

# Computing Infrastructures - Notes - v2.0.0

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## Preface

Every theory section in these notes has been taken from two sources:

- The Datacenter as a Computer: Designing Warehouse-Scale Machines, Third Edition. [2]
- Quantitative System Performance: Computer System Analysis Using Queueing Network Models. [4]
- Course slides. [6]

About:



These notes are an unofficial resource and shouldn't replace the course material or any other book on computing infrastructure. It is not made for commercial purposes. I've made the following notes to help me improve my knowledge and maybe it can be helpful for everyone.

As I have highlighted, a student should choose the teacher's material or a book on the topic. These notes can only be a helpful material.

# Contents

<b>1 Data Center and Computing Infrastructure</b>	<b>5</b>
<b>2 Hardware Infrastructures</b>	<b>6</b>
2.1 System-level . . . . .	6
2.1.1 Computing Infrastructures and Data Center Architectures . . . . .	6
2.1.1.1 Overview of Computing Infrastructures . . . . .	6
2.1.1.2 The Datacenter as a Computer . . . . .	13
2.1.1.3 Warehouse-Scale Computers . . . . .	16
2.1.1.4 Multiple Data Centers . . . . .	19
2.1.1.5 Availability in WSCs and DCs . . . . .	21
2.1.1.6 Architectural Overview of WSCs . . . . .	22
2.2 Node-level . . . . .	25
2.2.1 Server (computation, HW accelerators) . . . . .	25
2.2.1.1 Tower Server . . . . .	27
2.2.1.2 Rack Servers . . . . .	28
2.2.1.3 Blade Servers . . . . .	30
2.2.1.4 Machine Learning . . . . .	31
2.2.2 Storage (type, technology) . . . . .	34
2.2.2.1 Files . . . . .	35
2.2.2.2 HDD . . . . .	39
2.2.2.3 SSD . . . . .	45
2.2.2.4 RAID . . . . .	57
2.2.2.5 DAS, NAS and SAN . . . . .	80
2.2.3 Networking (architecture and technology) . . . . .	83
2.2.3.1 Fundamental concepts . . . . .	83
2.2.3.2 Switch-centric: classical Three-Tier architecture . . . . .	85
2.2.3.3 Switch-centric: Leaf-Spine architectures . . . . .	88
2.2.3.4 Server-centric and hybrid architectures . . . . .	96
2.3 Building level . . . . .	102
2.3.1 Cooling systems . . . . .	104
2.3.2 Power supply . . . . .	107
2.3.3 Data Center availability . . . . .	108
<b>3 Software Infrastructure</b>	<b>109</b>
3.1 Virtualization . . . . .	109
3.1.1 What is a Virtual Machine? . . . . .	109
3.1.1.1 Process VM . . . . .	111
3.1.1.2 System VM . . . . .	112
3.1.2 Virtualization Implementation . . . . .	113
3.1.3 Virtual Machine Managers (VMM) . . . . .	114
3.1.3.1 Full virtualization . . . . .	117
3.1.3.2 Paravirtualization . . . . .	118
3.1.3.3 Containers . . . . .	120
3.2 Computing Architectures . . . . .	122
3.2.1 Cloud Computing . . . . .	122
3.2.1.1 Server Consolidation . . . . .	122
3.2.1.2 Services provided by cloud . . . . .	123
3.2.1.3 Types of clouds . . . . .	126

<b>4 Methods</b>	<b>127</b>
4.1 Reliability and availability of data centers . . . . .	127
4.1.1 Introduction . . . . .	127
4.1.2 Reliability and Availability . . . . .	133
4.1.3 Reliability Block Diagrams (RBDs) . . . . .	141
4.1.3.1 R out of N redundancy (RooN) . . . . .	149
4.1.3.2 Triple Modular Redundancy (TMR) . . . . .	150
4.1.3.3 Standby redundancy . . . . .	153
4.2 Disk performance . . . . .	155
4.2.1 HDD . . . . .	155
4.2.2 RAID . . . . .	160
4.3 Scalability and performance of data centers . . . . .	166
4.3.1 Evaluate system quality . . . . .	166
4.3.2 Queueing Networks . . . . .	168
4.3.2.1 Definition . . . . .	168
4.3.2.2 Characteristics . . . . .	169
4.3.3 Operational Laws . . . . .	173
4.3.3.1 Basic measurements . . . . .	173
4.3.3.2 Utilization Law . . . . .	175
4.3.3.3 Little's Law . . . . .	175
4.3.3.4 Interactive Response Time Law . . . . .	178
4.3.3.5 Visit count . . . . .	178
4.3.3.6 Forced Flow Law . . . . .	179
4.3.3.7 Utilization Law with Service Demand . . . . .	179
4.3.3.8 Response and Residence Times . . . . .	180
4.3.4 Bounding Analysis . . . . .	181
4.3.4.1 Introduction . . . . .	181
4.3.4.2 Asymptotic bounds . . . . .	182
<b>5 Exams</b>	<b>188</b>
5.1 2025 . . . . .	188
5.1.1 February 3 . . . . .	188
5.1.2 January 13 . . . . .	194
5.2 2024 . . . . .	202
5.2.1 September 5 . . . . .	202
5.2.2 June 12 . . . . .	209
5.2.3 February 7 . . . . .	216
5.3 2023 . . . . .	225
5.3.1 July 7 . . . . .	225
<b>Index</b>	<b>236</b>

## 1 Data Center and Computing Infrastructure

There's no single definition of a Data Center, but it can be summarized as follows.

### Definition 1: Data Center

**Data Centers** are buildings where multiple servers and communications equipment are co-located for common environmental requirements, physical security, and ease of maintenance. [2]

### Definition 2: Computing Infrastructure

A **Computing Infrastructure** (or IT Infrastructure) is a technological infrastructure that provides hardware and software for computation to other systems and services.

Traditional data centres have the following characteristics:

- **Host a large number** of relatively small or medium sized **applications**;
- Each **application is running on a dedicated HW infrastructure** that is de-coupled and protected from other systems in the same facility;
- **Applications tend not to communicate each other.**

Those **data centers** host hardware and software for **multiple organizational units** or even **different companies**.

## 2 Hardware Infrastructures

### 2.1 System-level

#### 2.1.1 Computing Infrastructures and Data Center Architectures

##### 2.1.1.1 Overview of Computing Infrastructures

The **Computing Continuum** is a distributed computing environment that seamlessly integrates endpoints (IoT devices), edge computing, and cloud computing to optimize data processing across different layers of infrastructure. Therefore, it consists of three main layer:

1. **Endpoints** (IoT Devices & Sensors) - The **Data Collectors**. At the very edge of the continuum, we find Endpoints. They are small, low-power devices embedded with sensors that collect and transmit data.

##### ❖ Examples

- A **temperature sensor** in a smart home, detecting room conditions.
- A **fitness tracker** measuring heart rate and step count.
- A **manufacturing robot** equipped with vibration sensors to detect faults.

**⚠ Challenges.** While IoT devices are great at collecting data, they have limited processing power and cannot perform complex calculations. As a result, they often send raw data to the next level for further analysis.

2. **Edge & Fog Computing** - Processing Data Close to the Source. To reduce the dependence on cloud processing, the Edge Computing layer introduces **local computation** at the network's edge. This means that instead of sending all raw data to the cloud, some processing occurs closer to where the data is generated.

##### ❖ Examples

- **Smart security cameras** analyzing video footage locally to detect intruders before sending alerts to a cloud-based security system.
- **Autonomous vehicles** processing sensor data in real-time to make split-second driving decisions without relying on a remote server.

**⚠ Fog Computing vs. Edge Computing.** Fog Computing refers to processing data at an intermediate level, such as an IoT gateway or a local network node.

- Edge Computing happens directly on the device producing the data.
- Fog Computing moves processing to a nearby network gateway or edge server.

### ✓ Advantages

- ✓ **Lower latency**: Decisions are made **faster** since they don't rely on a cloud response.
- ✓ **Bandwidth savings**: Only important data is sent to the cloud, reducing network congestion.
- ✓ **Privacy and security**: Some data can remain **local**, avoiding unnecessary cloud exposure.

**⚠ Challenges**. While Edge Computing is beneficial, it **requires additional hardware** and **power** at the network's edge, which can **increase infrastructure complexity and costs**.

3. **Cloud Computing** - The Powerhouse of Large-Scale Processing. At the top of the continuum, cloud computing provides **massive storage and computation capabilities**. It is well-suited for applications that require significant computational resources, such as big data analytics, machine learning training, scalable web services (e.g., Netflix, YouTube, Amazon AWS).

### ✖ Examples

- **AI model training** is typically done in cloud data centers because it requires significant GPU/TPU power.
- **E-commerce platforms** like Amazon use cloud computing to manage global inventory and transactions.
- **Streaming services** store and distribute high-quality video content from cloud servers.

### ✓ Advantages

- ✓ **Scalability**: Computing power can be adjusted based on demand.
- ✓ **Resource efficiency**: Data centers consolidate computing, making operations more cost-effective.
- ✓ **Advanced analytics**: Supports complex workloads like deep learning and data mining.

### ⚠ Challenges

- **Latency issues** make real-time decision-making difficult.
- **Network dependency**: A constant internet connection is required.
- **High operational costs** for companies relying solely on cloud resources.

To summarize Computing Continuum creates a balanced computing environment by ensuring that workloads are distributed intelligently across IoT, edge, and cloud layers.

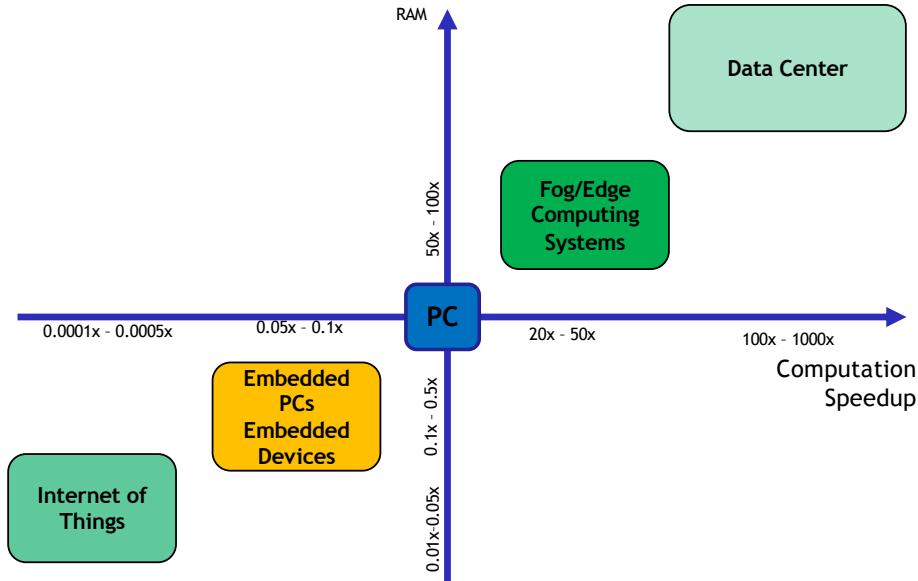


Figure 1: Examples of Computing Infrastructures. [7]

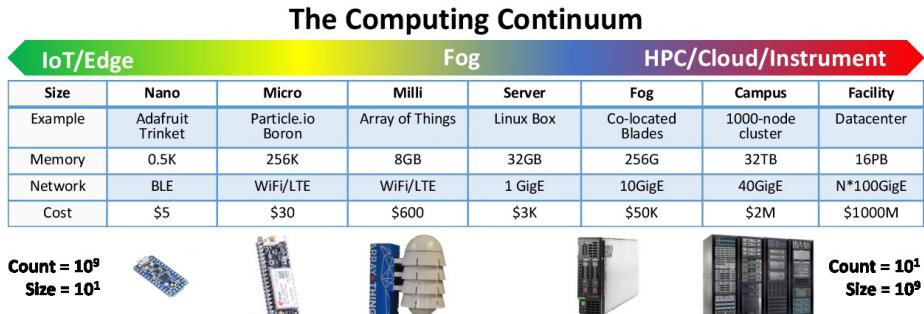


Figure 2: This figure represents the Computing Continuum, how different computing layers interact to process data efficiently. It is a hierarchical structure moving from IoT devices at the left (closest to the data source) to cloud computing at the right (handling large-scale processing). [7]

In the following pages, we analyze the computing infrastructures mentioned in the previous example.

## Data Centers

The definition of a Data Centers can be found on page 5.

### ✓ Data Centers Advantages

- Lower IT costs.
- High Performance.
- Instant software updates.
- “Unlimited” storage capacity.
- Increased data reliability.
- Universal data access.
- Device Independence.

### 👎 Data Centers Disadvantages

- Require a constant internet connection.
- Do not work well with low-speed connections.
- Hardware Features might be limited.
- Privacy and security issues.
- High power Consumption.
- Latency in taking decision.

## Internet-of-Things (IoT)

An **Internet of Things (IoT)** device is any everyday object embedded with sensors, software, and internet connectivity.

This allows to collect and exchange data with other devices and systems, typically over the internet, with limited need of process and store data.

Some **examples** are [Arduino](#), [STM32](#), [ESP32](#), [Particle Argon](#).

### ✓ Internet-of-Things Advantages

- Highly Pervasive.
- Wireless connection.
- Battery Powered.
- Low costs.
- Sensing and actuating.

### ❗ Internet-of-Things Disadvantages

- Low computing ability.
  - Constraints on energy.
  - Constraints on memory (RAM/FLASH).
  - Difficulties in programming.
- 

## Embedded (System) PCs

An **Embedded System** is a computer system, a combination of a computer processor, computer memory, and input/output peripheral devices, that has a dedicated function within a larger mechanical or electronic system.

A few **examples**: [Odroid](#), [Raspberry](#), [jetson nano](#), [Google Coral](#).

### ✓ Embedded System Advantages

- Persuasive computing.
- High performance unit.
- Availability of development boards.
- Programmed as PC.
- Large community.

### ❗ Embedded System Disadvantages

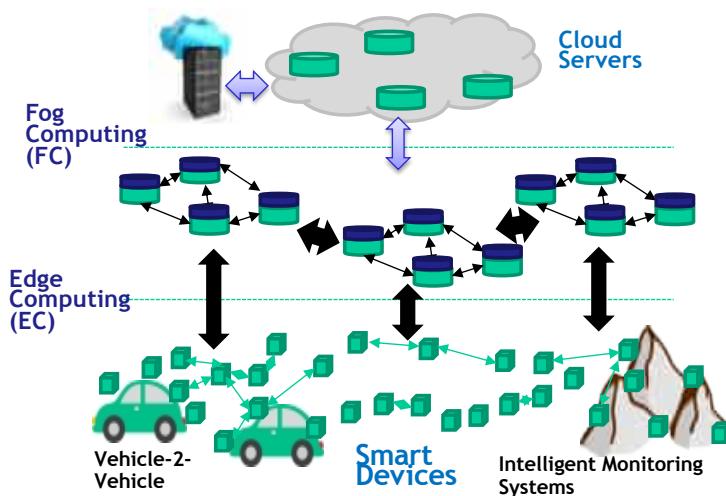
- Pretty high power consumption.
- (Some) Hardware design has to be done.

## Edge/Fog Computing Systems

The key **difference** between **Fog Computing** and **Edge Computing** is associated with the location **where the data is processed**:

- In **edge computing**, the data is processed closest to the sensors.
- In **fog computing**, the computing is moved to processors linked to a local area network (IoT gateway).

Edge computing places the intelligence in the connected devices themselves, whereas, fog computing puts in the local area network.



### ✓ Fog/Edge Advantages

- High computational capacity.
- Distributed computing.
- Privacy and security.
- Reduced Latency in making a decision.

### ❗ Fog/Edge Disadvantages

- Require a power connection.
- Require connection with the Cloud.

Feature	Edge Computing	Fog Computing
<b>Location</b>	Directly on device or nearby device.	Intermediary devices between edge and cloud.
<b>Processing Power</b>	Limited due to device constraints, sending data to central server for analysis.	More powerful than edge devices. However, sending data to a central server for analysis.
<b>Primary Function</b>	Real-time decision-making, low latency. However, central server analyzing combined data and sending only relevant information further.	Pre-process and aggregate data, reduce bandwidth usage. However, central server analyzing combined data and sending only relevant information further.
<b>Advantages</b>	Low latency, reduced reliance on cloud, security for sensitive data.	Bandwidth efficiency, lower cloud costs, complex analysis capabilities.
<b>Disadvantages</b>	Limited processing power, single device focus.	Increased complexity, additional infrastructure cost.

Table 1: Differences between Edge and Fog Computing Systems.

### 2.1.1.2 The Datacenter as a Computer

The concept of treating the datacenter itself as a singular, unified computing system represents a significant evolution in computing infrastructures. Traditionally, computing resources were individually managed and isolated (client-server computing); now, the paradigm shifts towards collective resource management and holistic infrastructure design (datacenter-based computing, particularly Warehouse-Scale Computers, WSCs).

#### ✓ User Experience Improvements

For end-users, the shift to centralized computing in datacenters provides significant advantages:

- **Ease of Management. No need for local configuration or backups.**

- ✓ Users no longer need to manually configure and maintain software or hardware on their personal devices.
- ✓ Centralized cloud-based systems handle updates, security patches, and maintenance automatically.

- **Ubiquity of Access**

- ✓ **Users can access services and data from any device, anywhere,** as long as they have an internet connection.
- ✓ This allows for seamless synchronization<sup>1</sup> across multiple devices (e.g., accessing Google Drive files from a laptop, tablet, or phone).

- **Reduced Hardware Dependencies**

- ✓ Computing power is shifted from end-user devices to cloud services.
- ✓ Even low-powered devices (e.g., smartphones, Chromebooks) can perform complex tasks by offloading computation to datacenters.

For example, cloud-based applications like Google Docs allow real-time document editing across multiple devices without requiring powerful local hardware.

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<sup>1</sup>Seamless synchronization: The automatic and continuous updating of data across multiple devices or platforms without user intervention, ensuring consistency and accessibility in real-time.

### ✓ Advantages for Service Providers (vendors)

From the perspective of software and hardware vendors, the transition to data-center computing brings several operational and economic benefits.

- **Software-as-a-Service (SaaS) Enables Faster Development**

- ✗ Traditional software development involved deploying updates individually to millions of heterogeneous client devices.
- ✓ Now, **cloud-based applications** allow:
  - \* Centralized software deployment.
  - \* Rapid updates and feature rollouts.
  - \* Easier bug fixes and security patches.

For example, instead of releasing a new version of Microsoft Office every few years, Microsoft now provides Microsoft 365, where updates are continuously applied.

- **Simplified Hardware Deployment**

- ✗ Traditional software development required compatibility with millions of different client hardware configurations.
- ✓ Now, with server-side computing, companies **only need to support a few well-tested hardware platforms** in their datacenters.

For example, instead of optimizing software for thousands of different PC models, Google can optimize Gmail and YouTube to run efficiently in their controlled cloud environment.

- **Better Resource Utilization**

- ✓ Datacenters allow for **efficient resource allocation**, ensuring that computing power is shared dynamically across multiple applications.
- ✓ Cloud providers can achieve **high resource utilization**, reducing costs and improving performance.

For example, cloud providers like AWS and Google Cloud use containerization (e.g., Kubernetes) to dynamically allocate computing resources to workloads as needed.

### ✓ Benefits of Server-Side Computing

Beyond user experience and vendor advantages, server-side computing enables several key technological improvements.

- **Faster Introduction of New Hardware**

- ✗ In a traditional computing model, upgrading hardware required end-users to buy new devices.
- ✓ In a datacenter-centric model, **hardware upgrades happen in the cloud**, where service providers can deploy: new processors, AI accelerators (e.g., TPUs, GPUs), more efficient storage solutions.

For example, Google introduced TPUs (Tensor Processing Units) for machine learning, allowing AI workloads to run more efficiently in their datacenters without requiring users to upgrade their devices.

- **Cost Efficiency for Large-Scale Applications**

- ✗ Many applications require enormous computational resources that are impractical for client devices.
- ✓ Running these applications in datacenters allows for **better scaling** and **lower cost per user**.

For example, Google Search processes billions of queries daily, requiring petabytes of storage and high-speed computation. Another example is training deep learning models (e.g., ChatGPT, image recognition, autonomous vehicles) is computationally expensive and only feasible in large datacenters.

### 2.1.1.3 Warehouse-Scale Computers

With the advent of server-side computing and large-scale Internet services, a new class of computing systems emerged: **Warehouse-Scale Computers (WSCs)**. These systems were designed to meet the unique requirements of large-scale applications, which often involve multiple interdependent programs interacting within a unified infrastructure. Characteristics of WSCs are:

- Unlike traditional data centers, **WSCs** are not just collections of servers, but **complete computing environments**.
- A single WSC might consist of **thousands of servers**, all working together as a **single, large computing unit**.
- **WSCs support complex, large-scale services** such as:
  - Search engines (Google Search, Bing)
  - Cloud-based email (Gmail, Outlook)
  - Online maps and navigation services (Google Maps, Waze)
  - Machine learning and artificial intelligence platforms (Google's TensorFlow, OpenAI's models)

The scale at which these systems operate requires a fundamentally different architectural approach—one optimized for efficiency, scalability, and unified resource management.

#### Definition 1: Warehouse-Scale Computers (WSCs)

**Warehouse-Scale Computers (WSCs)** is a computing system designed to operate at an extreme scale, integrating massive software infrastructure, vast data repositories, and a unified hardware platform to function as a single, cohesive computing entity, typically owned and managed by a single organization.

### ⚠ Warehouse-Scale Computers vs. Traditional Data Centers

- **Traditional Data Centers: A More Fragmented Approach.** A traditional data center is a facility that houses a collection of servers and networking equipment, providing computing resources for various applications and organizations. These environments are characterized by:
  - A **diverse range of applications**, each running on **its own dedicated hardware infrastructure**.
  - **Applications that do not communicate** with one another or share resources.
  - A **multi-tenant model**, where hardware and software are used by **multiple organizations or business units**.

This model works well for enterprises hosting multiple independent applications, such as corporate databases, enterprise software, and web hosting services.

- **Warehouse-Scale Computers: A Unified Approach.** In contrast, WSCs are designed to function as a **single, highly integrated computing unit**. Unlike traditional data centers, which support numerous small applications in isolation, WSCs are optimized for **massive, unified workloads** controlled by a **single organization**. Key characteristics of WSCs include:

- **Homogeneous hardware and software:** The infrastructure is standardized, making it easier to manage and scale.
- **Centralized resource management:** Instead of treating each server as an independent entity, WSCs manage computing resources dynamically across a large-scale cluster.
- **Support for large-scale applications:** WSCs are built to run a **small number of massive applications**, such as search engines, AI models, or cloud services.

By shifting towards WSCs, companies like Google, Amazon, and Microsoft have been able to achieve better efficiency, scalability, and cost-effectiveness, leading to the next evolution of computing infrastructure.

For example, when we perform a Google Search, the request is processed across multiple servers simultaneously in a WSC, with different servers handling indexing, ranking, and query matching. The user only sees the final result, but behind the scenes, thousands of machines collaborate in milliseconds.

- **Ownership**

- **Traditional DC:** Multiple organizations/tenants
- **WSCs:** Single organization

- **Application Scale**

- **Traditional DC:** Many small-to-medium apps
- **WSCs:** Few massive applications

- **Hardware**

- **Traditional DC:** Heterogeneous, diverse setups
- **WSCs:** Homogeneous architecture

- **Resource Management**

- **Traditional DC:** Isolated per application
- **WSCs:** Centralized, dynamic allocation

- **Software Execution**

- **Traditional DC:** Independent workloads
- **WSCs:** Interdependent, large-scale services

### ⌚ From Data Centers to WSCs and Back

Initially, WSCs were designed exclusively for handling large-scale, internet-facing applications. However, as cloud computing evolved, the **lines between traditional data centers and warehouse-scale computing began to blur**. Modern cloud computing is a convergence of these two models: traditional Datacenter and WSC.

- Today's public cloud platforms (AWS, Google Cloud, Microsoft Azure) run many small applications, much like traditional data centers.
- These **applications rely on Virtual Machines (VMs) and Containers**, which efficiently distribute workloads across a warehouse-scale infrastructure.

Era	Computing Model	Example
Past	Traditional Data Centers	Enterprise IT infrastructure
Present	Warehouse-Scale Computers	Google Search, AI training
Future	Hybrid WSC-DC Model	Cloud computing (AWS)

#### 2.1.1.4 Multiple Data Centers

The **architecture of modern computing infrastructure** is not limited to single data centers but rather extends across multiple, geographically distributed facilities.

##### 💡 Why use multiple datacenters?

A single datacenter can host and process workloads, but distributing computing infrastructure across multiple facilities offers several **advantages**:

- ✓ **Lower Latency for Users.** When **datacenters are closer to users**, request-response times are reduced. Services like Google Search, Netflix streaming, and cloud gaming benefit from regional datacenters.
- ✓ **Improved Throughput & Load Balancing**
  - Spreading requests across multiple locations prevents bottlenecks.
  - Global services handle millions of requests per second, which would overload a single facility.
- ✓ **Disaster Recovery & Fault Tolerance**
  - If one datacenter fails (due to power outages, natural disasters, or cyberattacks), another can take over.
  - Redundancy ensures minimal downtime for mission-critical applications.

#### ☷ The Hierarchical Organization of Multi-Datacenter Infrastructure

To effectively distribute workloads and ensure resilience, cloud providers divide their infrastructure into a **structured hierarchy**.

1. **Geographic Areas (GAs).** The **highest level of organization**, defined by geopolitical boundaries or country-specific regulations. The primary factor is data residency laws, ensuring compliance with legal frameworks (e.g., GDPR in Europe).

##### Example 1: Geographic Area

For example, a GA might represent North America, Europe, or Asia-Pacific. A user in France may have their data processed within Europe to comply with EU data protection regulations.

2. **Computing Regions (CRs)**. A finer granularity within Geographic Areas, representing large-scale infrastructure within a geographic region. Each GA contains at least two Computing Regions for redundancy. Key characteristics:

- Users see computing regions as isolated environments where they can deploy workloads.
- Multiple DCs exist within a region but are not individually exposed to users.
- Latency-defined perimeter: Ensures that intra-region latency remains within 2ms for round-trip communication.
- Distance considerations:
  - Datacenters within a region are hundreds of miles apart.
  - This protects against localized failures (e.g., natural disasters, power grid failures).

#### Example 2: Computing Region

AWS has “US-East-1” (Virginia) and “US-West-1” (California) as distinct computing regions.

3. **Availability Zones (AZs)**. Within a Computing Region, datacenters are further divided into Availability Zones (AZs).

- *What are Availability Zones?*
  - Physically separate datacenters within a region, each with redundant power, cooling, and networking.
  - Fault isolation ensures that failures in one AZ do not affect others.
  - Designed for mission-critical applications that require continuous availability.
- *How they work?*
  - Application-level synchronous replication occurs across multiple AZs, ensuring data consistency.
  - A minimum of three AZs per region is recommended for quorum-based decision-making.
- *Example Scenarios*
  - Customer 1 deploys services in a single AZ, risking downtime if the AZ fails.
  - Customer 2 uses multi-AZ deployment, ensuring failover in case of failure.
  - Customer 3 distributes workloads across multiple AZs, achieving full redundancy.

With the rise of low-latency applications, modern cloud providers go beyond central data centers by deploying **Edge Locations**. They are smaller facilities located closer to the user. They are used to cache frequently accessed data and accelerate content delivery. Commonly used in content delivery networks (CDNs) such as Cloudflare, AWS CloudFront, and Akamai.

### Example 3: Edge Locations

- Streaming services (Netflix, YouTube): Caching popular videos at Edge Locations reduces buffering.
- Cloud gaming (NVIDIA GeForce Now, Xbox Cloud Gaming): Minimizing latency for real-time responsiveness.
- IoT applications: Autonomous cars and smart cities require ultra-fast data processing near the source.

#### 2.1.1.5 Availability in WSCs and DCs

**Availability is a critical factor** in datacenter and warehouse-scale computing since these **infrastructures host mission-critical applications that must remain operational with minimal downtime**. Achieving high availability requires fault-tolerant architectures, redundancy, and proactive failure management.

**Availability** is measured as the **percentage of uptime over a given period** (usually a year). Another important topic is the **Service Level Agreement (SLA)**, which is a **formal contract between a service provider** (e.g., AWS, Google Cloud, Microsoft Azure) **and a customer** that **defines the expected level of service reliability, availability, and performance**. If the provider fails to meet the SLA, the customer may receive compensation (e.g., service credits or refunds).

Avail. (%)	Downtime/Year	Use Case
99.90%	≈ 8.8 hours	Single-instance VMs with premium storage
99.95%	≈ 4.4 hours	Availability Sets (AS) within a datacenter
99.99%	≈ 1 hour	Availability Zones (AZs) for redundancy

Table 2: Availability Targets and Downtime Limits.

The **higher the availability**, the **less downtime is tolerated**, requiring advanced fault-tolerance strategies.

### 2.1.1.6 Architectural Overview of WSCs

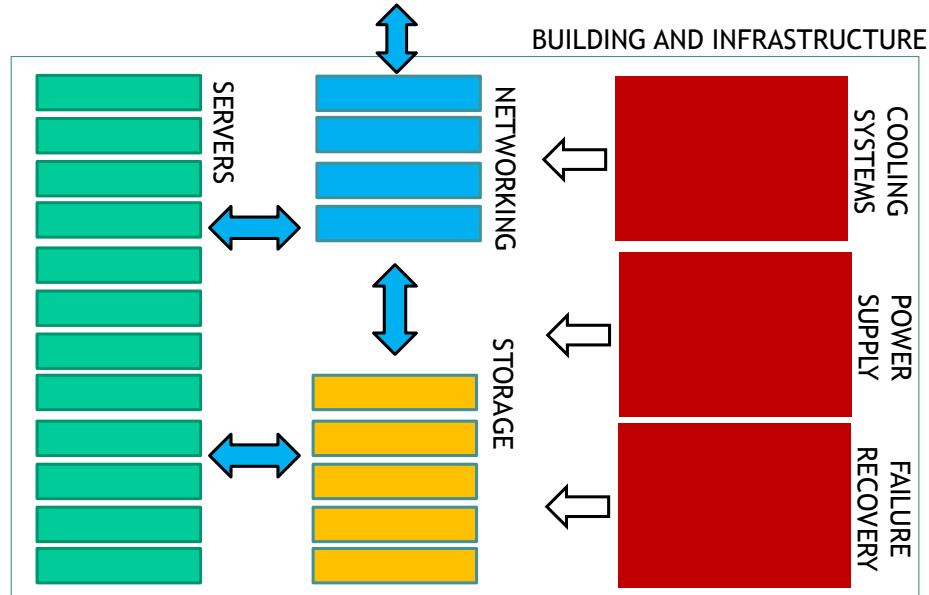


Figure 3: Architectural overview of Warehouse-Scale Computing.

The **architecture** of Warehouse-Scale Computers (WSCs) is **designed to handle massive-scale computing workloads** by integrating computation, storage, networking, power management, and infrastructure into a unified system. While specific implementations may vary, the overall architectural organization remains relatively stable, focusing on scalability, efficiency, and resilience.

A WSC is more than just a collection of servers; it is a tightly integrated computing environment that requires specialized hardware, networking, and infrastructure. Its architecture consists of several key components:

- **Servers (Compute Layer)**, section 2.2.1, page 25.
  - Primary processing units handling computation.
  - A wide variety of server configurations:
    - \* **General-purpose CPUs** (Intel, AMD) for standard workloads.
    - \* **Accelerators** (GPUs, TPUs, FPGAs) for AI, ML, and specialized computations.
    - \* **Local storage options** (HDD, SSD) for high-speed data access.
  - Servers are arranged in racks, interconnected through a high-speed network.

Servers, which host application workloads and services, are the **basic building blocks** of WSCs.

- **Storage Systems**, section 2.2.2, page 34.
  - **Data storage is fundamental** to WSCs, as they host large-scale datasets and distributed applications.
  - Three primary **types of storage** (section 2.2.2.5, page 80):
    1. **Direct Attached Storage (DAS)**, local storage connected to individual servers.
    2. **Network Attached Storage (NAS)**, centralized storage accessible over a network.
    3. **Storage Area Networks (SAN)**, high-performance, block-level storage for large-scale applications.
  - **Storage technologies** include:
    1. **Hard Disk Drives (HDDs)** (section 2.2.2.2, page 39), used for cost-efficient, high-capacity storage.
    2. **Solid-State Drives (SSDs)** (section 2.2.2.3, page 45), faster, but more expensive, used for high-speed access.
    3. **Tape Storage**, rare but still used for archival data and backups.

**Storage is managed through distributed file systems and RAID configurations** for redundancy and fault tolerance.

- **Networking Infrastructure**, section 2.2.3, page 83.
  - The Datacenter Network (DCN) **enables communication** between **servers, storage, and external users**.
  - Key network components:
    - \* **Switches & routers**, direct data traffic within and outside the WSC.
    - \* **Load balancers**, distribute incoming workloads efficiently across servers.
    - \* **Firewalls & security gateways**, protect against cyber threats.
    - \* **DNS/DHCP servers**, manage internal IP addressing and service discovery.
  - Low-latency, high-bandwidth connections are crucial for large-scale data processing.

**Networking is the backbone** that ensures seamless data exchange between different parts of the WSC.

- **Cooling Systems & Environmental Control**, section 2.3.1, page 104.
  - WSCs generate **massive amounts of heat**, requiring **advanced cooling solutions**:
    - \* **Air cooling**, traditional method using fans and airflow management.
    - \* **Liquid cooling**, more efficient, uses liquid-cooled pipes to dissipate heat.
    - \* **Immersion cooling**, servers are submerged in non-conductive liquid for superior heat dissipation.

