

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

## DATA STRUCTURES IN R

LIKE A VECTOR, AN ARRAY  
CAN ONLY HAVE ELEMENTS OF  
THE **SAME TYPE**

### ARRAY

AN ARRAY HAS IT'S ELEMENTS ARRANGED  
IN **DIMENSIONS** (ROW, COLUMNS ETC)

1
2
5

1	3	5	9
---	---	---	---

## 1-DIMENSIONAL ARRAYS

LIST  
VECTOR  
DATAFRAME  
MATRIX

## DATA STRUCTURES IN R

LIKE A VECTOR, AN ARRAY  
CAN ONLY HAVE ELEMENTS  
OF THE **SAME TYPE**

AN ARRAY HAS ITS ELEMENTS ARRANGED IN  
**DIMENSIONS** (ROW, COLUMNS ETC)

### 1-DIMENSIONAL ARRAYS

1	1	3	5	9
2				
5				

## ARRAY

### A 2-DIMENSIONAL ARRAY

IS A STACK OF 1 DIMENSIONAL ARRAYS

1	3	5	9
2	7	4	3
5	8	9	7

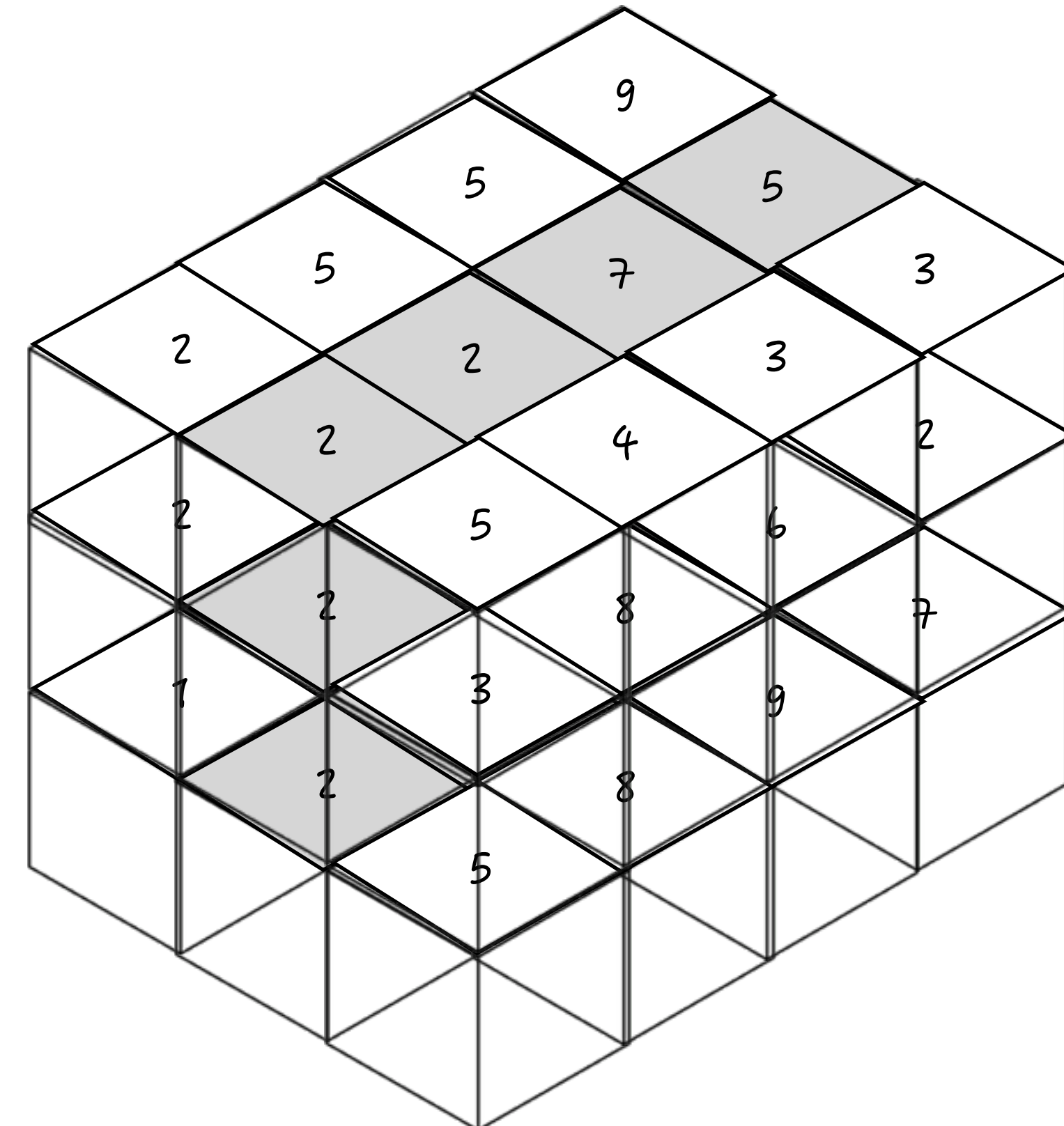
LIST  
VECTOR  
DATAFRAME  
MATRIX

## DATA STRUCTURES IN R

### ARRAY

### A 3-DIMENSIONAL ARRAY

IS A STACK OF 2 DIMENSIONAL ARRAYS



LIST  
VECTOR  
DATAFRAME  
MATRIX

LIKE A VECTOR, AN ARRAY  
CAN ONLY HAVE ELEMENTS  
OF THE SAME TYPE

AN ARRAY HAS IT'S ELEMENTS ARRANGED IN  
DIMENSIONS (ROW, COLUMNS ETC)

### 1-DIMENSIONAL ARRAYS

1	1	3	5	9
2				
5				

### A 2-DIMENSIONAL ARRAY

IS A STACK OF 1 DIMENSIONAL ARRAYS

1	3	5	9
2	7	4	3
5	8	9	7

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

AN ARRAY IS A VECTOR, WITH  
AN ADDITIONAL ATTRIBUTE  
**DIMENSIONS**

A VECTOR IS A FLAT STRUCTURE, IT  
HAS NO ROWS, COLUMNS OR OTHER  
DIMENSIONS

```
myVector <- 1:10  
myVector  
[1]  1  2  3  4  5  6  7  8  9 10
```

