CS383 Course Project Specification

Version 5.0

Last Modified on April 9, 2022

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1 Introduction

In this project, you are required to implement an *interpreter* for the programming language SimPL (pronounced *simple*). SimPL is a simplified dialect of ML, which can be used for both *functional* and *imperative* programming. This specification presents a definition of SimPL and provides guidelines to help you implement the interpreter.

2 Lexical Definition

The lexical definition of SimPL consists of four aspects: comments, atoms, keywords, and operators.

2.1 Comments

- Comments in SimPL are enclosed by pairs of (* and *).
- Comments are nestable, e.g. (* (* *) *) is a valid comment, while (* (* *) is invalid.
- A comment can spread over multiple lines.
- Comments and whitespaces (spaces, tabs, newlines) should be ignored and not evaluated.

2.2 Atoms

- Atoms are either integer literals or identifiers.
- Integer literals are matched by regular expression [0-9]+.
- Integer literals only represent non-negative integers less than 2³¹.
- Integer literals are in decimal format, and leading zeros are insignificant, e.g. both 0123 and 000123 represent the integer 123.
- Identifiers are matched by regular expression [a-z] [a-zA-Z0-9']*.

2.3 Keywords

All the following identifiers are keywords. Related keywords are grouped in the same line for better readability. Keywords cannot be bound to anything.

• nil

- ref
- fn rec
- let in end
- if then else
- while do
- true false
- not andalso orelse

2.4 Operators

```
+ - * / % ~
= <> < <= > >=
:: () =>
:= !
, ; ( )
```

3 Syntax

- All SimPL programs are expressions. **Exp** is the set of all expressions.
- Names are non-keyword identifiers. Var is the set of all names.
- Expressions, names, and integer literals are denoted by meta variables e, x, and n.
- Unary operator $uop \in \{ \text{-}, \text{not}, ! \}$
- Binary operator $bop \in \{+, -, *, /, \%, =, <>, <, <=, >, >=, and also, or else, ::, :=, ;\}$

Expression <i>e</i>	::=	n	integer literal
		x	name
		true	true value
		false	false value
		nil	empty list
		$\mathtt{ref}\; e$	reference creation
		$fn x \Rightarrow e$	function
		$rec x \Rightarrow e$	recursion
		(e, e)	pair construction
		иор е	unary operation
		e bop e	binary operation
		e e	application
		let x = e in e end	binding
		$\verb if e \verb then e \verb else e$	conditional
		while $e \ do \ e$	loop
		()	unit
		(e)	grouping

3.1 Operator Precedence

Priority	Operator(s)	Associativity
1	;	left
2	:=	none
3	orelse	right
4	andalso	right
5	= <> < <= > >=	none
6	::	right
7	+ -	left
8	* / %	left
9	(application)	left
10	~ not !	right

4 Typing

4.1 Definition

The set of all types **Typ** is the smallest set satisfying the following rules.

- int \in Typ, bool \in Typ, unit \in Typ
- $\forall t \in \mathbf{Typ}, t \, \mathtt{list} \in \mathbf{Typ}$
- $\forall t \in \mathbf{Typ}, t \, \mathtt{ref} \in \mathbf{Typ}$
- $\forall t_1, t_2 \in \mathbf{Typ}, t_1 \times t_2 \in \mathbf{Typ}$
- $\forall t_1, t_2 \in \mathbf{Typ}, t_1 \rightarrow t_2 \in \mathbf{Typ}$

Type environment Γ : **Var** \rightarrow **Typ** is a mapping from names to arbitrary types. The replacement of x with t in Γ , i.e. $\Gamma[x:t]$, is defined as follows.

$$\Gamma[x:t](y) = \begin{cases} t & \text{if } x = y \\ \Gamma(y) & \text{otherwise} \end{cases}$$

