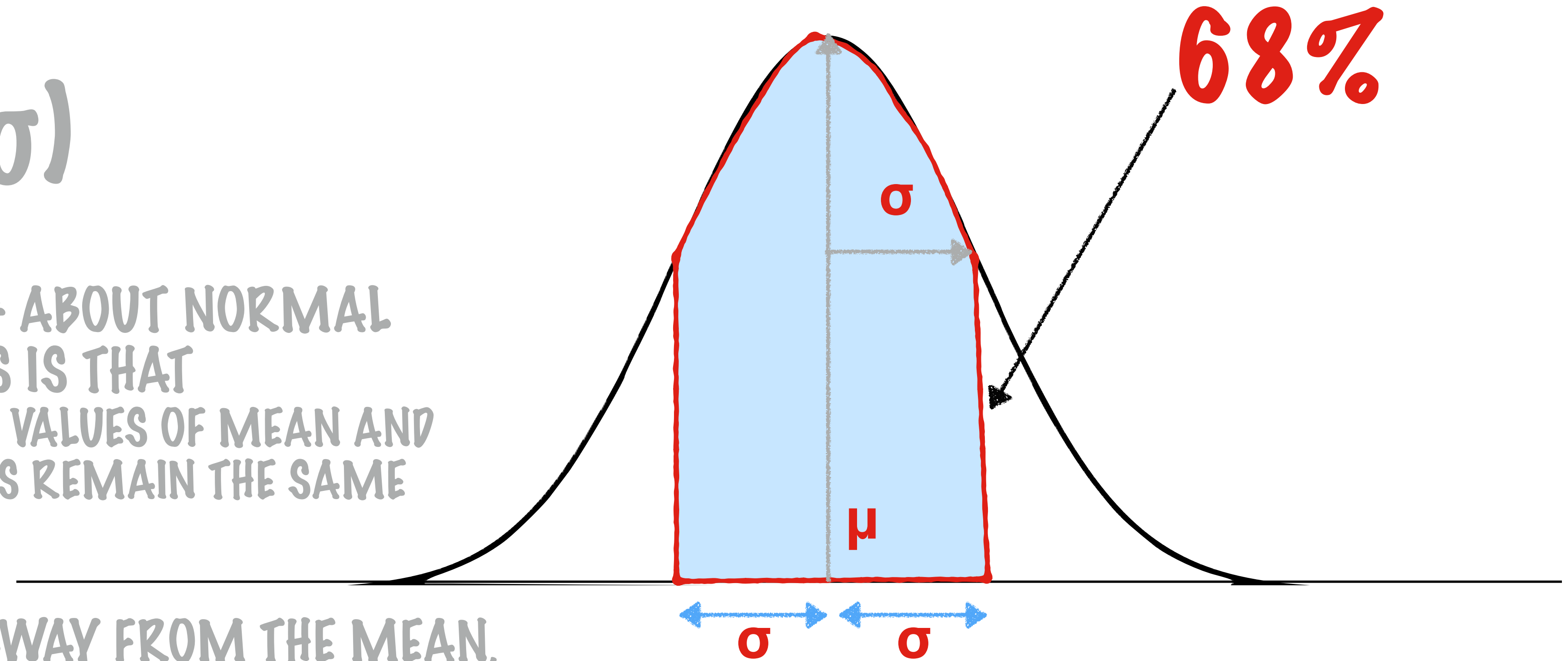
**AS YOU MOVE FURTHER AWAY FROM THE MEAN,
THE PROBABILITY DECREASES EXPONENTIALLY**

NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

THE SECOND COOL THING ABOUT NORMAL DISTRIBUTIONS IS THAT REGARDLESS OF THE ACTUAL VALUES OF MEAN AND SD SOME CHARACTERISTICS REMAIN THE SAME

