Spiking + Oja + LCA = image comprehension and compression

Equations governing our 2 months at the Darpa Innovation House in Arlington, VA

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Average firing counts over interval τ :

$$n_j^{\mathcal{T}}(t + \Delta t) = e^{\frac{-\Delta t}{\mathcal{T}}} \left[A_j(t) + n_j^{\mathcal{T}}(t) \right]$$
 (1)

Average firing rate over interval τ :

$$f_i^{\tau}(t) = \frac{n_i^{\tau}(t)}{\tau} \tag{2}$$

Feed-forward weight adaptation:

$$\Delta Q(t) = \beta \left\{ [Oja] \cdot [STDP] - decay \right\}$$

$$Q_{ij}(t + \Delta t) = Q_{ij}(t) + \beta \left\{$$

$$f_{Y_j}^{\tau_{Oja}}(t) \left[f_{X_i}^{\tau_{Oja}}(t) - Q_{ij}(t) f_{Y_j}^{\tau_{Oja}}(t) \right] \cdot$$

$$\left[\lambda_P A_Y(t) n_{X_i}^{\tau_P}(t) - \lambda_D A_{X_i}(t) n_{Y_j}^{\tau_D}(t) \right] -$$

$$\alpha_{dec} Q_{ij}(t) \right\}$$
(3)

where β is a learning rate:

$$\beta = dw Max \cdot \frac{\Delta t}{\tau_{oja} f_o}$$

Neuron adaptive firing threshold:

$$V_j^{th} = V_j^{adpt} + e^{\frac{-\Delta t}{T_{V_{th}}}} \left(V_j^{th} - V_j^{adpt} \right)$$
 (4)

where

$$V_{j}^{adpt}(0) = V_{j}^{thRest}$$

$$V_{j}^{adpt}(t + \Delta t) = V_{j}^{adpt}(t) + \frac{\Delta t}{\tau_{THR}} \left[f_{j}^{\tau_{o}}(t) - f_{o} \right] \frac{V_{scale}}{f_{o}}$$
(5)

Lateral inhibition:

$$w_{jk}(t + \Delta t) + = \frac{\Delta t}{\tau_{INH}} \left[f_j^{\tau_{LCA}}(t) f_k^{\tau_{LCA}}(t) - f_o^2 \right] \frac{1}{f_o^2}$$
 (6)

Current scales for τ values

$$au_{oja} \approx 50 - 200ms$$
 $au_P \approx 10 - 20ms$
 $au_D \approx 20 - 40ms$
 $au_{LCA} \approx au_{oja}$
 $au_o = rac{1}{f_o}$
 $au_{THR} \gg au_o$
 $au_{INH} \gg au_{LCA}$
 $au_{V_{th}} \approx 5ms$

Current values for constants:

$$V_{thRest} = -55mV$$

$$V_{rest} = -70mV$$

$$V_{scale} \approx V_{thRest} - V_{rest}$$