Typing rules:

$$\frac{\Gamma \vdash n : \text{int}}{\Gamma \vdash n : \text{int}} \qquad (T-\text{Int}) \qquad \frac{\Gamma \vdash \text{true} : \text{bool}}{\Gamma \vdash \text{true} : \text{bool}} \qquad (T-\text{True}) \qquad \frac{\Gamma \vdash \text{nil} : \alpha \text{ list}}{\Gamma \vdash \text{nil} : \alpha \text{ list}} \qquad (T-\text{Nil})$$

$$\frac{\Gamma(x) = t}{\Gamma \vdash x : t} \qquad (T-\text{Name}) \qquad \frac{\Gamma \vdash \text{true} : \text{bool}}{\Gamma \vdash \text{false} : \text{bool}} \qquad (T-\text{False}) \qquad \frac{\Gamma \vdash e : t}{\Gamma \vdash (e) : t} \qquad (T-\text{Nil})$$

$$\frac{\Gamma(x) : t_1 \vdash e : t_2}{\Gamma \vdash \text{fn} x \Rightarrow e : t_1 \rightarrow t_2} \qquad (T-\text{Fn}) \qquad \frac{\Gamma \vdash e : \text{int}}{\Gamma \vdash e : \text{bool}} \qquad (T-\text{Not}) \qquad \frac{\Gamma \vdash e_1 : unit}{\Gamma \vdash e_2 : t_2} \qquad (T-\text{Seq})$$

$$\frac{\Gamma(x) : t_1 \vdash e : t_2}{\Gamma \vdash (e) : t} \qquad (T-\text{Not}) \qquad \frac{\Gamma \vdash e_1 : unit}{\Gamma \vdash e_2 : t_2} \qquad (T-\text{Seq})$$

$$\frac{\Gamma \vdash e:t}{\Gamma \vdash ref \ e:t \operatorname{ref}} \qquad (T-\operatorname{Ref}) \qquad \frac{\Gamma \vdash e_1: \operatorname{int} \quad \Gamma \vdash e_2: \operatorname{int} \quad bop \in \{+, -, *, /, \%\}}{\Gamma \vdash e_1 \operatorname{bop} e_2: \operatorname{int}} \qquad (T-\operatorname{Arith})$$

$$\frac{\Gamma \vdash e_1: t \operatorname{ref} \quad \Gamma \vdash e_2: t}{\Gamma \vdash e_1: \operatorname{ref} \quad \Gamma \vdash e_2: t} \qquad (T-\operatorname{Assign}) \qquad \frac{\Gamma \vdash e_1: \operatorname{int} \quad \Gamma \vdash e_2: \operatorname{int} \quad bop \in \{<, <=, >, >=\}}{\Gamma \vdash e_1 \operatorname{bop} e_2: \operatorname{bool}} \qquad (T-\operatorname{Ref})$$

$$\frac{\Gamma \vdash e_1: t \operatorname{ref}}{\Gamma \vdash e_1: t} \qquad (T-\operatorname{Deref}) \qquad \frac{\Gamma \vdash e_1: \alpha \quad \Gamma \vdash e_2: \alpha \quad bop \in \{<, <>\}}{\Gamma \vdash e_1 \operatorname{bop} e_2: \operatorname{bool}} \qquad (T-\operatorname{Eq})$$

$$\frac{\Gamma \vdash e_1: t_1 \quad \Gamma \vdash e_2: t_2}{\Gamma \vdash (e_1, e_2): t_1 \times t_2} \qquad (T-\operatorname{Pair}) \qquad \frac{\Gamma \vdash e_1: \operatorname{bool} \quad \Gamma \vdash e_2: \operatorname{bool}}{\Gamma \vdash e_1 \operatorname{andalso} e_2: \operatorname{bool}} \qquad (T-\operatorname{AndAlso})$$

$$\frac{\Gamma \vdash e_1: t \quad \Gamma \vdash e_2: t \operatorname{list}}{\Gamma \vdash e_1: e_2: t \operatorname{list}} \qquad (T-\operatorname{Cons}) \qquad \frac{\Gamma \vdash e_1: \operatorname{bool} \quad \Gamma \vdash e_2: \operatorname{bool}}{\Gamma \vdash e_1 \operatorname{orelse} e_2: \operatorname{bool}} \qquad (T-\operatorname{Orellse})$$

$$\frac{\Gamma \vdash e_1: t_2 \to t_1 \quad \Gamma \vdash e_2: t_2}{\Gamma \vdash e_1: e_2: t_1} \qquad (T-\operatorname{App}) \qquad \frac{\Gamma \vdash e_1: \operatorname{bool} \quad \Gamma \vdash e_2: t \quad \Gamma \vdash e_3: t}{\Gamma \vdash \operatorname{inf} e_1 \operatorname{then} e_2 \operatorname{else} e_3: t} \qquad (T-\operatorname{Cond})$$