**Cooling solutions are essential** for optimizing energy efficiency and maintaining server performance.

- **Power Supply & Energy Management**, section 2.3.2, page 107.
  - WSCs consume enormous amounts of power, requiring dedicated energy management systems:
    - \* Datacenters can consume up to 650 MW (equivalent to 100,000 or more households).
    - \* Redundant power supplies ensure uptime in case of power failures.
    - \* Renewable energy sources (solar, wind) are increasingly used to reduce environmental impact.
  - Uninterruptible Power Supplies (UPS) & Backup Generators prevent downtime.

**Power infrastructure is designed for high efficiency and reliability**, ensuring continuous operation.

- **Failure Recovery & Fault Tolerance**
  - High availability (99.99%) is a core requirement for WSCs.
  - Key failure management strategies:
    - \* Redundant hardware and storage replication to prevent data loss.
    - \* Automated failure detection and mitigation through AI-driven monitoring.
    - \* Multi-region and multi-zone deployments for disaster recovery.

**Resilience is built into every layer** to minimize disruptions and downtime.

## 2.2 Node-level

### 2.2.1 Server (computation, HW accelerators)

A **Server** is a computing system designed to manage, process, and deliver data or services to other computers (clients) over a network. In the context of datacenters and Warehouse-Scale Computers (WSCs), servers are the **atomic units of computation**, the fundamental building blocks of the entire system architecture.

Though **conceptually similar to a desktop PC**, servers **differ** in critical ways:

- They are **significantly more powerful**, scalable, and modular.
- They are designed for **continuous operation**, high availability, and **dense physical packaging** within a rack structure.

Servers in modern datacenters must balance **performance**, **density**, **power efficiency**, and **maintainability**.

### ≡ Server Types

**Server form** factors **define how** servers are **physically organized** and **deployed** in datacenter environments. There are three principal types:

1. **Tower Servers** (section 2.2.1.1, page 27). Resemble traditional desktop PCs. They are ideal for small-scale deployments or low-density use cases.
  - ✓ **Pros:** Easy to upgrade, good cooling, low cost.
  - ✗ **Cons:** Large footprint, not optimized for rack deployment.
2. **Rack Servers** (section 2.2.1.2, page 28). Designed to slide **into a rack** (standardized shelves) in units (U); e.g., 1U = 1.75 inches. It is the most common server format in datacenters.
  - ✓ **Pros:** High compute density, easy to cable and scale.
  - ✗ **Cons:** Requires dedicated infrastructure (rack, cooling, power).
3. **Blade Servers** (section 2.2.1.3, page 30). Extremely compact and multiple blades share power, cooling, and networking through a **blade enclosure**. It is excellent for environments where space and energy are at a premium.
  - ✓ **Pros:** Highest density and modularity, centralized management.
  - ✗ **Cons:** Higher initial cost, vendor lock-in, increased heat density.

## ❖ Server Architecture

Servers are typically **integrated into a tray or blade enclosure**, which contains:

- **Motherboard**: The central PCB that **interconnects all components**.
- **Chipset**: **Manages data flow** between CPU, RAM, storage, and peripherals.
- **Expansion slots**: For GPUs, network cards, and other **accelerators**.

Servers in WSCs tend to **use homogeneous hardware/software platforms** to simplify large-scale orchestration and maintenance.

## ■ Server Architecture

The **Motherboard** acts as a **central nervous system for the server**, it hosts:

- **CPU sockets** (e.g., up to 2 for dual Xeon systems)
- **DIMM slots** for RAM
- **Storage connectors** (e.g., SATA, NVMe)
- **NIC slots** (Network Interface Cards)

This level of configurability allows tailoring servers for compute-heavy, memory-bound, or I/O-intensive applications.

### 2.2.1.1 Tower Server

A **Tower Server** is a type of server designed in a vertical, standalone chassis that closely resembles a **standard tower desktop computer**. Unlike blade or rack servers, which are designed for high-density environments, tower servers prioritize **simplicity and accessibility**, often at the cost of physical footprint.

- **Structure:** Independent, **vertical** case (not meant for rack mounting).
- **Deployment:** Common in small businesses, branch offices, or settings where only a few servers are needed.
- **Internal layout:** Lots of **space for expansion components** like disks or PCIe cards.

#### ✓ Advantages

- ✓ **Scalability & Ease of Upgrade.** Easy to open and **upgrade**, users can add storage, memory, or cards as needed.
- ✓ **Cost-Effective.** Usually the **cheapest server type**, suitable for budget-constrained environments.
- ✓ **Easy Cooling.** Due to **low component density**, natural airflow is often sufficient. Less need for specialized cooling systems.

#### ✗ Limitations

- ✗ **Space Consumption** Tower servers consume **significant physical space** and don't scale well in quantity.
- ✗ **Basic Performance** They usually **offer lower performance and redundancy** compared to enterprise-grade rack or blade servers.
- ✗ **Cable Management** Not ideal for structured environments, cables can become messy and hard to manage.

### 2.2.1.2 Rack Servers

A **Rack Server** is a server built specifically to be **mounted vertically in standardized racks**, which are metallic shelves designed to hold multiple servers and IT components. Rack servers are the **default choice** in medium to large-scale datacenters, balancing compute density, modularity, and serviceability.

#### ■ Physical Standardization

- Servers are stored in racks which follow a global standard:
  - 1U (**Rack Unit**) = 1.75 inches (44.45 mm) in height.
  - Servers may come in 1U, 2U, 4U, up to 10U formats depending on power and component density.
- Racks also house other components: networking switches, storage arrays, power distribution units (PDUs), and cooling units.

This **standardization allows for efficient vertical stacking** of servers, optimizing physical space and simplifying cabling.

#### ■ Racks as More Than Just Shelves

A rack is not just a mechanical holder, it is **part of the power, networking, and management infrastructure of the datacenter**:

- **Power Infrastructure:**
  - Shared power distribution units.
  - Battery backup (UPS).
  - Power conversion units.
- **Networking:**
  - Top of Rack (ToR) switches connect all servers in the rack to the datacenter network fabric.
  - Simplifies cabling and reduces latency.
- **Cooling:** designed for front-to-back airflow, aligned with datacenter cooling strategy (e.g., cold aisle containment).
- **Dimensions** can vary, but the classic rack is 19 inches wide and up to 48 inches deep.

### ✓ Advantages

- ✓ **Modularity:** Individual servers can be **hot-swapped**, upgraded, or replaced **without disrupting others**.
- ✓ **Failure Containment:** Easy to **isolate and service a failed node** without bringing down the system.
- ✓ **Cable Management:** Organized by rear/backplanes or Top-of-Rack (ToR) switches.
- ✓ **Cost-Efficient Scaling:** **Scales vertically** at relatively lower incremental cost compared to other formats.

### ✗ Challenges

- ✗ **High Power Demand:** Higher component density requires more energy and advanced cooling systems.
- ✗ **Thermal Hotspots:** Tight stacking can cause **hot zones**, especially with accelerator-heavy nodes.
- ✗ **Maintenance Overhead:** Large racks with tens of servers can become **complex to manage** physically as systems scale.

### 2.2.1.3 Blade Servers

**Blade Servers** represent the **most advanced evolution** in server form factors. They are designed to **maximize space efficiency** and **centralized manageability**, making them ideal for **large-scale enterprise datacenters** and **high-performance computing environments**.

A blade server is essentially a **stripped-down, ultra-thin server board** (the “blade”) that fits into a blade enclosure, a shared chassis providing:

- Power
- Cooling
- Networking
- Centralized management

The enclosure conforms to the same **rack unit standard (U)**, allowing it to integrate seamlessly with existing rack infrastructure. We can think of a blade system as a server equivalent of a modular bookshelf, where each “book” is a full server, and the “bookshelf” provides shared power, ventilation, and data connectivity.

#### ✓ Advantages

- ✓ **Compactness & Density:** The **smallest physical form factor** among all servers, allowing high-density deployments within a minimal footprint.
- ✓ **Minimal Cabling:** The **shared backplane** removes the need for complex cabling; power and network connections are centralized.
- ✓ **Centralized Management:** Blade systems typically include **unified management interfaces** (e.g., iLO, iDRAC) to monitor and configure blades collectively.
- ✓ **Scalability & Reliability:** New blades can be added with minimal disruption; enclosures support **load balancing** and **failover mechanisms**.
- ✓ **Uniform Infrastructure:** Simplifies deployment with **shared cooling**, **network fabrics**, and **power redundancy**.

#### ✗ Disadvantages

- ✗ **High Initial Cost:** Blade enclosures and vendor-specific blades often demand **significant upfront investment**.
- ✗ **Vendor Lock-In:** Typically, only blades from the **same manufacturer** (e.g., HPE, Dell, Cisco) **are compatible** with a given enclosure.
- ✗ **Thermal Density:** The compact form causes **higher heat output per rack unit**, requiring advanced HVAC design and monitoring.
- ✗ **Limited Flexibility:** While modular, blade systems trade off flexibility for density, upgrades and replacements may be **constrained by the enclosure's architecture**.

### 2.2.1.4 Machine Learning

While Moore's Law historically predicted that transistor density would double every 18-24 months, the **growth in ML model complexity** has surpassed this pace. Since 2013, compute demand for AI training has doubled approximately **every 3.5 months**. This exponential curve far exceeds the capabilities of general-purpose CPUs, triggering a renaissance in specialized hardware.

#### ❷ What is Machine Learning?

At its core, **Machine Learning (ML)** refers to **computational methods** that enable systems to **learn from data** without being explicitly programmed. Rather than defining rules manually, ML allows a system to build a model from **patterns observed in examples**.

In supervised learning:

- A system learns a **target function**  $y = f(x)$  that **maps inputs** (features) **to outputs** (labels).
- This is **done using a training dataset**  $(x_1, y_1), \dots, (x_N, y_N)$ , and the model is later tested on unseen inputs.

Applications include: classification (e.g., cat vs. dog), regression (e.g., predicting flight delays), image recognition, speech synthesis, fraud detection, etc.

#### ❸ Artificial Neural Networks (ANNs)

**Artificial Neural Networks (ANNs)** are a **subset of ML models** inspired by the human brain. They consist of **layers of interconnected neurons**, including:

- **Input layer**: receives the data
- **Hidden layers**: transform data using weighted functions and nonlinear activations
- **Output layer**: produces the prediction

The key learning mechanisms are:

- **Backpropagation**: adjusts weights based on the error between prediction and actual target.
- **Gradient descent**: optimizes the model parameters iteratively.

#### ❹ Hardware Acceleration: Why ML Needs More Than CPUs

Modern ML, particularly **deep learning**, is computationally expensive. Training models like GPT or ResNet involves processing **billions of parameters** across massive datasets. To meet these demands, **Warehouse-Scale Computers (WSCs)** integrate **specialized accelerators such as**:

- **Graphics Processing Units (GPUs).** GPUs are highly parallel processors originally designed for graphics rendering but are now extensively used for ML because they:

- Execute the **same operation across many data elements in parallel** (SIMD).
- Accelerate matrix operations central to deep learning.
- Support ML frameworks via CUDA, OpenCL, OpenMP, SYCL, etc.

GPUs are often housed in **PCIe-attached trays**, interconnected via NVLink or NVSwitch for ultra-fast data exchange.

Distributed training across multiple GPUs requires **low-latency, high-bandwidth interconnects**. Performance can also be bottlenecked by slowest learner or network synchronization delays.

- **Tensor Processing Units (TPUs).** Developed by Google, TPUs are **domain-specific architectures** designed **specifically for ML workloads**. TPU generations:

- **TPUv1:** Inference-only, connected via PCIe.
- **TPUv2:** Supports both training and inference; includes MXUs (matrix units) and high-bandwidth memory (HBM).
- **TPUv3:** Liquid-cooled, supercomputing-class performance. Up to 100 PFLOPS per pod.
- **TPUv4/TPUv5:**
  - \* v4 pod: 4096 devices
  - \* v5e: cost-efficient variant
  - \* v5p: high-performance variant scalable to 8000+ devices
  - \* Used in global data centers since 2023

A **TPU Pod** aggregates **hundreds of TPU cores with shared memory** and custom high-speed networks for massive parallelism.

- **Field-Programmable Gate Arrays (FPGAs).** FPGAs offer **customizable digital logic** that can be reprogrammed after manufacturing.

- Flexible hardware, can be reconfigured for different algorithms.
- Suitable for:
  - \* Network acceleration
  - \* Security tasks (e.g., encryption)
  - \* Data analytics
  - \* Specialized ML inference

For example, Microsoft Azure integrates FPGAs for infrastructure efficiency, lowering carbon footprint and improving hardware reuse.

Feature	GPU	TPU	FPGA
Purpose	General-purpose ML compute	ML-specific acceleration (esp. DL)	Flexible, reconfigurable hardware
Programmability	CUDA, OpenCL, etc.	TensorFlow, PyTorch (high-level)	VHDL, Verilog (low-level, HDL)
Flexibility	High	Medium (optimized for tensors)	Very high (reprogrammable)
Efficiency	Good	Excellent (for tensor ops)	Excellent (for specific pipelines)
Use Case	Training + Inference	Training + Inference	Offloading, network, analytics

Table 3: Summary: GPU vs TPU vs FPGA.

	✓ Advantages	✗ Disadvantages
<b>CPU</b>	<ul style="list-style-type: none"> <li>✓ Easy to be programmed and support any programming framework.</li> <li>✓ Fast design space exploration and run your applications.</li> </ul>	<ul style="list-style-type: none"> <li>✗ Suited only for simple AI models that do not take long to train and for small models with small training set.</li> </ul>
<b>GPU</b>	<ul style="list-style-type: none"> <li>✓ Ideal for applications in which data need to be processed in parallel like the pixels of images or videos.</li> </ul>	<ul style="list-style-type: none"> <li>✗ Programmed in languages like CUDA and OpenCL and therefore provide limited flexibility compared to CPUs.</li> </ul>
<b>TPU</b>	<ul style="list-style-type: none"> <li>✓ Very fast at performing dense vector and matrix computations and are specialized on running very fast programming based on Tensorflow.</li> </ul>	<ul style="list-style-type: none"> <li>✗ For applications and models based on the Tensorflow.</li> <li>✗ Lower flexibility compared to CPUs and GPUs.</li> </ul>
<b>FPGA</b>	<ul style="list-style-type: none"> <li>✓ Higher performance, lower cost and lower power consumption compared to other options like CPUs and GPU.</li> </ul>	<ul style="list-style-type: none"> <li>✗ Programmed using OpenCL and High-Level Synthesis (HLS).</li> <li>✗ Limited flexibility compared to other platforms.</li> </ul>

Table 4: Comparison of CPU, GPU, TPU and FPGA.

### 2.2.2 Storage (type, technology)

Data has significantly grown in the last few years due to sensors, industry 4.0, AI, etc. The growth favours the **centralized storage strategy** that is focused on the following:

- Limiting redundant data
- Automatizing replication and backup
- Reducing management costs

The *storage technologies* are many. One of the oldest but still used is the **Hard Disk Drive (HDD)**, a magnetic disk with mechanical interactions. However, the mechanical nature of HDDs imposes physical limits on access speed and reliability. In contrast, **Solid-State Drive (SSD)**, which lack moving parts and are built using NAND flash memory, offer significantly faster access times and better durability. The **Non-Volatile Memory express (NVMe)** also exists, which is the **latest industry standard** for running PCIe<sup>2</sup> SSDs.

In terms of cost per terabyte, NVMe drives are currently the most expensive (typically €100-200 for 1 TB), followed by SSDs (€70-100), while HDDs remain the most economical option (€40-60). This price-performance hierarchy makes hybrid storage architectures (HDD + SSD) increasingly appealing:

- A speed storage technology (**SSD or NVMe**) as **cache** and **several HDDs for storage**. It is a combination used by some servers: a small SSD with a large HDD to have a faster disk.
- Some HDD manufacturers produce Solid State Hybrid Disks (SSHD) that combine a small SSD with a large HDD in a single unit.

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<sup>2</sup>**PCIe (peripheral component interconnect express)**. is an interface standard for connecting high-speed components

### 2.2.2.1 Files

The operating system views the disk as a **flat collection of independently addressable data blocks**. Each **block** is assigned a unique **LBA (Logical Block Address)**, enabling efficient data referencing and organization. To streamline access and reduce management overhead, the **OS typically groups these blocks into clusters**, larger units that serve as the minimum granularity for disk I/O operations.

Clusters typically range in size from a single disk sector (512 bytes or 4 KB) up to 128 sectors (64 KB), depending on the file system configuration. Each cluster may store either:

- **File data.** The actual contents of user files.
- **Metadata.** System-level information necessary to support the file system,:
  - File and directory names
  - Folder hierarchies and symbolic links
  - Timestamps (creation, modification, access)
  - Ownership and access control data
  - **Links to the LBA where the file content can be located on the disk**

Consequently, the **disk space is divided into different cluster types** based on their purpose:

- Metadata:
  - **Fixed-position metadata clusters**, used to initialize and mount the file system
  - **Variable-position metadata clusters**, which manage directories and symbolic links
- **File data clusters**, containing the actual contents of files
- **Unused clusters**, which are free and available for future allocations

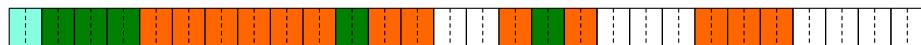


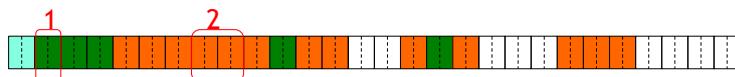
Figure 4: A cluster can be seen visually as an array. In this image, for example, we've shown three types of cluster: metadata fixed position (blue), metadata variable position (green), file data (orange), unused space (white).

The following explanation introduces some basic operations on the files to see what happens inside the disks.

- **File Reading**

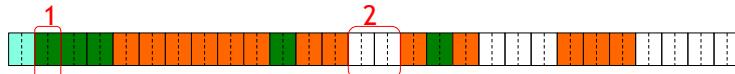
1. **Access the Metadata.** Before the system knows **where** the file is stored on disk, it must find information about the file, called metadata. This metadata is stored in **variable-position metadata clusters**. These clusters are not always in the same place on disk, they move and grow as the system evolves.
2. **Locate the File's Data Blocks (clusters)** and **Read the Actual Content**. Once the OS has the metadata, it now knows:
  - Which **Logical Block Addresses (LBAs)** contain the data.
  - **How many clusters need to be read** to get the full content.

It uses this information to issue **read commands** to the disk controller. Finally, the **disk accesses the physical sectors or clusters** indicated by the LBAs and transfers that data into main memory (RAM).



- **File Writing**

1. **Access Metadata to Find Free Space.** The operating system first checks the file system's metadata to find a free area of disk space where it can store our new data.
2. Once free space is identified, the OS:
  - **Allocates** one or more clusters, depending on the file size
  - **Writes our data** into these clusters on the physical disk



Since the *file system can only access clusters*, the **actual space taken up by a file on a disk is always a multiple of the cluster size**. Given:

- $s$ , the *file size*
- $c$ , the *cluster size*

Then the **actual size on the disk  $a$**  can be calculated as:

$$a = \left\lceil \frac{s}{c} \right\rceil \times c \quad (1)$$

Where ceil rounds a number up to the nearest integer. It's also possible to calculate the **amount of disk space wasted by organising the file into clusters (wasted disk space  $w$ )**:

$$w = a - s \quad (2)$$

A formal way to refer to wasted disk space is **internal fragmentation** of files.

### Example 4: internal fragmentation

- File size: 27 byte
- Cluster size: 8 byte

The *actual size* on the disk is:

$$a = \left\lceil \frac{27}{8} \right\rceil \cdot 8 = \lceil 3.375 \rceil \cdot 8 = 4 \cdot 8 = 32 \text{ byte}$$

And the internal fragmentation  $w$  is:

$$w = 32 - 27 = 5 \text{ byte}$$

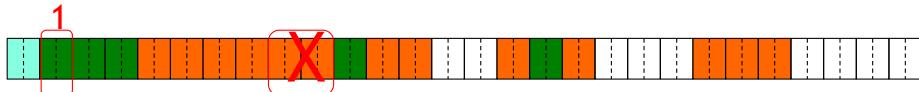
- **Deleting**

1. The file system updates its metadata structures to:

- Remove the file name from the directory
- Mark the clusters where the file was stored as free or available
- Optionally, update timestamps or record deletion events

**⚠ Importantly: The data itself is not erased at this stage.**

The actual bytes remain on disk until they are overwritten by another file.



- **External fragmentation**. It happens when there are enough free clusters on the disk to store a file, but not all together (not contiguous). So, when the system tries to write a large file, it must split it into smaller parts and place them in different, scattered locations on the disk.

**💡 Why does this happen?** Over time, as files are created, deleted, resized, or moved, the disk becomes less organized. Clusters are freed in different spots, and the available space is no longer one big continuous area. So:

- A new file cannot fit in one continuous chunk.
- The OS stores it in multiple non-adjacent clusters.

This is called **external fragmentation** because: the fragmentation is not inside the file itself, but in the way its data is laid out externally across the disk.

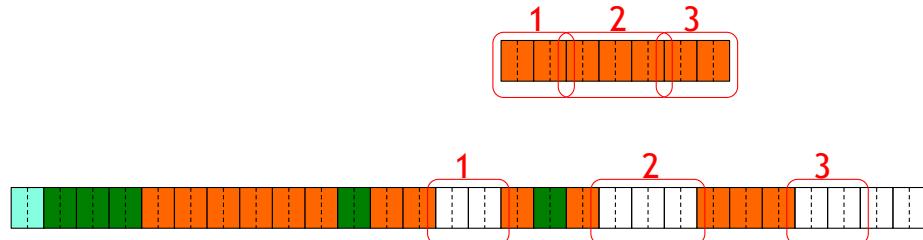


Figure 5: Each number (1, 2, 3) corresponds to a portion (chunk) of a file. A file that was meant to be stored as [1] [2] [3] (contiguously) has instead been broken into parts and stored in a scattered layout across different disk clusters. This situation represents **external fragmentation**, where the file system could not find a large enough continuous block of free space to store the file all together.

### 2.2.2.2 HDD

A **Hard Disk Drive (HDD)** is a **data storage device that uses rotating disks (platters) coated with magnetic material.**

**Data is read randomly**, meaning individual data blocks can be stored or retrieved in any order rather than sequentially.

An HDD consists of one or more rigid (*hard*) rotating disks (platters) with magnetic heads arranged on a moving actuator arm to read and write data to the surfaces.

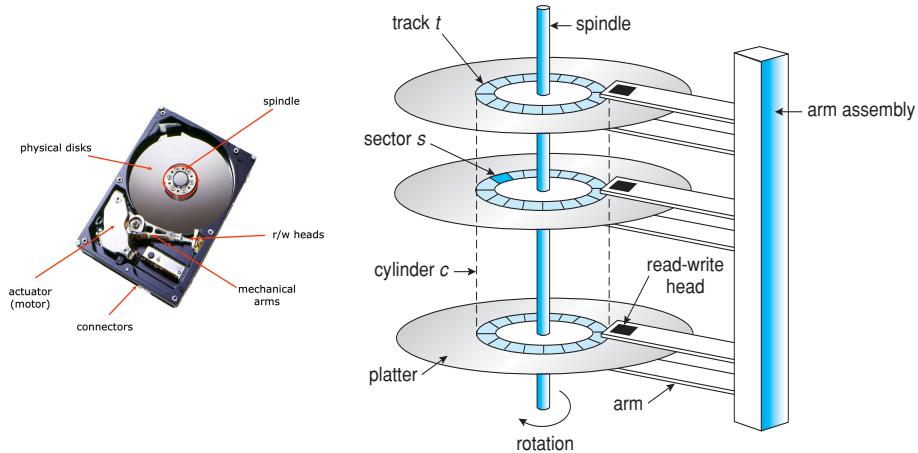


Figure 6: Hard Drive Disk anatomy.

Externally, hard drives expose a large number of **sectors** (blocks):

- Typically, 512 or 4096 bytes.
- Individual **sector writes are atomic**.
- Multiple sectors write it may be interrupted (**torn write**<sup>3</sup>).

The geometry of the drive:

- The sectors are arranged into **tracks**.
- A **cylinder** is a particular track on multiple platters.
- Tracks are arranged in concentric circles on **platters**.
- A disk may have multiple double-sided platters.

The **driver motor spins the platters at a constant rate**, measured in **Revolutions Per Minute (RPM)**.

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<sup>3</sup>Torn writes happen when only part of a multi-sector update is written successfully to disk.

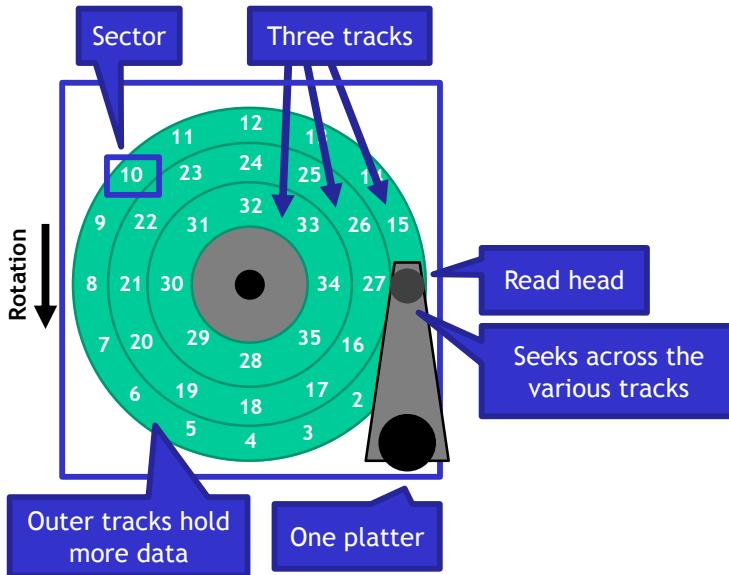


Figure 7: Example of HDD geometry.

The geometry of an HDD refers to the **physical layout** of data on the surface of a spinning disk. Figure 7 shows this:

- **One Platter.** The circular surface shown is a platter, which is a rigid, magnetic-coated disk where data is stored. Most HDDs have multiple platters stacked vertically, but here we focus on one for simplicity.
- **Tracks.** The platter is divided into concentric circles called tracks. Each track is a circular path that the read/write head can follow. In the figure 7, we see three tracks, each larger than the last, moving outward from the center.
- **Sectors.** Each track is divided into pie-like slices called sectors. A sector is the smallest physical unit that can be read or written on a disk (typically 512 bytes or 4 KB). The numbers (0 to 35) represent sector identifiers along the circular tracks. Note how the outer tracks contain more sectors because they have a larger circumference, so they can physically hold more data; this is known as Zone Bit Recording (ZBR), not mentioned in the course.
- **Read/Write head.** The read head is shown floating above the platter. It moves radially across the surface to switch from one track to another (this is called seek). Once on the correct track, the head waits for the desired sector to rotate beneath it (rotational latency), and then it reads/writes data.
- **Rotation and seek behavior.** The platter spins at high speed (e.g., 7200 RPM). As it rotates, the sectors pass under the stationary head. Data is accessed when the correct sector aligns with the head.

### ⚠ Types of Delay in disk Access

When a file is read from or written to a disk, especially an HDD, the total time taken is influenced by several delays. These are due to the mechanical and electronic processes involved in locating and transferring the data. Exists **four types of delay**:

- **Rotational Delay** (a.k.a. **Rotational Latency**) is the **time needed for the disk to rotate so that the desired sector aligns with the read/write head**. It depends on the RPM (Revolutions Per Minute) of the disk.
- **Seek Delay** is the **delay caused by the mechanical movement of the read/write head as it travels from one track to another** on a spinning disk. It is the dominant mechanical delay in many HDD operations, especially for random access patterns.
- **How it works.** Moving the head involves a sequence of physical phases:
  1. **Acceleration:** the actuator moves the head out of its resting position.
  2. **Coasting:** the head glides at a constant speed (if the distance is large).
  3. **Deceleration:** the actuator slows down to avoid overshooting.
  4. **Settling:** a short pause to stabilize the head at the desired track.
- **Transfer time** is the **time required to actually move the data**, once the head is correctly positioned over the desired sector. It's the final step in the I/O pipeline, where data is **read from or written to** the magnetic surface.

### ❓ What affects transfer time?

1. **Rotational Speed (RPM)**, determines how quickly sectors pass under the head.
2. **Data density**, more tightly packed data, more data per second read.
3. **Size of the request**, reading more data takes more time.

Even though it's much shorter than seek or rotation delays, **transfer time scales with data size**. For large sequential reads, transfer time becomes more relevant, especially when seek and rotation delays are minimized.

- **Controller Overhead** is the **non-mechanical delay introduced by the disk controller**, which is the hardware interface between the OS and the physical disk. It involves:
  - **Buffer management:** transferring data between disk and system memory (often using DMA).
  - **Interrupt processing:** informing the OS when the I/O operation is complete.
  - **Command translation:** converting OS-level I/O requests into device specific actions (e.g., SATA/NVMe commands).

- **Scheduling and queueing:** organize I/O operations for efficiency.

To see how these delays are calculated, we suggest you refer to the performance section 4.2, about HDD 4.2.1, page 155.

## Cache

Hard Disk Drives (HDDs) are mechanical devices, and their performance is often limited by seek times and rotational latency. To partially overcome these limits, **many HDDs integrate a small (8, 16, 32 MB) amount of fast memory** (RAM) on the controller board, this is the **cache** or **track buffer**. The key functions of HDD cache are:

1. **Read Caching.** When the disk reads a block from the platter, it may also load **adjacent blocks** into the cache, expecting that they might be requested next (a technique known as **read-ahead**).

### Pros

- ✓ If the next read request is for cached data, the disk can respond **instantly** from fast RAM.
- ✓ This avoids mechanical movement and **cuts seek and rotational delays**.
- ✓ Very effective for **sequential reads**.

2. **Write Caching.** There are two strategies here:

- (a) **Write-Back Cache** (Faster, Riskier). The HDD **reports the completion of the write operation** as soon as the data is in the cache, **before it is actually written to the platter**. Actual writing to disk happens later, in the background.

### Pros

- ✓ Faster perceived performance
- ✓ Useful in workloads with many small writes

### Cons

- ✗ If power is lost before the data is flushed to disk, the **data is lost**. It is a **file system corruption risk!**
- ✗ This is why it's considered **dangerous in critical systems** without battery backup or UPS.

- (b) **Write-Through Cache** (Safer, Slower). The HDD only reports the completion of the write operation **after the data has been fully written to disk**. Safer, but **slower**, since the OS must wait for the mechanical operation to finish.

3. Hybrid Cache: **Flash-Based Caching.** Some modern HDDs integrate **small flash memory** used for **persistent caching**:

- Data stays even if the power goes out.
- Combines the speed of SSD with the capacity of HDD.
- Great for frequently accessed blocks (e.g., boot files, apps).

## ✖ Disk Scheduling

While **caching** helps improve disk performance, it **doesn't eliminate the delays caused by seek and rotational latency**, especially during random access patterns. In systems with many I/O requests (like in a database or OS kernel), it's crucial to **choose the right order** to process requests to **minimize head movement**. This is where disk scheduling algorithms come in.

Instead of serving I/O requests in the order they arrive, the **disk controller (or OS)** can render them to improve efficiency. It is possible:

- Because every **disk request** includes the **target position** (i.e., the cylinder/track).
- So we can **estimate the cost (seek time)** of each request and choose the most efficient order.

Common disk scheduling algorithms are:

### 1. First Come, First Serve (FCFC) (the worst)

**✖ How it works?** Requests are handled in the **order they arrive**.  
No optimization, simple queue processing.

**✓ Pros**

- ✓ (Naive) Easy to implement

**✗ Cons**

- ✗ Can lead to **long seek distances** (i.e., inefficient head movement)

### 2. Shortest Seek Time First (SSTF) (great performance, but watch out for starvation)

**✖ How it works?** Always serve the request **closest to the current head position**.

**✓ Pros**

- ✓ Minimizes **total head movement**.
- ✓ Efficient in practice.

**✗ Cons**

- ✗ Can lead to **starvation**: distant requests may never be served if new close requests keep arriving.

### 3. SCAN (Elevator Algorithm) (good performance as SSTF, but fairer)

**✖ How it works?** The head **moves in one direction** (like an elevator), serving all requests in that direction. When it reaches the end, it **reverses direction**.

**✓ Pros**

- ✓ Good worst-case behavior.
- ✓ **No starvation**, every request will eventually be served.

**✗ Cons**

✗ Requests at **edges** of the disk may have **longer wait times**.

4. **Circular SCAN (C-SCAN)** (fair, but less efficient than SCAN in some cases)

**✗ How it works?** Like SCAN, but head **only moves in one direction**. When it reaches the end, it **jumps back** to the beginning (like a circular elevator).

**✓ Pros**

✓ More **uniform wait time** for all requests.

**✗ Cons**

✗ Longer total movement (because of the jump).

5. **C-LOOK** (smart compromise between performance and fairness)

**✗ How it works?** Like C-SCAN, but instead of going to the physical end of the disk, the head **only goes as far as the last request in that direction**, then **jumps back to the smallest request**.

**✓ Pros**

✓ **Saves movement** compared to full C-SCAN.

✓ Still **avoids starvation**.

Algorithm	Fairness	Risk of Starvation	Strategy
FCFS	✓ Yes	✗ None	Serve in arrival order
SSTF	✗ No	⚠ Possible	Serve closest request
SCAN	✓ Yes	✗ None	Elevator (back & forth)
C-SCAN	✓ Yes	✗ None	One-direction sweep (circular)
C-LOOK	✓ Yes	✗ None	One-direction sweep (limited)

Table 5: Scheduling Algorithms.

### 2.2.2.3 SSD

A **Solid-State Drive (SSD)** is a **non-volatile storage device** that retains data without power. Unlike traditional Hard Disk Drives (HDDs), an SSD has **no mechanical parts**, *no spinning platters, no moving heads*. Internally, it's made of **transistors**, similar to those found in CPUs and RAM. It includes a **controller**, which **manages read/write operations**, wear leveling, garbage collection, and interface emulation. SSDs often adopt HDD-compatible interfaces (e.g., SATA, PCIe/NVMe) and form factors (2.5", M.2) for backward compatibility. Offers **higher performance** than HDDs, especially in **random access latency** and IOPS.