BY ASSIGNING **DIMENSIONS** TO A VECTOR  
YOU CAN TURN **A VECTOR INTO AN ARRAY**



## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
myVector <- 1:10
```


```
myVector
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
myArray <- myVector
```

2 - DIMENSIONAL ARRAY

```
dim(myArray) <- c(5, 2)
```



THE DIMENSIONS OF AN ARRAY ARE  
EXPRESSED BY AN INTEGER VECTOR

THE LENGTH OF THE DIMENSION VECTOR  
TELLS US THE NUMBER OF DIMENSIONS

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
myVector <- 1:10
```

```
myVector
```

```
[1]  1  2  3  4  5  6  7  8  9 10
```

```
myArray <- myVector
```

```
dim(myArray) <- c(5, 2)
```

THE FIRST DIMENSION IS THE NUMBER OF ROWS

THE SECOND DIMENSION IS THE NUMBER OF COLUMNS

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
myVector <- 1:10
```

```
myVector
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
myArray <- myVector
```

```
dim(myArray) <- c(5, 2)
```

AN ARRAY CAN HAVE **AS MANY  
DIMENSIONS** AS YOU LIKE...**AS LONG AS**

**THE PRODUCT OF ALL THE DIMENSIONS = NUMBER OF ELEMENTS IN THE ARRAY**



# EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
myVector <- 1:10
```

```
myVector
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
myArray <- myVector
```

```
dim(myArray) <- c(5, 2)
```

WHEN YOU **ASSIGN**  
**DIMENSIONS** TO A VECTOR

THE ELEMENTS OF THE VECTOR ARE  
**ARRANGED ALONG THE DIMENSIONS**

THE ARRAY IS FILLED ALONG **THE ROWS**  
**FIRST, THEN THE COLUMNS, AND SO ON**

5 ROWS

2 COLUMNS

	,1	,2
1,	1	6
2,	2	7
3,	3	8
4,	4	9
5,	5	10

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
myVector <- 1:10
```

```
myVector
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
myArray <- myVector
```

```
dim(myArray) <- c(5, 2)
```

```
myArray
```

	[, 1]	[, 2]
[1, ]	1	6
[2, ]	2	7
[3, ]	3	8
[4, ]	4	9
[5, ]	5	10

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
myVector <- 1:10  
myVector  
[1] 1 2 3 4 5 6 7 8 9 10
```

```
myArray <- myVector  
dim(myArray) <- c(5,2)
```

```
myArray  
      [,1] [,2]  
[1,] 1    6  
[2,] 2    7  
[3,] 3    8  
[4,] 4    9  
[5,] 5   10
```

**THESE 2 COMMANDS  
TURNED THE VECTOR  
myVector INTO AN ARRAY**

```
anotherArray <- array(c(1:12), dim = c(3,2,2))
```

**THE ARRAY FUNCTION DOES  
EXACTLY THIS IN JUST ONE STEP**

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
anotherArray <- array(c(1:12), dim = c(3,2,2))
```

THE **VECTOR** TO BE  
CONVERTED TO AN **ARRAY**

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
anotherArray <- array(c(1:12), dim = c(3, 2, 2))
```

# DIMENSIONS OF THE ARRAY



## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
anotherArray <- array(c(1:12), dim = c(3, 2, 2))
```

THIS IS A 3 DIMENSIONAL ARRAY

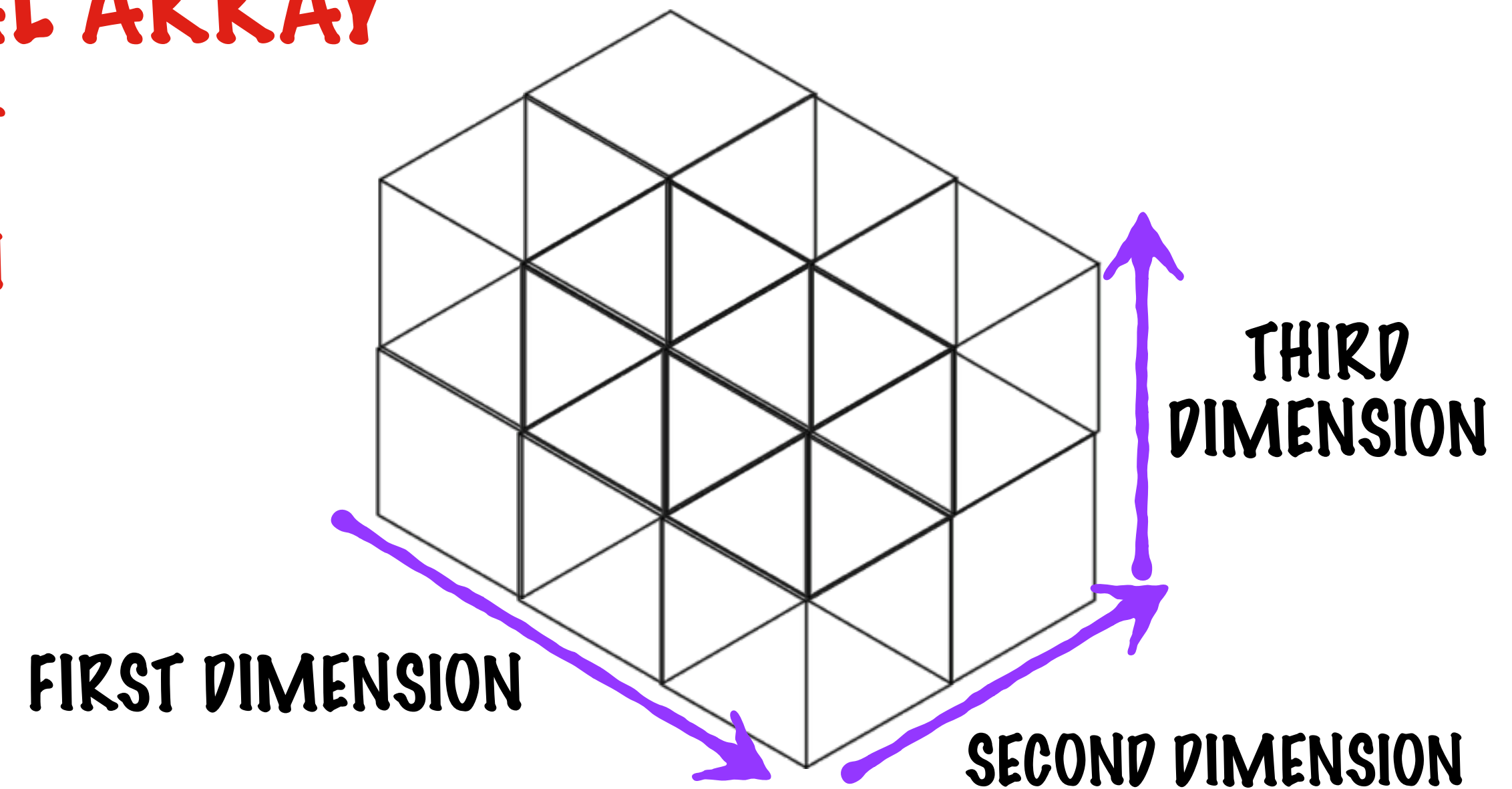
IT WILL FIRST BE FILLED **ALONG THE ROWS, THEN COLUMNS**  
AND THEN THE **3RD DIMENSION**

# EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
anotherArray <- array(c(1:12), dim = c(3, 2, 2))
```

