

$$\begin{aligned}
a_{11}^{11}+a_{11}^{21}+a_{11}^{12}+a_{11}^{22}+a_{21}^{11}+a_{21}^{21}+a_{21}^{12}+a_{21}^{22} &= -24e_1 \otimes e_1 \otimes f^1 \otimes f^1 - 12e_2 \otimes e_1 \otimes f^1 \otimes f^1 + 48e_1 \otimes e_2 \otimes f^1 \otimes f^1 + 24e_2 \otimes e_2 \otimes f^1 \otimes f^1 + 8e_1 \otimes e_1 \otimes f^2 \otimes f^1 + 4e_2 \otimes e_1 \otimes f^2 \otimes f^1 - 16e_1 \otimes e_2 \otimes f^2 \otimes f^1 - 8e_2 \otimes e_2 \otimes f^2 \otimes f^1 = \\
&= 4 \left(-6e_1 \otimes e_1 \otimes f^1 - 3e_2 \otimes e_1 \otimes f^1 + 12e_1 \otimes e_2 \otimes f^1 + 6e_2 \otimes e_2 \otimes f^1 + 2e_1 \otimes e_1 \otimes f^2 + e_2 \otimes e_1 \otimes f^2 - 4e_1 \otimes e_2 \otimes f^2 - 2e_2 \otimes e_2 \otimes f^2 \right) \otimes f^1 = \\
&= 4 \left(3(-2e_1 \otimes e_1 - e_2 \otimes e_1 + 4e_1 \otimes e_2 + 2e_2 \otimes e_2) \otimes f^1 - (-2e_1 \otimes e_1 - e_2 \otimes e_1 + 4e_1 \otimes e_2 + 2e_2 \otimes e_2) \otimes f^2 \right) \otimes f^1 = 4(-2e_1 \otimes e_1 - e_2 \otimes e_1 + 4e_1 \otimes e_2 + 2e_2 \otimes e_2) (3f^1 - f^2) \otimes f^1 = \\
&= 4(-(2e_1 + e_2) \otimes e_1 + 2(2e_1 + e_2) \otimes e_2) (3f^1 - f^2) \otimes f^1 = 4(2e_1 + e_2) (-e_1 + 2e_2) (3f^1 - f^2) \otimes f^1
\end{aligned}$$

$$\begin{aligned}
a_{12}^{11}+a_{12}^{21}+a_{12}^{12}+a_{12}^{22}+a_{22}^{11}+a_{22}^{21}+a_{22}^{12}+a_{22}^{22} &= -12e_1 \otimes e_1 \otimes f^1 \otimes f^2 - 6e_2 \otimes e_1 \otimes f^1 \otimes f^2 + 24e_1 \otimes e_2 \otimes f^1 \otimes f^2 + 12e_2 \otimes e_2 \otimes f^1 \otimes f^2 + 4e_1 \otimes e_1 \otimes f^2 \otimes f^2 + 2e_2 \otimes e_1 \otimes f^2 \otimes f^2 - 8e_1 \otimes e_2 \otimes f^2 \otimes f^2 - 4e_2 \otimes e_2 \otimes f^2 \otimes f^2 = \\
&= 2 \left(-6e_1 \otimes e_1 \otimes f^1 - 3e_2 \otimes e_1 \otimes f^1 + 12e_1 \otimes e_2 \otimes f^1 + 6e_2 \otimes e_2 \otimes f^1 + 2e_1 \otimes e_1 \otimes f^2 + e_2 \otimes e_1 \otimes f^2 - 4e_1 \otimes e_2 \otimes f^2 - 2e_2 \otimes e_2 \otimes f^2 \right) \otimes f^2 = \\
&= 2 \left(-3(2e_1 \otimes e_1 + e_2 \otimes e_1 - 4e_1 \otimes e_2 - 2e_2 \otimes e_2) \otimes f^1 + (2e_1 \otimes e_1 + e_2 \otimes e_1 - 4e_1 \otimes e_2 - 2e_2 \otimes e_2) \otimes f^2 \right) \otimes f^2 = -2(2e_1 \otimes e_1 + e_2 \otimes e_1 - 4e_1 \otimes e_2 - 2e_2 \otimes e_2) (-3f^1 + f^2) \otimes f^2 = \\
&= -2(-(2e_1 + e_2) \otimes e_1 + 2(2e_1 + e_2) \otimes e_2) (-3f^1 + f^2) \otimes f^2 = 2(2e_1 + e_2) (-e_1 + 2e_2) (3f^1 - f^2) \otimes f^2
\end{aligned}$$

Результирующее разложение тензора:

$$a = 4(2e_1 + e_2) (-e_1 + 2e_2) (3f^1 - f^2) \otimes f^1 + 2(2e_1 + e_2) (-e_1 + 2e_2) (3f^1 - f^2) \otimes f^2 = (2e_1 + e_2) (-e_1 + 2e_2) (3f^1 - f^2) (4f^1 + 2f^2)$$