#### Flash Cell Technologies: Storing Bits in NAND

Modern SSDs use **NAND Flash Memory**, where data is stored in memory **cells**. Each cell can store one or more bits:

Cell Type	Bits per Cell	Characteristics
SLC	1	Fastest, most durable (up to 100k cycles), expensive
MLC	2	Slower than SLC, less durable, more dense
TLC	3	Used in most consumer SSDs; cheaper
QLC	4	High density, lower endurance
PLC	5	Experimental/extremely high density, low endurance

Increasing the number of **bits per cell** improves **capacity and cost-efficiency**, but reduces **endurance** and **performance**. Each cell type requires more precise voltage thresholds and incurs **more error correction and wear**.

#### Internal Organization

Solid-State Drives are built on NAND flash memory, which is **internally structured in a hierarchical manner** to optimize storage density and access efficiency.

- **Cell**: Basic storage unit (SLC, MLC, TLC, etc.) storing bits via trapped electrons.

- **Page**: The **smallest unit that can be read or written**. Typically 4-16 KB.

Pages can be:

- ✓ **Valid (In-use)**, contain active, readable data.
- ✗ **Dirty (Invalid)**, hold obsolete or overwritten data.
  - **Empty (Erased)**, ready to be programmed (written).

- **Block**: The **smallest unit that can be erased**. Usually contains 64-256 pages.

A block might have a capacity of 128-256 KB, composed of many smaller pages. Each **page** maps to a **Logical Block Address (LBA)** visible to the OS.

### Deepening: Logical Block Address (LBA)

The **Logical Block Address (LBA)** is a key abstraction used by operating systems and file systems to refer to storage locations on a disk (HDD or SSD) in a simple, sequential manner.

**LBA is an index number** that uniquely identifies a fixed-size block of data (typically 512 bytes or 4 KB) on a storage device. It **hides the physical layout** of the drive (cylinders, heads, sectors) and presents a **flat address space** to the OS.

*How does it work with SSDs?* The OS issues read/write commands to specific LBA addresses. Internally, the SSD controller translates each LBA to a **physical location** in flash memory using a structure called the **Flash Translation Layer (FTL)**. This mapping is **dynamic** due to wear leveling, garbage collection, and bad block management.

In summary, the LBA is how the operating system sees the disk. Instead, the physical address is where the data actually resides inside the SSD.

Key operations are:

- **READ**: reads data from a **page**.
- **PROGRAM**: writes to a **page** (only if it's empty).
- **ERASE**: wipes an entire **block** (required before rewriting any page in that block).

The **important limitation** is that flash memory **cannot overwrite data in place**, we have to erase the whole block before reusing it. This lead to a **read-modify-erase-write cycle** even for simple updates.

### ⚠ Write Amplification Phenomenon

**Write Amplification** refers to the phenomenon where **the amount of actual data written to the NAND flash is greater than what the host system requested to write**.

② *Why does Write Amplification happen in SSDs?* It stems from the **erase-before-write constraint** of NAND flash memory:

1. **(Flash) Pages can only be written once**, and to change them, we must erase the **entire block** (which may contain many pages).
2. If we modify even a **small piece of data**, the SSD:
  - Allocates a new page for the updated data.
  - Marks the old page as invalid (dirty).
  - Eventually, **copies all valid pages** from a block, **erases the block**, and **rewrites it** (this is called **garbage collection**).

So a 4KB write might cause **hundreds of KBs** to be written internally!

### Example 5: Write Amplification

Given a hypothetical SSD:

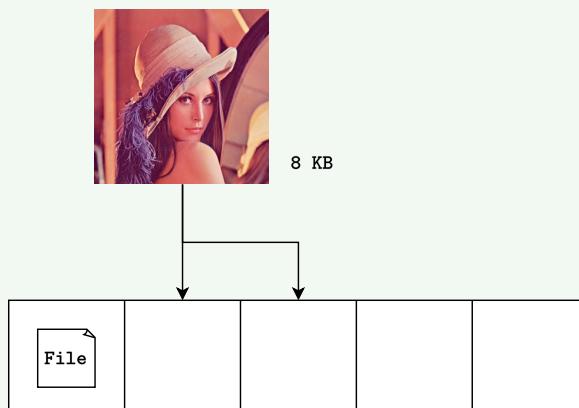
- Page Size: 4 KB
- Block Size: 5 Pages
- Drive Size: 1 Block
- Read Speed: 2 KB/s
- Write Speed: 1 KB/s

1. Write a 4 KB .txt file.

- One page used (page size  $\div$  file dimension);
- Time: 4 seconds (write speed  $\times$  file dimension,  $1 \text{ KB/s} \times 4 \text{ KB}$ ).

2. Write an 8 KB .png

- Takes 2 pages;
- There are 3 pages used in total;
- Time: 8 seconds.



3. Delete the 4 KB .txt file

- The first page is now **invalid** (dirty), but still **physically used**;
- The SSD cannot reuse it until the whole block is erased.

4. Write a 12 KB image

- OS sees “3 free pages”, but **only 2 are truly empty**;
- Can’t fit 12 KB in 2 empty pages.

*What happens internally?*

- (a) SSD reads the 8 KB of still-valid pages from NAND into a temporary cache.  
This step takes 4 seconds (size to read  $\div$  read speed).
- (b) Marks the 1st page (old .txt, step 1) as discarded.
- (c) Places the new 12 KB into the cache.
- (d) **Erases the entire 20 KB block** (this is mandatory before rewriting any page)
- (e) **Rewrites:**
  - 8 KB old data
  - 12 KB new data

This step takes 20 seconds to write to the NAND.

The OS thought it was just a 12 KB write and expected only 12 seconds. But the SSD actually wrote 20 KB and read 8 KB (24 seconds total). This is a case of write amplification caused by limited empty pages, erase-before-write constraint, and the need to preserve valid data.

A direct mapping between Logical and Physical pages is not feasible inside the SSD. Therefore, each SSD has an FTL component that makes the SSD *look like an HDD*.

### ⌚ Flash Translation Layer (FTL)

The **Flash Translation Layer (FTL)** is the hidden “brain” of an SSD, it **makes NAND flash usable in the same way as a traditional hard disk**, despite its very different constraints.

**Translates Logical Block Addresses (LBA)** (see page 46) from the operating system into actual **physical locations** in the NAND flash. Also, it makes the SSD behave like an HDD to the OS (abstracts away erase-before-write and wear issues).

⌚ **Why We Need Translation?** Direct LBA to physical mapping isn’t feasible because:

- ✗ Flash memory **can’t overwrite in-place** (must erase first)
- ✗ Pages are grouped into blocks and must be programmed **in order**.
- ✗ Flash memory blocks **wear out over time**, requiring wear balancing.

The FTL responsibilities are:

1. **Address Mapping.** Maintains a **mapping table**, logical to physical page. Supports dynamic remapping when data is updated (e.g., a page becomes dirty and is relocated).

2. **Log-Structured Writes.** Uses log-structured techniques: **writes go to the next available page** in an erased block. It ensures writes are sequential (within a block), reducing write amplification and improving performance.
3. **Garbage Collection.** Identifies blocks full of **invalid/dirty pages**. Reads out remaining valid pages, erases the block, and rewrites valid data + new data elsewhere. Necessary to free up space for future writes.
4. **Wear Leveling.** Flash cells can only endure a limited number of erases. FTL spreads out writes across all blocks to **prevent early death** of heavily used regions.

#### Example 6: Log-Structured FTL

Setup:

- **Page size:** 4 KB
- **Block size:** 4 pages (total 16 KB per block)
- **Initial condition:** all pages are marked **INVALID**
- **Action:** perform a series of logical writes

Assume that a page size is 4 KB and a block consists of four pages. The write list is (**Write(pageNumber, value)**):

- **Write(100, a1)** → write value **a1** to logical page 100
- **Write(101, a2)** → write value **a2** to logical page 101
- **Write(2000, b1)** → write value **b1** to logical page 2000
- **Write(2001, b2)** → write value **b2** to logical page 2001
- **Write(100, c1)** → overwrite logical page 100 with value **c1**
- **Write(101, c2)** → overwrite logical page 101 with value **c2**

The steps are:

1. The initial state is with all pages marked as **INVALID(i)**:

Block:	0				1				2			
Page:	00	01	02	03	04	05	06	07	08	09	10	11
Content:	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]
State:	i	i	i	i	i	i	i	i	i	i	i	i

2. Erase block zero:

Block:	0				1				2			
Page:	00	01	02	03	04	05	06	07	08	09	10	11
Content:	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]
State:	E	E	E	E	i	i	i	i	i	i	i	i

3. Program pages in order and update mapping information (first `Write(100, a1)`):

Table: 100 → 0												Memory	
Block:	0				1				2				
Page:	00	01	02	03	04	05	06	07	08	09	10	11	Flash Chip
Content:	a1												
State:	V	E	E	E	i	i	i	i	i	i	i	i	

4. After performing four writes (`Write(100, a1)`, `Write(101, a2)`, `Write(2000, b1)`, `Write(2001, b2)`):

Table: 100 → 0 101 → 1 2000 → 2 2001 → 3												Memory	
Block:	0				1				2				
Page:	00	01	02	03	04	05	06	07	08	09	10	11	Flash Chip
Content:	a1	a2	b1	b2									
State:	V	V	V	V	i	i	i	i	i	i	i	i	

5. After updating 100 and 101:

Table: 100 → 4 101 → 5 2000 → 2 2001 → 3												Memory	
Block:	0				1				2				
Page:	00	01	02	03	04	05	06	07	08	09	10	11	Flash Chip
Content:	a1	a2	b1	b2	c1	c2							
State:	V	V	V	V	V	V	E	E	i	i	i	i	

## ❷ Why Garbage Collection Exists

In SSDs, data cannot be updated in place, when a page is modified:

- The **old version becomes obsolete** (marked *invalid*).
- The **new version** is written to a **fresh page**.
- Over time, blocks fill with **invalid pages**, this is called *garbage*.

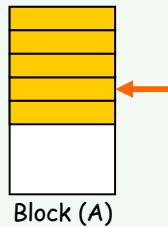
**Garbage Collection (GC)** is the process of **reclaiming space** by **erasing blocks that contain invalid pages**. It works like this:

1. **Identify a block** that has invalid (dirty) pages.
2. **Copy** any still-valid pages into a new block.
3. **Erase** the **original block** completely (erasing works only at block granularity).
4. **Update** the **mapping table** to reflect new page locations.

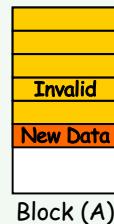
**Example 7: how garbage collection works**

The steps are:

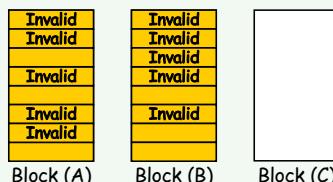
1. Update request for existing data:



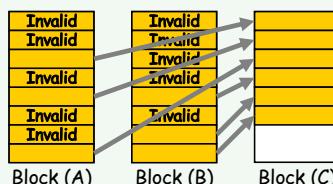
2. Find a free page, and save the new data:



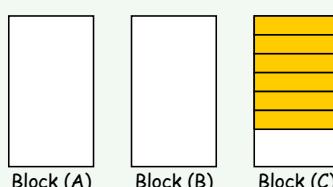
3. This scenario may continue until there are not enough free blocks:



4. Collect valid pages into a free block:



5. Update the map table and erase invalid (obsolete) blocks:



### ⚠ Three Major Problems of SSD Architecture

1. **Garbage Collection Is Expensive.** Garbage collection (GC) in SSDs is **unavoidable** due to the nature of NAND flash memory: flash **cannot overwrite pages**, only erase entire blocks.

It is so expensive because it requires reading valid data (read cost), rewriting that data (write cost), and erasing entire blocks. If blocks are **partially valid**, even small updates can trigger **large internal data movement**. This leads to write amplification, effective write speed and wear on NAND cells.

The **more valid data** in a block, the **higher the cost** of GC.

- **Ideal case:** reclaim blocks with only invalid pages (no migration needed).
- **Realistic case:** migrate live data, high overhead.

### ✓ Mitigation Techniques

- **Overprovisioning.** Reserve extra flash capacity that the user can't see. More space, then delayed GC.
- **Background GC.** Perform GC during **idle periods** to avoid disrupting foreground writes.
- **Write buffering.** Use DRAM/SRAM to accumulate small writes and reduce fragmentation.
- **Hot/Cold Separation.** Store frequently updated data (hot) separately from rarely updated data (cold).

2. **The Ambiguity of Delete.** In traditional file systems (especially on HDDs), **deleting a file** simply:

- Removes the file's metadata (e.g., from the file system's directory tree).
- Does **not erase or inform the disk that the data blocks are invalid**.

This behavior is fine for HDDs, which can overwrite sectors anytime. But for SSDs, this **creates a serious mismatch**.

SSDs rely on Garbage Collection (GC) to free space. GC assumes that **only invalid pages** can be discarded. However:

- The SSD sees no distinction between “old” and “deleted” data unless explicitly told.
- So even **deleted files look valid** to the SSD.
- When GC runs, it **copies all pages** it believes to be valid, including junk!

This causes SSDs to waste time and NAND endurance **preserving deleted data**.

**✓ How to Fix it: TRIM / UNMAP.** Modern OSs and SSD interfaces support special commands: TRIM (SATA) and UNMAP (SCSI/NVMe).

These commands allow the **OS** to explicitly tell the **SSD**: these Logical Block Addresses (LBAs) are no longer valid, feel free to erase them.

3. **Mapping Table Size and FTL Scalability.** In an SSD, the **Flash Translation Layer (FTL)** maps: **Logical Block Addresses (LBAs)** from the **OS** to **physical flash pages**. This mapping is essential because:

- Flash memory can't overwrite in place
- Pages must be written sequentially
- Blocks must be erased before reuse

So the SSD keeps an **internal mapping table** to know where every logical page actually resides.

The mapping table grows proportionally with: **drive capacity**, and **granularity of mapping**.

#### ✓ FTL Strategies to Cope

- **Block-Level Mapping.** The FTL maps each **logical block number (LBN)** to a **physical block number (PBN)**. All pages within that block are assumed to map 1:1.

#### ✓ Pros

- \* **Very small mapping table**
- \* Efficient in **sequential-write** workloads (e.g. logging, archiving).

#### ✗ Cons

- \* **Terrible for random writes:** to update just 1 page, the entire block must be read, modified, erased, rewritten.
- \* Results in very **high write amplification**.

#### Example 8: Block Mapping

The first four writes:

- Write(2000, a)
- Write(2002, c)
- Write(2001, b)
- Write(2003, d)

Table: 500 → 0				Memory								Flash Chip
Block:	0	1	2	04	05	06	07	08	09	10	11	
Page:	00 01 02 03	04 05 06 07	08 09 10 11									
Content:	a b c d											
State:	V V V V	i i i i	i i i i									

And finally the last one:

- Write(2002, c')

Table: 500 → 4												Memory	
Block:	0				1				2				Flash Chip
Page:	00	01	02	03	04	05	06	07	08	09	10	11	
Content:	[ ]	[ ]	[ ]	[ ]	a	b	c'	d	[ ]	[ ]	[ ]		
State:	E	E	E	E	V	V	V	V	i	i	i		

- **Hybrid FTL**. Combine the best of Block-Level Mapping for most pages and use **Page-Level Mapping** (FTL maps each logical page number to a physical page number) for small updates. Often implemented using a **log block buffer**.

#### ✓ Pros

- \* Lower memory usage than pure page-level
- \* Lower write amplification than pure block-level

#### ✗ Cons

- \* More complex logic (copy-back handling, log merging)
- \* Still suffers from some write amplification during **log cleaning**

### Example 9: Hybrid Mapping

Let's suppose the following sequence:

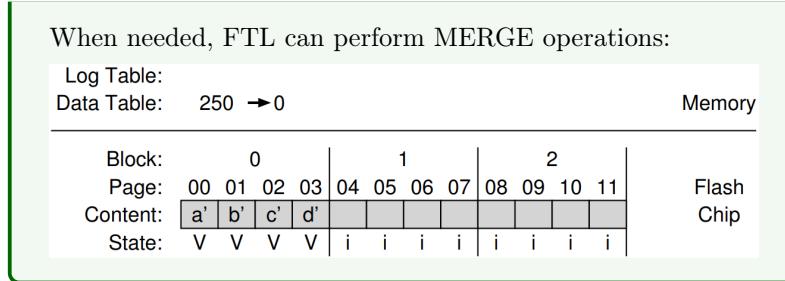
- Write(1000, a)
- Write(1001, b)
- Write(1002, c)
- Write(1003, d)

Log Table:												Memory	
Data Table: 250 → 8													
Block:	0				1				2				Flash Chip
Page:	00	01	02	03	04	05	06	07	08	09	10	11	
Content:	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	[ ]	a	b	c	d	
State:	i	i	i	i	i	i	i	i	V	V	V	V	

Let's update some pages:

- Write(1000, a')
- Write(1001, b')
- Write(1002, c')
- FTL updates only the page mapping information

Log Table: 1000→0 1001→1 1002→2 1003→3												Memory	
Data Table: 250 → 8													
Block:	0				1				2				Flash Chip
Page:	00	01	02	03	04	05	06	07	08	09	10	11	
Content:	a'	b'	c'	d'	[ ]	[ ]	[ ]	[ ]	a	b	c	d	
State:	V	V	V	V	i	i	i	i	V	V	V	V	



- **Page mapping plus caching** (a.k.a. **Demand-based FTL (DFTL)**).

Keep **only a portion** of the page-level mapping table in DRAM (a cache). Store the full mapping table in **flash itself**. On cache miss, **read the mapping** from flash into RAM (like a page table swap-in).

#### ✓ Pros

- \* **Scales to very large SSDs with low DRAM footprint**
- \* Maintains page-level flexibility without storing entire table in RAM

#### ✗ Cons

- \* Mapping lookup incurs **read latency** on cache misses
- \* More complex metadata management (must protect flash-stored tables)

#### ✓ The importance of Wear Leveling

Flash memory has a **limited number of erase/write (EW) cycles**:

- Each block can only sustain  $\approx$ 3,000 to 100,000 cycles (depending on type: SLC, MLC, TLC, QLC).
- If some blocks are used more than others (write **skew**), they **wear out faster**.

Without intervention, the SSD's lifespan would be determined by its **most heavily used block**. Ensure that **all blocks** in the SSD **wear out evenly** to: maximize **overall drive lifetime**, avoid **early failure** due to localized hot spots.

#### ⌚ How Wear Leveling works? The Flash Translation Layer (FTL):

1. Monitors **erase/write cycles** per block.
2. Identifies **cold blocks** (rarely updated, long-lived data).
3. Periodically:
  - **Reads** valid data from cold blocks
  - **Moves** it to fresher blocks
  - **Erases** and **reuses** the original blocks

Even cold blocks are “rotated” to ensure wear balance.

There are three types of Wear Leveling:

- **Dynamic:** Spread writes among blocks not currently holding static data
- **Static:** Occasionally move long-lived (cold) data to give its block a rest
- **Hybrid:** Combine both (used in most SSDs)

### ⚠ Wear Leveling Disadvantages

- **Increases Write Amplification:** moving cold data incurs extra writes.
- **Consumes bandwidth:** periodic copying reduces performance.
- **Complexity:** requires tracking per-block wear counts and scheduling background operations.

However, to **partially fix** this, a simple policy to apply is that each flash block has an **Erase/Write Cycle Counter** and maintains the value of:

$$|\text{Max (EW cycle)} - \text{Min (EW cycle)}| < \varepsilon \quad (3)$$

Where  $\varepsilon$  is a system-defined Wear Leveling threshold.

### ⚠ HDD vs SSD

UBER and TBW are two metrics help quantify how **reliable and durable a storage device is over time and under heavy use**.

- **Unrecoverable Bit Error Ratio (UBER):** The probability that a bit cannot be recovered correctly by the device, even after error correction.

$$\text{UBER} = \frac{\text{Number of unrecoverable bit errors}}{\text{Total bits read}} \quad (4)$$

A lower UBER means **better data reliability**.

- **Endurance rating: Terabytes Written (TBW):** The total amount of data we can write to the SSD over its warrantied lifetime before cells are expected to wear out.

$$\text{TBW} = \text{Endurance rating of the SSD (from manufacturer)} \quad (5)$$

For example, a 250 GB SSD with TBW = 70 TB, we can write:  $70 \div 365 = 190 \text{ GB/day}$ .

### 2.2.2.4 RAID

#### ⌚ How is RAID born?

Before 1980, **JBOD (Just a Bunch Of Disks)** was a common setup before the advent of disk arrays and RAID. JBOD simply **connects multiple physical disks to a system**, but each disk operates **independently**. There's **no striping** and **no redundancy**. Each disk has its **own mount point**, and the operating system or user decides where to store data. If one disk fails, **only the data on that disk is lost**, no protection or recovery is provided. **Performance bottlenecks** also occurred as CPUs became faster than disk I/O.

Researchers at UC Berkeley (notably Patterson, Gibson and Katz) proposed using **multiple cheaper disks** together: treat **many small, inexpensive disks** as **one large logical disk**. These were called **Disk Arrays**. The main idea was to achieve higher performance and more memory through parallelism.

- Disk Arrays appear as a **single logical high-performance disk**.
- Use **data striping** and **parallel access**, but these **weren't formalized or optimized** in the early implementation. This is because the core idea was to spread data across multiple disks to improve throughput (multiple disks serving different I/Os) and latency (multiple I/Os in parallel reduce queue wait time). But the **parallelism was often implicit**, not exposed to the software or the user. Some arrays allowed **concurrent I/O by accident**, not design. **I/O scheduling** was hardware-specific, **not standardized**.

#### ✓ Key improvements:

- ✓ **Parallel Access:** Multiple disks could serve I/O requests simultaneously.
- ✓ **Performance Boost:** Higher bandwidth and lower latency via concurrent disk activity.
- ✓ **Scalability:** Easy to increase capacity by adding disks.
- ✓ **Lower Cost per GB:** Used **multiple small, cheap disks** instead of one large expensive disk.
- ✓ **Modular Architecture:** Allowed easier maintenance, replacement, and upgrades.

#### ✗ Limitations:

- ✗ **No Standard Striping:** Striping (if present) was non-standard and not guaranteed.
- ✗ **No Redundancy:** If a disk failed, **data was lost**, arrays were vulnerable.
- ✗ **No RAID Levels:** No formal trade-offs between performance/reliability (e.g. RAID 0-6).
- ✗ **No Fault Tolerance Mechanism:** No automatic reconstruction, hot spares, or parity.

✖ **Limited Write Optimization:** RAID improved performance (esp. for writes) using smart parity layouts.

In 1988, the same researchers published the seminal paper: “A Case for Redundant Arrays of Inexpensive Disks (RAID)” [8]. They made two key contributions:

- They **formally introduced RAID**: not just disk arrays, but structured ones that also **handle reliability** via redundancy.
- They **defined RAID levels** (RAID 0 to RAID 5 in the original paper), each with different trade-offs between: *performance, reliability and storage efficiency*.

RAID was important because it **solved the reliability problem introduced by disk arrays**. Disk Arrays solved performance and capacity, but RAID solved reliability too, combining **Data Striping** (performance) and **Redundancy** (reliability).

#### Definition 2: RAID

**RAID (Redundant Array of Independent Disks)** is a **storage technology** that **combines multiple physical disks into a single logical unit** to improve performance, reliability, or both, by using data striping, redundancy, or both.

RAID is based on two core techniques: **Data Striping** (for performance, splits data across disks), and **Redundancy** (for reliability, adds fault tolerance via mirroring or parity).

Exists different RAID levels. Each level defines a strategy for:

- *How data is striped*
- *How redundancy is added*
- *What failure modes are tolerated*
- *How performance and capacity are affected*

## >Data Striping

**Data Striping** is the technique of **splitting data into small chunks** (called **stripe units**) and distributing them **across multiple disks in a round-robin manner**. Used primarily to **improve performance** by **enabling parallel disk access**. It does **not add redundancy** by itself.

- **Stripe Unit:** The amount of **data written to a single disk** before moving to the next one. Can be in **bits, bytes, blocks or KBs**. Small stripe unit, better parallelism for large files. Large stripe unit, fewer disk operations for small reads.
- **Stripe Width:** The **number of disks** over which the data is stripped. If we have 4 disks participating in stripping, stripe width is 4. **Determines how many disks work in parallel** for a given I/O.
- How are **Multiple Independent I/O Requests** processed? Small, random I/O requests from **different applications or users**. RAID can **process them in parallel** on different disks. As result: **lower disk queue lengths and faster response times**.
- How is a **Single Multiple-Block I/O Request** processed? A **large read or write operation** on a big file (e.g., a video or a database query). Striping lets **multiple disks work together** to serve this one big request. As result, **much faster data transfer** compared to using one disk.

## Redundancy

**Redundancy** is the method of **adding extra information to protect data from disk failures**. If a disk fails, the system can **reconstruct the missing data using the redundant information**. Redundancy is *essential* because:

- Disk arrays use many disk, and **more disk, higher risk of failure**.
- RAID introduces redundancy to **tolerate and recover from failures**.

There are two types of redundancy:

1. **Data Duplication (Mirroring)**. Every block of data is **copied exactly** to another disk. Used in RAID 1 and RAID 10.
  - ✓ Can survive **complete disk failures**.
  - ✓ Fast reads (can load-balance between mirrors).
  - ✗ **Wastes 50%** of storage (one disk stores only a copy).
2. **Parity-Based Redundancy**. Adds a **calculated parity block** (usually XOR) that allows **rebuilding lost data**. Used in RAID 5 and RAID 6.
  - ✓ More **storage-efficient** than mirroring.
  - ✓ Can tolerate 1 (RAID 5) or 2 (RAID 6) disk failures.
  - ✗ **Writes are slower** (need to read/update parity on each write).

❓ Why is it called “Redundant Array”? Because RAID stores more than just our data, it stores the redundant data necessary to protect it.

### ☰ RAID levels

A **RAID level** defines a specific way to organize **striping** and **redundancy** across multiple disks. Each level balances **three key trade-offs**:

- ⌚ **Performance:** *How fast are reads/writes?*
- 🛡 **Fault Tolerance:** *Can it survive disk failure?*
- **Storage Efficiency:** *How much usable space is left?*

RAID	Striping	Redundancy	Tolerates Failure?	Main Benefit
0	✓	✗ None	✗ No	Max speed, no protection
1	✗	✓ Mirroring	✓ 1 disk	Reliability via copies
5	✓	✓ Parity (rotated)	✓ 1 disk	Balance of perf + space
6	✓	✓ Dual Parity	✓ 2 disks	Extra protection

Table 6: Standard RAID Levels: RAID 4 is not shown because it is rarely used; RAID 5 has the same concept but eliminates RAID 4’s limitations. RAID 2 and 3 are also not shown because they are not covered in this course.

Each RAID level is a **design pattern** that answer: “*How can I spread and protect data across multiple disks to meet my performance, capacity, and reliability goals?*”.

Topic	Page
RAID 0	61
RAID 1	64
RAID 0 + 1	64
RAID 1 + 0	65
RAID 4	68
RAID 5	72
RAID 6	76
Comparison and characteristics of RAID levels	77

Table 7: RAID - Table of Contents.

## RAID 0 - Striping Without Redundancy

**RAID 0** splits (stripes) data across multiple disks to increase performance. It does not provide redundancy: if one disk fails, all data is lost.

### Structure

- **Data Striping:** ✓ Yes (block-level)
- **Redundancy:** ✗ None
- **Minimum disks:** 2
- **Fault Tolerance:** ✗ 0 disks, a single failure is fatal
- **Storage Efficiency:** ✓ 100% (all capacity is usable)

### When is it used?

High performance environments where data loss is acceptable, such as temporary data storage, video editing, gaming, scratch disks or caches.

### Performance

Operation	Result
Reads	✓ Much faster (parallel access)
Writes	✓ Much faster (split writes)
Failure	✗ One disk dies, all lost

### Advantages

- **Lower cost** because it does not employ redundancy (no error-correcting codes are computed and stored).
- **Best read/write performance** (it does not need to update redundant data and is parallelized).

### Disadvantages

- **Zero fault tolerance.**
- High risk: the failure rate is equal to the sum of all disk failure probabilities.

### ❖ How does it work?

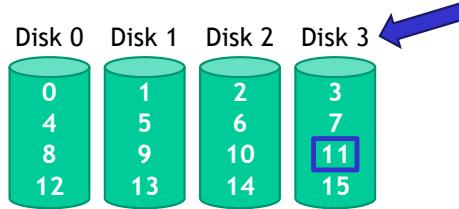
The main idea of RAID 0 is to use several physical disks as **a single logical disk by striping** data across them (splitting data into small blocks and writing them in **round-robin fashion** across all  $N$  disks). This approach improves performance:

- **Sequential access** is distributed across all disks, increased transfer rate.
- **Random access** naturally spreads I/O load across disks, lower latency and better throughput.

The system uses the following formulas to **determine which disk and offset holds a given logical block**:

$$\begin{aligned} \text{Disk index} &= \text{logical\_block\_number \% number\_of\_disks} \\ \text{Block Offset} &= \frac{\text{logical\_block\_number}}{\text{number\_of\_disks}} \end{aligned} \quad (6)$$

For example, the command `read block 11` in a 4-disk array gives disk 3 as the index and block 2 as the offset on that disk.



This formula allows the RAID controller to locate any block **without metadata**, just with arithmetic.

The choice of chunk size is critical because it affects performance at this level. The **Chunk Size** (also called **Stripe Unit** size) is the amount of **data written to each disk before moving to the next one**.

The impact of chunk size is evident:

- **Small chunks** → better **parallelism** (each access touches more disks).
- **Large chunks** → lower **seek overhead** (each file uses fewer disks).

In practice, typical RAID arrays use 64 KB chunks as a **balanced** (tradeoff) default.

### Measuring Performance

- **Measuring Sequential Transfer Rate.** For large sequential I/O, the transfer time includes:
  1. **Seek time** (page 155)
  2. **Rotational latency**
  3. **Actual Data Transfer Time:**

$$S = \frac{\text{transfer\_size}}{\text{time\_to\_access}} = \frac{\text{data\_size}}{\text{disk\_rate}} \quad (7)$$

For example, suppose there is 7 ms of *seek time*, 3 ms of *rotational latency*, and 10 MB of *data to transfer* at a *disk rate* of 50 MB/s. The total time is given by the seek time, rotational latency, and the time taken to transfer the data:

$$\text{Time} = 7 \text{ ms} + 3 \text{ ms} + (10 \text{ MB} \div 50 \text{ MB/s}) = 210 \text{ ms}$$

Thus, the sequential throughput is:

$$S = 10 \text{ MB} \div 0.21 \text{ s} = 47.62 \text{ MB/s}$$

In RAID 0 with  $N$  disks, the **Total Sequential Throughput** is:

$$\text{Total Sequential Throughput} = N \times S \quad (8)$$

$S$  is the sequential throughput for a single disk in the system.

- **Measuring Random Transfer Rate.** For small random accesses, latency dominates over transfer. Using the same example as before, but changing the file size to 10 KB, the time is as follows:

$$\text{Time} = 7 \text{ ms} + 3 \text{ ms} + (10 \text{ KB} \div 50 \text{ MB/s}) = 0.98 \text{ MB/s}$$

Resulting random throughput:

$$R = 10 \text{ KB} \div 0.98 \text{ ms} = 10.2 \text{ MB/s}$$

In RAID 0 with  $N$  disks, the **Total Random Throughput** is:

$$\text{Total Random Throughput} = N \times R \quad (9)$$

$R$  is the random throughput for a single disk in the system.

Feature	Description
<b>Capacity</b>	$N$ , all disk space is usable (no redundancy)
<b>Reliability</b>	$0$ , MTTDL (Mean Time To Data Loss) = MTTF (Mean Time To Failure)
<b>Performance</b>	It provides full parallelization for both random and sequential throughput

## RAID 1 - Mirroring

RAID 0 offers performance, but **no protection** against failures. **RAID 1 solves this** by maintaining **two identical copies of all data** (mirroring).

- ✓ **High reliability:** if one disk fails, the second copy is used seamlessly.
- ✓ **Fast reads:** can read from either disk (or balance across them).
- ⚠ The **write speed** is slightly slower than that of a single disk because the **data must be written to both disks**.
- ✗ **High cost:** only **50% of total disk space** is usable.

In theory, RAID 1 can use **more than 2 disks** to mirror data, but rarely done due to **very high costs** (only  $1 \div N$  capacity used), and too much overhead for typical storage needs. In other words, more than 2-way mirroring is possible but **not practical**.

### ❷ Why combined RAID levels at all?

RAID 1 is great, but it has its **limits**. It mirrors data, meaning one disk has the data and the other disk has a copy of it. Therefore, we always need pairs of disks. With two disks, RAID 1 is simple and reliable. But what if we want to use more than two disks and want both high reliability and high performance? We want to **combine the reliability that RAID 1 provides with the performance and scalability that RAID 0 provides**. In other words, how do we structure the disks as their number increases to get the best of both RAID 0 and RAID 1? The answer lies in the RAID 10 and RAID 01 techniques.

The goal of combining RAID levels is to achieve both reliability and performance. The combination is **generally written as RAID  $x + y$**  (sometimes called RAID  $xy$ ), meaning we **first** apply RAID  $x$  to small groups of disks and **then** apply RAID  $y$  on top of those groups.

We divide  $n \times m$  total disks into  $m$  groups, each containing  $n$  disks.