**THIS IS A 3 DIMENSIONAL ARRAY**

IT WILL FIRST BE FILLED **ALONG  
THE ROWS, THEN COLUMNS  
AND THEN THE 3RD DIMENSION**



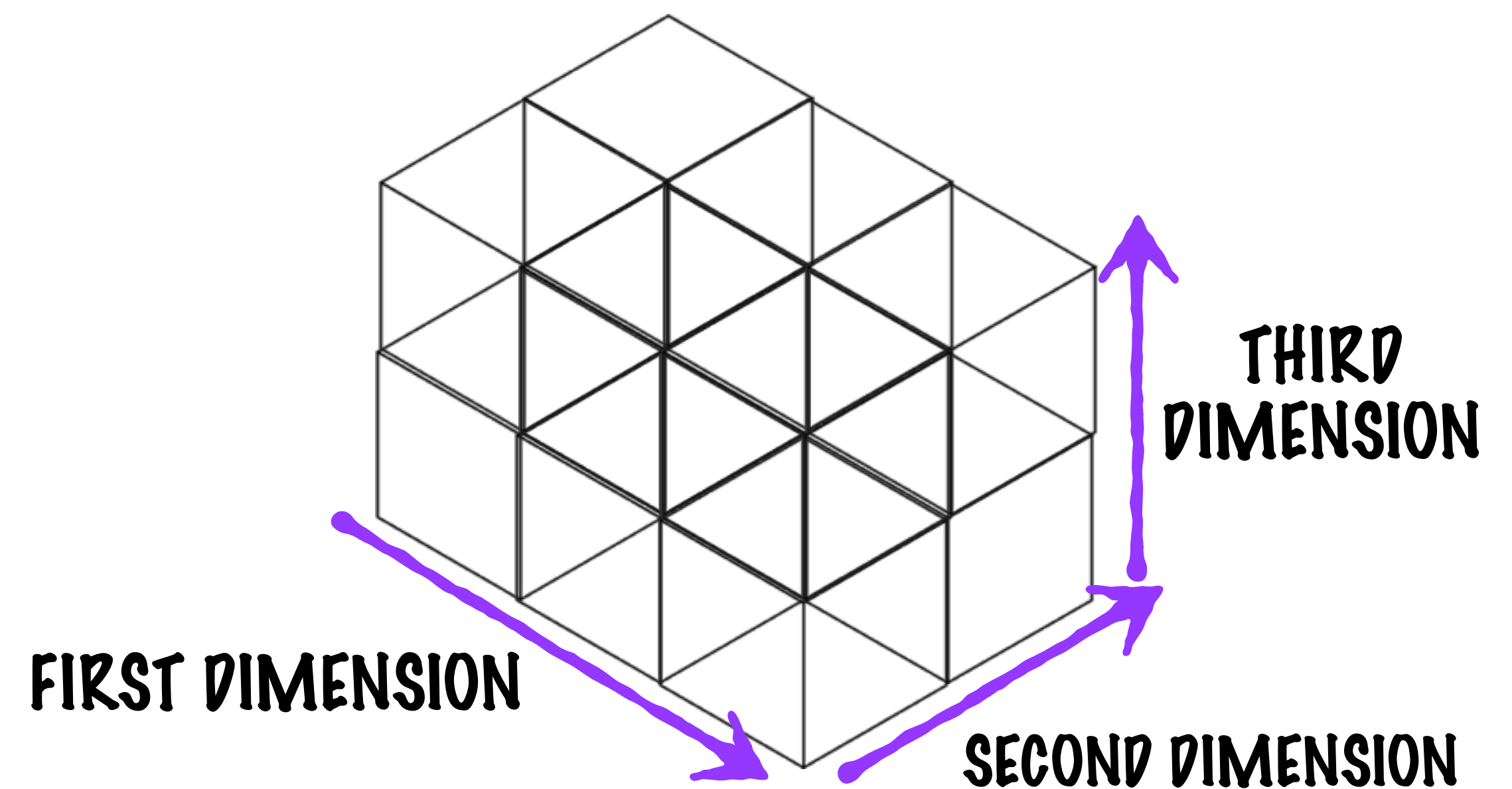
# EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
anotherArray <- array(c(1:12), dim = c(3,2,2))  
anotherArray
```

	[ , 1 ]	[ , 2 ]
[ 1, ]	1	4
[ 2, ]	2	5
[ 3, ]	3	6

	[ , 1 ]	[ , 2 ]
[ 1, ]	7	10
[ 2, ]	8	11
[ 3, ]	9	12



## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

BUT THE VECTOR ONLY  
HAS 2 ELEMENTS

THIS ARRAY EXPECTS TO  
HAVE 6 ELEMENTS

```
thirdArray <- array(c(1,0) , dim = c(2,3) )
```

**RECYCLING** TO THE RESCUE :)

WHAT IF THE VECTOR IS TOO SHORT TO FILL THE  
ARRAY OF SPECIFIED DIMENSIONS?

## EXAMPLE 20: CREATING AN ARRAY FROM A VECTOR