$$\frac{\Gamma \vdash e_1: t_1 \quad \Gamma[x: t_1] \vdash e_2: t_2}{\Gamma \vdash \operatorname{el} e_2: \operatorname{then} e_2: \operatorname{else} e_3: t} \qquad (T-\operatorname{Cond})$$

$$\frac{\Gamma \vdash e_1: t_1 \quad \Gamma[x: t_1] \vdash e_2: t_2}{\Gamma \vdash \operatorname{el} e_1: \operatorname{el} e_2: \operatorname{end} e_2: \operatorname{else} e_3: t} \qquad (T-\operatorname{Cond})$$

4.2 Polymorphism

There is no explicit type annotations in SimPL. So principal type inference is necessary.

1. Some constraint typing rules:

You need to think of how to deal with other cases.

2. Unification algorithm:

$$\overline{(S,\{int=int\}\cup q)->(S,q)}$$

$$\overline{(S,\{bool=bool\}\cup q)->(S,q)}$$

$$\overline{(S,\{a=a\}\cup q)->(S,q)}$$

$$\overline{(S,\{s_{11}->s_{12}=s_{21}->s_{22}\}\cup q)->(S,\{s_{11}=s_{21},s_{12}=s_{22}\}\cup q)}$$

$$\overline{(S,\{a=s\}\cup q)->([a=s]\circ S,q[s/a])}^{(a\ not\ in\ FV(s))}$$

$$\overline{(S,\{s=a\}\cup q)->([a=s]\circ S,q[s/a])}^{(a\ not\ in\ FV(s))}$$

3. Let-Polymorphism is also needed.

$$\begin{split} &\frac{\Gamma \vdash e_2[e_1/x] : t_2 \quad \Gamma \vdash e_1 : t_1}{\Gamma \vdash \text{let } x = e_1 \text{ in } e_2 \text{ end } : t_2} \\ &\frac{\Gamma \vdash e_2[e_1/x] : t_2, q_1 \quad \Gamma \vdash e_1 : t_1}{\Gamma \vdash \text{let } x = e_1 \text{ in } e_2 \text{ end } : t_2, q_1} \end{split} \tag{CT-LetPoly}$$

5 Semantics

5.1 State

A state $s \in \mathbf{State}$ is a triple (E, M, p) where $E \in \mathbf{Env}$ is the environment, $M \in \mathbf{Mem}$ is the memory, and $p \in \mathbb{N}$ is the memory pointer.

$$State = Env \times Mem \times \mathbb{N}$$

$$Env = Var \rightarrow Val \cup Rec$$

$$Mem = \mathbb{N} \rightarrow Val$$

Both the environment and the memory are updateable mappings. Given an updateable mapping $f: X \to Y$, the updated mapping $f[x \mapsto y]$, where $x \in X$, $y \in Y$, is defined as

$$f[x \mapsto y](x') = \begin{cases} y & \text{if } x = x' \\ f(x) & \text{otherwise.} \end{cases}$$

Val consists of integers, booleans, lists, references, pairs, and functions. Rec is the set of recursions.

$$\begin{aligned} \mathbf{Val} &= \bigcup_{t \in \mathbf{Typ}} \mathcal{V}_t \\ \mathcal{V}_{\text{unit}} &= \{\text{unit}\} \\ \mathcal{V}_{\text{int}} &= \mathbb{Z} = \{\cdots, -3, -2, -1, 0, 1, 2, 3, \cdots\} \\ \mathcal{V}_{\text{bool}} &= \mathbb{B} = \{\mathbf{tt}, \mathbf{ff}\} \\ \mathcal{V}_{t \text{ list}} &= \bigcup_{i=0}^{\infty} \mathcal{V}_{t \text{ list}}^{(i)} \\ \mathcal{V}_{t \text{ list}}^{(0)} &= \{\text{nil}\} \\ \mathcal{V}_{t \text{ list}}^{(i+1)} &= \{\text{cons}\} \times \mathcal{V}_t \times \mathcal{V}_{t \text{ list}}^{(i)} \\ \mathcal{V}_{t \text{ ref}} &= \{\text{ref}\} \times \mathbb{N} \\ \mathcal{V}_{t_1 \times t_2} &= \{\text{pair}\} \times \mathcal{V}_{t_1} \times \mathcal{V}_{t_2} \\ \mathcal{V}_{t_1 \to t_2} &= \mathcal{V}_{t_1} \mathcal{V}_{t_2} \subseteq \{\text{fun}\} \times \mathbf{Env} \times \mathbf{Var} \times \mathbf{Exp} \\ \mathbf{Rec} &= \{\text{rec}\} \times \mathbf{Env} \times \mathbf{Var} \times \mathbf{Exp} \end{aligned}$$