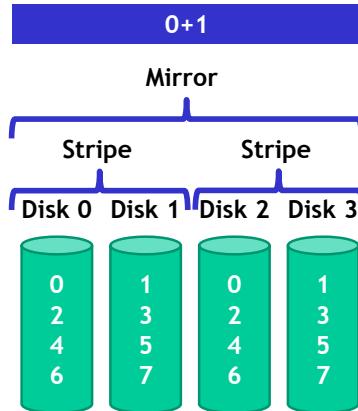
1. Apply RAID  $x$  to each group.
2. Apply RAID  $y$  to the  $m$  groups, treating each group as a “logical disk”.

There are two possible combinations at this level:

- **RAID 0 + 1** is a **striped array of mirrored sets**. It combines the performance of RAID 0 and the fault tolerance of RAID 1, but with **some limitations**.

The structure consists of a **minimum of 4 disks**:

1. **Start with striping** (RAID 0): split data across 2 or more disks for performance.
2. **Then mirror the whole striped group** (RAID 1).



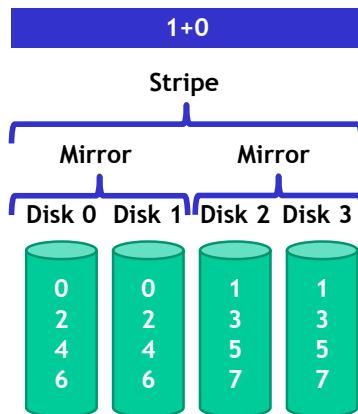
**⚠ RAID 0 + 1: Failure Behavior.** If any one disk fails, the system still works using the mirrored group. But if a disk fails in each stripe, all data is lost. After the first failure, the array degrades into pure RAID 0, losing redundancy.

Aspect	Value
Usable space	50% (half is mirror)
Read speed	✓ High (parallel reads)
Write speed	⚠ Slower (must write both copies)
Reliability	✓ Tolerates 1 disk failure (in same group)

- **RAID 1 + 0** combines **mirroring (RAID 1)** and **striping (RAID 0)**. First, data is **mirrored**, then it is **striped** across mirrored pairs. It offers **high performance** (like RAID 0), **high fault tolerance** (like RAID 1).

The structure consists of a **minimum of 4 disks**:

1. **Create mirrored pairs (RAID 1)**
2. **Stripe data across pairs (RAID 0)**



### ⚠ RAID 1 + 0: Failure Tolerance

- ✓ Can survive **multiple disk failures**, as long as **only one per mirrored pair**.
- ✗ If both disks in a mirrored pair fail, data loss.

RAID 10 is **more fault-tolerance than RAID 01**, especially in cases of multiple failures. Because each mirrored pair in RAID 10 is self-contained:

- If one disk in a pair fails, only **that pair** needs to be rebuilt (not the entire array).
- The rest of the array **remains fully operational** and can keep serving requests.

In RAID 01:

- A single disk failure disables **half of the array**.
- A second failure in the other half = total data loss.

Aspect	Value
Usable space	50% of total (because of mirroring)
Read speed	✓ Very fast (parallel reads from mirrors)
Write speed	✓ Faster than RAID 5/6 (no parity calc.)
Reliability	✓ High (survives multiple failures safely)

Widely used in databases, transactional systems, and virtualized environments where both performance and fault tolerance are critical.

In conclusion, RAID 10 is created by **first mirroring disks and then striping** across the mirrored pairs. This configuration provides **faster read and write** speeds and **greater fault tolerance** than RAID 01, making it ideal for high-load systems.

### 📊 Measuring Performance

- **Capacity**. Total usable space is  $N \div 2$ , since each block is stored twice, only **50% of disk space** is usable.
- **Reliability**. Can **survive 1 disk failure** guaranteed. In best-case scenarios, can survive **up to  $N \div 2$  disk failures**, if no two are mirrors of each other. However, if **both disks in a mirrored pair fail**, data is lost.

- **Sequential Performance**

- **Sequential Write**. Writes must go to both copies, then halved throughput:

$$\text{Sequential Write} = \left( \frac{N}{2} \right) \times S \quad (10)$$

-  **Sequential Read.** In theory, reads could be optimized, but usually reads are directed to **only one disk per mirror**. So, **half of the disks are idle** during reads:

$$\text{Sequential Read} = \left(\frac{N}{2}\right) \times S \quad (11)$$

- **Random Access Performance**

-  **Random Read.** Best case for RAID 1. Reads can be **load-balanced** across all  $N$  disks. System can choose which mirror is less busy, then fully parallel.

$$\text{Random Read} = N \times R \quad (12)$$

-  **Random Write.** Writes must go to both disks in each pair. Only  $N \div 2$  mirrors, then only  $N \div 2$  writes happen in parallel.

$$\text{Random Write} = \left(\frac{N}{2}\right) \times R \quad (13)$$

RAID 1 provides **excellent reliability** and **great random read performance**. Its main limitations are only 50% of storage is usable, and sequential throughput is limited to half the potential.

### The Consistent Update Problem

In RAID 1, every write must be done **twice** (once per mirror). This raises a **consistency issue**: *what if the system crashes or loses power after writing to one disk, but before writing to the other?*

- One mirror has the **updated data**
- The other mirror has **state (old) data**
- The two copies are now **out of sync**

This violates the **atomicity** principle (a write must be **all or nothing**, either all mirrors are updated or none).

 **How it's handled.** Many RAID controllers implement a **Write-Ahead Log (WAL)**:

- A special **non-volatile memory area** (battery-backed cache).
- Writes are first saved into the log **before** writing to disks.
- If power fails, the controller can use the log to:
  - Complete the write
  - Or roll it back (to restore consistency)

This ensures that mirrored copies stay **synchronized**, even after failure.

## RAID 4 - Parity Drive

**RAID 4** uses **block-level striping** (like RAID 0), but adds a **dedicated parity disk** to provide **fault tolerance**.

### ❖ Parity Calculation

Parity is computed using the **XOR** (**exclusive OR**) operation. For example, 4 blocks per stripe:

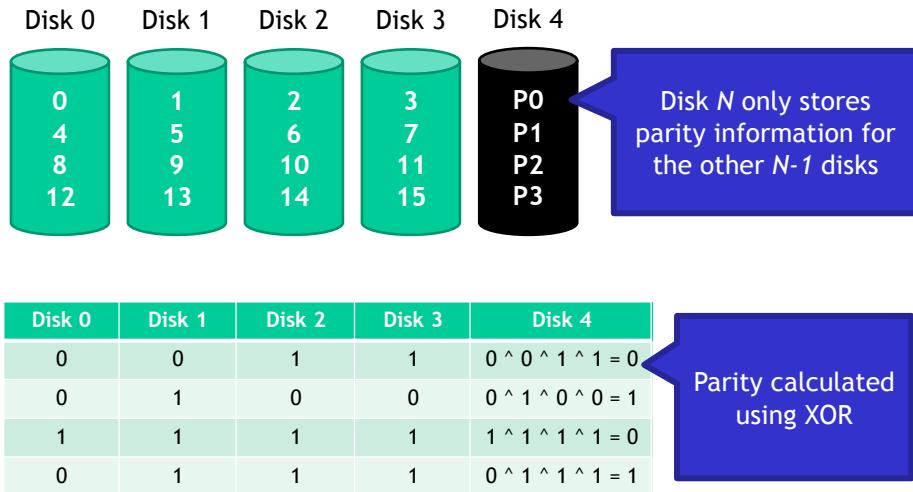


Figure 8: RAID 4 - *How does it work?*

It is used XOR because it has a special property: if we know all but one value, we can **reconstruct the missing one**. For example, if Disk 2 is lost, it can be reconstructed using an XOR operation with Disks 0, 1, and 3 and the Parity unit.

### ✓ Pros and ✗ Cons

- ✓ Fault tolerance: can survive **1 disk failure**.
- ✓ More **space-efficient** than RAID 1 (only 1 disk used for redundancy).
- ✗ **Parity disk is a bottleneck**. Every write must update parity, then a single disk becomes overloaded.
- ✗ Write performance is poor compared to RAID 0 or RAID 10.

### ❖ How does it work?

- **Updating Parity on Write in RAID 4.** When we **modify a block** in RAID 4, we must also update the **parity block** in that stripe. There are two ways to do it:

1. **Additive Parity.** Recalculate parity using all the blocks in the stripe. Steps:
  - (a) **Read all other data blocks** in the stripe.
  - (b) XOR them together to get the **new parity**.

**✓ Simple and correct**, but **✗ expensive** because must **read all blocks** to recompute.
2. **Subtractive Parity** (Efficient: modify incrementally). Update the parity by using a **mathematical trick**:

$$\text{New Parity} = \text{Old Parity} \oplus \text{Old Data} \oplus \text{New Data} \quad (14)$$

This works thanks to the **reversible XOR** property:

$$A \oplus A = 0, \quad A \oplus 0 = A$$

**✓ Very efficient** because only need to read the block being written (**old value**) and the **old parity block**.

- **Reads in RAID 4.** Reads in RAID 4 are **fast and efficient**, especially compared to writes. Data is **striped across all data disks**, and the **parity disk is not involved** in normal reads. There are two possible read scenarios:

1. **Sequential Read.** Large, continuous read (e.g., loading big file). Data is read in **parallel** from all data disks. It is **fast**, each disk reads part of the file simultaneously.
2. **Random Read.** Small, scattered reads (e.g., database lookups). Still efficient because:
  - Each disk can handle **its own read** in parallel.
  - Parity disk is **not touched** during a normal read.

As we saw at the beginning, if a data **disk fails**, the missing block is **reconstructed using XOR**:

$$D_{\text{missing}} = P \oplus D_1 \oplus D_2 \oplus D_3 \oplus \dots$$

Read recovery is still possible, it is just slower.

- **Serial Writes in RAID 4.** Serial writes mean writing **a sequence of blocks** that all belong to the **same stripe**, typically during large, contiguous writes (e.g., streaming, backups).

In RAID 4, data is **striped** across all data disks. The **parity for each stripe** is stored in a **dedicated parity disk**.

During serial writes, each data disk receives **one block** from the stripe. The **parity disk** is updated **once per stripe**. Since all writes hit the same stripe, the **parity disk becomes a bottleneck**.

Operation	Description
Data writes	✓ Parallel across data disks
Parity update	✗ Centralized
Bottleneck	Parity disk handles <b>every stripe's write</b>
Comparison	Same structure as read, then but <b>parity slows it</b>

Even though data writes are parallel, all serial writes in the same stripe **converge on the parity disk**, making it the **main point of contention**.

- **Random Writes in RAID 4.** A **random write** updates **one block** somewhere on disk, not the entire stripe. This is common in databases, file systems, and OS workloads.

The writing process for each block is as follows:

1. **Read** the **old data block** and the **old parity block**.
2. **Compute** the parity block:

$$P_{\text{new}} = D_{\text{old}} \oplus D_{\text{new}} \oplus P_{\text{old}}$$

This efficiently updates parity using subtraction (XOR).

3. **Write** the **new data block** and the **updated parity block**

⚠ The main problem here is the **bottleneck** caused by the parity disk. Even though the data block may change on **any disk**, the **parity block is always on the same disk**. **Each write operation must read from and write to that disk**. This creates **serialization**, only one parity update can occur at a time. Even with multiple writes to different data disks, they all **wait for the parity disk**.

Operation	Behavior
Data writes	✓ Fast (per disk)
Parity update	✗ Always goes to the <b>same disk</b>
Bottleneck	⚠ Parity disk handles <b>every write</b>
Overall	✗ <b>Terrible performance</b> on random writes

### Measuring Performance

- **Capacity:**  $N - 1$ . One disk is used exclusively for parity, so it is **not usable for data**.
- **Reliability:** can tolerate **1 disk failure** (any one of the data or parity disks). But if a disk fails, the system can still serve data using parity reconstruction. However, write and read performance becomes **massively degraded** (especially if parity disk is affected).
- **Read/Write Performance**

Operation	Performance	Notes
<b>Sequential Read</b>	$(N - 1) \times S$	✓ Full parallelism across all data disks
<b>Sequential Write</b>	$(N - 1) \times S$	✓ Parallel as long as writes hit different stripes
<b>Random Read</b>	$(N - 1) \times R$	✓ Reads avoid parity disk, then high parallel performance
<b>Random Write</b>	$R \div 2$	✗ Terrible, every write must access parity disk twice

Parity disk becomes a **point of contention for every write**. Causes **serialization of random writes**, reducing overall throughput drastically.

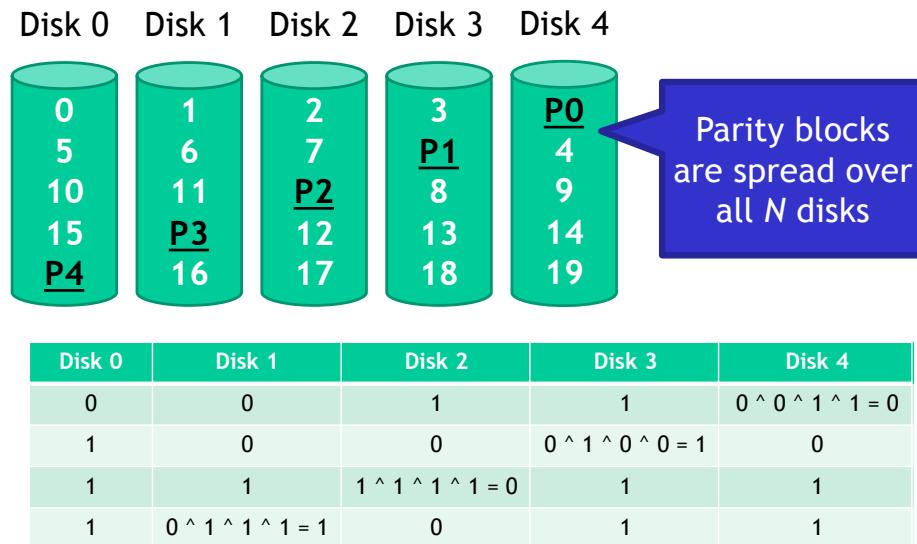
In conclusion, RAID 4 provides ample capacity and quick sequential input/output (I/O) thanks to block-level striping. It uses one dedicated parity disk for fault recovery. However, its **main weakness is its poor random write performance**, as all writes target the same parity disk. This is why RAID 4 is rarely used in practice and led to the development of **RAID 5**, which solves this issue by distributing parity.

## RAID 5 - Rotating Parity

**RAID 5** extends RAID 4 by using **distributed (rotating) parity**. This removes the **bottleneck of the single parity disk**.

### ❖ How does it work?

In RAID 4, parity is always stored on a **dedicated parity disk**, causes a bottleneck. In RAID 5, parity is **spread (rotated)** across **all disks, one stripe at a time**.



**Parity position rotates** from one disk to the next. So **each disk holds both data and some parity**; there's no dedicated parity disk. However, parity is still computed using the XOR operation, and the operand depends on the disks that calculate it. For example, Disk 4 will calculate the XOR using Disks 0, 1, 2, and 3. Disk 3 will use disks 0, 1, 2, and 4, and so on for the others.

### ❓ What happens during a Random Write?

Like in RAID 4, RAID 5 must **preserve parity** whenever data changes. A **random write** modifies only one block in a stripe, so we use an efficient **subtractive parity update**.

#### 1. Read

- (a) Read the *old data block*
- (b) Read the *old parity block*

#### 2. Compute. Use XOR subtraction:

$$P_{\text{new}} = D_{\text{old}} \oplus D_{\text{new}} \oplus P_{\text{old}}$$

### 3. Write

- (a) Write the *new data block*
- (b) Write the *updated parity block*

In total, there are **4 disk operations**: 2 reads (old data and old parity) and 2 writes (new data and new parity).

## 💡 RAID 5 improvement over RAID 4

In **RAID 4**, all parity writes go the **same disk**, and this creates a **bottleneck**. **RAID 5 solves** this slowdown by **rotating the parity**. Parity updates are spread across all disks, which distributes the load evenly. This allows **random writes to occur in parallel**, eliminating serialization due to a single disk. This is obviously much better than RAID 4.

### 📊 Analysis

- **Capacity:**  $N - 1$  disks. Same as RAID 4, one disk's worth of capacity is used for **distributed parity**.
- **Reliability:** tolerates 1 **disk failure**. However, during partial outage the degraded mode phenomena is highlighted, because all missing data must be reconstructed on-the-fly using parity, which causes massive performance degradation.
- **Read/Write Performance**

Operation	Performance	Notes
<b>Sequential Read</b>	$(N - 1) \times S$	➡ Same as RAID 4, striping across data disks
<b>Sequential Write</b>	$(N - 1) \times S$	✓ Fully parallel if stripes span across disks
<b>Random Read</b>	$N \times R$	💡 Better than RAID 4, all disks can be read in parallel
<b>Random Write</b>	$\frac{N}{4} \times R$	💡 Better than RAID 4, writes are distributed. However, each write requires an additional 2 reads and 2 writes for parity updates.

For each random write, we have 2 reads and 2 writes with  $N$  disks and parallelism. The **throughput** is:

$$\text{Throughput} \approx \frac{N}{4} \times R \quad (15)$$

### ⌚ Mean Time To Failure (MTTF) of RAID 5

When we have **one failed disk**, the array is running degraded, it's still working but *vulnerable*. To lose data, we need a **second disk** to fail *while* the first failed disk is being rebuilt or replaced. So the chance of losing data is: “*what's the chance that any other disk fails during the repair window?*”.

Suppose the Mean Time To Failure for a **single disk** is MTTF. The **failure rate** for a single disk is calculated using the well-known formula:  $\lambda = \frac{1}{\text{MTTF}}$ .

The **probability that a disk fails in a small time  $\Delta t$**  is about  $\lambda \cdot \Delta t$ . So, if the repair time is MTTR, the chance that a disk fails during that window is about:

$$P(\text{fail in MTTR}) = \frac{\text{MTTR}}{\text{MTTF}} \quad (16)$$

In other words, it indicates that during the MTTF time window, we use an MTTR time for repairs, showing how much of the window is used. It also indicates the **likelihood of a second disk failing during the vulnerable window**.

Now, the RAID 5 failure mechanism is combined by two parts:

1. **Wait for the first disk to fail.** We have  $G$  disks. As we have seen before, the failure rate of each disk is:

$$\lambda_{\text{disk}} = \frac{1}{\text{MTTF}_{\text{disk}}}$$

Since we have  $G$  parallel disks working together, the **failure rate of the entire system** is equal to the failure rate of each disk multiplied by  $G$ :

$$\lambda_{\text{system}} = G \times \lambda_{\text{disk}}$$

The mean time to the first failure is given by the ratio of one disk failure and the system's failure rate:

$$\text{MTTF}_{\text{first fail}} = \frac{1}{\lambda_{\text{system}}} = \frac{1}{G \times \lambda_{\text{disk}}} = \frac{1}{G \times \frac{1}{\text{MTTF}_{\text{disk}}}} = \frac{\text{MTTF}_{\text{disk}}}{G}$$

2. **Risk of a second disk failing while you rebuild.** When one disk fails, we have  $G - 1$  disks left. During the **vulnerable window** (MTTR), each remaining disk could fail. As we saw on page 74, the chance that one disk will fail within that window is:

$$P(\text{fail in MTTR}) = \frac{\text{MTTR}}{\text{MTTF}}$$

Since there are  $(G - 1)$  disks left, the risk multiplies:

$$P(\text{2nd fail}) = (G - 1) \times P(\text{fail in MTTR}) = (G - 1) \times \frac{\text{MTTR}}{\text{MTTF}}$$

We now have everything we need to calculate the **MTTF of the RAID 5**:

$$\begin{aligned}
 \text{MTTF}_{\text{RAID}5} &= \text{MTTF to 1st fail} \times \frac{1}{P(\text{2nd fail during rebuild})} \\
 &= \frac{\text{MTTF}_{\text{disk}}}{G} \cdot \frac{1}{(G - 1) \cdot \frac{\text{MTTR}}{\text{MTTF}}} \\
 &= \frac{\text{MTTF}_{\text{disk}}^2}{G \cdot (G - 1) \cdot \text{MTTR}}
 \end{aligned} \tag{17}$$

In conclusion, RAID 5 provides a good **trade-off between capacity, reliability, and performance**. It avoids RAID 4's parity bottleneck by using **rotating parity**, enabling better parallelism for **random writes**. However, in case of a disk failure, **performance degrades** significantly due to **on-the-fly parity reconstruction**.

## RAID 6 - Dual Parity

**RAID 6** is an extension of RAID 5 that adds a second independent parity block per stripe. This allows it to tolerate two simultaneous disk failures, a major reliability upgrade over RAID 5.

### ❖ How does it work?

It can tolerate up to 2 concurrent disk failures. Uses two different types of parity:

- **P parity**: is the same as in RAID 5, a “simple” XOR (exclusive-or) of the data blocks in a stripe.
- **Q parity**: is more complex. It is generated using **Reed-Solomon** coding, a mathematical technique over **Galois Fields (GF)**, which enables the correction of multiple simultaneous failures.

Each parity serves a different purpose:

- **P (XOR parity)** handles one disk failure.
- **Q (Reed-Solomon parity)** can handle a second failure that isn’t linearly dependent on the first one.

This combination allows RAID 6 to recover from two simultaneous disk failures. In simple terms:

- If we lose 1 disk, we can **recover using XOR** (as in RAID 5).
- If we lose 2 disks, the system **solves a set of linear equations** (using **P** and **Q**) **to recover the missing data**.

This requires the two parities to be **independent**, so their information isn’t redundant.

The **disk configuration requires  $N + 2$  disks**.  $N$  are data disks, and 2 are distributed parity blocks ( $P$  and  $Q$ ) per stripe. The **minimum configuration** requires at least **4 data disks**, for a total of **6 disks minimum**.

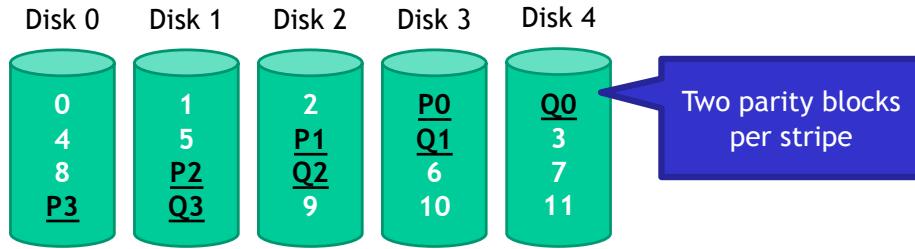
### ⚠ Write Performance

Write performance is **slower than with RAID 5**. Each write requires updating both parity blocks, necessitating at least **6 disk accesses**.

1. Read *old data*, read *parity block P*, and read *parity block Q*
2. Write *new data*, write *new parity block P*, and write *new parity block Q*

High overhead makes RAID 6 **slower on random writes**, but **safer**.

In summary, **RAID 6** adds a second, independent parity block ( $P + Q$ ) per stripe, enabling recovery from two simultaneous disk failures. RAID 6 uses Reed-Solomon coding for the  $Q$  parity and distributes both parity blocks across all disks. Although **RAID 6 is more fault-tolerant than RAID 5**, it suffers from **higher write overhead**, requiring at least **6 I/O operations per write**.



### Comparison and characteristics of RAID levels

The following table shows eight fundamental properties of the RAID levels.

- $N$ : number of drives
- $R$ : random access speed
- $S$ : sequential access speed
- $D$ : latency to access a single disk

	RAID 0	RAID 1	RAID 4	RAID 5
<b>Capacity</b>	$N$	$N \div 2$	$N - 1$	$N - 1$
<b>Reliability</b>	0	$1 \vee N \div 2$	1	1
<b>Sequential Read</b>	$N \times S$	$(N \div 2) \times S$	$(N - 1) \times S$	$(N - 1) \times S$
<b>Sequential Write</b>	$N \times S$	$(N \div 2) \times S$	$(N - 1) \times S$	$(N - 1) \times S$
<b>Random Read</b>	$N \times R$	$N \times R$	$(N - 1) \times R$	$N \times R$
<b>Random Write</b>	$N \times R$	$(N \div 2) \times R$	$R \div 2$	$(N \div 4) \times R$
<b>Read</b>	$D$	$D$	$D$	$D$
<b>Write</b>	$D$	$D$	$2 \times D$	$2 \times D$

Table 8: Comparison of RAID levels.

Where the throughput is:

- Sequential Read
- Sequential Write
- Random Read
- Random Write

And the latency is:

- Read
- Write

RAID	Capacity	Reliability	Read Perf.	Write Perf.	Rebuild Performance
0	100%	N/A	✓ Very good	✓ Very good	✓ Good
1	50%	✓ Excellent	✓ Very good	✓ Good	✓ Good
5	$\frac{(n-1)}{n}$	✓ Good	✓ Good	✗ Fair	✗ Poor
6	$\frac{(n-2)}{n}$	✓ Excellent	✓ Very good	✗ Poor	✗ Poor
1 + 0	50%	✓ Excellent	✓ Very good	✓ Good	✓ Good

Table 9: Characteristics of RAID levels.

- **Best Performance and Capacity:** RAID 0.
- **Maximum Fault Tolerance:** RAID 1 or RAID 6, with RAID 1+0 often preferred over 0 + 1.
- **Balanced Solution** (Space, Performance, Recoverability): RAID 5.

We report the RAID level comparison here. This is for utility reasons. It is on page 60.

RAID	Striping	Redundancy	Tolerates Failure?	Main Benefit
0	✓	✗ None	✗ No	Max speed, no protection
1	✗	✓ Mirroring	✓ 1 disk	Reliability via copies
5	✓	✓ Parity (rotated)	✓ 1 disk	Balance of perf + space
6	✓	✓ Dual Parity	✓ 2 disks	Extra protection

Final Considerations and Adopted Techniques:

- **Hot Spare Disk.** A *hot spare* is a **physical disk** already installed and powered in the system but **not actively used** to store data or parity. It's **just waiting**.

This is important because when a **disk** in a RAID array **fails**, **rebuilding** the array, i.e., reconstructing lost data using parity, can **take hours or days**, depending on the disk size and load. However, **with a hot spare**:

- ✓ The controller **immediately** starts rebuilding the lost data onto the spare.
- ✓ No need for human intervention to replace the disk.
- ✓ It reduces downtime and risk of further data loss during the rebuild period.

The mechanics of a Formula 1 team are a **great analogy**. The pit crew remains inactive for most of the race. However, the moment the car enters the pit lane, the crew acts immediately and precisely, replacing tires or making adjustments in a matter of seconds. Similarly, the hot spare disk is not part of the active array during normal operations. However, as soon as a failure occurs, the hot spare disk begins the rebuild process, helping to quickly restore full redundancy.

- **Hardware vs Software RAID**

- **Hardware RAID.** Implemented via a **dedicated RAID controller card** or built into the motherboard.

- ✓ **Pros**

- ✓ **High performance:** RAID logic is offloaded from the CPU.
    - ✓ Usually includes a battery-backend **cache to improve write speed and protect against power loss.**

- ✗ **Cons**

- ✗ **Portability issue:** if the controller fails and we move the disks to another machine with a different controller, the array might not be recognized.

- ✗ **Expensive.**

- **Software RAID.** Managed by the **operating system** (e.g., Linux `mdadm`, Windows Storage Spaces).

- ✓ **Pros**

- ✓ **Cheap and flexible.**
    - ✓ **Easy to migrate:** disks can often be moved to a different machine and reassembled.

- ✗ **Cons**

- ✗ **Slower performance** because the host CPU handles parity and I/O operations.

- ✗ **Less reliable** under high load or system crashes.

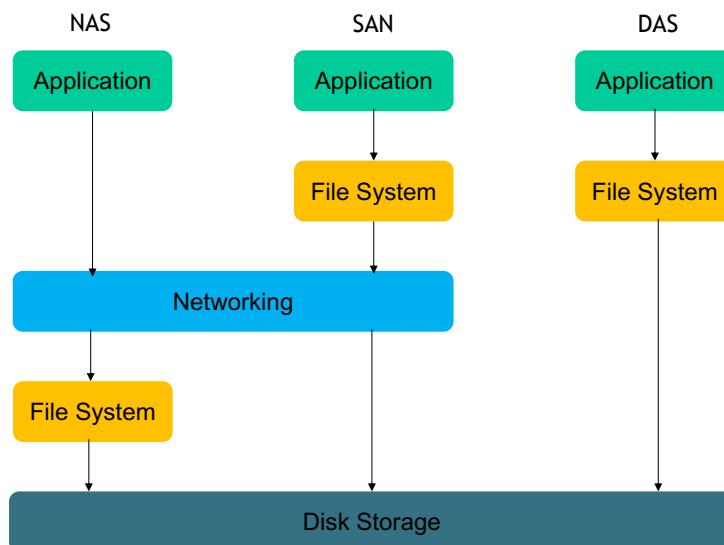
- ✗ Vulnerable to the **consistent update problem** (page 67).

### 2.2.2.5 DAS, NAS and SAN

As the last argument, we introduce **three different typologies** of storage systems:

- **Direct Attached Storage (DAS)** is a **storage system directly attached to a server or workstation**. They are visible as disks/volumes by the client OS.
- **Network Attached Storage (NAS)** is a **computer connected to a network that provides only file-based data storage services** (e.g. FTP, Network File System) to other devices on the network and is visible as File Server to the client OS.
- **Storage Area Networks (SAN)** are **remote storage units connected to a PC using a specific networking technology** (e.g. Fiber Channel) and are visible as disks/volumes by the client OS.

In the following schema, we can see a simple architectural comparison.



#### ✓ DAS features

DAS is a **storage system directly attached to a server or workstation**. The term is used to differentiate non-networked storage from SAN and NAS. The **main features** are:

- Limited scalability.
- Complex manageability.
- Limited performance.
- To read files in other machines (the “file sharing” protocol of the OS must be used).

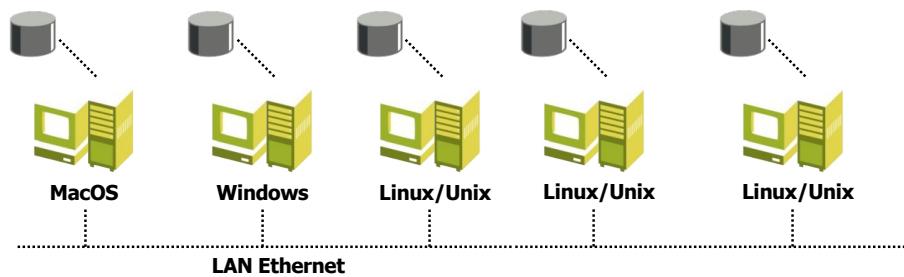


Figure 9: DAS architecture.

Note that all the **external disks connected to a PC with a point-to-point protocol can be considered DAS**.

### ✓ NAS features

A NAS unit is a **computer connected to a network that provides only file-based data storage services to other devices on the network**. NAS systems contain one or more hard disks, often organized into logical redundant storage containers or RAID. Finally, **NAS provides file-access services to the hosts connected to a TCP/IP network through Networked File Systems/SAMBA**. Each NAS element has its IP address. Furthermore, each NAS has good scalability.

The **main differences between DAS and NAS** are:

- DAS is simply an **extension of an existing server** and is **not necessarily networked**.
- NAS is designed as an easy and self-contained solution for **sharing files over the network**.

Regarding **performance**, NAS depends mainly on the speed and congestion of the network.

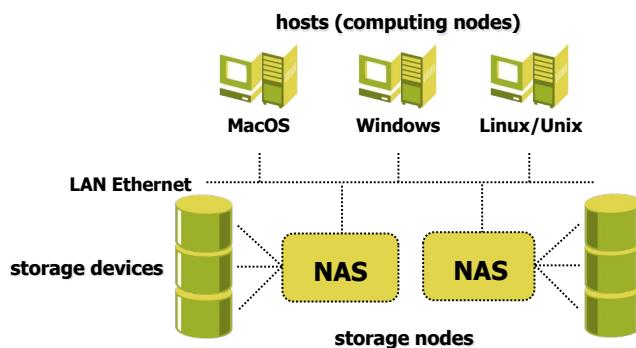


Figure 10: NAS architecture.

### ✓ SAN features

SANs are remote storage units connected to servers using a specific networking technology. SANs have a particular network dedicated to accessing storage devices. It has two distinct networks: one TCP/IP and another dedicated network (e.g. Fiber Channel). It has a high scalability.

The main difference between a NAS and a SAN is that:

- **NAS appears to the client OS as a file server.** Then, the client can map network drives to shares on that server.
- **A disk available through a SAN still appears to the client OS as a disk.** It will be visible in the disks and volumes management utilities (along with the client's disks) and available to be formatted with a file system.

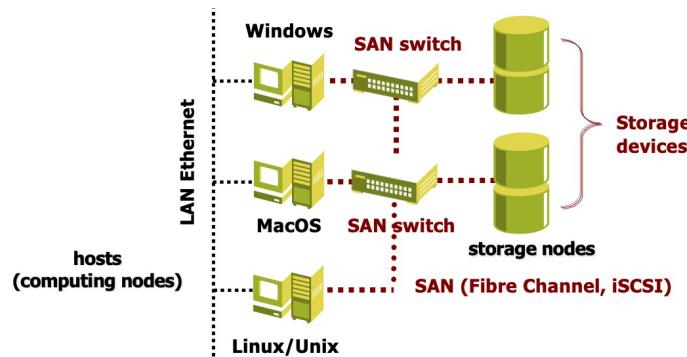


Figure 11: SAN architecture.

