

$$f(x) = \sin \frac{x}{2}$$

$$f'(x) = \cos \frac{x}{2} \cdot \frac{1}{2}$$

$$f''(x) = -\sin \frac{x}{2} \cdot \left(\frac{1}{2^2}\right)$$

$$f'''(x) = -\cos \frac{x}{2} \cdot \left(\frac{1}{2^3}\right)$$

$$f^{(n)}(x) = \frac{1}{2^n} \cdot (-1)^{\lfloor \frac{n}{2} \rfloor} \cdot \sin \frac{x}{2} \quad \text{DLA } n \text{ PARZYSTEW}$$

$$f^{(n)}(x) = \frac{1}{2^n} \cdot (-1)^{\lfloor \frac{n}{2} \rfloor} \cdot \cos \frac{x}{2} \quad \text{DLA } n \text{ NIEPARZYSTEW}$$

$$\max_{x \in [0,1]} |f(x) - L_n(x)| = \max_{x \in [0,1]} \left| \frac{f^{(n+1)}(\xi)}{(n+1)!} \cdot P_n(x) \right| \leq \max_{x \in [0,1]} \left| \frac{P_n(x)}{2^{n+1} \cdot (n+1)!} \right| \leq \frac{1}{2^{n+1} \cdot (n+1)!}$$

$$|P_{n+1}(x)| \leq 1 \quad \text{NIE MA LEPSZEGO?}$$

$$\frac{1}{2^{n+1} \cdot (n+1)!} \leq 10^{-15}$$

$$\text{DLA } n=13$$