5.2 Rules

Judgement form: $E, M, p; e \downarrow M', p'; v$ where $E \in \mathbf{Env}, M, M' \in \mathbf{Mem}, p \in \mathbb{N}, e \in \mathbf{Exp}, v \in \mathbf{Val}$

$$\frac{\mathbf{n} = \mathcal{N}[n]}{E,M,p;n} \qquad (E-INT)$$

$$\frac{E(x) = (\operatorname{rec}, E_1, x_1, e_1) \quad E_1, M, p; \operatorname{rec} x_1 \Rightarrow e_1 \Downarrow M', p'; v}{E,M,p;x \Downarrow M',p';v} \qquad (E-Name1)$$

$$\frac{E(x) = v}{E,M,p;x \Downarrow M,p;v} \qquad (E-Name2)$$

$$\frac{E(x) = v}{E,M,p;x \Downarrow M,p;v} \qquad (E-True)$$

$$\frac{E,M,p;\operatorname{false} \Downarrow M,p;\operatorname{ff}}{E,M,p;\operatorname{false} \Downarrow M,p;\operatorname{ff}} \qquad (E-False)$$

$$\frac{E,M,p;\operatorname{false} \Downarrow M,p;\operatorname{fi}}{E,M,p;\operatorname{fil} \Downarrow M,p;\operatorname{nil}} \qquad (E-Name2)$$

$$\frac{E,M,p;\operatorname{fil} \Downarrow M,p;\operatorname{nil}}{E,M,p;\operatorname{fil} \Downarrow M,p;v} \qquad (E-Group)$$

$$\frac{E,M,p;\operatorname{fil} \Downarrow M',p';v \quad M' = M''[p \mapsto v]}{E,M,p;\operatorname{fil} \iff M'',p';v = M'' = M''[p_1 \mapsto v]} \qquad (E-ReF)$$

$$\frac{E,M,p;\operatorname{fil} \iff M',p';\operatorname{fil} \iff M'',p';\operatorname{fil} \iff M'',p';v = M'' = M''[p_1 \mapsto v]}{E,M,p;\operatorname{fil} \iff M',p';v = M'' = M''[p_1 \mapsto v]} \qquad (E-Assign)$$

$$\frac{E,M,p;\operatorname{fil} \implies e_2 \Downarrow M',p';\operatorname{fil} \iff M'',p';v = M''(p_1)}{E,M,p;\operatorname{fil} \iff M',p';v = M''(p_1)} \qquad (E-Deref)$$