	Application Domain	Advantages	Disadvantages
DAS	<ul style="list-style-type: none"> <li>• Budget constraints</li> <li>• Simple storage solutions</li> </ul>	<ul style="list-style-type: none"> <li>• Easy setup</li> <li>• Low cost</li> <li>• High performance</li> </ul>	<ul style="list-style-type: none"> <li>• Limited accessibility</li> <li>• Limited scalability</li> <li>• No central management and backup</li> </ul>
NAS	<ul style="list-style-type: none"> <li>• File storage and sharing</li> <li>• Big Data</li> </ul>	<ul style="list-style-type: none"> <li>• Scalability</li> <li>• Greater accessibility</li> <li>• Performance</li> </ul>	<ul style="list-style-type: none"> <li>• Increased LAN traffic</li> <li>• Performance limitations</li> <li>• Security and reliability</li> </ul>
SAN	<ul style="list-style-type: none"> <li>• DBMS</li> <li>• Virtualized environments</li> </ul>	<ul style="list-style-type: none"> <li>• Improved performance</li> <li>• Greater scalability</li> <li>• Improved availability</li> </ul>	<ul style="list-style-type: none"> <li>• Costs</li> <li>• Complex setup and maintenance</li> </ul>

Figure 12: DAS vs. NAS vs. SAN

### 2.2.3 Networking (architecture and technology)

#### 2.2.3.1 Fundamental concepts

In the data centre, servers' *performance increases* over time, and the demand for inter-server *bandwidth also increases*.

One **initial solution** is to double the aggregate compute or storage capacity by **doubling the number of compute or storage elements**. The initial solution is horizontal scaling at the edge; we simply add more leaf switches with enough ports to handle the extra servers. However, **this only works locally because the fundamental issue is deeper**.

Since servers first connect to leaf switches, **adding twice as many servers results in twice as many ports on the leaf switches**. Thus, our **total edge bandwidth doubles**. For instance, if each leaf switch supports 40 servers at 1 Gbps, adding 40 more servers requires either an additional leaf switch or an expansion of the existing switch, doubling our total edge capacity. Thus, the **Leaf Bandwidth** is essentially the **sum of all connections between servers and their closest switches**.

❸ **What is the problem with this naïve solution?** The critical point is that doubling the leaf bandwidth **only handles server-to-leaf traffic**. However, if **all servers must be able to talk to all other servers**, traffic must cross the entire DCN (Data Center Network). This way, the middle of the network, the **bisection, is not scaled**. If every server wants to communicate with every other server, then there must be enough internal network capacity to support all of these connections simultaneously. In other words, doubling the bandwidth of the leaves is trivial (we just add ports), but **doubling the bisection bandwidth is not**.

#### ❹ **What is the bisection bandwidth?**

**Bisection Bandwidth** is the total **network bandwidth available** to carry traffic between two halves of a network if we split it down the middle.

Imagine our whole datacenter network is a grid of racks and switches. Draw an imaginary **line** that cuts it into two equal sides.

- All the network links **crossing that line** are our **bisection**.
- The **sum of the bandwidth of those links** is the **bisection bandwidth**.

In practice, this means that if **half of our servers** try to send data to the **other half simultaneously**, the **bisection bandwidth** tells us the **maximum total amount of traffic** that can be pushed across the split **at once**.

### Example 10: Bisection Bandwidth

Suppose:

- 100 servers in total, 50 on the left, 50 on the right.
- Between left and right sides, there are 10 uplinks of 10 Gbps each.

So Bisection Bandwidth =  $10 \text{ links} \times 10 \text{ Gbps} = 100 \text{ Gbps}$ . So:

- Max total traffic left  $\rightarrow$  right = 100 Gbps
- Max total traffic right  $\rightarrow$  left = 100 Gbps

If the servers try to send more than that across the split, packets get queued, then we get delays or packet drops.

## ② How to design a data center network? Design principles

There are many design principles to follow:

- **Very scalable** in order to support a vast number of servers;
- **Minimum cost** in terms of basic building blocks (e.g. switches);
- **Modular** to reuse simple basic modules;
- **Reliable and resilient**;
- It may exploit novel/proprietary technologies and protocols incompatible with legacy Internet.

The **Data Center Network (DCN)** connects a data centre's computing and storage units to achieve optimum performance. It can be **classified** into **three main categories**:

- **DCN Switch-centric architectures.** DCN uses switches to perform packet forwarding.<sup>4</sup>
- **DCN Server-centric architectures.** DCN uses servers with multiple Network Interface Cards (NICs)<sup>5</sup> to act as switches and perform other computational functions.
- **DCN Hybrid architectures.** DCN combines switches and servers for packet forwarding.

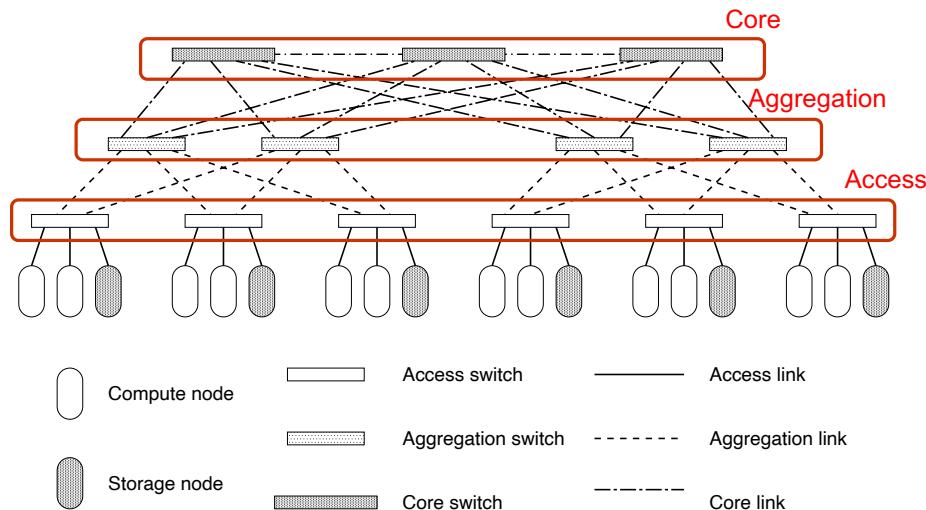
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<sup>4</sup>**Packet forwarding** is the passing of packets from one network segment to another by nodes on a computer network.

<sup>5</sup>A **Network Interface Cards (NICs)** is a computer hardware component that connects a computer to a computer network.

### 2.2.3.2 Switch-centric: classical Three-Tier architecture

The **Three-Tier architecture**, also called **Three Layer architecture**, configures the network in three different layers:



It is a simple Data Center Network topology.

- The servers are connected to the DCN through access switches.
- Each access-level switch is connected to at least two aggregation-level switches.
- Aggregation-level switches are connected to core-level switches (gateways).

#### ✓ Advantages

1. Bandwidth can be increased by increasing the switches at the core and aggregation layers, and by using routing protocols such as Equal Cost Multiple Path (ECMP) that equally shares the traffic among different routes.
2. Very simple solution.

#### 👎 Cons

1. Very expensive in large data centers because the upper layers require faster network equipments.
2. Cost very high in term of acquisition and energy consumption.

In the **access layer**, there are two possible architectures:

- **ToR (Top-of-Rack) architecture.** It is a **switching architecture** for connecting servers **inside a rack** to the rest of the datacenter network. The idea is simple, we place a **network switch at the top of each rack**, this is the **Top-of-Rack switch (ToR switch)**. All servers inside that rack connect **upwards** to that switch. The ToR switch then connects **upstream** to aggregation/core switches that connect the whole datacenter.

In other words, it **aggregates** all the server links in that rack.

### ✓ Advantages

1. **Simpler cabling** because the number of cables is limited. Short cables run only from each server up to the rack's top.
2. **Lower costs** because the number of ports per switch is limited.

### 👎 Cons

**Higher complexity** for switch management. Because there are more devices to manage (for example, with 100 racks, there are 100 top-of-rack switches) the control is distributed rather than centralized. This requires a more careful design to prevent loops or misconfigurations.

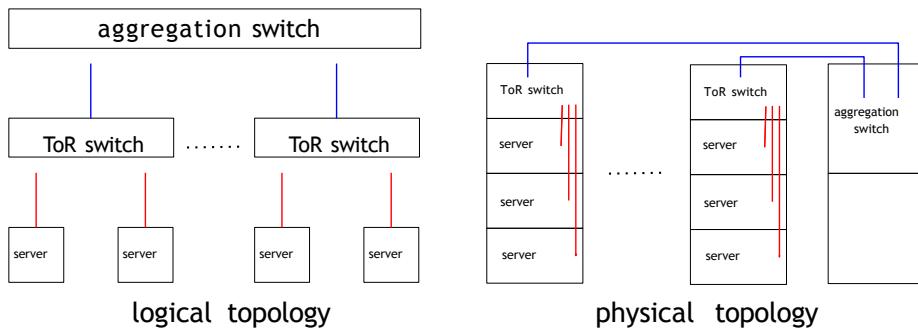


Figure 13: ToR (Top-of-Rack) architecture.

- **EoR (End-of-Row) architecture.** It is a classic **datacenter network architecture** for connecting racks of servers.

Instead of putting a small switch **inside each rack**, we put **one larger switch at the end of each row** of racks. Servers in each rack connect **horizontally** to this shared switch.

❓ **How does it work physically?** Imagine a row of 10 racks. Each rack has no ToR switch, instead:

- Servers in the rack have **longer cables** that run **horizontally** to the big EoR switch.
- That EoR switch aggregates all server connections from the whole row.

- The EoR switch then uplinks to the aggregation/core layer.

### ✓ Advantages

**Simpler switch management.**

### 👎 Cons

The aggregation switches must have a larger number of ports, then:

1. **Complex cabling:** Longer cables from every server to the end of the row.
2. **High risk with a fault:** If the EoR switch fails, then whole row loses network.
3. **Longer cables then higher costs.**

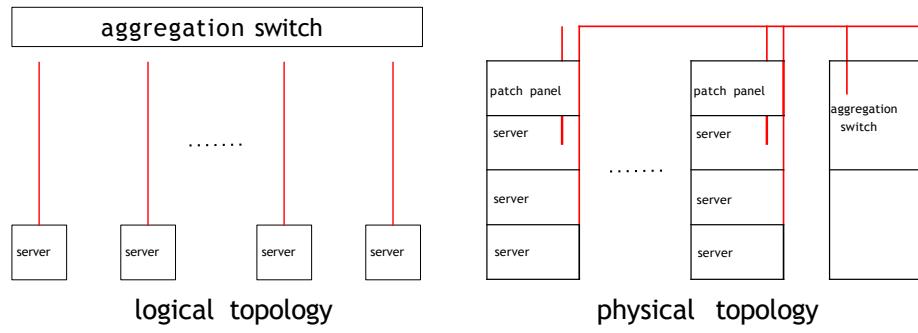


Figure 14: EoR (End-of-Row) architecture.

### 2.2.3.3 Switch-centric: Leaf-Spine architectures

The **Leaf-Spine Architecture** is a two-tier network topology used in modern data centers to handle massive **East-West traffic** and **maximize bisection bandwidth**.

- **Leaf switches** are the “bottom layer”. These are basically **ToR (Top-of-Rack)** switches, they connect directly to the servers in each rack.
- **Spine switches** are the “top layer”. These are high-capacity core switches. They interconnect all the Leaf switches with each other.

So every Leaf switch is connected to every Spine switch.

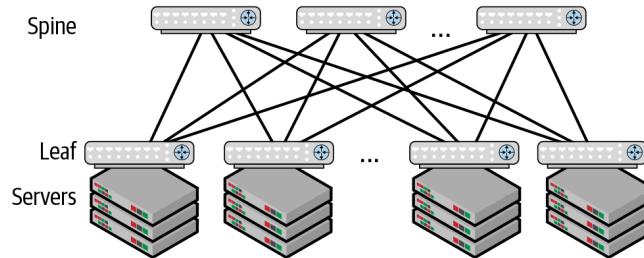


Figure 15: Leaf-Spine architecture.

❷ **What problem does it solve?** The classic 3-tier DCN designs (page 85) **don't scale bisection bandwidth linearly**. They easily become bottlenecks if many servers talk to each other. Leaf-Spine fixes this by:

- ✓ Providing multiple parallel paths between any two racks.
- ✓ Ensuring that **bandwidth stays predictable** as we add more racks and more spines.
- ✓ Using equal-cost multipath (ECMP) to load-balance flows across all available paths.

❸ **What is a Clos network, and how is it linked to leaf-spine architecture?**

Originally, the **Clos network** was invented by Charles Clos (1952) for telephone switches. It's a **multi-stage switching fabric** that allows us to build a big non-blocking switch **out of many small cheap switches**. The core idea: instead of one giant switch, we **connect multiple small switches in stages** to get scalable bandwidth **with multiple paths**. In datacenter networking, the **Clos design** maps naturally to modern switch hardware.

❹ **Why is Clos good for datacenters?** In huge datacenters:

- We want **full bisection bandwidth**: any server can talk to any other at line rate.

- We can't build a single giant switch with thousands of ports, that's impractical.
- Instead, we interconnect many small switches in a **Clos-like fabric** to provide multiple paths and load balancing.

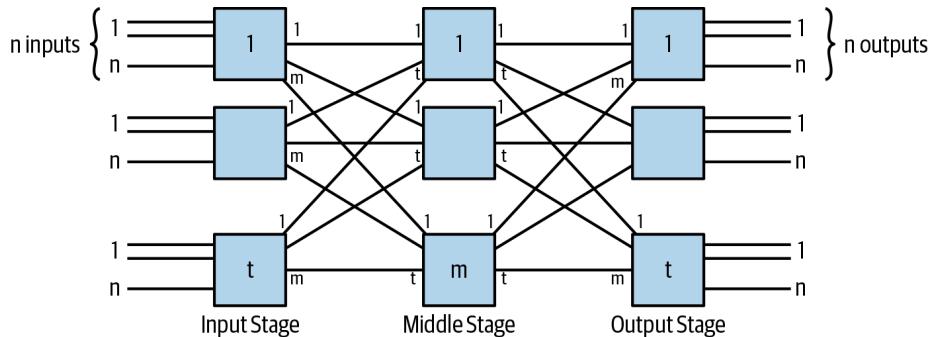
**Q How does the Leaf-Spine topology come from Clos?** Leaf-Spine is basically the **simplest practical version** of a 2-stage or 3-stage **Clos network**, tailored for Ethernet.

**❖ Formal Definition.** A **Clos network** is a **multi-stage interconnection network** defined by three integers:

- $n$ : number of inputs per input module.
- $m$ : number of middle-stage switches.
- $k$ : number of output ports per output module.

A classic 3-stage Clos is defined as  $C(n, m, k)$ :

- Stage 1:  $k$  input modules, each with  $n$  input ports.
- Stage 2:  $m$  middle-stage switches.
- Stage 3:  $k$  output modules, each with  $n$  output ports.



- Each input module connects to every middle-stage switch.
- Each middle-stage switch connects to every output module.
- So every path crosses: 1 input module, 1 middle-stage switch, 1 output module.

This network has two main non-blocking conditions:

- The Clos network is **rearrangeably non-blocking** if:  $m \geq n$  (number of middle-stage switches is greater or equal than number of inputs per input module). So **we can rearrange connections to always find a path**.

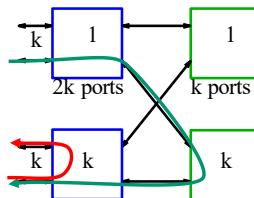
- The Clos network is **strictly non-blocking** if:  $m \geq 2n - 1$  (the number of middle-stage switches is greater than or equal to twice the number of inputs per input module minus one).

We **mapped** the **Clos network** in data centers **to the leaf-spine architecture**:

- The **input modules** become the **Leaf switches**.
- The **middle-stage** switches become the **Spine switches**.
- The **output modules** fold back to the same Leafs (because Ethernet is bidirectional).

They often simplify by setting:  $n = m = k$ . The Leaf-Spine architecture now has:

- Each **Leaf** switch has  **$2k$  bidirectional ports**:
  - $k$  ports to servers (down).
  - $k$  ports up to the Spines.
- Each **Spine** switch has  **$k$  bidirectional ports**: one link to each Leaf.



In order to achieve **full bandwidth**, **each Leaf must be connected to each Spine**. So the total number of **uplinks per Leaf** is equal to the number of Spines.

In summary:

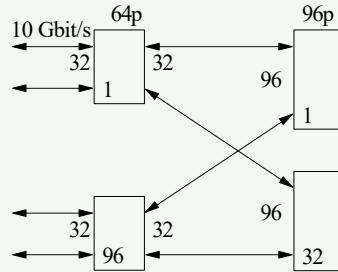
$$\begin{cases} \text{Leaves: } 2k \text{ bidirectional ports} \\ \text{Spines: } k \text{ bidirectional ports} \\ \text{Every Leaf connects to every Spine} \\ \text{Full bisection if } m \geq k. \end{cases}$$

### Example 11: DNC design

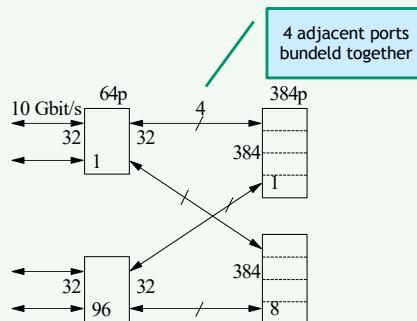
There are 3072 servers and 3072 ports available at 10 Gbit/s. Provides a leaf-spine design.

There are **two possible designs**.

1. The first consists of 96 switches with 64 ports and 32 switches with 96 ports.



2. The second has only 8 switches but they have more ports: 384 ( $8 \times 384 = 3072$ ).

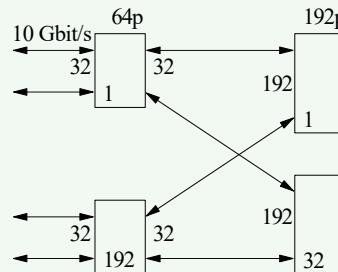


### Example 12: DNC design

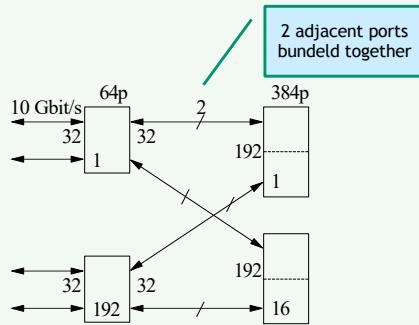
There are 6144 servers and 6144 ports available at 10 Gbit/s. Provides a leaf-spine design.

There are **two possible designs**.

1. The first consists of 192 switches with 64 ports and 32 switches with 192 ports.



2. The second has only 16 switches but they have more ports: 384 ( $16 \times 384 = 6144$ ).



### ❓ Why do we scale to a 3-tier Clos?

When our datacenter gets **huge**, even a classic 2-tier Leaf-Spine hits limits:

- The number of **uplinks per Leaf** is fixed by switch port count.
- The number of Spines we can connect to is also limited by the port count on the Spines.

So to connect *thousands* of racks at full bisection bandwidth, we need more stages. This is exactly what the **Fat-Tree (or 3-stage Clos)** solves.

A **Fat-Tree (or 3-stage Clos)** is just a multi-level **Clos network** where link capacity *increases* closer to the core, so the “tree” looks **fat** in the middle. The key idea is:

- Small switches at the **edge**.
- Bigger bandwidth links and more switches at the **aggregation and core layers**.
- So the middle of the network doesn’t become a bottleneck.

It is called “fat” because, in a normal tree, the higher up we go, the fewer branches there are, creating bottlenecks. In a Fat-Tree, we keep adding enough parallel links/switches so total bandwidth stays equal across any “slice”. So every layer has enough capacity to preserve full bisection bandwidth.

### ❓ How it works? 3-tier.

A classic Fat-Tree has:

- **Edge (Leaf)**: ToR switches in racks, connect to servers and Aggregation.
- **Aggregation (Middle)**: Aggregate Leafs, uplink to Core.
- **Core (Spine/Superspine)**: Connect Aggregations together.

So it's basically a Clos  $C(n, m, k)$ :

Edge stage → Middle stage → Core stage → Middle stage → Edge

### 💡 Why do we call it Pod-based?

When we have *thousands* of racks, it's unmanageable to think of *one giant switch fabric*. So we divide the whole fabric **into repeated building blocks** called Pods. A **PoD (Point of Delivery)**, in datacenter design, is a **modular, repeatable unit** of:

- Racks + Power + Leaf + Aggregation Switches.
- Often also cooling and structured cabling.

A POD is like a **mini-datacenter inside the datacenter**.

### 📘 A Scalable, Commodity Data Center Network Architecture [1]

The paper “*A Scalable, Commodity Data Center Network Architecture*” [1] explains a famous datacenter Clos design that shows how we can build a **non-blocking DCN** with commodity switches. The idea is:

- We have a **fixed switch port count**: each switch has  $k$  ports.
- The goal is to **connect as many servers as possible** with full bisection bandwidth, no oversubscription<sup>6</sup>.
- The Fat-Tree does this by arranging switches in **pods** and a **core layer**.

In the classic Fat-Tree, we choose:  $P = 2k$ , where  $P$  is the number of **pods**, and  $k$  is the **number of ports per switch**. All switches are assumed to be the same commodity switch.

Each **pod** has:

- $k$  Edge switches. Each edge switchL
  - Connects **down** to servers:  $\frac{k}{2}$  ports.
  - Connects **up** to Aggregations:  $\frac{k}{2}$  ports.
- $k$  Aggregation switches. Each Aggregation switch:
  - Connects **down** to Edge:  $\frac{k}{2}$  ports.
  - Connects **up** to Core:  $\frac{k}{2}$  ports.

<sup>6</sup>Oversubscription is when the total potential demand for bandwidth exceeds the actual available capacity. It's like building a highway with fewer lanes than the number of cars that could be on it, because we're betting not everyone will drive at once.

So each Edge switch connects to:

$$\frac{k}{2} \text{ servers} + \frac{k}{2} \text{ uplinks} = k \text{ total ports}$$

**Total servers per pod:**

$$k \text{ Edge switches} \times \frac{k}{2} \text{ servers each} = \frac{k^2}{2}$$

But because there are  $P$  pods, the total servers are:

$$\text{Total servers} = \underbrace{\frac{k^2}{2}}_{\text{per pod}} \times P$$

However, we adopted a generalized variant:

$$\text{Total servers} = k^2 P \quad (18)$$

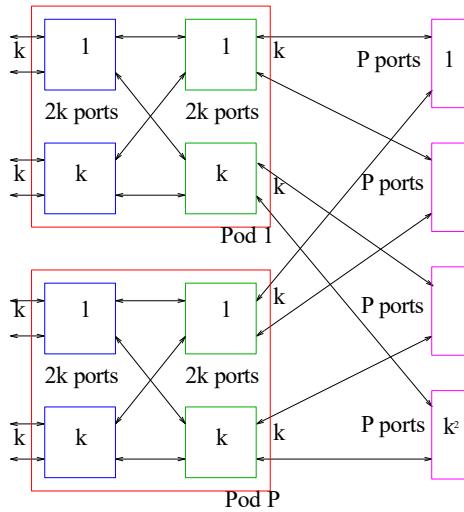


Figure 16: Explanation of Fat-Tree Network.

### Example 13: Fat-Tree with $2k$ pods and $k = 2$

Suppose a Fat-Tree has  $2k$  pods:  $P = 2k$ . Each pod has its Edge and Aggregate layers. The core ties all pods together.

- If  $P = 2k$ , then the total servers are:

$$\text{Total servers} = k^2 \times P = k^2 \times 2k = 2k^3$$

So the  $k$ -ary Fat-Tree connects  $2k^3$  servers.

- If each pod:

$$k\text{Edge} + k\text{Aggregation} \Rightarrow 2k\text{switches}$$

With  $P$  pods, we have  $2k \cdot P$  switches in pods. Also, at the Core layer we have  $k^2$  Core switches. So **total switches**:

$$2kP + k^2 \xrightarrow{P=2k} 2k \cdot (2k) + k^2 = 4k^2 + k^2 = 5k^2$$

For  $k = 2$ , we have:

- $P = 4$  pods.
- Core:  $k^2 = 2^2 = 4$  switches.
- Total servers:  $2k^3 = 2 \times 2^3 = 16$ .
- Total switches:  $5k^2 = 5 \times 4 = 20$ .

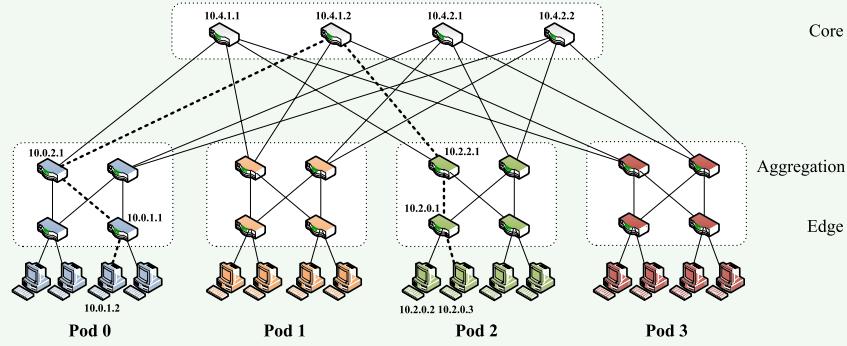


Figure 17: Simple fat-tree topology. Using the two-level routing tables, packets from source 10.0.1.2 to destination 10.2.0.3 would take the dashed path. [1]

Classic  $k$ -ary Fat-Tree:

$$\left\{ \begin{array}{l} P = 2k, \\ \text{Total servers} = 2k^3, \\ \text{Total switches} = 5k^2, \\ \text{Core switches} = k^2, \\ \text{Pods} = 2k. \end{array} \right.$$

### 2.2.3.4 Server-centric and hybrid architectures

In **server-centric** architectures:

- The servers themselves **help do the routing** and **forward traffic**.
- The network topology is built **partly in software**, with direct server-to-server links.
- Switches are minimal or even absent, the servers form the fabric.

So the key idea is that servers are not passive endpoints, but they **actively forward packets** for each other.

#### 💡 CamCube: a concrete example

**CamCube** was an experimental **server-centric datacenter network** developed at the University of Cambridge around 2010. The key features are:

- Each server has multiple NICs.
- Servers are connected in a **3D torus** or **cube-like mesh** (hence “CamCube”).
- There are **no traditional switches**, servers route packets directly to each other.

A CamCube server has **several network ports** (e.g., 6 in the 3D grid). Links go **directly to neighboring servers**. Packets hop from server to server, using custom routing software running **on the servers themselves**. Routing decisions are done in the OS or application layer.

#### ❓ Why do this?

- Reduce or eliminate expensive switches.
- Achieve high bisection bandwidth using cheap NICs and cables.
- Expose the **topology directly to applications**, so apps can optimize data placement and routing.

For example, a key-value store could decide to place replicas on “neighbor” servers in the CamCube coordinate space to minimize hops.

#### ✓ Advantages

- Cheap commodity hardware (just NICs and cables).
- Flexible (easy to experiment with custom routing).
- Tight integration between network and application logic.

### 👎 Disadvantages

- Adds **routing overhead** on servers.
- Makes the OS and application design more complex.
- Harder to scale wiring neatly, 3D torus cabling is tricky in real racks.
- Server failure impacts routing, so resilience needs extra software.

The hybrid architectures are **DCell**, **BCube** and **MDCube**.

### ❓ What is DCell?

**DCell** is a **server-centric datacenter network** proposed by Microsoft Research (Guo et al., 2008). The key idea is build a large-scale datacenter network **without big switches**, using small commodity switches and **servers inter-connecting themselves recursively**.

In DCell each **server** is connected to:

- A **mini switch** (commodity, dumb, small, no big core).
- **Other servers directly**, in a clever recursive pattern.

The result is a **highly scalable, fault-tolerant topology** built by **recursively composing many small building blocks**. The core concept is **recursive construction**. We start with a  $\text{DCell}_0$ , the basic unit, then **combine multiple DCells into bigger DCells**.

1.  $\text{DCell}_0$ , smallest unit. Contains  $n$  servers and one mini switch. Inside:
  - Each server has one port to the switch (for local communication).
  - Each server has **one more port** for direct links to other DCells.
2.  $\text{DCell}_1$ , we take  $k = n + 1$   $\text{DCell}_0$  units. Connect them **directly** using the extra server ports, and each server has direct links to other DCells.
3.  $\text{DCell}_2$ , we take  $k = n + 1$   $\text{DCell}_1$  units. Connect them recursively in the same way.

And so on. At each level, the network expands **exponentially**.

### ✅ Advantages

- **Scalability**: The recursive structure lets us scale to hundreds of thousands of servers using small switches and extra server NICs.
- **Server-centric**: Servers handle routing logic, they decide how to forward packets to reach other servers.
- **Fault tolerance**: Many redundant paths. If one server or link fails, routing can find alternate paths.

### 👎 Disadvantages

- Needs extra NICs per server, then **more cabling complexity**.
- Routing at server level adds **CPU overhead**.
- Recursive **cabling** can be operationally **hard** at large physical scales.
- **Performance can degrade if too many servers fail**, the fault tolerance is not free.

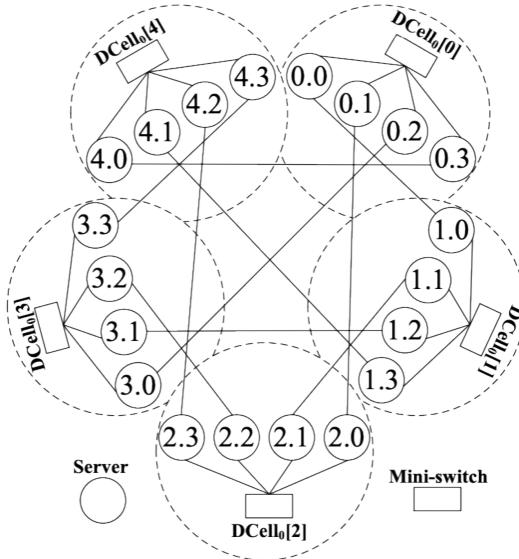


Figure 18: DCell hybrid architecture.

### ❓ What is BCube?

**BCube** is a **server-centric datacenter network topology** proposed by Microsoft Research (Guo et al., 2009), same lab that proposed DCell. It was designed specifically for **modular datacenters**, think **container-based clusters** or shipping container datacenters.

Like DCell, BCube:

- Uses **commodity mini-switches** (no big expensive core switches).
- Gives each server **multiple NICs**.
- Builds high bisection bandwidth by **using direct server-switch-server paths**.

But instead of recursive hierarchy (DCell), BCube uses a **layered, multi-level cube-like structure with structured direct links**.

### ✓ Advantages

- **Server-centric:** servers handle multi-path routing.
- **High fault tolerance:** if one path fails, many alternative switch levels are available.
- **Great for modular scale:** we can design BCube units as self-contained shipping containers.
- **Full bisection bandwidth:** as we add levels, we add more disjoint paths.

### 👎 Disadvantages

- **Limited scalability.**
- **High cabling costs.**

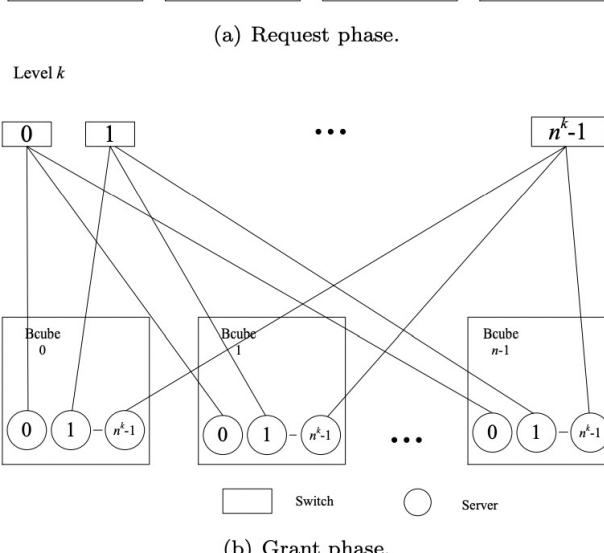
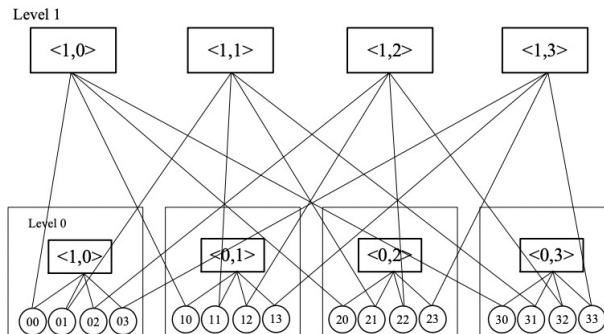


Figure 19: BCube hybrid architecture.

### ❓ What is MDCube?

MDCube is a **modular datacenter network architecture** that combines multiple BCubes into a higher-level *interconnected cube*. It's literally: **Modular Datacenter Cube (MDCube)**. Proposed by the same researchers (Microsoft Research, 2011) to tackle the problem: “*BCube works well for modular, container-sized datacenters; but what if we need to scale to mega-datacenters built from many BCube containers?*”.

Each **BCube** is treated as a **building block**. We interconnect multiple BCubes in a **higher-level topology** (like a hypercube or torus). The result is a **multi-level hybrid**:

- Inside: each module is a BCube.
- Outside: the modules are linked by structured interconnects.

MDCube is **hybrid** because:

- It combines **server-centric routing** inside the BCube.
- It uses **structured interconnects** *between* modules, like classic network topologies.
- It blends **switch-centric** commodity switches (inside BCube) with **server centric** direct links (between BCubes).

### ✅ Advantages

- Keeps switch cost low.
- Good for container-based datacenters.

### ❗ Disadvantages

Still operationally tricky, then many NICs, custom routing software.