AS YOU MOVE FURTHER AWAY FROM THE MEAN, THE PROBABILITY DECREASES EXPONENTIALLY



P(VALUE IS WITHIN 1 SD FROM THE MEAN) = 68%

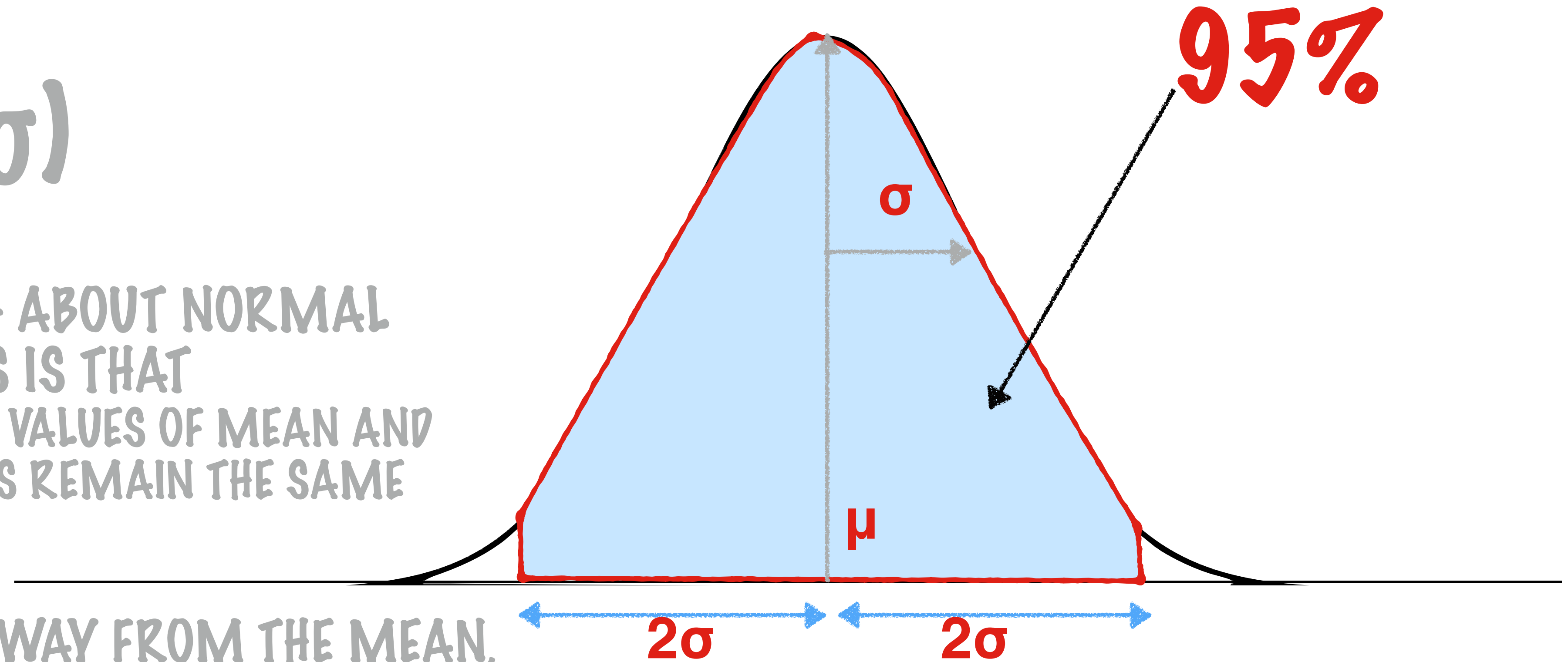
THIS IS REGARDLESS OF THE VALUE OF MEAN, SD

NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

THE SECOND COOL THING ABOUT NORMAL DISTRIBUTIONS IS THAT REGARDLESS OF THE ACTUAL VALUES OF MEAN AND SD SOME CHARACTERISTICS REMAIN THE SAME