```
thirdArray <- array(c(1,0) , dim = c(2,3))  
thirdArray
```

	[,1]	[,2]	[,3]
[1,]	1	1	1
[2,]	0	0	0

**RECYCLING** TO THE RESCUE :)

**A COOL USE OF RECYCLING IS  
TO CREATE CONSTANT ARRAYS**

```
arrayOfZeros <- array(0, dim = c(100,100))
```



# EXAMPLE 21: INDEXING AN ARRAY

# EXAMPLE 21: INDEXING AN ARRAY

TO INDEX AN **ARRAY** YOU NEED AS MANY  
**SUBSCRIPTS** AS THERE ARE **DIMENSIONS**

<b>A</b>	<b>A<sub>1</sub></b>	<b>A<sub>2</sub></b>	<b>A<sub>3</sub></b>	<b>A<sub>4</sub></b>
	1	3	5	9

IS A **ONE DIMENSIONAL ARRAY**

TO INDEX AN ELEMENT IN **A** YOU  
NEED ONLY **1 SUBSCRIPT**

# EXAMPLE 21: INDEXING AN ARRAY

TO INDEX AN **ARRAY** YOU NEED AS MANY  
**SUBSCRIPTS** AS THERE ARE **DIMENSIONS**

**B** IS A 2 DIMENSIONAL ARRAY

1	3	5	9
2	7	4	3
5	8	9	7

**B**<sub>23</sub> IS THE ELEMENT IN THE **SECOND ROW**  
AND THE **THIRD COLUMN**

TO INDEX AN ELEMENT IN **B** YOU  
NEED **2 SUBSCRIPTS**

# EXAMPLE 21: INDEXING AN ARRAY

```
anotherArray <- array(c(1:12), dim = c(3,2,2))
```

anotherArray

The diagram illustrates a 3D array structure. A blue oval encloses the first two dimensions (rows and columns), with an arrow pointing to the dimension '1' in the header. A purple oval encloses the third dimension (depth), with an arrow pointing to the dimension '2' in the header. An orange oval highlights the element at index [2, 2, 1], which is the value 5. Arrows from the text 'anotherArray IS A 3-DIMENSIONAL ARRAY' point to these three dimensions. An arrow from the code 'anotherArray[2, 2, 1]' points to the highlighted element 5.

	[ , 1 ]	[ , 2 ]
[ 1, ]	1	4
[ 2, ]	2	5
[ 3, ]	3	6

anotherArray IS A  
3-DIMENSIONAL  
ARRAY

```
anotherArray[2, 2, 1]
```

	[ , 1 ]	[ , 2 ]
[ 1, ]	7	10
[ 2, ]	8	11
[ 3, ]	9	12

TO INDEX AN ELEMENT IN  
anotherArray YOU NEED 3  
SUBSCRIPTS

# EXAMPLE 21: INDEXING AN ARRAY

```
anotherArray <- array(c(1:12), dim = c(3,2,2))  
anotherArray
```

		[ ,1]	[ ,2]
[1, ]		1	4
[2, ]		2	5
[3, ]		3	6

```
anotherArray[2:3,1:2,1]
```

	[ ,1]	[ ,2]
[1, ]	7	10
[2, ]	8	11
[3, ]	9	12

TO INDEX A **SUBSECTION** OF AN  
ARRAY YOU CAN USE A **VECTOR**  
IN PLACE OF **EACH SUBSCRIPT**



# EXAMPLE 21: INDEXING AN ARRAY

```
anotherArray <- array(c(1:12), dim = c(3,2,2))  
anotherArray
```

		1	
		[,1]	[,2]
[1,]		1	4
[2,]		2	5
[3,]		3	6
		2	

		[,1]	[,2]
[1,]		7	10
[2,]		8	11
[3,]		9	12

```
anotherArray[2:3,1:2,1]
```

```
anotherArray[2:3,,1]
```

**IF YOU LEAVE A SUBSCRIPT  
BLANK, THAT IS EQUIVALENT TO  
SELECTING ALL THE VALUES IN  
THE CORRESPONDING DIMENSION**

# EXAMPLE 21: INDEXING AN ARRAY

```
anotherArray <- array(c(1:12), dim = c(3,2,2))
```

```
anotherArray
```

```
, , 1
```

```
      [,1] [,2]
```

```
[1,]     1     4
```

```
[2,]     2     5
```

```
[3,]     3     6
```

```
, , 2
```

```
      [,1] [,2]
```

```
[1,]     7    10
```

```
[2,]     8    11
```

```
[3,]     9    12
```

```
indexArray <- array(c(1:2), dim=c(2,3))
```

```
indexArray
```

```
      [,1] [,2] [,3]
```

```
[1,]     1     1     1
```

```
[2,]     2     2     2
```

```
anotherArray[indexArray]
```

**YOU CAN ALSO USE A 2  
DIMENSIONAL ARRAY (A  
MATRIX) TO INDEX A SPECIFIC  
SET OF ELEMENTS**

# EXAMPLE 21: INDEXING AN ARRAY

```
anotherArray <- array(c(1:12), dim = c(3,2,2))
```

```
anotherArray
```

```
, , 1
```

```
  [,1] [,2]
```

```
[1,]  1  4
```

```
[2,]  2  5
```

```
[3,]  3  6
```

```
, , 2
```

```
  [,1] [,2]
```

```
[1,]  7 10
```

```
[2,]  8 11
```

```
[3,]  9 12
```

```
indexArray <- array(c(1:2), dim=c(2,3))
```

```
indexArray
```

```
  [,1] [,2] [,3]
```

```
[1,]  1  1  1
```

```
[2,]  2  2  2
```

```
anotherArray[indexArray]
```

```
[1]  1 11
```

**EACH ROW IN THE INDEX  
ARRAY REFERS TO ONE  
ELEMENT THAT SHOULD BE  
SELECTED**

## EXAMPLE 22: OPERATIONS BETWEEN 2 ARRAYS

## EXAMPLE 22: OPERATIONS BETWEEN 2 ARRAYS

```
a <- array(1:6, dim = c(2, 3))  
b <- array(7:12, dim = c(2, 3))  
a * b
```

FOR AN OPERATION INVOLVING 2  
ARRAYS, BOTH ARRAYS MUST BE OF  
THE SAME DIMENSION



# EXAMPLE 22: OPERATIONS BETWEEN 2 ARRAYS