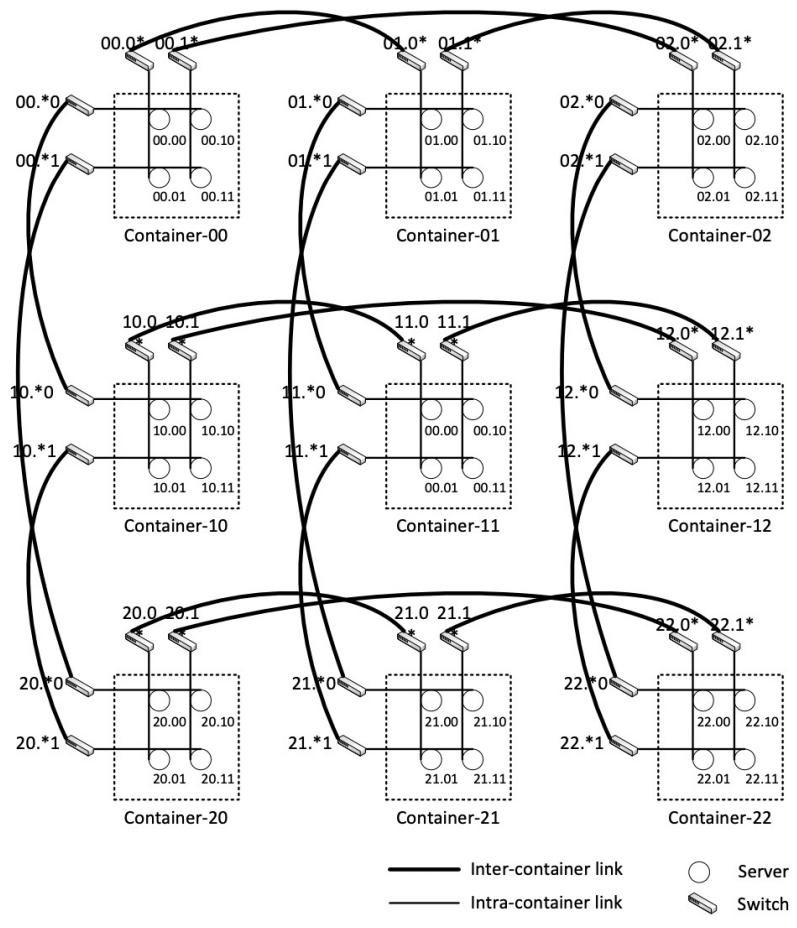


Figure 20: MDCube hybrid architecture.

### 2.3 Building level

The main components of a typical data center are:

- Cooling system (blue):
  - Water storage
  - Cooling towers
  - Chillers
  - Fan coil air handling units
- Power supply (red):
  - Utility power
  - Transformers
  - Backup generation/power distribution
  - Power bus
- Computation storage networking (green):
  - Networking room

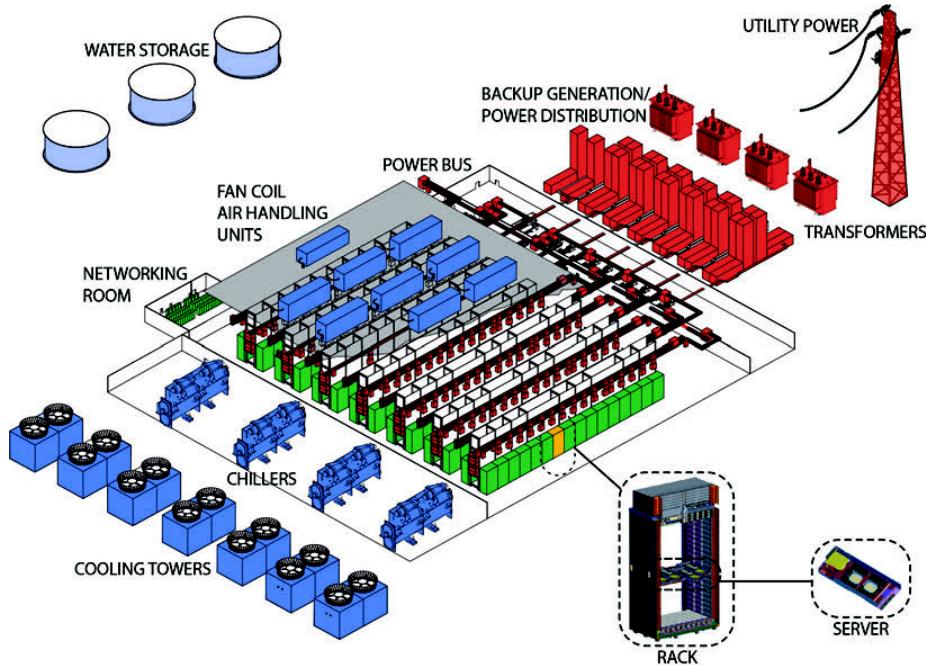


Figure 21: The main components of a typical data center. [2]

The warehouse scale computer or data centre has other important components related to **power delivery**, **cooling** and **building infrastructure** that also need to be considered.

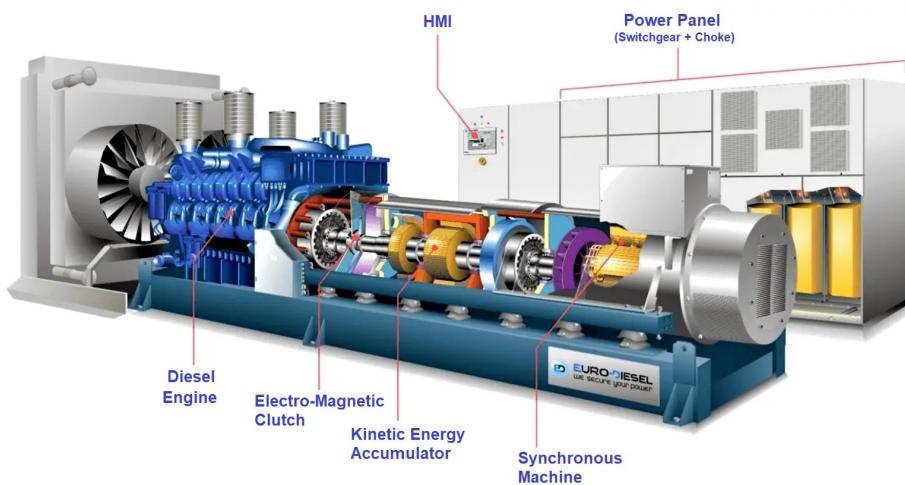


Figure 22: A Rotary UPS system.

In order to protect against power failure, battery and diesel generators are used to back up the external supply.

A **UPS (uninterruptible power supply or source)** is a **continual power system that provides automated backup electric power to a load when the input power source or mains power fails**. There are many types of UPS, but in general, in the DC, the **Rotary UPS system** is used.

A rotary UPS uses the inertia of a high-mass spinning flywheel to provide short-term ride-through in the event of power loss.

### 2.3.1 Cooling systems

The IT equipment generates a lot of heat. To avoid troubles, cooling systems have been installed. Unfortunately, they are costly components of the data center, and they are composed of **coolers**, **heat exchangers** and **cold water tanks**.

Some techniques exist to improve cooling systems without throwing away too much money.

**Open-Loop systems** refer to the **use of cold outside air to either help the production of chilled water or directly cool servers**. It is not entirely free in the sense of zero cost, but it involves **very low energy costs** compared to chillers.

**Closed-Loop systems** come in many forms, the most common being the air circuit on the data centre floor. It is grouped by number of loops:

- **One loop.** The **main goal is to isolate and remove heat from the servers and transport it to a heat exchanger**. So the cold air flows to the servers, heats up, and eventually reaches a heat exchanger to cool it down again for the next cycle through the servers.

#### ✓ Advantages

It can be very efficient.

#### ⚠ Cons

- It doesn't work in all climates;
- It requires filtering of airborne particulates;
- Can introduce complex control problems.

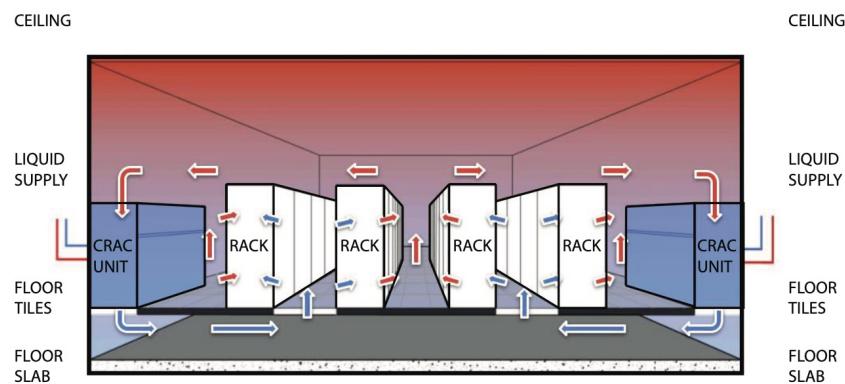
- **Two loops.** The airflow through the underfloor plenum, the racks, and back to the **CRAC (computer room air conditioning)** defines the primary air circuit as the first loop. The second loop (the liquid supply inside the CRAC units) leads directly from the CRAC to the external heat exchangers (typically placed on the building roof) that discharge the heat to the environment.

#### ✓ Advantages

- Easy to implement;
- Relatively inexpensive to construct;
- Offers isolation from external contamination.

#### ⚠ Cons

Typically have lower operational efficiency.



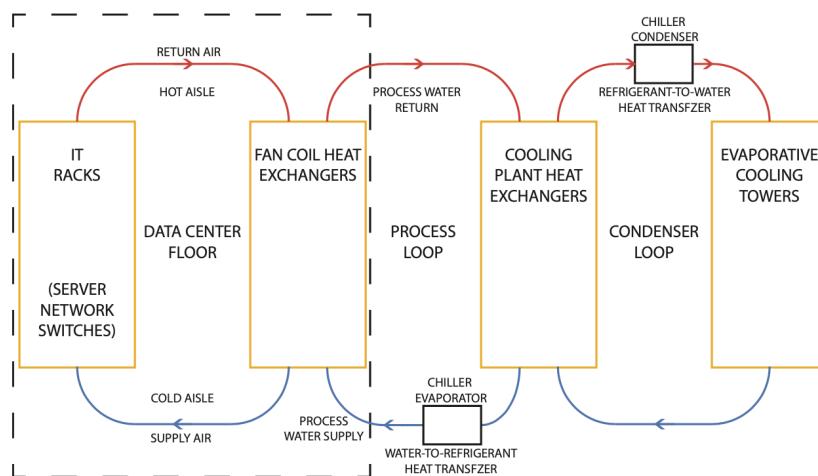
- **Three loops.** It is used in large-scale data centres. The architecture can be viewed in the following figure.

#### ✓ Advantages

- It offers contaminant protection;
- It offers good efficiency.

#### ⚠ Cons

- It is the most expensive to construct;
- It has moderately complex controls.



First loop to the left, second loop in the middle and third loop to the right.

### 💡 How each rack is cooled?

There are three ways to cool each rack:

- **In-Rack cooler.** It adds an air-to-water heat exchanger at the back of a rack so the hot air exiting the servers immediately flows over coils cooled by water, reducing the path between server exhaust and CRAC input.
- **In-Row cooling.** It works like in-rack cooling, except the **cooling coils** are not in the rack but **adjacent to the rack**.

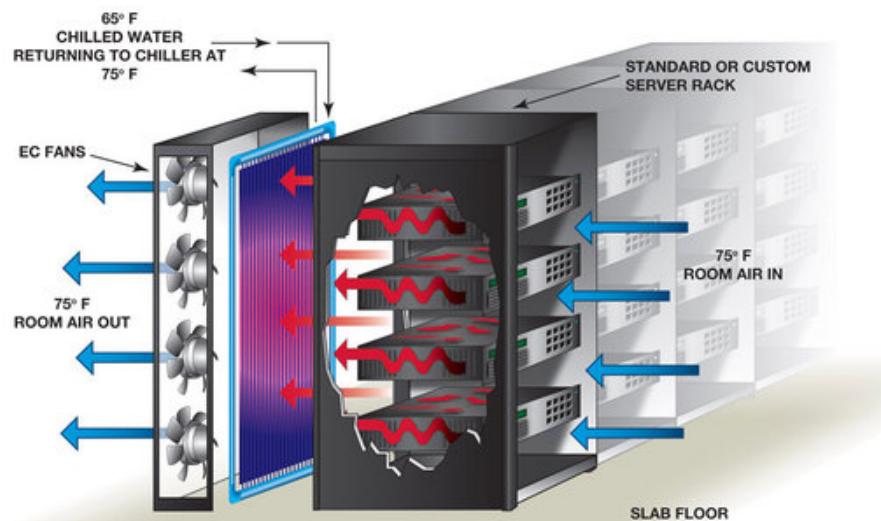


Figure 23: In-Row Cooling Mechanism (source: [Energy Start](#)).

- **Liquid cooling.** We can directly cool server components using cold plates. The liquid circulating through the heat skins transports the heat to a liquid-to-air or liquid-to-liquid heat exchanger that can be placed close to the tray or rack or be part of the data centre building (such as a cooling tower).

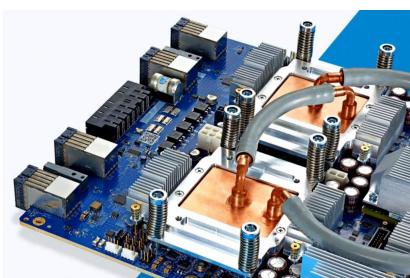


Figure 24: Liquid Cooling Mechanism.

### 2.3.2 Power supply

#### ② What is the problem?

Data centre power consumption is an issue since it can reach several milliwatts. **Cooling usually requires about half the energy the IT equipment requires** (servers + network + disks). Finally, **energy transformation also wastes** much energy when running a data centre.

#### ③ Is there a metric to measure energy efficiency?

First of all, **no!** Several metrics are helpful to understand how a data centre spends in terms of energy.

One of the most critical metrics is **Power Usage Effectiveness (PUE)**. It is the **ratio of the total amount of energy used by a DC facility to the energy delivered to the computing equipment**:

$$\text{PUE} = \frac{\text{Total Facility Power}}{\text{IT Equipment Power}} \quad (19)$$

Where the **Total Facility Power** is calculated as:

$$\text{TFP} = \text{covers IT systems} + \text{other equipment} \quad (20)$$

Where the covers IT systems are servers, network, storage, and other equipment are cooling, UPS, switch gear, generators, lights, fans.

Finally, the **Data Center Infrastructure Efficiency (DCiE)** is the inverse of PUE:

$$\text{DCiE} = \text{PUE}^{-1} = \frac{\text{IT Equipment Power}}{\text{Total Facility Power}} \quad (21)$$

For **example**, the level of efficiency is shown here:

PUE	DCiE	Level of Efficiency
3.0	33%	Very Inefficient
2.5	40%	Inefficient
2.0	50%	Average
1.5	67%	Efficient
1.2	83%	Very Efficient

### 2.3.3 Data Center availability

The Data Center availability is defined by in four different tier level. Each one has its own requirements:

Tier Level	Requirements
1	<ul style="list-style-type: none"> <li>• Single non-redundant distribution path serving the IT equipment.</li> <li>• Non-redundant capacity components.</li> <li>• Basic site infrastructure with expected availability of 99.671%.</li> </ul>
2	<ul style="list-style-type: none"> <li>• Meets or exceeds all Tier 1 requirements.</li> <li>• Redundant site infrastructure capacity components with expected availability of 99.741%.</li> </ul>
3	<ul style="list-style-type: none"> <li>• Meets or exceeds all Tier 2 requirements.</li> <li>• Multiple independent distribution paths serving the IT equipment.</li> <li>• All IT equipment must be dual-powered and fully compatible with the topology of a site's architecture.</li> <li>• Concurrently maintainable site infrastructure with expected availability of 99.982%.</li> </ul>
4	<ul style="list-style-type: none"> <li>• Meets or exceeds all Tier 3 requirements.</li> <li>• All cooling equipment is independently dual-powered, including chillers and heating, ventilating and air conditioning (HVAC) systems.</li> <li>• Fault-tolerant site infrastructure with electrical power storage and distribution facilities with expected availability of 99.995%.</li> </ul>

Table 10: Data Center availability.

## 3 Software Infrastructure

### 3.1 Virtualization

#### 3.1.1 What is a Virtual Machine?

A **Virtual Machine (VM)** is a **logical abstraction** able to **provide a virtualized execution environment**. More specifically, a VM:

- Provides identical software behavior
- Consists in a combination of physical machine and virtualizing software
- May appear as different resources than physical machine
- May result in different level of performances

Exists two type of Virtual Machine: Process VM (page 111) and System VM (page 112).

#### ❓ What's the difference between a physical machine and a virtual machine?

First of all, the **physical machine** is the computer that can **host n virtual machines**.

Furthermore, every VM is based on hypervisor software (also known as a virtual machine manager or monitor VMM, page 114). The hypervisor runs as an application on the host operating system (hosted hypervisor) or rests directly on the hardware of the physical machine (bare-metal hypervisor) and manages the hardware resources provided by the host system. The **hypervisor software creates an abstraction layer between physical hardware and virtual machines. Each VM runs isolated from the host system and other guest systems on its own virtual environment.** This is referred to as encapsulation.

Processes within a virtual machine do not affect the host or other VMs on the same hardware.

So, to sum up:

1. **Physical machines** are the computers that can **host n virtual machines**.
2. Each **physical machine has a hypervisor (VMM)** already enabled or asleep on the hardware. **It manages the resources made available by the physical machine.**
3. Each **virtual machine has its own virtual environment**, so they are **encapsulated, isolated environments.**

Obviously, the statement is not true if there is a “*virtual machine escape attack*”, but we don’t count those extreme cases. [9]

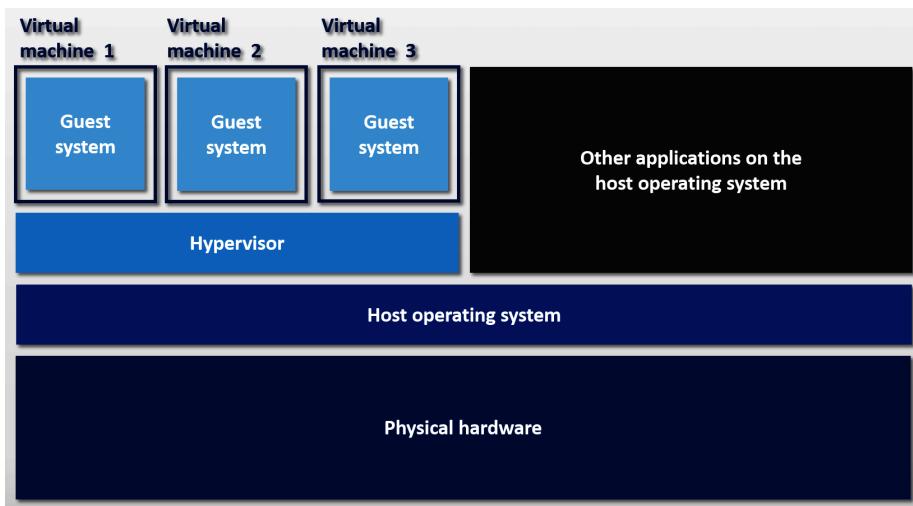


Figure 25: Operating system view if there are VMs in the physical machine  
(source: [ionos](#)).

A little terminology about *host* and *guest*:

- **Host**: the underlying platform supporting the environment/system.
- **Guest**: the software that runs in the Virtual Machine environment as the guest.

### 3.1.1.1 Process VM

A **Process Virtual Machine**, sometimes called an application virtual machine, or Managed Runtime Environment (MRE), **runs as a normal application inside a host OS and supports a single process**.

The **Virtual Machine is created when that process begins and destroyed when it ends**. A good example is the Java Virtual Machine JVM (see more [here](#)).

The purpose of a process VM is to execute a computer program in a platform-independent environment, meaning it can run on a variety of hardware or software.

The virtualizing software:

- is placed at the ABI<sup>7</sup>, on top of the OS/hardware combination.
- emulates both user-level instructions and operating system calls.
- is usually called Runtime Software.

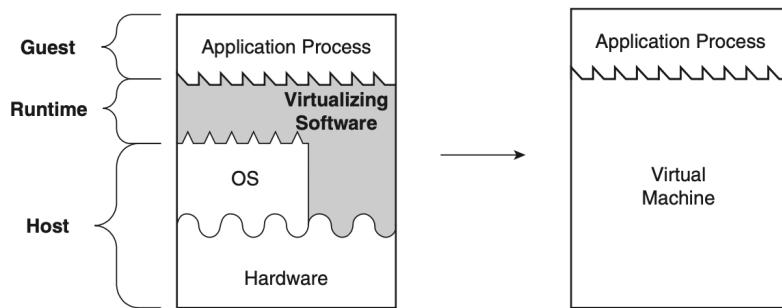


Figure 26: Process VM.

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<sup>7</sup>An **Application Binary Interface (ABI)** corresponds to “*Operating system machine level*”.

### 3.1.1.2 System VM

**System Virtual Machines** are substitutes for real machines and **provide all the functionalities of an actual operating system**. It provides operating system running in it access to underlying hardware resources (networking, I/O, GUI).

With a system VM, the hypervisor will access the underlying machine's resources, giving the user the same capabilities the host device offers.

The **virtualization software is called Virtual Machine Monitor (VMM)**.

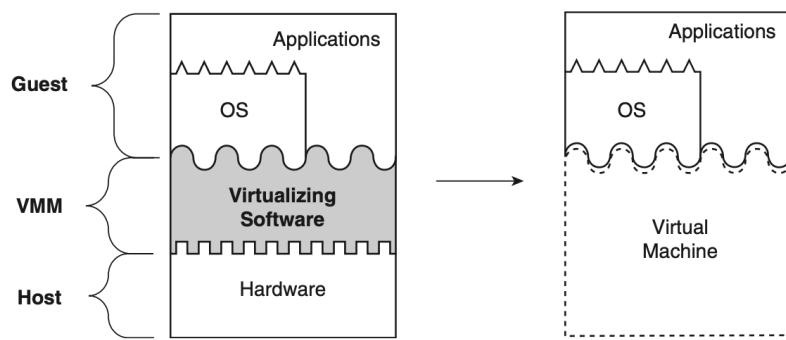


Figure 27: System VM.

### 3.1.2 Virtualization Implementation

Consider a typical layered architecture of a system by adding layers between layers of the execution stack. Depending on where the new layer is placed, we get different types of virtualization. The virtualization technologies are:

- **Hardware-level virtualization.** The **virtualization layer is placed between hardware and OS**. The interface seen by OS and application might be different from the physical one.
- **Application-level virtualization.** The **virtualization layer is placed between the OS and some application** (e.g. JVM). It provides the same interface to the applications. The applications run in their environment, *independently* from OS.
- **System-level virtualization.** The **virtualization layers provides the interface of a physical machine to a secondary OS and a set of application running in it, allowing them to run on top of an existing OS**. It is placed between the system's OS and other OS (e.g. VMware, VirtualBox). We can enable several OSs to run on a single hardware.

The properties of virtualization technologies are:

- **Partitioning**
  - Execution of multiple OSs on a single physical machine;
  - Partitioning of resources between the different VMs.
- **Isolation**
  - Fault tolerance and security (hardware level);
  - Advanced resource control to guarantee performance (managed by the hypervisor).
- **Encapsulation**
  - The entire state of a VM can be saved in a file (e.g. freeze and restart the execution);
  - Because a VM is a file, can be copied/moved as a file.
- **Hardware independence**
  - Provisioning/migration of a given VM on a given physical server.

### 3.1.3 Virtual Machine Managers (VMM)

A **Virtual Machine Manager (VMM)** is an application that:

- **Manages the VMs;**
- **Mediates access to the hardware resources** on the physical host system;
- **Intercepts and handles any privileged or protected instructions issued by the VMs.**

This type of virtualization typically runs virtual machines whose operating system, libraries, and utilities have been compiled for the same type of processor and instruction set as the physical machine on which the virtual systems are running.

Note that the Virtual Machine Manager (VMM) can be referred to by different names and also different meanings:

- **Virtual Machine Manager (VMM).** The virtualization software.
- **Virtual Machine Monitor.** A virtualization software that runs directly on the hardware.
- **Hypervisor.** A VMM or Hypervisor that is also used to create, configure and maintain virtualized resources. It provides a user-friendly interface to the underlying virtualization software.

There are two types of hypervisor:

- **Type 1 Hypervisor or Bare Metal Hypervisor** (or **Native Hypervisor**). The term *bare metal* refers to the fact that **there is no operating system between the virtualization software and the hardware**. The virtualization software resides on the “bare metal” or the hard disk of the hardware, where the operating system is usually installed.

Then, the **hypervisor takes direct control of the hardware**.

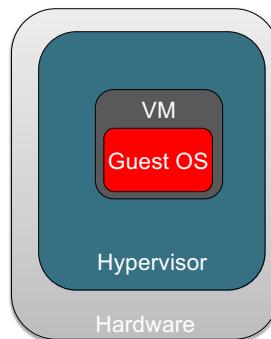


Figure 28: View of the Bare Metal Hypervisor.

Bare Metal Hypervisors can also be **built in two ways**:

- **Monolithic architecture.** Device drivers run within the hypervisor.

 **Advantages**

- \* Better **performance**.
- \* Better **isolation**.

 **Disadvantages**

- \* Can run only on **hardware** for which the **hypervisor has drivers**.

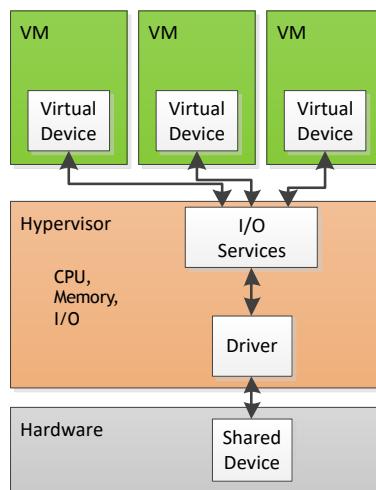


Figure 29: Monolithic architecture.

- **Microkernel architecture.** Device drivers run within a service virtual machine.

 **Advantages**

- \* **Smaller hypervisor.**
- \* **Leverages driver ecosystem** of an existing OS.
- \* Can use **third party driver** even if not always easy, recompiling might be required.

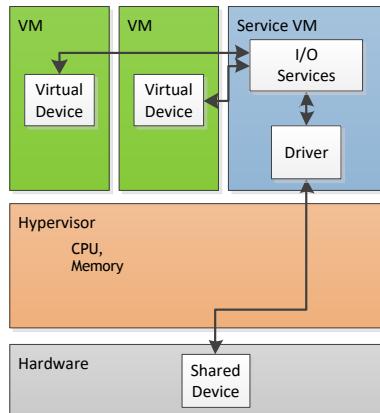


Figure 30: Microkernel architecture.

- **Type 2 Hypervisor or Hosted Hypervisor.** Hosted Hypervisors run within the operating system of the host machine. Although hosted hypervisors run within the OS, additional operating systems can be installed on top of it. Hosted hypervisors have higher latency than bare metal hypervisors because requests between the hardware and the hypervisor must pass through the extra layer of the OS.

This type of hypervisor is also called *hosted hypervisor*. Furthermore, the *Guest OS* is the one that runs in the VM, while applications run in the *Guest OS*. The *Host OS* controls the hardware of the system.

#### ✓ Advantages

- More flexible in terms of underlying hardware.
- Simpler to manage and configure.

#### 👎 Disadvantages

- The *Host OS* might consume a non-negligible set of physical resources.

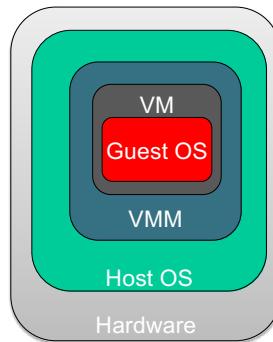


Figure 31: View of the Hosted Hypervisor.

The data is taken from [VMware](#).

### 3.1.3.1 Full virtualization

**Full virtualization** is a virtualization technique that **provides a complete simulation of the underlying hardware**.

In full virtualization, the **original operating system runs without knowing it's virtualized**, using translation to handle system calls.

In full virtualization, the **virtual machine completely isolates the guest OS from the virtualization layer and hardware**.

#### ✓ Advantages

- Running unmodified OS.
- Complete isolation.

#### 👎 Disadvantages

- Performance.
- Hypervisor mediation to allow the guest (or guests) and host to request and acknowledge tasks which would otherwise be executed in the virtual domain.
- Not allowed on all architectures.

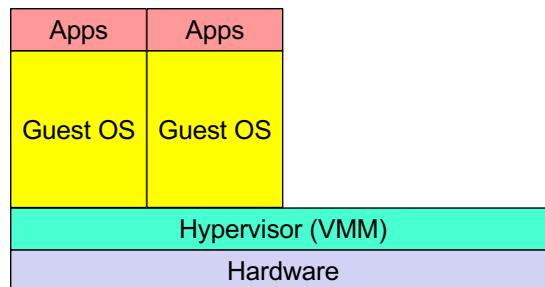


Figure 32: View of the Full Virtualization.

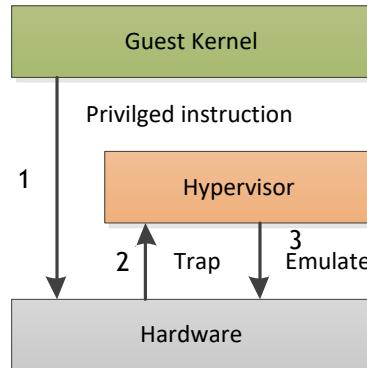


Figure 33: Full Virtualization flow.

### 3.1.3.2 Paravirtualization

**Paravirtualization** modifies the OS to use hypercalls instead of certain instructions, making the process more efficient but requiring changes before compiling.

Paravirtualization is a virtualization technique that uses hypercalls for operations to handle instructions at compile time. In paravirtualization, *guest OS* is not completely isolated but it is partially isolated by the virtual machine from the virtualization layer and hardware. VMware and Xen are some examples of paravirtualization.

Guest OS and VMM collaborates:

- VMM present to VMs an interface similar but not identical to that of the underlying hardware.
- To reduce guest's executions of tasks too expensive for the virtualized environment (by means of “**hooks**” to allow the guest(s) and host to request and acknowledge tasks which would otherwise be executed in the virtual domain, where execution performance is worse).

#### ✓ Advantages

- Simpler VMM.
- High Performance.

#### 👎 Disadvantages

- Modified Guest OS (cannot be used with traditional OSs).

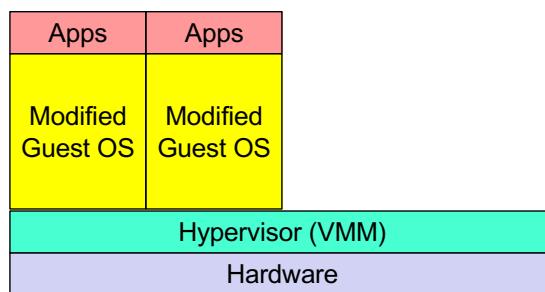


Figure 34: View of the Paravirtualization.

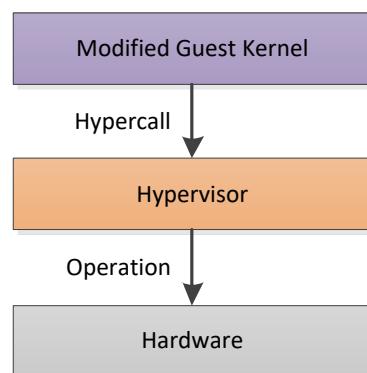


Figure 35: Paravirtualization flow.

### 3.1.3.3 Containers

**Containers** are **pre-configured packages**, with everything we need to execute the code (code, libraries, variables and configurations) in the target machine. Some well-known containers are Docker and Kubernetes.

The **main advantage** of containers is that their **behavior is predictable, repeatable and immutable**. When we create a “*master*” container and duplicate it on another server, we know exactly how it will be executed. There are **no unexpected errors when moving it to a new machine or between environments**.

#### Example 1

If we have a container for a website, we do not need to export/import the dev/testing/production environments. We just create a container containing the site and move it to the target environment.

Virtual machine provides hardware virtualization, while **containers provide virtualization at the operating system level**. The main difference is that the **containers share the host system kernel with other containers**.

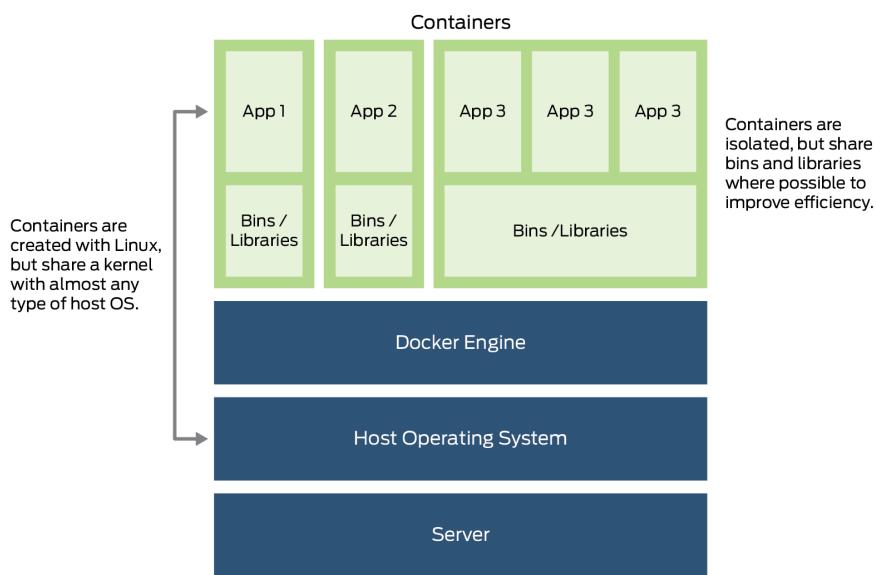


Figure 36: Containers architecture.

Some characteristics of containers:

- **Flexible**. Even the most complex application can be containerized.
- **Light**. The containers exploit and share the host kernel.
- **Interchangeable**. Updates can be distributed on the fly.
- **Portable**. We can create locally, deploy in the cloud and run anywhere.

- **Scalable.** It is possible to automatically increase and distribute replicas of the container.

- **Stackable.** Containers can be stacked vertically and on the fly.

Containers ease the deployment of applications and increase the scalability but they also impose a **modular application development where the modules are independent and uncoupled**.