$$\frac{E,M,p;\operatorname{fil} \implies e_3 \Downarrow M,p;\operatorname{fil} \implies e_3 \Downarrow M,p;\operatorname{fil} \implies e_3 \Downarrow M,p;\operatorname{fil} \implies e_3 \Downarrow M',p';v = M'',p';v = M'',p';v$$

```
E, M, p; e \downarrow \underline{M', p'; v \quad v' = -v}
                                                                                                                                            (E-NEG)
                                                                             E, M, p; \sim e \downarrow M', p'; v'
                    E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v = v_1 + v_2
                                                                                                                                            (E-ADD)
                                                \overline{E, M, p; e_1 + e_2 \downarrow M'', p''; v}
                    E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v = v_1 - v_2
                                                                                                                                             (E-SUB)
                                                E, M, p; e_1 - e_2 \downarrow M'', p''; v
                        E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v = v_1 v_2
                                                                                                                                           (E-MUL)
                                                  E, M, p; e_1 * e_2 \downarrow M'', p''; v
  E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_2 \neq 0 \quad v = v_1 \text{ div } v_2
                                                                                                                                             (E-DIV)
                                        E, M, p; e_1 / e_2 \downarrow M'', p''; v
  E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_2 \neq 0 \quad v = v_1 \mod v_2
                                                                                                                                           (E-Mod)
                                       E, M, p; e_1 \% e_2 \Downarrow M'', p''; v
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 < v_2
                                                                                                                                         (E-LESS1)
                         E, M, p; e_1 < e_2 \downarrow M'', p''; tt
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 \ge v_2
                                                                                                                                         (E-LESS2)
                         E, M, p; e_1 < e_2 \downarrow M'', p''; \mathbf{ff}
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 \leq v_2
                                                                                                                                     (E-LessEo1)
                        E, M, p; e_1 \le e_2 \Downarrow M'', p''; \mathbf{tt}
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 > v_2
                                                                                                                                     (E-LESSEQ2)
                        E, M, p; e_1 \le e_2 \Downarrow M'', p''; \mathbf{ff}
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 > v_2
                                                                                                                                  (E-GREATER1)
                        E, M, p; e_1 > e_2 \downarrow M'', p''; tt
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 \leq v_2
                                                                                                                                  (E-GREATER2)
                         E, M, p; e_1 > e_2 \downarrow M'', p''; \mathbf{ff}
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 \ge v_2
                                                                                                                             (E-GREATEREO1)
                        E, M, p; e_1 >= e_2 \Downarrow M'', p''; \mathbf{tt}
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 < v_2
                                                                                                                             (E-GREATEREQ2)
                        E, M, p; e_1 >= e_2 \downarrow M'', p''; \mathbf{ff}
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 = v_2
                                                                                                                                            (E-EQ1)
                         E, M, p; e_1 = e_2 \Downarrow M'', p''; tt
E,M,p;e_1 \Downarrow M',p';v_1 \quad E,M',p';e_2 \Downarrow M'',p'';v_2 \quad v_1 \neq v_2
                                                                                                                                            (E-EQ2)
                         E, M, p; e_1 = e_2 \downarrow M'', p''; \mathbf{ff}
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 \neq v_2
                                                                                                                                          (E-NEQ1)
                        E, M, p; e_1 \Leftrightarrow e_2 \downarrow M'', p''; \mathbf{tt}
E, M, p; e_1 \downarrow M', p'; v_1 \quad E, M', p'; e_2 \downarrow M'', p''; v_2 \quad v_1 = v_2
                                                                                                                                          (E-NEQ2)
                        E, M, p; e_1 \iff e_2 \downarrow M'', p''; \mathbf{ff}
```

$$\frac{E, M, p; e \Downarrow M', p'; \mathbf{tt}}{E, M, p; \text{not } e \Downarrow M', p'; \mathbf{ff}} \qquad (E-\text{NoT1})$$

$$\frac{E, M, p; e \Downarrow M', p'; \mathbf{ff}}{E, M, p; \text{not } e \Downarrow M', p'; \mathbf{tt}} \qquad (E-\text{NoT2})$$

$$\frac{E, M, p; e_1 \Downarrow M', p'; \mathbf{tt}}{E, M, p; e_1 \text{ andalso } e_2 \Downarrow M'', p''; v} \qquad (E-\text{AndAlso1})$$

$$\frac{E, M, p; e_1 \text{ andalso } e_2 \Downarrow M'', p'; \mathbf{ff}}{E, M, p; e_1 \text{ andalso } e_2 \Downarrow M', p'; \mathbf{ff}} \qquad (E-\text{AndAlso2})$$

$$\frac{E, M, p; e_1 \Downarrow M', p; \mathbf{ff}}{E, M, p; e_1 \text{ orelse } e_2 \Downarrow M', p'; \mathbf{tt}} \qquad (E-\text{Orelse1})$$

$$\frac{E, M, p; e_1 \Downarrow M', p'; \mathbf{ff}}{E, M, p; e_1 \text{ orelse } e_2 \Downarrow M'', p''; v} \qquad (E-\text{Orelse2})$$

$$\frac{E, M, p; e_1 \Downarrow M', p'; v_1 \qquad E, M', p'; e_2 \Downarrow M'', p''; v_2}{E, M, p; e_1 \bowtie M', p'; e_2 \Downarrow M'', p''; v_2} \qquad (E-\text{SeQ})$$

$$\frac{E, M, p; e_1 \Downarrow M', p'; v_1 \qquad E, M', p'; e_2 \Downarrow M'', p''; v_2}{E, M, p; \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \Downarrow M'', p''; v} \qquad (E-\text{ConD1})$$

$$\frac{E, M, p; e_1 \Downarrow M', p'; \mathbf{ff}}{E, M, p; \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \Downarrow M'', p''; v} \qquad (E-\text{ConD2})$$