```
a <- array(1:6, dim = c(2,3))  
b <- array(7:12, dim = c(2,3))  
a * b
```

	[,1]	[,2]	[,3]	
[1,]	7	27	55	
[2,]	16	40	72	

THE OPERATION IS PERFORMED  
**ELEMENT-WISE** I.E. BETWEEN  
**CORRESPONDING ELEMENTS** OF  
BOTH ARRAYS

THE **RESULT** IS AN ARRAY  
WITH **SAME DIMENSIONS**  
AS THE INPUT ARRAYS

## EXAMPLE 22: OPERATIONS BETWEEN 2 ARRAYS

```
a <- array(1:6, dim = c(2,3))
```

```
b <- array(7:12, dim = c(2,3))
```

```
a * b
```

```
[,1] [,2] [,3]
```

```
[1,]      7      27      55
```

```
[2,]     16      40      72
```

```
c <- array(13:18, dim = c(3,2))
```

```
a - c
```

```
Error in a - c : non-conformable arrays
```

IF THE ARRAYS  
ARE OF DIFFERENT  
DIMENSIONS AN  
ERROR WILL BE  
THROWN

# EXAMPLE 23: OPERATIONS BETWEEN AN ARRAY AND A VECTOR

## EXAMPLE 23: OPERATIONS BETWEEN AN ARRAY AND A VECTOR

FOR AN OPERATION BETWEEN  
AN ARRAY AND A VECTOR,

`a * b`

`a - c`

LENGTH OF THE VECTOR  
MUST BE  $\leq$   
SIZE OF THE ARRAY

## EXAMPLE 23: OPERATIONS BETWEEN AN ARRAY AND A VECTOR

a

	[,1]	[,2]	[,3]
[1,]	1	3	5
[2,]	2	4	6

```
sameLength <- 1:6  
shorterVector <- 1:2  
longerVector <- 1:10
```

**a** IS AN ARRAY OF SIZE 6  
I.E. IT HAS 6 ELEMENTS

LET'S LOOK  
AT 3 CASES

## EXAMPLE 23: OPERATIONS BETWEEN AN ARRAY AND A VECTOR

```
a
      [,1] [,2] [,3]
[1,]     1     3     5
[2,]     2     4     6
sameLength <- 1:6
shorterVector <- 1:2
longerVector <- 1:10
a + sameLength
      [,1] [,2] [,3]
[1,]     2     6    10
[2,]     4     8    12
```

a \* b

**IF THE VECTOR'S LENGTH  
IS EQUAL TO THE ARRAY  
SIZE, THEN THE  
OPERATION IS APPLIED  
ELEMENT-WISE**



## EXAMPLE 23: OPERATIONS BETWEEN AN ARRAY AND A VECTOR

a

```
      [,1] [,2] [,3]  
[1,]    1    3    5  
[2,]    2    4    6
```

```
sameLength <- 1:6
```

```
shorterVector <- 1:2
```

```
longerVector <- 1:10
```

```
a - shorterVector
```

```
      [,1] [,2] [,3]  
[1,]     0     2     4  
[2,]     0     2     4
```

a

1	3	5
2	4	6

shorterVector

1	1	1
2	2	2

IF THE **VECTOR IS SHORTER**,  
IT IS **RECYCLED** AS MANY  
TIMES AS NEEDED

## EXAMPLE 23: OPERATIONS BETWEEN AN ARRAY AND A VECTOR

a

	[,1]	[,2]	[,3]
[1,]	1	3	5
[2,]	2	4	6

```
sameLength <- 1:6
```

```
shorterVector <- 1:2
```

```
longerVector <- 1:10
```

```
a / longerVector
```

```
dims [product 6] do not match the length of object [10]
```

IF THE **VECTOR** IS  
**LONGER**, AN **ERROR**  
IS THROWN

# EXAMPLE 24 : OUTER PRODUCTS

## EXAMPLE 24 : OUTER PRODUCTS

THE OUTER PRODUCT OF 2 ARRAYS IS AN ARRAY WITH  
ELEMENT-WISE PRODUCTS OF  
EVERY PAIR OF ELEMENTS FROM  
BOTH ARRAYS

LET'S TAKE AN  
EXAMPLE

ONE OR BOTH OF THE ARRAYS  
COULD ALSO BE VECTORS  
TREATING VECTORS AS 1  
DIMENSIONAL ARRAYS

## EXAMPLE 24 : OUTER PRODUCTS

ONE OR BOTH OF THE  
ARRAYS COULD ALSO BE  
VECTORS

TREATING VECTORS AS 1  
DIMENSIONAL ARRAYS

LET'S TAKE AN  
EXAMPLE

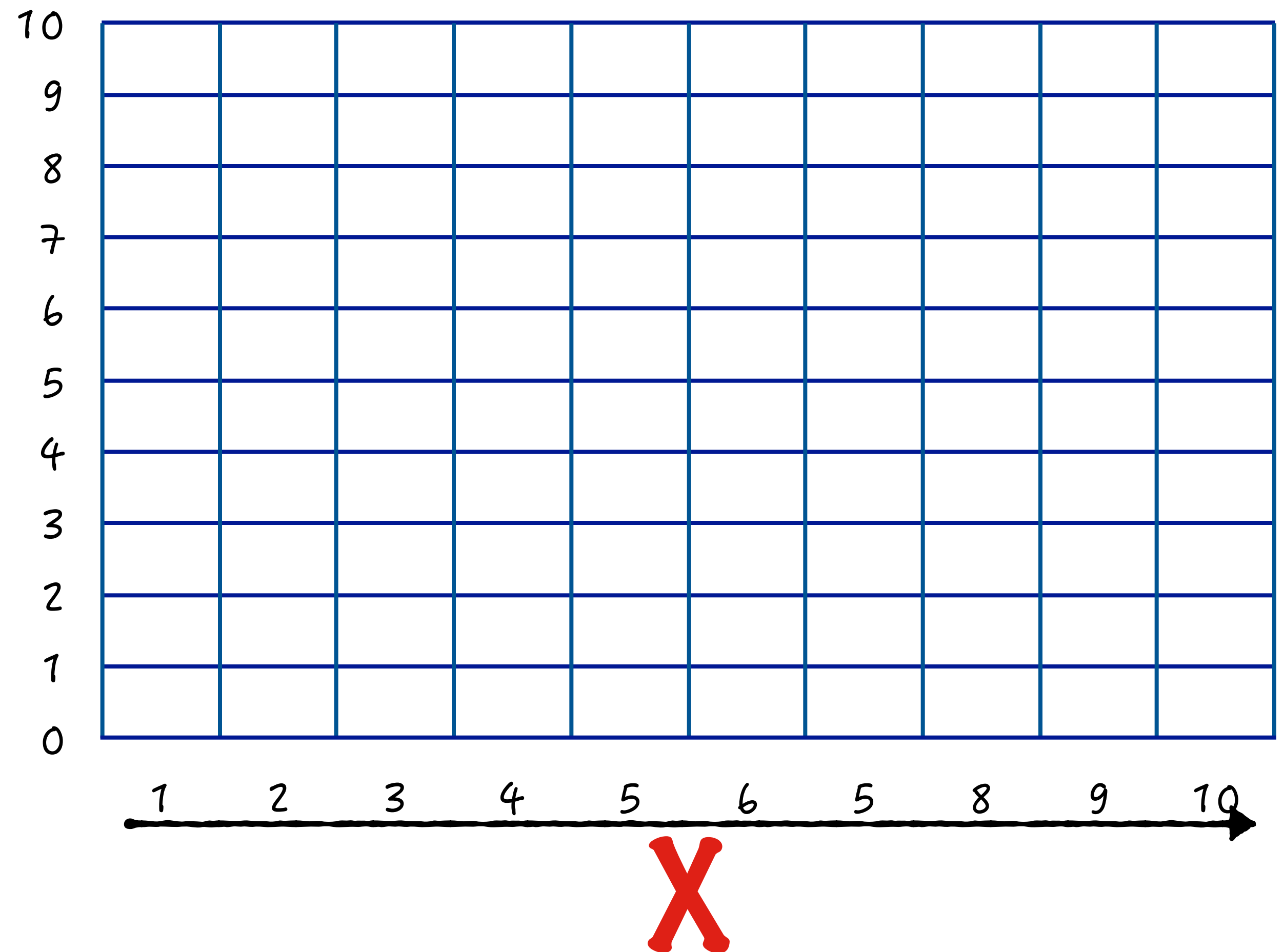
## EXAMPLE 24 : OUTER PRODUCTS

# LET'S SAY WE HAVE A 10x10 GRID