### ② Container Use Cases

- Make our **local development** and **build workflow faster**, more efficient and lighter.
- Run **standalone services and applications** consistently **across multiple environments**.
- Use **containers to create isolated instances to run tests**. For example, to create a db server SQL already configured to run tests.
- **Build and test complex applications and architectures on a local host** before deploying to a production environment.
- **Build a multi-user Platform-as-a-Service (PaaS) infrastructure**.
- Provide lightweight, stand-alone sandbox environments for developing, testing and teaching technologies such as the Unix shell or a programming language.
- **Software as a Service (SaaS) applications**.

## 3.2 Computing Architectures

### 3.2.1 Cloud Computing

**Cloud Computing** is a coherent, large-scale, publicly accessible **collection of computing, storage and networking resources**. It is usually available via web service calls over the Internet. The business is based on short or long term access on a pay-per-use basis.

The **cloud is implemented through virtualization**. This involves **partitioning hardware resources (CPU, RAM, etc.) and sharing them between multiple virtual machines (VMs)**. This model ensures performance isolation and security. The Virtual Machine Monitor (VMM) manages access to physical resources between running VMs. The pros and cons of virtualization are explained in the dedicated chapter 3.1 (page 109).

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#### 3.2.1.1 Server Consolidation

**Server Consolidation** in cloud computing refers to the process of combining multiple servers into a single, more powerful server or cluster of servers.

This can be done to **improve the efficiency and cost effectiveness of the cloud computing environment**.

Server Consolidation is typically **achieved through the use of virtualization technology**, which allows **multiple virtual servers to run on a single physical server**. This enables better utilization of resources, as well as improved scalability and flexibility. It also allows organizations to reduce the number of physical servers they need to maintain, which can lead to cost savings on hardware, power and cooling.

In the context of server consolidation, **Consolidation Management** is the **migration from physical to virtual machines**.

Let us just say that the **characteristics** of this technique are:

- **Scalability.** It is possible to move VMs without disrupting the applications running in them.
- **Automatic scalability.** In addition to scalability, it is also possible to automatically balance workloads according to set limits and guarantees.
- **High availability.** Servers and applications are protected against component and system failures.

### ⌚ Server Consolidation Advantages

The benefits of server consolidation are:

- Different operating systems can run on the same hardware.
  - Higher hardware utilization means less hardware is needed (lower acquisition and maintenance costs).
  - Continued use of legacy software.
  - Application independent of hardware.
- 

#### 3.2.1.2 Services provided by cloud

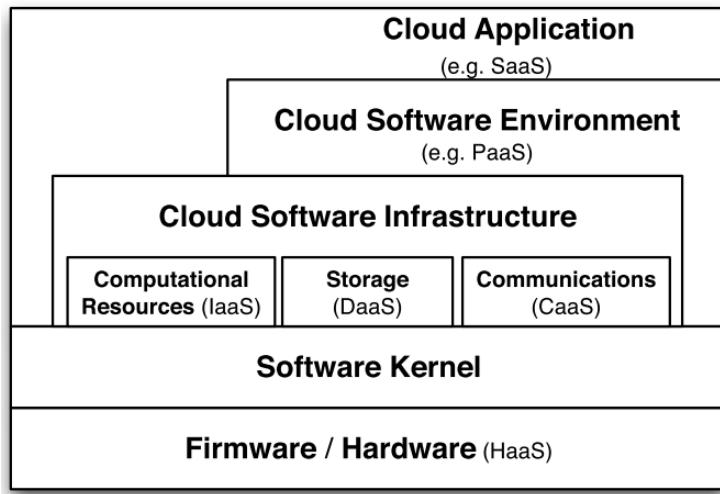
**Cloud Computing** is a model for providing convenient, on-demand network access to a shared pool of configurable computing resources, such as networks, servers, storage, applications and services. Anything that can be quickly provisioned and released with minimal management or interaction with the service provider.

“**X as a service**” (rendered as \*aaS in acronyms) is a phrasal template for any business model in which a product use is offered as a subscription-based service rather than as an artifact owned and maintained by the customer. [3]

There is a wide variety of “**as-a-Service**” terms used to describe services offered in clouds.

- AaaS - Architecture as a Service
- BaaS - Business as a Service
- CaaS - Communication as a Service
- CRMaaS - CRM as a Service
- DaaS - Data as a Service
- DBaaS - Database as a Service
- EaaS - Ethernet as a Service
- FaaS - Frameworks/Function as a Service
- GaaS - Globalization/Governance as a Service
- HaaS - Hardware as a Service
- IaaS - Infrastructure/Integration as a Service
- IDaaS - Identity as a Service
- ITaaS - IT as a Service
- LaaS - Lending as a Service
- MaaS - Mashups as a Service
- OaaS - Organization/Operations as a Service
- SaaS - Software as a Service
- StaaS - Storage as a Service
- PaaS - Platform as a Service
- TaaS - Technology/Testing as a Service
- VaaS - Voice as a Service

The **main services** provided by the cloud are shown in the image below.



- **Cloud Application Layer:** SaaS (Software as a Service). Users access the services provided by this layer through web portals and may be charged for using them.

Cloud applications can be developed on the cloud software environments or infrastructure components.

Some **examples** include [Gmail](#), [Webex](#), [Google Docs](#).

- **Cloud Software Environment Layer:** PaaS (Platform as a Service). Users are **application developers**.

Vendors provide developers with a **programming language level environment with a well-defined API**. It has many advantages:

- Ease the interaction between the environment and applications.
- Accelerate deployment.
- Support scalability.

Some **examples** are [Amazon Lambda](#) and [Microsoft Azure](#).

- **Cloud Software Infrastructure Layer:** provides resources to the higher-level layers.

- **Computational Resources Layer:** IaaS (Infrastructure as a Service). The vendor provides **virtual machines to developers**. Then the pros and cons are related to the virtual machines.

#### ✓ Advantages

- \* Flexibility.
- \* Root access to the virtual machine to fine-tune settings and customize installed software.

### 👎 Disadvantages

- \* Performance impact.
- \* Inability to provide strong SLA guarantees.

Some examples are [Amazon EC2](#), [Google Compute Engine](#), [IBM Cloud](#).

- **Storage Layer:** DaaS (Data as a Service). This layer allows users to:

1. **Store** their **data** on remote disks.
2. **Access data from anywhere at any time.**

It allows cloud applications to scale beyond their limited server requirements:

- \* High Reliability: Availability, Reliability, Performance.
- \* Replication.
- \* Data consistency.

Some examples are [DropBox](#) or [GoogleDrive](#).

- **Communications Layer:** CaaS (Communication as a Service). This layer guarantees:

- \* **Communication capability:** service-oriented, configurable, planable, predictable, and reliable.
- \* Network security, dynamic provisioning of virtual overlays for traffic isolation or dedicated bandwidth, guaranteed message delay, communication encryption, and network monitoring.

### 3.2.1.3 Types of clouds

There are 4 types of clouds:

- A **Public Cloud** is one that is made available to the public by a specific organization that also hosts the service.

A third-party provider maintains the hardware, relevant software, and licenses in a globally distributed network of data centers. You can access exactly what you need on demand, at any scale, from any device you choose.

The providers have a large infrastructure available on a rental basis and provide full customer self-service. Accountability is based on e-commerce.

- A **Private Cloud** is used for a single organization and can be hosted internally or externally.

Internally managed data centers. The **organization sets up a virtualization environment on its own servers**: in its own data center, in the data center of a managed service provider.

#### ✓ Advantages

- We have **total control over every aspect** of the infrastructure.
- We get the benefits of virtualization.

#### 👎 Disadvantages

- It lacks the freedom from capital investment and flexibility.

- A **Community Cloud** is a type of cloud shared by multiple organizations; typically hosted externally, but can also be hosted internally by one of the organizations.

A single cloud managed by multiple federated organizations that combine multiple organizations allows for economies of scale, and resources can be shared and used by one organization while the others are not using them.

Technically, it is similar to a private cloud because they share the same software and the same problems, but it requires a more complex accounting system.

Hosted locally or externally. Typically, community clouds share infrastructure between participants. However, they may be hosted by a separate, dedicated organization or by only a small subset of partners.

- A **Hybrid Cloud** is a type of cloud that is a composition of two or more clouds (private, community, or public) that remain unique entities but are interconnected to provide the benefits of multiple deployment models; hosted internally and externally.

Hybrid clouds are a combination of any of the previous types. Typically, companies are keeping their private cloud, but that they may be subject to unpredictable peaks of load. In this case, the company rents resources from other types of cloud.

## 4 Methods

### 4.1 Reliability and availability of data centers

#### 4.1.1 Introduction

**Dependability** is a **comprehensive measure** of how much we can **trust** a system to perform its expected function correctly and consistently over time.

Dependability is not a single property but a **composite of multiple inter-related concerns**, some more related to system correctness (reliability, availability), others more to protection (safety, security). In large-scale systems like datacenters, **dependability is not optimal**, it is integral to Service Level Agreement (SLAs)<sup>8</sup>, customer trust, and legal compliance (e.g., data protection laws)<sup>9</sup>.

#### Core Attributes of Dependability

Attribute	Meaning	Analogy / Data Center View
<b>Reliability</b>	Continuity of correct service	A web server not crashing or corrupting data for long periods.
<b>Availability</b>	Readiness for correct service	Can the system serve requests <i>right now?</i>
<b>Maintainability</b>	Ability for easy maintenance	Hot-swappable disks, modular servers.
<b>Safety</b>	Absence of catastrophic consequences	E.g., fail-safes in a power system to avoid fire/electrical hazard.
<b>Security</b>	Confidentiality and integrity of data	Access control, data encryption, intrusion prevention.

#### Example 1: Cloud Service Provider

Image Google Cloud or AWS:

- **Reliability:** Our VMs shouldn't crash without reason.
- **Availability:** We must access our cloud database anytime.
- **Maintainability:** They update the hypervisor with zero downtime.
- **Safety:** If a cooling system fails, automatic shutdown prevents hardware fire.

<sup>8</sup>A **Service Level Agreement (SLA)** is a contract between a service provider and a customer that defines the expected level of service. It typically includes metrics like availability, performance, and response times, along with remedies if the provider fails to meet those standards.

<sup>9</sup>**Legal compliance** in data protection laws ensures that organizations handle personal data responsibly and in accordance with regulations. In the EU, the *General Data Protection Regulation (GDPR)* is the primary framework, setting strict rules on data collection, processing, and storage. Globally, different countries have their own laws, such as the *California Consumer Privacy Act (CCPA)* in the U.S., and similar regulations emerging worldwide.

- **Security:** Data encryption at rest and in transit, isolation across tenants.

### ⌚ Do we really need to care about Dependability?

First, we'll explore intuition. Even when a system is *well-designed*, passes *functional verification*, meets *performance and energy constraints*, it can still **fail!** Why? Because real-world conditions and **non-functional factors** can break even perfectly specified systems.

So dependability is necessary because **failures are inevitable**. They stem from **multiple layers of system stack**, including:

Source	Example
<b>Hardware aging</b>	Transistor degradation, wear-out mechanisms.
<b>Manufacturing defects</b>	Process variation, cosmic rays.
<b>Design flaws</b>	Logic errors, incorrect specifications.
<b>Software bugs</b>	Memory leaks, race conditions, kernel panics.
<b>System misconfiguration</b>	Wrong firewall rule, VM setting.
<b>External disturbances</b>	Electromagnetic interference, overheating.
<b>Human errors</b>	Mistakes by admins, developers.
<b>Malicious attacks</b>	DoS, ransomware, data exfiltration.

Even a tiny misbehavior in one layer can cascade through the entire system.

### ⚠ Consequences of Undependability

Let's categorize **why lack of dependability is dangerous**, especially in data centers:

1. **High Economic Cost:** Downtime may cause lost transactions, SLA violations, brand damage.
2. **Information Loss:** Permanent deletion or corruption of critical data (e.g., backups overwritten, logs lost).
3. **Cascade Failures:** One component failure affects dependent services (e.g., cloud outages).
4. **User Distrust:** If users don't trust the service, they abandon it.
5. **Security & Safety Hazards:** leaked credentials, incorrect data processing and in physical systems, risk to human life (think healthcare or industrial systems).

### ⌚ When to Think About Dependability?

Short answer: **Always**. Dependability is **not an optional**, it must be **considered** throughout the **entire system lifecycle**: *design-time, deployment, run-time*, and even *decommissioning*. We think about dependability:

- At **Design-Time**, the main goal is to **prevent as many failures as possible before the system is deployed**. This is when we:
  - **Analyze**: Model the system and predict how it behaves under faults.
  - **Measure**: Evaluate expected MTTF, availability, error rates.
  - **Optimize**: Adjust design to improve weak points (e.g., redundancy, replication).
  - **Verify**: Perform fault-injection, static analysis, formal verification.
- At **Run-Time**, no matter how good our design is, **failures will still happen** in the field. So **we must**:
  - **Detect**: **Monitor system** state to spot abnormal behavior.
  - **Diagnose**: **Understand root causes** (e.g., logs, telemetry).
  - **React**: **Automatically correct** or **isolate** the problem.

For example rebooting a crashed VM, replacing a failed disk in a RAID array or routing traffic away from an unhealthy load balancer.

### ⚠️ Why Distinguish Development-Time vs Operation-Time Failures?

These two types of failures have completely different roots, so we must use different strategies to handle them.

- **Development-Time Failures**. These are **errors that are introduced during system creation**, in the design, coding or configuration phase.

#### ✖ Examples

- \* A bug in the file system code that causes data corruption.
- \* A wrong assumption in system specifications.
- \* An incorrect server configuration (e.g., firewall blocking valid ports).
- \* A logic error in redundancy management (e.g., mirrored disk not syncing).

#### ✓ Solutions

- \* These **should be avoided** before deployment.
- \* They're addressed using:
  - **Testing** (unit, integration, fault-injection)
  - **Verification** (formal methods, code reviews)
  - **Validation** (does it meet real-world expectations?)

**⚠️ If a system fails** due to a development-time error, it means there was something **wrong in how it was built**.

- **Operation-Time Failures.** These are **failures that happen while the system is running**, even if the system was perfectly designed.

### ❖ Examples

- \* A hard disk physically fails after 3 years.
- \* A memory bit flips due to cosmic radiation (soft error).
- \* The power supply overheats due to dust.
- \* A data center operator accidentally disconnects a cable.
- \* A hacker exploits an unknown vulnerability.

### ✓ Solutions

- \* These **cannot be entirely avoided**, because hardware ages, users make mistakes, environments are unpredictable.
- \* They **must be handled at runtime** with:
  - Monitoring
  - Redundancy / Fault tolerance
  - Error correction & self-repair

**A** If a system fails at runtime, it's not necessarily badly designed, reality is imperfect, and we need to plan for that.

## ② Where to Apply Dependability?

Originally, dependability was essential only in a few extreme environments, systems where a failure could endanger lives, waste millions or billions, be unacceptable by definition (space, nuclear, aviation). The **types of Critical Systems**:

- **Mission-Critical Systems.** The **mission is not completed if a failure occurs**. Some examples are satellites (loss = mission failure), unmanned vehicles (e.g., drones, crash = loss of platform and data). **Dependability ensures the system fulfills its intended goal**.
- **Safety-Critical Systems.** If a failure occurs, human life is at risk. Some examples are aircraft control (system crash = airplane crash), nuclear plant controls (meltdown). Here, the **cost of failure is catastrophic**.

**Dependability today is no longer limited** to space and nuclear systems. Now it's **central to computing infrastructures**, including data centers, cloud platforms, edge devices, etc. Why? Because a failure today in these systems can disrupt global services (e.g., Gmail outage), leak personal data, etc.

## ⌚ How to Provide Dependability?

Provide Dependability means designing our system (hardware and software) in a way that it **keeps working**, even when **things go wrong**, or at least, it fails in a **safe and recoverable way**. There are **two main strategies** to achieve this:

1. **Failure Avoidance** (try not to fail). This approach is like saying: “*let me build the system so well that it doesn’t break*”. For example, use very reliable hardware, run a lot of testing before deploying our software, do quality control in factories to catch early hardware faults, and use formally verified algorithms in critical parts.

This approach is **good, but expensive**, and we **can’t predict everything**.

### Example 2: Failure Avoidance Analogy

Like buying a car and checking *everything* before leaving the factory: brakes, oil, tires, engine. So it’s unlikely to break.

2. **Failure Tolerance** (prepare for when it does fail). This approach accepts the fact that something **will** go wrong. So let us prepare the system to **detect, contain, and recover** from the problem.

For example, use RAID for disks, use ECC memory (it can correct small memory errors automatically), monitor servers, and in the cloud, if one data center goes down, reroute to another.

This is **essential in data centers**, because with thousands of machines, failures are guaranteed.

### Example 3: Failure Tolerance Analogy

Like having a spare tire in our car, a seatbelt, and road assistance. We’re ready when things go wrong.

## ⌚ Where Can We Add Dependability?

We can “*add dependability*” at different layers:

- **Hardware Level.** Make components themselves very reliable.
  - ✓ Use robust materials.
  - ✓ Use parts that are known to last a long time.
  - ✗ Expensive, and maybe slow (old, stable tech).
- **Architecture/System Design Level.** Make the **structure of the system** fault-tolerant.
  - ✓ Duplicate components (e.g., 2 power supplies, RAID).
  - ✓ Create **clusters**: if one server fails, others can take over
  - ✗ More machines, more space, higher cost.

- **Software Level.** Add dependability using **code**.
  - ✓ Detect problems: logs, alerts, health checks.
  - ✓ Retry or restart automatically.
  - ✓ Recover from failures (e.g., checkpoint/restart in HPC).
  - ✓ Cheaper and flexible.
  - ✗ Needs smart design and might slow down performance.

### ⚠ There ain't no such thing as a free lunch (TANSTAAFL)

It is impossible to get something for nothing. We always **pay** for dependability:

We Pay In...	Why?
<b>Money</b>	Redundant servers, better hardware.
<b>Time</b>	Development of testing and recovery logic.
<b>Performance</b>	Extra steps for safety and monitoring.

### 4.1.2 Reliability and Availability

#### Definition 1: Reliability

**Reliability** is the probability that a system or component performs its **required functions**, under **stated conditions**, for a **specified period of time** without failure.

According to IEEE Std 610.12-1990: “*The ability of a system or component to perform its required functions under stated conditions for a specified period of time.*”

#### ✓ Mathematical Definition

Let  $R(t)$  be the reliability function, representing the **probability that the system has not failed during the time interval  $[0, t]$** :

$$R(t) = P(\text{No failure during } [0, t]) \quad \text{given system was operational at } t = 0 \quad (22)$$

- $t$  is the time. Reliability always **depends on the target time window**  $t$ . For example, a system may be reliable over 10 minutes, but not over 10 hours. In critical systems (like avionics or nuclear control), **even a short failure** is unacceptable, this makes **reliability extremely stringent**.
- It is a **non-increasing** function over time.
- $R(0) = 1$ : at time 0, the system is assumed to be *working*.
- $R(t) = 0$  as  $t \rightarrow \infty$ : over infinite time, failure becomes certain.

We can also determine **Unreliability** given the reliability function. Let  $Q(t)$  be the unreliability function:

$$Q(t) = 1 - R(t) \quad (23)$$

This express the probability that the system **has failed** by time  $t$ .

#### ↳ Typical Behavior

The failure rate  $\lambda(t)$  may vary over the life of a component:

- **Early stage**: high initial failure due to manufacturing defects.
- **Mid-life**: constant or random failure rate, this is the region of interest in most reliability modeling.
- **End-of-life**: failure rate increases due to wear-out (aging, stress).

### Definition 2: Availability

**Availability** is the probability that a system is **operational and accessible** when it is required to be used.

It represents how much of the time a system is **actually up and running**, accounting for both its reliability and its ability to **recover from failures**.

According to IEEE Std 610.12-1990: “*The degree to which a system or component is operational and accessible when required for use.*”

While **reliability** focuses on *continuous correct operation*, **availability** emphasizes the **readiness for use** at a given moment, even after failures occur and are repaired.

### ✓ Mathematical Definition

For **steady-state availability**:

$$\text{Availability} = \frac{\text{Uptime}}{\text{Uptime} + \text{Downtime}} \quad (24)$$

Formally,  $A(t)$  is the probability that the system is **operational** (not failed) at a given time  $t$ :

$$A(t) = P(\text{System is working at time } t) \quad (25)$$

In other words, it's the probability that the system is **ready for service** at time  $t$ .

- **Non-Repairable Systems.** If the system **cannot be repaired**, then:

$$A(t) = R(t)$$

The availability equals the reliability (it will eventually fail and stay failed).

- **Repairable.** For **repairable systems**:

$$A(t) \geq R(t)$$

Because even if the system fails, it may be restored and become available again.

We can also determine **Unavailability** given the availability function:

$$\text{Probability that the system is not operational at time } t = 1 - A(t) \quad (26)$$

### Difference from Reliability

Concept	Reliability	Availability
<b>Meaning</b>	No failure in a given time	System is up when needed
<b>Failure OK?</b>	✗ No, failure terminates reliability	✓ Yes, if system recovers quickly
<b>Focus</b>	Time-to-failure	Service continuity
<b>Measurement</b>	Probability of survival	Fraction of time operational
<b>Example</b>	Pacemaker, airplane engine	Cloud server, ATM, database system

A common shorthand for availability levels:

Number of 9s	Avail. (%)	Max Downtime	Typical Applications
2 nines	99.00%	≈ 3.65 days	Home internet, non-critical sites
3 nines	99.90%	≈ 8.76 hours	Web services, small business apps
4 nines	99.99%	≈ 52.6 minutes	Enterprise systems
5 nines	99.999%	≈ 5.26 minutes	Telco switches, high-end data centers
6 nines	99.9999%	≈ 31.5 seconds	Mission-critical infra (e.g. finance)

**■■ Reliability & Availability: Related Indices**

These indices are used to **quantify** how reliable and/or available a system is over time.

**1. Mean Time To Failure (MTTF)**

**≡ Definition.** The **average time** that a system operates before experiencing the **first failure**.

$$\text{MTTF} = \int_0^{\infty} R(t) dt \quad (27)$$

**❖ Used for:** Non-repairable systems or to model **time to first failure** in repairable systems.

**2. Mean Time Between Failures (MTBF)**

**≡ Definition.** The **average time** between **two consecutive failures**, including the time to repair.

$$\text{MTBF} = \text{MTTF} + \text{MTTR} \quad (28)$$

Where MTTR is the Mean Time To Repair. Sometimes, **repair time is negligible**, so  $\text{MTBF} \approx \text{MTTF}$ .

**❖ Used for:** Repairable systems.

**3. Failures In Time (FIT)**

**≡ Definition.** The number of expected failures **per billion** ( $10^9$ ) hours of operation.

$$\text{MTBF (in hours)} = \frac{10^9}{\text{FIT}} \quad (29)$$

**❖ Used for:** Common in hardware reliability (e.g., CPU/SSD specs).

**4. Failure Rate  $\lambda$ .** For exponential failure distributions:

$$R(t) = e^{-\lambda t} \Rightarrow \lambda = \frac{1}{\text{MTTF}} \quad (30)$$

It gives the **instantaneous likelihood** of failure per unit time.

### ❓ How to Compute Reliability? Empirical Evaluation

Let's suppose we want to estimate reliability based on **real-world observations** (e.g. testing 1000 SSDs in a lab). Here's how:

1. **Initial Setup.** Deploy  $n_0$  **independent and statistically identical elements** at time  $t = 0$ . All start in identical operating conditions:  $n(0) = n_0$ .
2. **Failure Observation.** Over time, observe the **number of elements still working** at time  $t$ , denoted as  $n(t)$ . For each unit  $i$ , record its **time to failure**:  $t_1, t_2, \dots, t_{n_0}$ .
3. **Assumption.** Times to failure  $\tau_i$  are **independent realizations** of a random variable  $\tau$ .
4. **Empirical Reliability Function**

$$R(t) \approx \frac{n(t)}{n_0} \quad (31)$$

It estimates the **probability** that a system is still operational at time  $t$ . As the number of samples  $n_0 \rightarrow \infty$ , this ratio converges to the true reliability function:

$$\frac{n(t)}{n_0} \longrightarrow R(t) \quad (32)$$

This is useful for **empirical validation** of theoretical models (like exponential reliability). Often used in *burn-in testing*, *field reports*, and *accelerated life tests*.

#### Example 4

Suppose we start testing 1000 servers at time  $t = 0$ . After 3000 hours, only 980 are still working:

$$R(3000) \approx \frac{980}{1000} = 0.98$$

We repeat this for multiple  $t$ -values to plot the empirical reliability curve.

### ❓ What to do with $R(t)$ ? And why compute $R(t)$ ?

The goal is to determine the **expected reliability** (or failure behavior) of **complex systems**, such as a data center or a warehouse-scale machine, **over time**. This includes:

1. **Computing MTTF (Mean Time To Failure).** Once we know the reliability function  $R(t)$ , we can compute:

$$\text{MTTF} = \int_0^\infty R(t) dt$$

This gives the **expected lifetime** of a component or system before it fails. It is essential for predictive maintenance, capacity planning and warranty.

2. **Composing System Reliability from Components.** Computation of the overall reliability starting from the components' one. Systems are usually composed of multiple **subsystems** (e.g. disks, servers, switches). Each component has its own reliability  $R_i(t)$ . Using **Reliability Block Diagrams** or other composition models, we derive:

$$R_{\text{system}}(t) = f(R_1(t), R_2(t), \dots, R_n(t))$$

3. **Exponential Reliability Assumption.** We consider only a reliability with an exponential distribution: constant failure rate. This simplifies all analysis:

$$R(t) = e^{-\lambda t}$$

Constant failure rate  $\lambda$ , then memoryless behavior.

- ② **What does “memoryless” mean?** In probability theory, a **memoryless distribution** is one where: *the probability that a system survives an additional time  $s$  does not depend on how long it has already survived.* Mathematically, for the **exponential distribution**:

$$\mathbb{P}(T > t + s \mid T > t) = \mathbb{P}(T > s)$$

This is what makes it *memoryless*: **the past does not matter**.

- ③ **Why does constant  $\lambda$  imply memorylessness?** If  $R(t) = e^{-\lambda t}$ , then:

- The **failure rate**  $\lambda$  is constant.
- The distribution of time-to-failure  $T$  is exponential.

This means that a component that has been running for 1000 hours is **just as likely to fail in the next 100 hours** as a brand-new one.

- ≡ **Analogy** Image a light bulb modeled with exponential failure. We don't get closer to failure as time passes. Whether it's 10 hours old or 1000 hours old, its probability of lasting the next hour is always the same.

Common for modeling random failure phase (middle or bathtub curve). Makes MTTF easy to compute:

$$\text{MTTF} = \frac{1}{\lambda} \quad (33)$$

## Reliability Terminology

1. **Fault**: a detect of flaw in te system, either in hardware or software. It is **passive** and may or may not lead to an error. For example, a fault occurs when an electromagnetic disturbance corrupts a radar signal of a drone.
2. **Error**: a deviation from the correct internal state of the system caused by a fault. An **error is active**, it is manifestation of the fault. For example, an error occurs when the wrong trajectory is computed for a drone based on faulty sensor input.
3. **Failure**: the **external deviation** from the expected service or behavior. It is **observable** by the user or system and may cause damage or interruption. A failure occurs, for example, when a drone crashes to the ground.

These stages form a chain:

Fault → Error → Failure

But the chain doesn't **always complete**. There are **two special cases**:

- ✓ **Non-Activated Fault**: a **fault exists** but never triggers an error.

### Example 5: Non-Activated Fault

A server in a cloud data center has a memory module with a **latent hardware fault**: a single DRAM cell is defective due to a manufacturing imperfection.

- ⚠ **Fault**: A memory cell in a non-critical area of RAM has a physical defect (e.g., stuck-at-1).
- ✓ **Error**: No error occurs because that specific memory address has **never been written or read**. Or, the OS allocates memory dynamically and that region is **never touched**.
- ✓ **Failure**: No incorrect behavior is ever observed by any application or user. The system continues operating normally, and the fault remains **inactive**, never triggered.

The **fault exists physically**, but it **never becomes active**, and thus causes **no error or failure**. This is a classic non-activated fault: it's a dormant effect that could lead to problems only under specific usage or workloads, but never does in the observed execution.

- ✓ **Non-Propagated (Absorbed) Error**: an error occurs but is **detected or corrected** before causing a failure. For example, if a drone calculates the wrong trajectory, but this is later corrected using radar data, this constitutes a **safe landing<sup>10</sup>** behavior and an instance of absorbed error.

<sup>10</sup>A **safe landing** is the **correct expected behavior** of the drone, the absence of failure, despite a temporary internal error.

### ⚠ Fault Hierarchy

The **Fault-Error-Failure** chain is **not flat or isolated**, it can cascade across components and abstraction levels, and grow into **critical or life-threatening** failures.

A **Fault Hierarchy** is a conceptual model that captures how **faults can propagate** and **escalate** through layers of a system, for example:

- **Low-level hardware fault:** a transistor in a CPU flips and causes a memory bitflip.
- **Mid-level software error:** the corrupted value leads to an incorrect instruction.
- **High-level system failure:** the OS kernel crashes and the entire system reboot.
- **Service-level failure:** web service becomes unavailable to users.
- **Mission-level hazard:** in critical systems, loss of control, safety violations, or even physical harm.

#### Example 6: Fault Hierarchy

Let's say we're dealing with an autonomous surgical robot:

- **Fault:** a memory bitflip due to cosmic radiation (hardware).
- **Error:** the control software computes the wrong joint angle (software logic).
- **Failure:** the robot arm moves incorrectly (physical layer).
- **Hazard:** causes injury to the patient (mission/life-threatening).

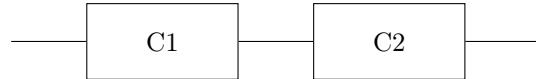
⌚ **Why it matters?** **Critical systems** (aviation, medical, autonomous driving) must block this chain early, ideally at the fault or error stage. This is the basis for fault tolerance, error detection and correction, and failure containment and recovery.

### 4.1.3 Reliability Block Diagrams (RBDs)

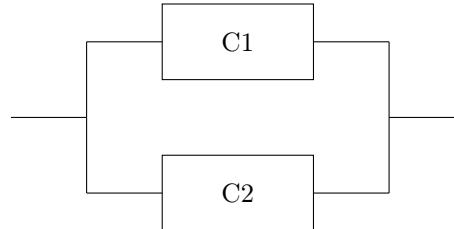
As we saw in the [Software Engineering for HPC course](#), a **Reliability Block Diagram (RBD)** is a *graphical and mathematical model* used to analyze the reliability of a system by representing how the success or failure of each component affects the overall system operation.

- **Inductive Model:** Starts from the reliability of individual components and builds up to the system.
- **Blocks:** Each block represents a **component or subsystem**, each with its own reliability function  $R_i(t)$ .
- **Connections**

- **Series:** All components must function for the system to work.



- **Parallel:** The system can work as long as at least one component works.



- **Model Topology:** The RBD structure **may not match the physical system layout**, as it's focused on *functional success paths* rather than actual wiring or data flow.

Every element in the RBD has its **own reliability**. Blocks are combined together to model all possible success paths.

### ✓ Mathematical Concepts

- **Series Configuration.** In a series system, all components must work for the system to function. If any single component fails, the whole system fails. In other words, the system failure is determined by the failure of the *first* component.

The formula is:

$$R_S(t) = R_{C1}(t) \cdot R_{C2}(t) \cdot \dots \cdot R_{Cn}(t) = \prod_{i=1}^n R_i(t) \quad (34)$$

Where:

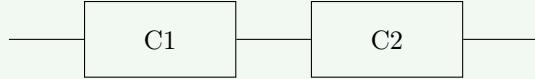
- $R_S(t)$ : system reliability at time  $t$ .
- $R_i(t)$ : reliability of the  $i^{\text{th}}$  component.

- This assumes **independent** component failures.

If each component has a **probability**  $R_i(t)$  of working, then the **joint probability** that **all work** is the **product**.

#### Example 7: Series Configuration

Consider, for example, the following model:



The reliability is:  $R_S(t) = R_{C1}(t) \cdot R_{C2}(t)$ .

- **Parallel Configuration.** In a **parallel system**, the system functions as long as **at least one component works**. This configuration is used for **redundancy**. In other words, the system fails when the *last* component fails.

The formula is:

$$R_S(t) = 1 - \prod_{i=1}^n [1 - R_i(t)] \quad (35)$$

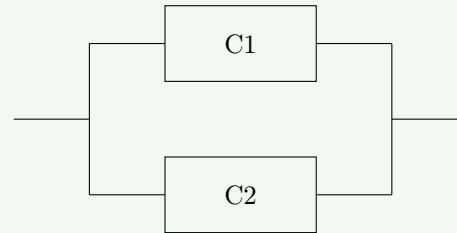
Where:

- \*  $1 - R_i(t)$ : failure probability of component  $i$ .
- \*  $\prod_{i=1}^n [1 - R_i(t)]$ : probability that **all fail**.
- \*  $1 - (\text{all fail})$ : probability that **at least one works**.

In summary, the system works in a parallel configuration **as long as at least one component is functioning**. This **design increases fault tolerance and improves reliability**.

#### Example 8: Parallel Configuration

Consider, for example, the following model:



The reliability is:  $R_S(t) = R_{C1}(t) + R_{C2}(t) - R_{C1}(t) \cdot R_{C2}(t)$ .

### ■ Other Series Formulas Related to Reliability

- **Reliability Function of Series Systems as one Exponential Component  $\lambda_S$ .** In a **series system**, all components must function for the system to work. If one fails, the system fails. For  $n$  components with exponential reliability:

$$R_S(t) = \prod_{i=1}^n R_i(t) = \prod_{i=1}^n e^{-\lambda_i t} = \exp \left( -t \sum_{i=1}^n \lambda_i \right) \quad (36)$$

We define:

$$\lambda_S = \sum_{i=1}^n \lambda_i \implies R_S(t) = e^{-\lambda_S t} \quad (37)$$

This models the **system as one exponential component** with rate  $\lambda_S$ .