 $E, M, p; e_1 \downarrow M', p'; \mathbf{ff}$

 $\overline{E, M, p}$; while e_1 do $e_2 \downarrow M', p'$; unit

(E-LOOP1)

(E-LOOP2)

5.3 Supplementary Details

- $\mathcal{N}[n]$ is the value of n, e.g. $\mathcal{N}[123] = 123$.
- If a and d are integers, with d non-zero, then a remainder $a \mod d$ is an integer r such that a = qd + r for some integer q, and with |r| < |d|. $a \operatorname{div} d = q$ is the quotient.

 $E, M, p; e_1 \downarrow M', p'; \mathbf{tt}$ $E, M', p'; e_2$; while e_1 do $e_2 \downarrow M'', p''; v$

E, M, p; while e_1 do $e_2 \downarrow M'', p''$; v

- Equality comparisons (= and ≠) work for any equality type.
 - $\forall n \in \mathbb{Z}, n = n$
 - tt = tt, ff = ff
 - nil = nil
 - $(cons, h_1, t_1) = (cons, h_2, t_2) \iff h_1 = h_2 \land t_1 = t_2$
 - $(ref, p_1) = (ref, p_2) \iff p_1 = p_2$
 - $(pair, a_1, b_1) = (pair, a_2, b_2) \iff a_1 = a_2 \land b_1 = b_2$
 - $-v_1 \neq v_2 \iff \neg(v_1 = v_2)$

6 Examples

```
1 let add = fn x => fn y => x + y
2 in add 1 2
end
4 (* ==> 3 *)
```

examples/plus.spl

```
let fact = rec f => fn x => if x=1 then 1 else x * (f (x-1))
in fact 4
end
(* ==> 24 *)
```

examples/factorial.spl

```
let gcd = rec g => fn a => fn b =>

if b=0 then a else g b (a % b)

in gcd 34986 3087

end

(* ==> 1029 *)
```

examples/gcd1.spl

examples/gcd2.spl

```
let
sum = rec sum =>
fn a => if a=nil
then 0
else hd a + sum (tl a)
in
sum (1::2::3::nil)
end
(* ==> 6 *)
```

examples/sum.spl

7 Implementation

7.1 Command-line Interface

You are required to implement the SimPL interpreter in Java, and submit a runnable JAR file, say SimPL.jar. Your interpreter should accept exactly one command-line argument, which is the path of the SimPL program, and then read the program file for execution. Your interpreter should output the result of the execution to the standard output (System.out).

- Your interpreter is started by using java -jar SimPL.jar program.spl.
- If there is a syntax error, output syntax error.
- If there is a type error, output type error.
- If there is a runtime error, output runtime error.
- If the result is an integer, output its value.
- If the result is **tt**, output **true**.
- If the result is **ff**, output **false**.
- If the result is nil, output nil.
- If the result is unit, output unit.
- If the result is a list, output list@ followed by its length.
- If the result is a reference, output ref@ followed by its content.
- If the result is a pair, output pair $0v_1 0v_2$ where v_i is *i*-th element of the pair.
- If the result is a function, output fun.
- · Spaces in the output are insignificant.
- For any test program, your interpreter has up to 5 seconds to execute it.
- Your interpreter is started in a sandbox environment and can only read the current test program.

7.2 Predefined Functions

```
fst: t_1 \times t_2 \rightarrow t_1
snd: t_1 \times t_2 \rightarrow t_2
hd: t \text{ list} \rightarrow t
tl: t \text{ list} \rightarrow t \text{ list}
fst(\text{pair}, v_1, v_2) = v_1
snd(\text{pair}, v_1, v_2) = v_2
hd(\text{cons}, v_1, v_2) = v_1
tl(\text{cons}, v_1, v_2) = v_2
hd(\text{nil}) = \text{error}
tl(\text{nil}) = \text{error}
```

fst, snd, hd, and tl are not keywords. They are predefined names in the topmost environment, work in the same way as user-defined functions, and can be bound to other values.

8 Bonus

- Mutually recursive combinator
- Infinite streams
- Garbage collection (of ref cells)
- Tail recursion
- Lazy evaluation
- Other features or optimizations