```
x <- array(1:10, dim = 10)
y <- 1:10
```

# X AND Y REPRESENT THE GRID

(WE'VE MADE ONE OF THEM A VECTOR JUST FOR KICKS)





# EXAMPLE 24 : OUTER PRODUCTS

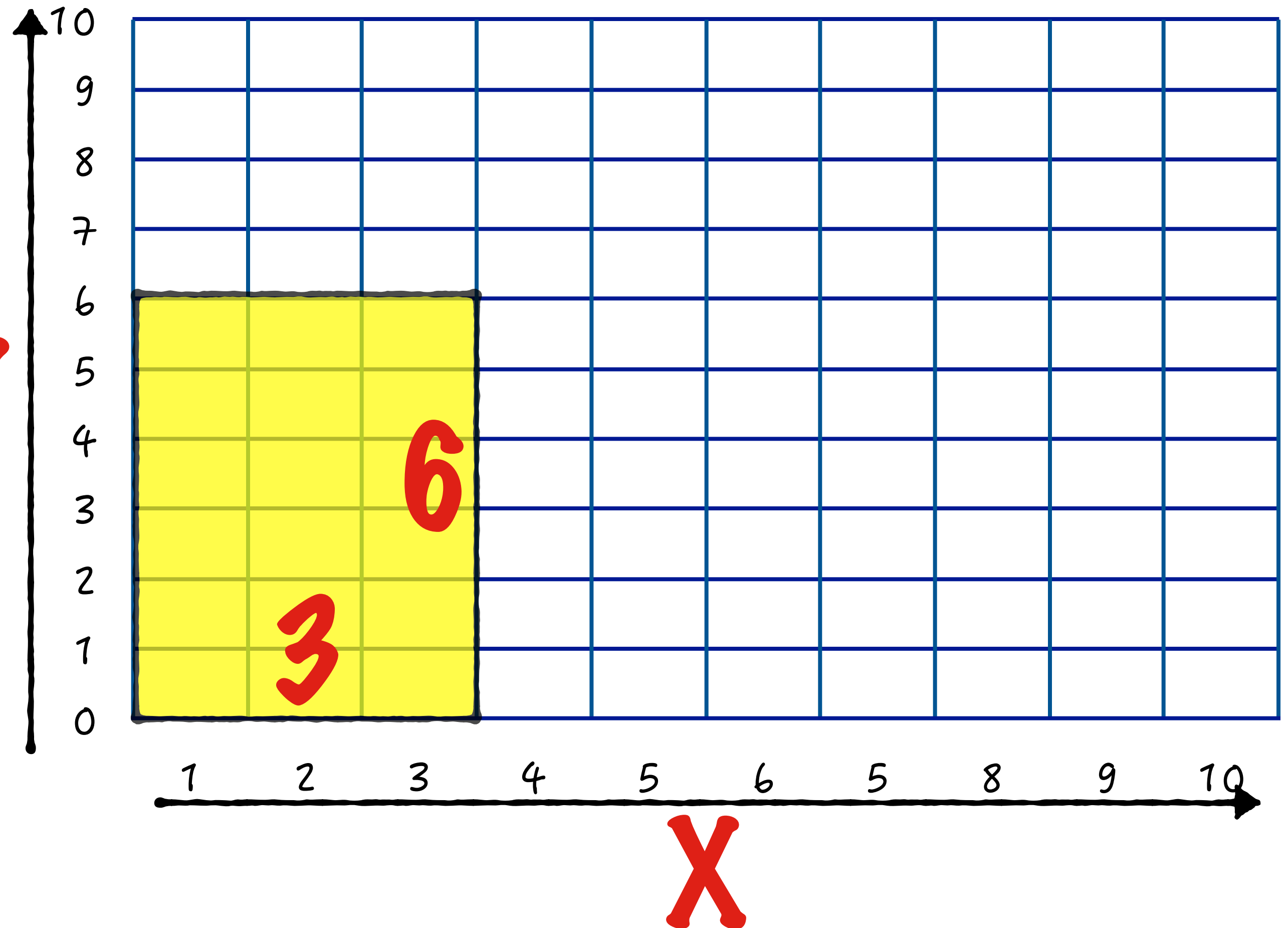
LET'S SAY WE HAVE  
A 10x10 GRID

