

$$P_0 = 1$$

$$V_0 = 1, V_1 = x, V_2 = x^2$$

$$P_1 = 1 - \frac{\langle x, 1 \rangle}{\langle 1, 1 \rangle} \cdot 1 = 1 - 0 \cdot 1 = x$$

$$P_2 = x^2 - \frac{\langle x^2, 1 \rangle}{\langle 1, 1 \rangle} \cdot 1 - \frac{\langle x^2, x \rangle}{\langle x, x \rangle} \cdot x = x^2 - \frac{2 \cdot (16 + 9 + 4 + 1)}{8} - \frac{0}{60} \cdot x = x^2 - \frac{60}{8} = x^2 - \frac{15}{2}$$

$q_{0.5}$

$$W_2^*(x) = \sum_{k=0}^2 a_k \cdot P_k(x)$$

$$a_k = \frac{\langle W, P_k \rangle}{\langle P_k, P_k \rangle}$$

$$a_0 = \frac{\langle W, P_0 \rangle}{\langle P_0, P_0 \rangle} = 0$$

$$a_1 = \frac{\langle W, P_1 \rangle}{\langle P_1, P_1 \rangle} = \frac{2 \cdot ((-5, 5) \cdot (-4) + (-3) \cdot (-5) + (-2) \cdot (-3, 2) + (-1) \cdot (-1))}{60} =$$

$$= \frac{2 \cdot 22 + 15 + 6 + 1}{30} = \frac{37 + 7, 4}{30} = \frac{44, 4}{30} = \frac{37}{25}$$

$$a_2 = \frac{\langle W, P_2 \rangle}{\langle P_2, P_2 \rangle} = 0$$

$$W_2^*(x) = 0 \cdot 1 + \frac{37}{25} \cdot x + 0 \cdot \left(x^2 - \frac{15}{2}\right) = \frac{37}{25}x$$