

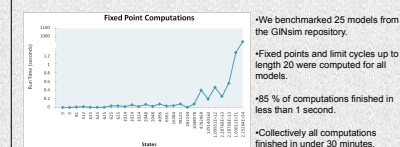
^aUniversity of Tennessee - Knoxville, Knoxville, TN 37996-2513, USA, ^bHarvey Mudd College, Claremont, CA 91711-5901, USA, ^cUniversity of North Carolina - Greensboro, Greensboro, NC 27402-6170, USA, ^dDepartment of Mathematics, Virginia Polytechnic Institute and State University, Blacksburg, VA 24061-0123, USA, ^eVirginia Bioinformatics Institute, Blacksburg, VA 24061-0477, USA, ^fDepartment of Mathematics, University of Nebraska-Lincoln, Lincoln NE 68588-0619, ^gDepartment of Mathematics and Statistics, American University of Sharjah, Sharjah, United Arab Emirates, ^hInstitute for Pure and Applied Mathematics, UCLA, Los Angeles, CA 90095-7121. * These three authors contributed equally

Methods

The algorithms were coded in the computer algebra system Macaulay2^[9]. Specifically we used Macaulay2 to compute the Gröbner basis of input functions within a quotient ring

In biological systems, most nodes only have a few direct neighbors. For instance, in gene regulatory networks, genes are regulated by only a handful of regulators^[7]. This means the PDSs representing such biological networks are sparse, i.e., the support of each polynomial is a small set of variables. It has been shown that computing Gröbner bases from sparse polynomials is more efficient in a finite field^[8]. Based on benchmark tests on our algorithms which compute fixed points, we show that our algorithms are, in fact, fast on large sparse systems. All benchmark tests were run on a 2.27 GHz processor.

91% of Gröbner bases computations finished in less than 30 seconds



For networks with a special structure, *conjunctive* and *disjunctive* Boolean networks, ADAL uses the algorithm described in Jarrah et al.^[11] which does not require a Gröbner basis computation and therefore can analyze larger systems. *Conjunctive* Boolean networks consist of functions containing only one monomial term, i.e. the functions use only the AND operator. Conversely, *disjunctive* Boolean Networks consist of functions which use only the OR operator. There is a closed formula to compute the cycle structure which depends solely on the wiring diagram.

For discrete models, analysis is usually done by simulation which is inefficient and even impossible for some large networks. By translating discrete models into algebraic models, we are able to use algorithms from abstract algebra to analyze the dynamics of networks that are too large for simulation. We implemented several algorithms and made them available through a web-interface called Analysis of Dynamic Algebraic Models (ADAM)². Algebraic Models can be inferred from experimental time course data with *Polynome* [10].

Wiring diagram – a graph representing the static relationship between nodes or genes by directed edges.

The wiring diagram represents the interaction of four genes involved in the lysogenic cycle of the Lambda Phage virus.

- red arrows signify inhibition
- green arrows signify activation.

The Lambda Phage virus has been extensively studied as a model organism and is a useful tool in molecular biology.

Output from ADAM for limit cycles of length 7 of the TCR Signaling Pathway

- The algorithms we developed are **fast** for sparse systems, a structure maintained by most biological systems.
- All algorithms have been included in the **software package ADAM**, which is user-friendly and available as a free web service.
- We hope to expand ADAM to an all-encompassing **Discrete Toolkit** which incorporates more analytical methods, better visualization, and automatic conversion for more model types.

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