

$$x_K \begin{matrix} -1 & 0 & 1 \\ y_K & -1 & 2 & -3 \end{matrix}$$

$$f_1(x) = Ax^3 + Bx^2 + Cx + D$$

$$f_2(x) = Ex^3 + Fx^2 + Gx + H$$

$$1^\circ f_1(-1) = -1 \Rightarrow -A + B - C + D = -1$$

$$f_1(0) = 2 \Rightarrow D = 2$$

$$f_2(0) = 2 \Rightarrow H = 2$$

$$f_2(1) = -3 \Rightarrow E + F + G + H = -3$$

$$2^\circ f_1'(0) = f_2'(0) \Rightarrow C = G$$

$$f_1''(0) = f_2''(0) \Rightarrow B = F$$

$$3^\circ f_1''(-1) = 0 \Rightarrow -6A + 2B = 0$$

$$f_2''(-1) = 0 \Rightarrow 6E + 2F = 0$$

$$\text{row} \left\{ \begin{array}{l} A = -2 \\ B = -6 \\ C = -1 \\ D = 2 \\ E = 2 \\ F = -6 \\ G = -1 \\ H = 2 \end{array} \right.$$

$$\left\{ \begin{array}{l} D = 2 \\ H = 2 \\ C = G \\ B = F \\ -A + B - C = -3 \\ E + B + C = -5 \\ -6A + 2B = 0 \\ A = -E \end{array} \right.$$

$$\begin{array}{r} -A + B - C = -3 \\ -A + B + C = -5 \\ \hline -2C = 2 \\ C = -1 \end{array}$$

$$B = -6$$

$$12 + 2B = 0$$

$$E = 2$$

$$\begin{array}{l} D = 2 \\ H = 2 \\ C = -1 \\ G = -1 \\ B = F \\ -A + B = -4 \\ E + B = -4 \\ -6A + 2B = 0 \\ -3A + B = 0 \\ -A + B = -4 \\ -2A = 4 \quad A = -2 \end{array}$$