```
x <- array(1:10, dim = 10)  
y <- 1:10
```

WE CAN DRAW RECTANGLES WITH  
ONE CORNER AT THE ORIGIN AND

COMPUTE THE AREA  $Y$

AREA = 18



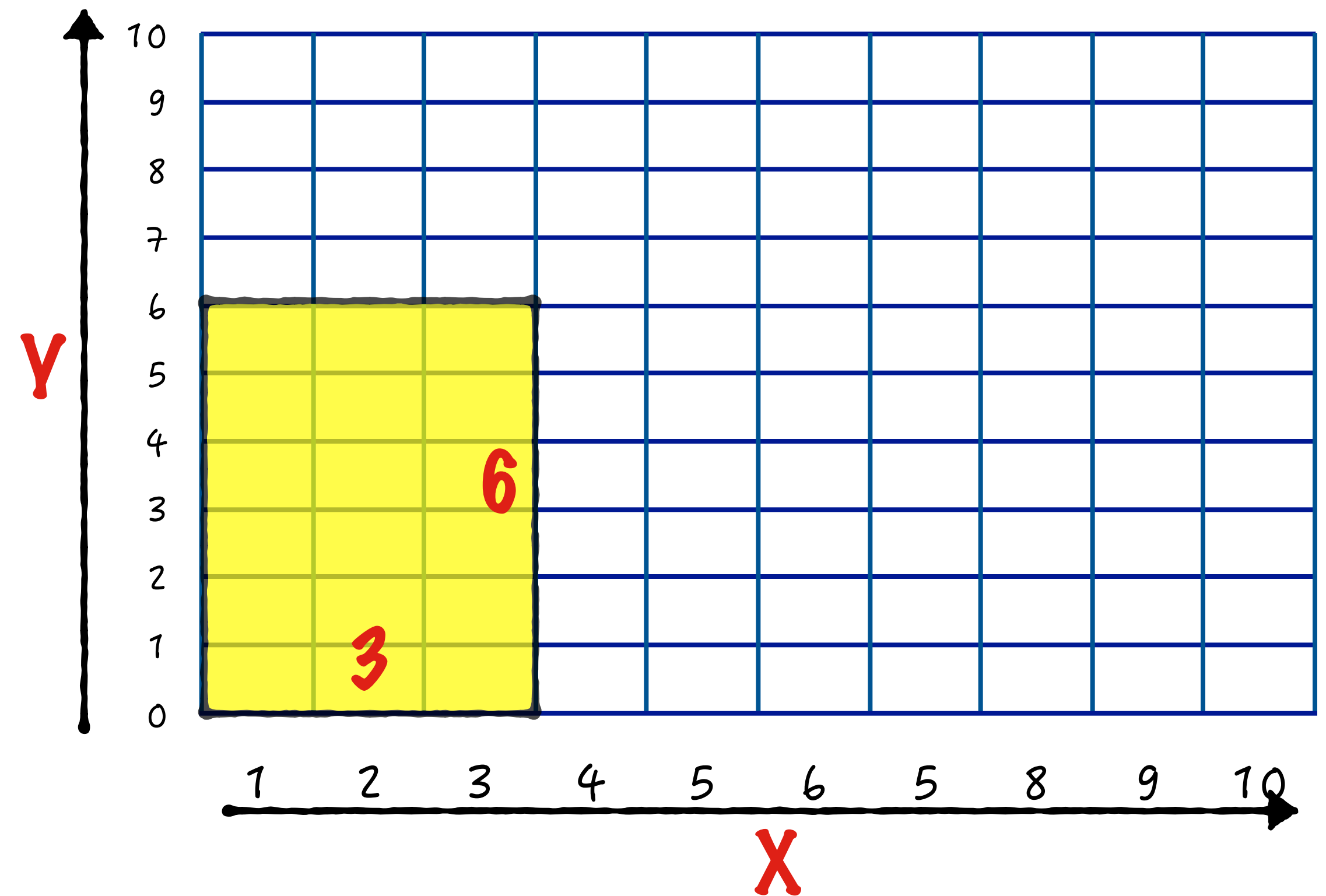
# EXAMPLE 24 : OUTER PRODUCTS

```
x <- array(1:10, dim = 10)
y <- 1:10
```

HOW DO WE COMPUTE THE  
AREAS OF **EVERY POSSIBLE**  
SUCH RECTANGLE?

**OUTER PRODUCT  
OF X AND Y**

