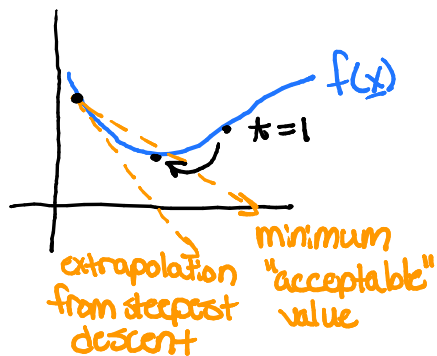


## lecture 16: line search

learning goals  
- apply simple line search heuristics

steepest descent can suggest a direction,  
but how far to go? with steepest descent no natural scale for  $t$

### backtracking line search



choose parameters  $\alpha \in (0, 1/2)$ ,  $\beta \in (0, 1)$

initialize  $t = 1$

while  $f(\underline{x} + t\underline{z}) > f(\underline{x}) + \alpha t \nabla f(\underline{x})^T \underline{z}$

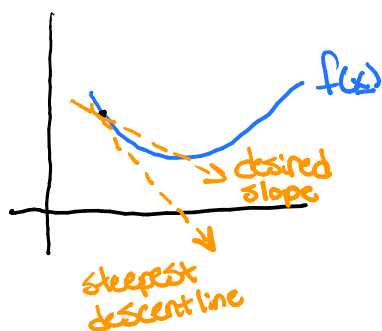
$t = \beta t$

start w/ "large" step, step back until decrease of function is acceptable

typically  $\alpha$  is small ( $\sim 10^{-3}$ ) and  $\beta \in (0.1, 0.8)$

backtracking line search ensures sufficient decrease  
if  $f(\underline{x})$  does not decrease enough, then step is not accepted

### curvature condition



sufficient decrease is always satisfied if steps are very small

to guard against too small steps, we can also introduce a curvature condition

$$\nabla f(\underline{x} + t\underline{z})^T \underline{z} \geq \gamma \nabla f(\underline{x})^T \underline{z}$$

with  $\gamma \in (\alpha, 1)$  (typically  $\gamma \in (0.1, 0.9)$ )

this ensures that derivative is decreasing as well

\* notebook example "correcting" previous bad steps,  
introduce unbalanced quadratic to motivate Newton's method