AS YOU MOVE FURTHER AWAY FROM THE MEAN, THE PROBABILITY DECREASES EXPONENTIALLY



P(VALUE IS WITHIN 2 SD FROM THE MEAN) = 95%

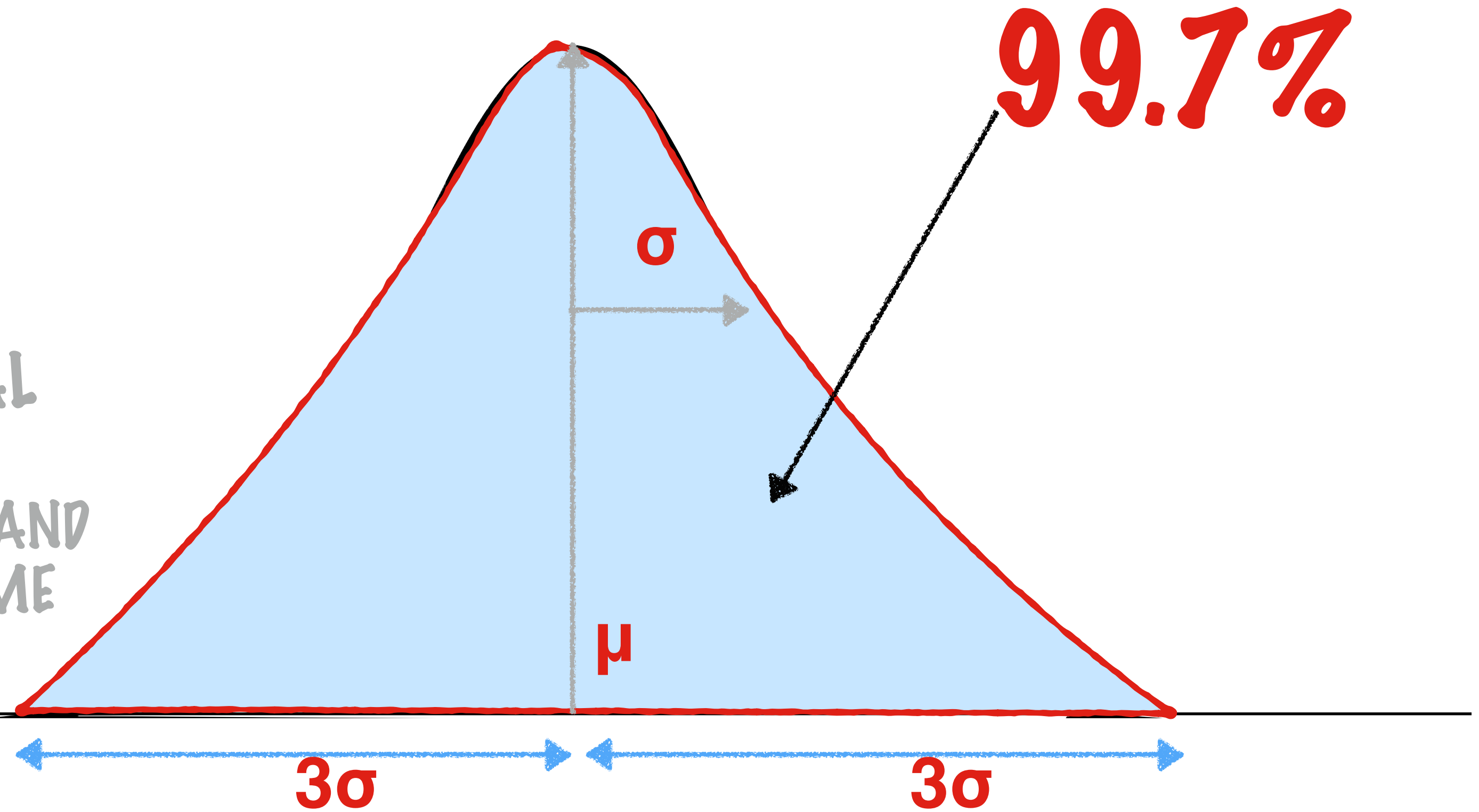
THIS IS REGARDLESS OF THE VALUE OF MEAN, SD

NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

THE SECOND COOL THING ABOUT NORMAL DISTRIBUTIONS IS THAT REGARDLESS OF THE ACTUAL VALUES OF MEAN AND SD SOME CHARACTERISTICS REMAIN THE SAME

AS YOU MOVE FURTHER AWAY FROM THE MEAN, THE PROBABILITY DECREASES EXPONENTIALLY



P(VALUE IS WITHIN 3 SD FROM THE MEAN) = 99.7%

THIS IS REGARDLESS OF THE VALUE OF MEAN, SD

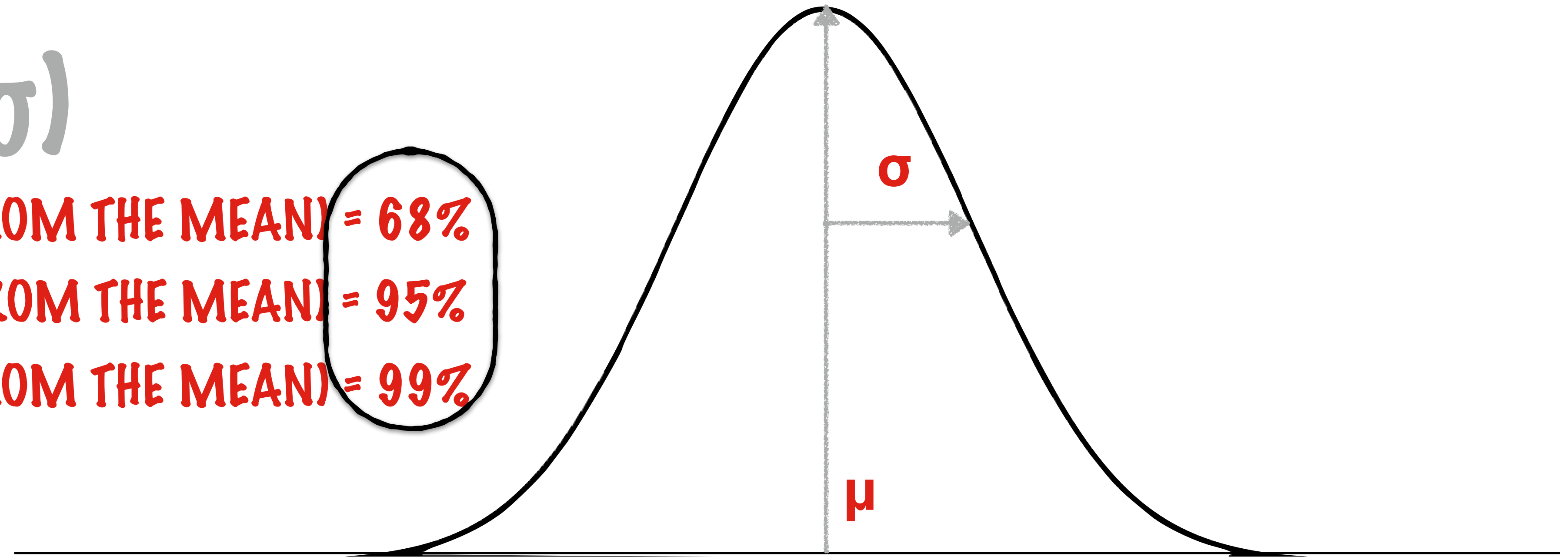
NORMAL DISTRIBUTION

$$f(x) = F(x, \mu, \sigma)$$

P(VALUE IS WITHIN 1 SD FROM THE MEAN) = 68%

P(VALUE IS WITHIN 2 SD FROM THE MEAN) = 95%

P(VALUE IS WITHIN 3 SD FROM THE MEAN) = 99%



THIS RULE IS VERY USEFUL FOR

1. **TESTING** WHETHER A DISTRIBUTION IS **NORMAL**

2. **FINDING OUTLIERS:** ANY VALUES MORE THAN 3σ AWAY FROM THE MEAN CAN BE TREATED AS OUTLIERS