```
x %O% y
```



# EXAMPLE 24 : OUTER PRODUCTS

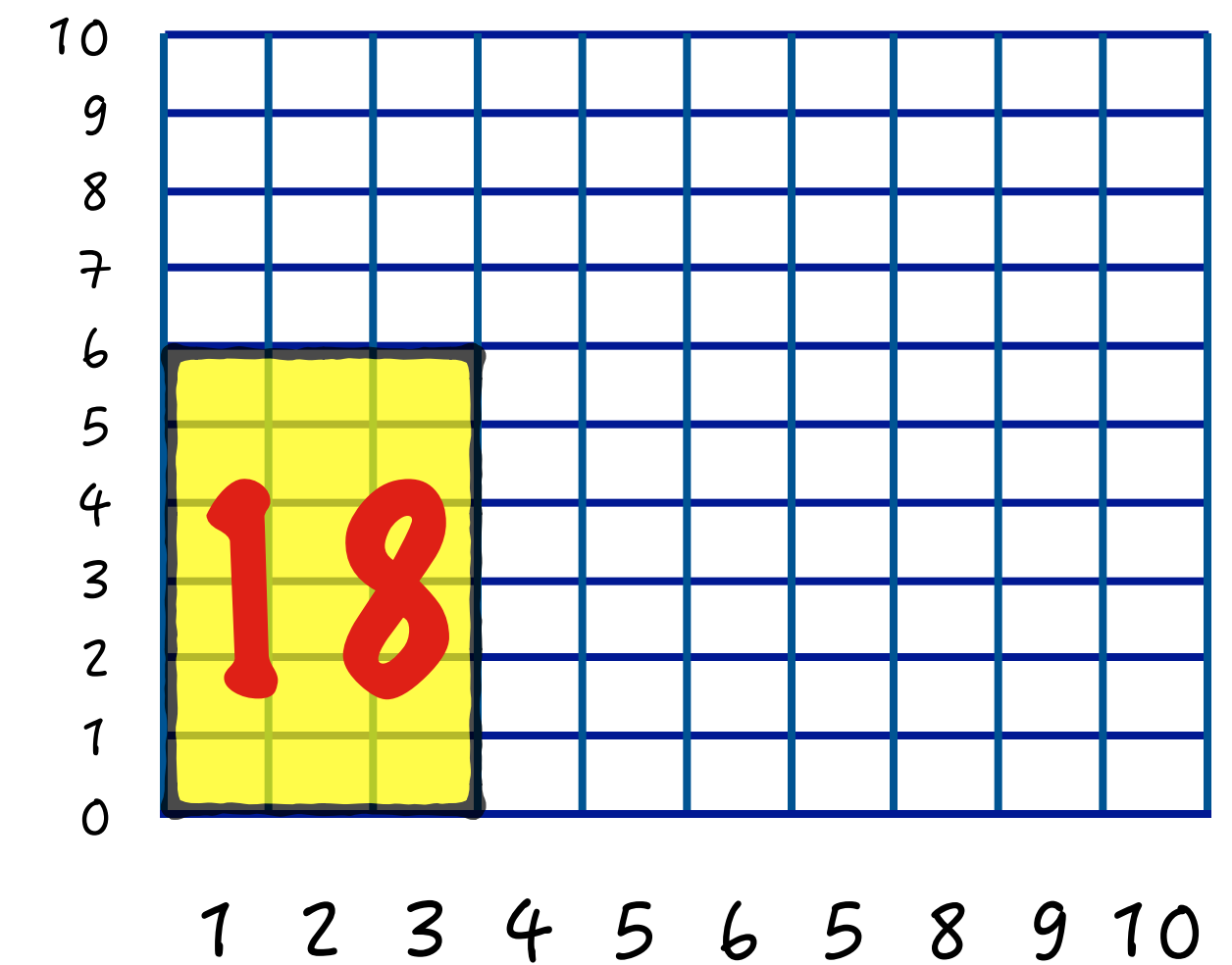
LET'S SAY WE HAVE A 10x10 GRID

```
x <- array(1:10, dim = 10)
```

```
y <- 1:10
```

```
x %O% y
```

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]	[,10]
[1,]	1	2	3	4	5	6	7	8	9	10
[2,]	2	4	6	8	10	12	14	16	18	20
[3,]	3	6	9	12	15	18	21	24	27	30
[4,]	4	8	12	16	20	24	28	32	36	40
[5,]	5	10	15	20	25	30	35	40	45	50
[6,]	6	12	18	24	30	36	42	48	54	60
[7,]	7	14	21	28	35	42	49	56	63	70
[8,]	8	16	24	32	40	48	56	64	72	80
[9,]	9	18	27	36	45	54	63	72	81	90
[10,]	10	20	30	40	50	60	70	80	90	100



THE OUTER PRODUCT  
IS A 10x10 ARRAY

EACH ELEMENT IS THE  
AREA OF ONE SUCH  
RECTANGLE

## EXAMPLE 24 : OUTER PRODUCTS

**AB IS THE OUTER PRODUCT  
OF 2 ARRAYS A AND B**

```
A <- array(1:18, dim = c(3, 2, 3))  
B <- array(19:36, dim = c(2, 3, 3))  
AB <- A %O% B  
dim(AB)  
[1] 3 2 3 2 3 3
```

**DIMENSIONS OF AB ARE  
FOUND BY CONCATENATING  
THE DIMENSIONS OF A AND B**

# EXAMPLE 24 : OUTER PRODUCTS

```
A <- array(1:18, dim = c(3, 2, 3))  
B <- array(19:36, dim = c(2, 3, 3))  
AB <- A %O% B  
dim(AB)  
[1] 3 2 3 2 3 3
```

```
AB[1, 2, 1, 2, 1, 1]
```

```
[1] 80
```

```
A[1, 2, 1] * B[2, 1, 1]
```

```
[1] 80
```

**EACH ELEMENT IN *AB* IS THE  
PRODUCT OF CORRESPONDING  
ELEMENTS IN *A* AND *B***

# EXAMPLE 24 : OUTER PRODUCTS

```
x <- array(1:10, dim = 10)
y <- 1:10
x %O% y
A <- array(1:18, dim = c(3,2,3))
B <- array(19:36, dim = c(2,3,3))
AB <- A %O% B
dim(AB)
[1] 3 2 3 2 3 3
AB[1,2,1,2,1,1]
[1] 80
A[1,2,1] * B[2,1,1]
[1] 80
```

EACH ELEMENT IN **AB** IS  
THE **PRODUCT** OF **ONE PAIR**  
**OF** ELEMENTS IN **A** AND **B**



# EXAMPLE 24 : OUTER PRODUCTS

```
x <- array(1:10, dim = 10)
y <- 1:10
x %O% y
A <- array(1:18, dim = c(3,2,3))
B <- array(19:36, dim = c(2,3,3))
AB <- A %O% B
dim(AB)
[1] 3 2 3 2 3 3
AB[1,2,1,2,1,1]
[1] 80
A[1,2,1] * B[2,1,1]
[1] 80
```

YOU CAN REPLACE THE \*  
WITH ANY OTHER OPERATOR  
OR FUNCTION USING OUTER()



# EXAMPLE 24 : OUTER PRODUCTS

```
x <- array(1:10, dim = 10)
y <- 1:10
x %o% y
A <- array(1:18, dim = c(3,2,3))
B <- array(19:36, dim = c(2,3,3))
AB <- A %o% B
dim(AB)
[1] 3 2 3 2 3 3
AB[1,2,1,2,1,1]
[1] 80
A[1,2,1] * B[2,1,1]
[1] 80
```

```
outerSumAB <- outer(A, B, "+")
```

YOU CAN REPLACE THE \*  
WITH ANY OTHER OPERATOR  
OR FUNCTION USING OUTER()