- **Failure in Time (FIT).** The **failure rate** of the whole system in series is:

$$\lambda_S = \sum_{i=1}^n \lambda_i \quad (38)$$

This tells us that **each new component added in series increases the failure rate**, reducing overall reliability.

- **Mean Time To Failure (MTTF).** For an exponential distribution:

$$\text{MTTF}_S = \frac{1}{\lambda_S} = \frac{1}{\sum_{i=1}^n \lambda_i} = \frac{1}{\sum_{i=1}^n \frac{1}{\text{MTTF}_i}} \quad (39)$$

Thus, the more components in series, the lower the systems's MTTF. If even one component is fragile, it significantly impacts the whole system.

- **Special Case: Identical Components.** Assume  $n$  components and **same failure rate  $\lambda$** , then:

$$\lambda_S = n \cdot \lambda \implies R_S(t) = e^{-n\lambda t} \quad (40)$$

And:

$$\text{MTTF}_S = \frac{1}{n \cdot \lambda} \quad (41)$$

System becomes  $n$  **time less reliable** than a single component.

- **Availability of Series System.** Let  $A_i = \frac{\text{MTTF}_i}{\text{MTTF}_i + \text{MTTR}_i}$  as the availability of component  $i$ , then:

$$A_S = \prod_{i=1}^n A_i \quad (42)$$

And **if all components are identical**:

$$A_S = A^n \quad (43)$$

Where:

$$A = \left( \frac{\text{MTTF}}{\text{MTTF} + \text{MTTR}} \right)^n$$

As with reliability, **availability degrades multiplicatively** in series configurations.

## ■ Other Parallel Formulas Related to Reliability

- **Reliability Function of Parallel Systems.** Let  $R_i(t)$  be the reliability of component  $i$ . Then the system reliability is:

$$R_S(t) = 1 - \prod_{i=1}^n [1 - R_i(t)]$$

- $1 - R_i(t)$ : probability that component  $i$  has failed by time  $t$ .
- $\prod(1 - R_i(t))$ : probability that **all components** have failed.
- So,  $1 - (\text{all failed})$ : probability that **at least one** is working.

- **Special Case: Identical Components.** If all  $n$  components have the **same reliability**  $R(t)$ , then:

$$R_S(t) = 1 - (1 - R(t))^n \quad (44)$$

As  $n$  increases,  $R_S(t) \rightarrow 1$ : very high system reliability.

- **Mean Time To Failure (MTTF).** For parallel systems with exponential reliabilities  $R_i(t) = e^{-\lambda_i t}$ , there is **no simple closed-form MTTF** in the general case, but for identical components, if  $R(t) = e^{-\lambda t}$ , then:

$$R_S(t) = 1 - (1 - e^{-\lambda t})^n \quad (45)$$

MTTF can be found via integration:

$$\text{MTTF}_S = \int_0^\infty R_S(t) dt \quad (46)$$

This yields increasingly large values as  $n$  increases (more redundancy, then more robust).

- **Availability of Parallel System.** Let  $A_i$  be the availability of component  $i$ , then:

$$A_S = 1 - \prod_{i=1}^n (1 - A_i) \quad (47)$$

If all components are the same:

$$A_S = 1 - (1 - A)^n \quad (48)$$

Where:

$$A = \frac{\text{MTTF}}{\text{MTTF} + \text{MTTR}} \quad (49)$$

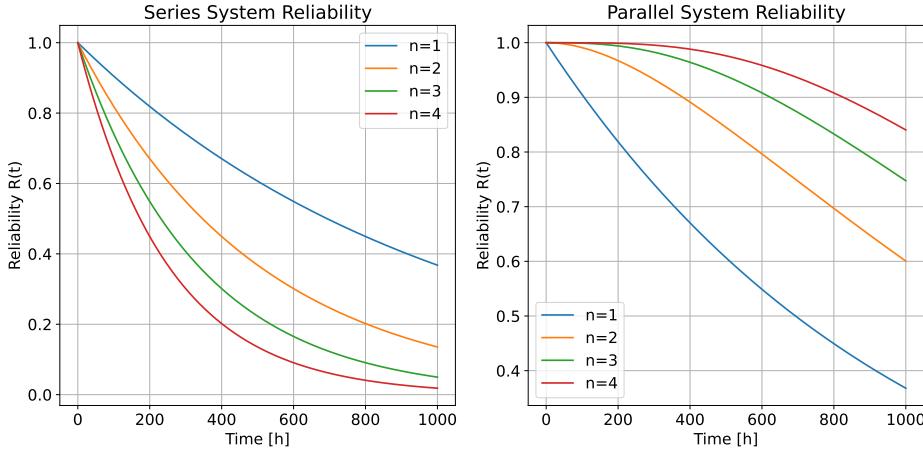


Figure 37: The **left plot** shows the series system reliability:

- Each line corresponds to a system composed of  $n = 1, 2, 3, 4$  components in **series**.
- The  $x$ -axis is time (0 to 1000 hours).
- The  $y$ -axis is the system reliability  $R_S(t)$ , which **decreases over time**.

For  $n = 1$ , the system is just a single component, standard exponential decay. As  $n$  increases, reliability drops **faster** because the **probability of at least one failure increases**. Mathematically:

$$R_S(t) = e^{-n\lambda t}$$

For example, with  $n = 4$ , the system becomes much less reliable in shorter timeframes. This means that series systems are fragile; the more components there are, the greater the chance of failure. It's like a chain: the system is only as strong as its weakest link.

The **right plot** shows the parallel system reliability:

- Each curve is a system with  $n = 1$  to  $n = 4$  components in **parallel**.
- The **system works as long as at least one component works**.

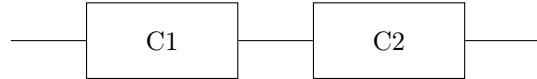
For  $n = 1$ , it's the same as the single-component series case. As  $n$  increases, reliability increases and curves stay higher for longer. Formula used:

$$R_S(t) = 1 - (1 - e^{-\lambda t})^n$$

The system becomes more fault-tolerant because it tolerates some component failures. This means that parallelism boosts reliability. With just 3 or 4 redundant units, reliability stays close to 1 for long durations.

## ◀ A quick recap

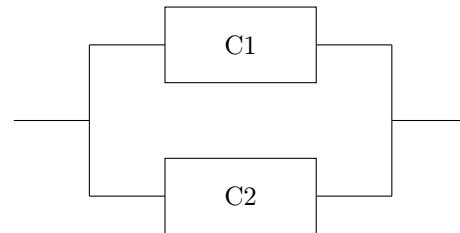
- **Series**



Reliability:

$$R_s = \prod_i^n R_i \implies R_s = R_{C1} \cdot R_{C2}$$

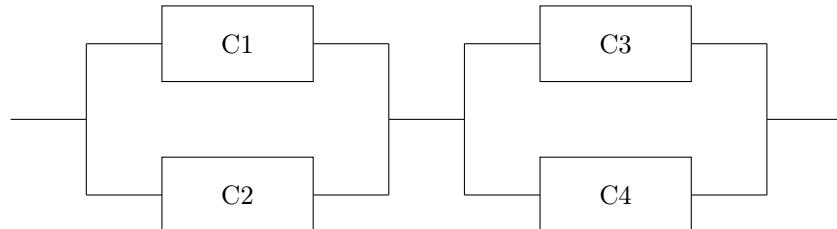
- **Parallel**



Reliability:

$$R_S(t) = R_{C1}(t) + R_{C2}(t) - R_{C1}(t) \cdot R_{C2}(t)$$

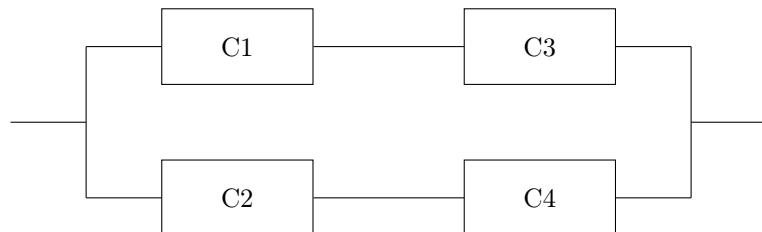
- **Series-Parallel (Component Redundancy)**



Reliability:

$$R_S(t) = (R_{C1} + R_{C2} - R_{C1} \cdot R_{C2}) \cdot (R_{C3} + R_{C4} - R_{C3} \cdot R_{C4})$$

- **Parallel-Series (System Redundancy)**

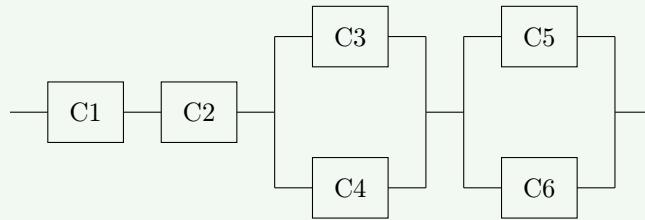


Reliability:

$$R_s = 1 - [(1 - R_{C1} \cdot R_{C3}) \cdot (1 - R_{C2} \cdot R_{C4})]$$

**Example 9: calculate the reliability of the system****?** Question

What is the Reliability of the entire system knowing the reliability of each component?



- $R_{C1} = 0.95$
- $R_{C2} = 0.97$
- $R_{C3} = 0.99$
- $R_{C4} = 0.99$
- $R_{C5} = 0.92$
- $R_{C6} = 0.92$

**✓ Solution**

1. Consider components  $C_1$  and  $C_2$ . The reliability, which we will call  $R_G$ , is then calculated as a *series*:

$$R_G = R_{C1} \cdot R_{C2} = 0.95 \cdot 0.97 = 0.9215$$

2. Consider components  $C_3$  and  $C_4$ . The reliability, which we will call  $R_H$ , is then calculated as a *parallel*:

$$\begin{aligned} R_H &= 1 - [(1 - R_{C3}) \cdot (1 - R_{C4})] \\ &= 1 - [(1 - 0.99) \cdot (1 - 0.99)] \\ &= 1 - 0.0001 \\ &= 0.9999 \end{aligned}$$

3. Consider components  $C_5$  and  $C_6$ . The reliability, which we will call  $R_I$ , is then calculated as in the previous step:

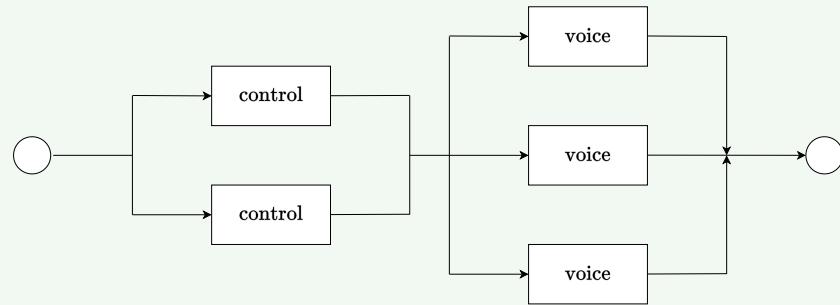
$$\begin{aligned} R_I &= 1 - [(1 - R_{C5}) \cdot (1 - R_{C6})] \\ &= 1 - [(1 - 0.92) \cdot (1 - 0.92)] \\ &= 1 - 0.0064 \\ &= 0.9936 \end{aligned}$$

4. Finally, we calculate the reliability of the system by multiplying each calculated component reliability:

$$\begin{aligned} R_s &= R_G \cdot R_H \cdot R_I \\ &= 0.9215 \cdot 0.9999 \cdot 0.9936 \\ &= 0.91551083976 \approx 0.9155 \end{aligned}$$

**Example 10: calculate reliability without numbers****?** Question

The system consists of 2 control blocks and 3 voice channels. The system is up when at least 1 control channel and at least 1 voice channel are up.

**✓** Solution

Reliability can be calculated in parallel, as it takes almost a component to work properly. Each control channel has reliability  $R_c$  and each voice channel has reliability  $R_v$ :

$$R = \left[1 - (1 - R_c)^2\right] \cdot \left[1 - (1 - R_v)^3\right]$$

#### 4.1.3.1 R out of N redundancy (RooN)

An **RooN (r out of n)** redundancy system **contains** both the **series system model** and the **parallel system model** as special cases. The system has  $n$  components that operate or fail independently of one another and as long as at least  $r$  of these components (any  $r$ ) survive, the system survives. [5]

A system with:

- $n$ : total number of identical components.
- $r$ : minimum number of components that must **work correctly**.

The system function **if at least  $r$  out of the  $n$  components are operational**. **System failure occurs when** the  $(n - r + 1)$ -th component failure occurs. [5]

But note an interesting observation:

- When  $r = n$ , the  $r$  out of  $n$  model reduces to the **series** model. [5]
- When  $r = 1$ , the  $r$  out of  $n$  model becomes the **parallel** model. [5]

In simple terms, **RooN** is a system made up of  $n$  identical replicas, where at least  $r$  replicas have to work well for the whole system to work well.

The reliability formula for the **RooN** system is:

$$R_s(t) = R_V \sum_{i=r}^n R_c^i (1 - R_c)^{n-i} \frac{n!}{i!(n-i)!} \quad (50)$$

Where:

- $n$ : total number of identical components.
- $R_c(t)$ : reliability of each component.
- $R_V(t)$ : reliability of the **voter** (which combines outputs).
- $R_S(t)$ : system reliability.
- $(1 - R_c)^{n-i}$ : failure probability of the remaining  $n - i$ .

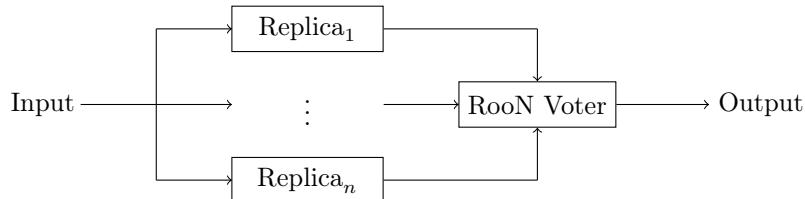


Figure 38: General structure of **RooN** system.

The reliability of the **central voter**  $R_V(t)$  is crucial. If the voter fails, the system fails, even if enough components are still working. In practice, voter reliability is either assumed perfect ( $R_V = 1$ ) or modeled separately.

#### 4.1.3.2 Triple Modular Redundancy (TMR)

**Triple Modular Redundancy (TMR)** is a fault-tolerant form of N-modular redundancy, in which three systems perform a process and the result is processed by a majority-voting system to produce a single output. If any one of the three systems fails, the other two systems can correct and mask the fault. In other words, it is a **special case of the r-out-of-n redundancy model**:

$$r = 2, \quad n = 3$$

- TMR consists of **three identical components** performing the **same task in parallel**.
- A voter *compares the outputs* and *selects the majority result*.
- The **system works correctly** as long as at least **two components** function correctly and the **voter does not fail**.

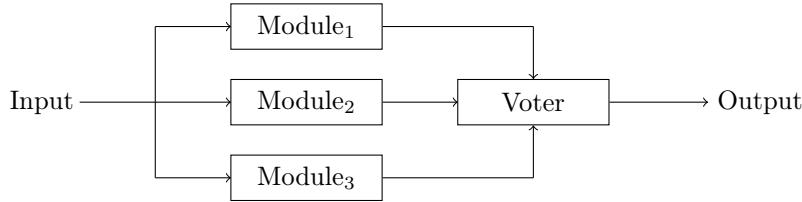


Figure 39: General structure of TMR system.

The **TMR Reliability**  $R_{\text{TMR}}$  is:

$$\begin{aligned} R_{\text{TMR}} &= R_v (3 \cdot R_m^2 - 2 \cdot R_m^3) \\ &= R_v [(2\text{-out-of-3 OK}) + (3\text{-out-of-3 OK})] \end{aligned} \quad (51)$$

Where:

- $R_m$ : reliability of a **module**.
- $R_v$ : reliability of the **voter**.
- $3 \cdot R_m^2$ : probability of exactly 2 modules working.
- $R_m^3$ : probability of all 3 modules working.

To **compute the Mean Time To Failure (MTTF)** of a Triple Modular Redundancy (TMR) system, assuming:

- **Identical components**: each with exponential reliability  $R_m(t) = e^{-\lambda t}$ .
- **Voter has perfect reliability**  $R_v = 1$  (or it's included later as a separate element).

The MTTF of a single component, for exponential reliability, is:

$$R(t) = e^{-\lambda t} \Rightarrow \text{MTTF} = \frac{1}{\lambda}$$

And the **MTTF of TMR system** is:

1. Using the TMR reliability:

$$R_{\text{TMR}}(t) = 3R_m^2(t) - 2R_m^3(t) = 3e^{-2(\lambda t)} - 2e^{-3(\lambda t)}$$

2. To find MTTF:

$$\text{MTTF}_{\text{TMR}} = \int_0^{\infty} R_{\text{TMR}}(t) dt$$

3. Compute:

$$\text{MTTF}_{\text{TMR}} = \int_0^{\infty} (3e^{-2\lambda t} - 2e^{-3\lambda t}) dt = \frac{3}{2\lambda} - \frac{2}{3\lambda}$$

4. Get common denominator:

$$\text{MTTF}_{\text{TMR}} = \left( \frac{9}{6\lambda} - \frac{4}{6\lambda} \right) = \frac{5}{6\lambda}$$

The final formula is:

$$\text{MTTF}_{\text{TMR}} = \frac{5}{6} \cdot \text{MTTF}_{\text{module}} \quad (52)$$

Where  $\text{MTTF}_{\text{module}}$  is the Mean Time To Failure of a single component in the system.

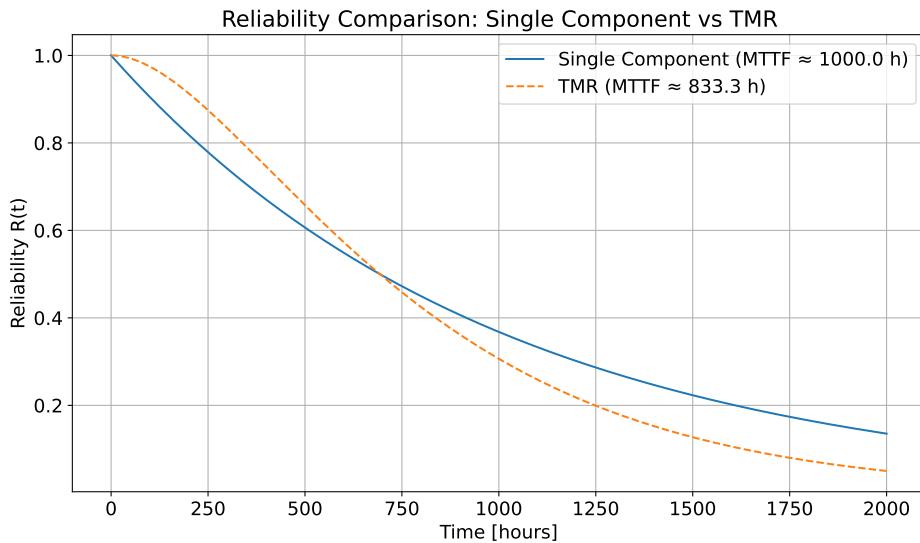


Figure 40: Plot comparing the reliability over time of a single component vs a TMR system.

### ⌚ TMR: good or bad?

Figure 151 shows the benchmark of a TMR system. At **early mission times** (before 700-800), **TMR has higher reliability**, meaning it's better at masking early failures. **Later in time** ( $> 1000$  hours), the **single component** eventually **becomes more reliable** because the three-module TMR setup is exposed to more cumulative risk.

However, Triple Modular Redundancy (TMR) is neither universally good nor bad. Like many engineering trade-offs, its value depends on the mission profile and system requirements.

#### ✓ When TMR is Good

- ✓ **Short mission durations:** TMR boosts reliability in early hours. For  $t < 0.7 \cdot \text{MTTF}_{\text{module}}$ , TMR outperforms a single module.
- ✓ **Safety-critical systems:** TMR can tolerate 1 permanent fault and mask transient faults, like radiation bit flips or noise.
- ✓ **Spacecraft / Avionics:** TMR is widely used in flight computers, satellites, and nuclear systems where failures are unacceptable.
- ✓ **High electromagnetic interference:** TMR can suppress soft errors (temporary glitches).
- ✓ **Voting logic is reliable:** If the voter is highly reliable (or replicated), the system benefits greatly from TMR.

⌚ **When TMR is Bad.** For **long mission durations**, TMR has a lower MTTF than a single module. So TMR is bad when long-term availability is key.

⌚ **What is the MTTF Threshold?** There exists a specific time  $t^*$  where:

$$R_{\text{TMR}}(t^*) = R_{\text{module}}(t^*)$$

- Before that time ( $t < t^*$ ), TMR has **higher reliability**.
- After that time ( $t > t^*$ ), TMR becomes **less reliable**.

Using numerical or symbolic solving, one finds that:

$$t^* \approx 0.693 \cdot \text{MTTF}_{\text{module}} = \frac{0.693}{\lambda}$$

This threshold corresponds to the time where:

$$R_{\text{TMR}}(t) = R_{\text{module}}(t)$$

Hence, we commonly approximate:

$$R_{\text{TMR}}(t) > R_{\text{module}}(t) \quad \text{for } t < 0.7 \cdot \text{MTTF}_{\text{module}} \quad (53)$$

#### 4.1.3.3 Standby redundancy

**Standby redundancy** is a fault-tolerance strategy where **redundant components are kept inactive** (in “standby mode”) until the **primary component fails**, at which point a **backup** is activated.

Unlike parallel redundancy, where all components run simultaneously, standby redundancy has **only one active component at a time**. It has two main roles:

1. **Primary replica**: operates under normal conditions.
2. **Standby (backup) replica(s)**: activated **only upon failure** of the primary.

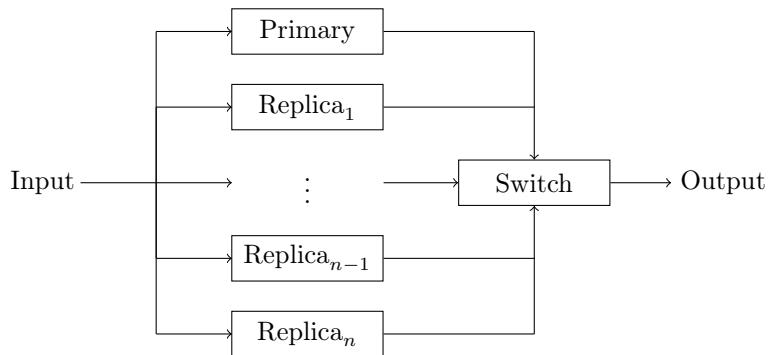


Figure 41: General standby redundancy strategy.

#### ❖ How it works?

It works as follows:

1. The **primary** performs all tasks.
2. A **monitoring mechanism** detects failure.
3. A **switching mechanism** disables the primary and **activates the standby**.

#### ⌚ Requirements for operation

Standby redundancy only works if the system includes:

- **Self-check mechanism**: Detects when the primary has failed.
- **Switch mechanism**: Transfers operation to the standby.

Standby Parallel Model	System Reliability
Equal failure rates, perfect switching	$R_s = e^{-\lambda t} (1 + \lambda t)$
Unequal failure rates, perfect switching	$R_s = e^{-\lambda_1 t} + \lambda_1 \frac{(e^{-\lambda_1 t} - e^{-\lambda_2 t})}{\lambda_2 - \lambda_1}$
Equal failure rates, imperfect switching	$R_s = e^{-\lambda t} (1 + R_{\text{switch}} \lambda t)$
Unequal failure rates, imperfect switching	$R_s = e^{-\lambda_1 t} + R_{\text{switch}} \lambda_1 \frac{(e^{-\lambda_1 t} - e^{-\lambda_2 t})}{\lambda_2 - \lambda_1}$

Table 11: Standby redundancy - Quick Formulas.

In the previous table we have:

- $R_s$ : System Reliability
- $\lambda$ : Failure Rate
- $t$ : Operating Time
- $R_{\text{switch}}$ : Switching Reliability

## 4.2 Disk performance

### 4.2.1 HDD

We can calculate some performance metrics related to the types of delay of HDD (page 41).

- **Full Rotation Delay**  $R$  is:

$$R = \frac{1}{\text{Disk RPM}} \quad (54)$$

And in seconds:

$$R_{\text{sec}} = 60 \times R \quad (55)$$

From the  $R_{\text{sec}}$  we can also calculate the **total rotation average**:

$$T_{\text{rotation AVG}} = \frac{R_{\text{sec}}}{2} \quad (56)$$

It is half of a full rotation, because on average, the sector will be halfway around the platter from the current head position.

- **Seek Time.** The time to seek from one track to another depends on the distance moved. In real systems, this relation isn't perfectly linear, but it's often approximated as (**seek average**):

$$T_{\text{seek AVG}} = \frac{T_{\text{seek MAX}}}{3} \quad (57)$$

Where  $T_{\text{seek MAX}}$  is the **time for the longest possible seek** (from *outermost* to *innermost* track) and the division by 3 assumes a **uniform random distribution of seeks** across the disk.

- **Transfer time.** It is the **time that data is either read from or written to the surface**. It **includes** the time the head needs to pass **on the sectors** and the **I/O transfer**:

$$T_{\text{transfer}} = \frac{\text{R/W of a sector}}{\text{Data transfer rate}} \quad (58)$$

The **total time to complete a disk I/O operation** is called the  $T_{\text{I/O}}$  **Service Time**:

$$T_{\text{I/O}} = T_{\text{seek}} + T_{\text{rotation}} + T_{\text{transfer}} + T_{\text{overhead}} \quad (59)$$

If the disk is shared among processes, we must also consider **queueing time**. And the **Response Time** is:

$$T_{\text{response}} = T_{\text{queue}} + T_{\text{I/O}} \quad (60)$$

Where  $T_{\text{queue}}$  depends on queue length, disk utilization rate, variance in request time, arrival rate of I/O requests.

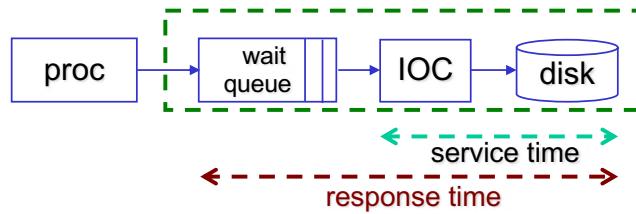


Figure 42: Service and response time.

### Exercise 1: Mean Service Time of an I/O operation

The data of the exercise are:

- Read/Write of a sector of 512 bytes (0.5 KB)
- Data transfer rate: 50 MB/sec
- Rotation speed: 10000 RPM (Round Per Minute)
- Mean seek time: 6 ms
- Overhead Controller: 0.2 ms

The goal is to calculate the average I/O service time. To calculate the *service time*  $T_{I/O}$ , we need the following information:

- ✓  $T_{\text{seek}}$ , which we already have, and it is 6 ms.
- ✗  $T_{\text{rotation}}$
- ✗  $T_{\text{transfer}}$
- ✓  $T_{\text{overhead}}$ , which we already have, and it is 0.2 ms.

We also know the rotation and transfer information, but we want to know the *mean* service time. Then we calculate the total rotation average  $T_{\text{rotation AVG}}$ :

$$\begin{aligned}
 R &= \frac{1}{\text{DiskRPM}} = \frac{1}{10000} = 0.0001 \\
 R_{\text{sec}} &= 60 \cdot R = 60 \cdot 0.0001 = 0.006 \text{ seconds} \\
 T_{\text{rotation AVG}} &= \frac{R_{\text{sec}}}{2} = \frac{0.006}{2} = 0.003 \text{ seconds} = 3 \text{ ms}
 \end{aligned}$$

Finally, the transfer time is easy to calculate because we have the R/W of a sector and the data transfer rate. First we do a conversions from

megabytes to kilobytes:

$$\begin{aligned}
 \text{Data transfer rate:} & \quad 50 \text{ MB/sec} \\
 & = 50 \cdot 1024 \text{ KB/sec} \\
 & = 51200 \text{ KB/sec} \\
 T_{\text{transfer}} & = \frac{0.5 \text{ KB/sec}}{51200 \text{ KB/sec}} \\
 & = 0.000009765625 \text{ sec} \cdot 1000 \\
 & = 0.009765625 \text{ ms} \approx 0.01 \text{ ms}
 \end{aligned}$$

The exercise can be completed by calculating the mean I/O service time required:

$$\begin{aligned}
 T_{\text{I/O}} & = T_{\text{seek}} + T_{\text{rotation}} + T_{\text{transfer}} + T_{\text{overhead}} \\
 T_{\text{I/O}} & = 6 + 3 + 0.01 + 0.2 = 9.21 \text{ ms}
 \end{aligned}$$

The I/O service time computed in the previous exercise (9.21 ms) assumes a **worst-case scenario**. This is very useful for understanding disk behavior, but it doesn't always reflect what happens in real workloads. It assumes:

1. Every time we read a small file or sector,
2. The read must seek to a new track,
3. And then wait for rotation to bring the right sector under the head

This is worst-case behavior, and happens when **files are very small**, so each one is just one block (e.g., 512 bytes); or disk is **heavily externally fragmented**, so even larger files are broken into scattered blocks. In such cases, **every access pays both seek and rotational delay**, making the access time slow and constant.

We can introduce a new metric that comes from the idea of measuring locality: **how often we can avoid seek and rotation delays**. We define **Data Locality  $DL$**  as:

$$DL = \% \text{ of blocks that can be accessed without new seek or rotation} \quad (61)$$

If **locality is high**, then most of our **data** is laid out in a nice, **sequential way**, therefore performance improves significantly. So, **locality determines whether our performance is close to best-case or worst-case**.

Thanks to the Data Locality, it is possible to calculate the **Average Service Time** by modifying the terms of *seek* and *rotation* of the Service Time equation (page 155):

$$T_{\text{I/O AVG}} = (1 - DL) \cdot (T_{\text{seek}} + T_{\text{rotation}}) + T_{\text{transfer}} + T_{\text{controller}} \quad (62)$$

### Exercise 2: Data Locality

The data of the exercise are:

- Read/Write of a sector of 512 bytes (0.5 KB)
- Data Locality:  $DL = 75\%$
- Data transfer rate: 50 MB/sec
- Rotation speed: 10000 RPM (Round Per Minute)
- Mean seek time: 6 ms
- Overhead Controller: 0.2 ms

Since the Data Locality is 75%, only 25% of the operations are affected by the DL:

$$(1 - DL) = (1 - 0.75) = 0.25$$

See the exercise on page 156 to understand the values of  $T_{\text{seek}}$ ,  $T_{\text{rotation}}$ ,  $T_{\text{transfer}}$  and  $T_{\text{overhead}}$ :

- $T_{\text{seek}} = 6$
- $T_{\text{rotation}} = 3$
- $T_{\text{transfer}} = 0.01$
- $T_{\text{overhead}} = 0.2$

Finally the average time for read/write a sector of 0.5 KB with a DL of 75% is:

$$\begin{aligned} T_{\text{I/O AVG}} &= 0.25 \cdot (6 + 3) + 0.01 + 0.2 \\ &= 0.25 \cdot 9 + 0.21 \\ &= 2.46 \text{ ms} \end{aligned}$$

### Exercise 3: Influence of “Not Optimal” Data Allocation

The data of the exercise are:

- 10 blocks of 1/10 MB for each block (10 blocks of 1/10 MB “not well” distributed on disk)
- $T_{\text{seek}} = 6 \text{ ms}$
- $T_{\text{rotation AVG}} = 3 \text{ ms}$
- Data transfer rate: 50 MB/sec

In the exercise you were asked to calculate the time taken to transfer a 1 MB file with 100% and 0% data locality:

- Data Locality equals to 100%:
  - An initial seek (6 ms)
  - A total rotation average (3 ms)
  - Now it’s possible to do the 1MB global transfer directly because there are no blocks to seek or rotation latency:

$$1 \text{ MB of } 50 \text{ MB} = \frac{1}{50} = 0.02 \text{ seconds} \cdot 1000 = 20 \text{ ms}$$

- The total time is:

$$T = 6 + 3 + 20 = 29 \text{ ms}$$

- Data Locality equals to 0%:
  - An initial seek (6 ms)
  - A total rotation average (3 ms)
  - In this case, it’s not possible to do a global transfer directly, because each block is affected by the seek or rotation latency. Then we have to transfer block by block and calculate the delay:

$$1 \text{ MB of } 10 \text{ MB} = \frac{1}{10} = 0.1 \text{ seconds} \cdot 1000 = 100 \text{ ms}$$

- The total time is:

$$T = (6 + 3 + 2) \cdot 10 = 110 \text{ ms}$$

Where 10 is the number of blocks.

Note: the controller times is not considered.

### 4.2.2 RAID

We can calculate some performance metrics related to the RAID technology (page 57).

- **MTTF (Mean Time To Failure)** is the **expected time before a disk fails**. It is usually provided by the manufacturer, based on statistical modeling (often assuming exponential failure distribution).

To calculate the MTTF for a Disk Array without redundancy, we must make the following assumptions:

- Constant Failure Rate;
- Exponentially distributed time to failure;
- Independent disk failures.

Then the formula is:

$$\text{MTTF}_{\text{array}} = \frac{\text{MTTF}_{\text{single disk}}}{\text{Number of Disks}} \quad (63)$$

This is because the array fails if **any one** of its disks fails; so the **failure rate of the system increases linearly with the number of disks**.

**⚠ RAID 0 and MTTF.** RAID 0 offers **no redundancy**, so it behaves like a pure array, and the **MTTF<sub>RAID 0</sub>**:

$$\text{MTTF}_{\text{RAID 0}} = \text{MTTF}_{\text{array}} = \frac{\text{MTTF}_{\text{single disk}}}{\text{Number of Disks}} \quad (64)$$

this is why RAID 0 is **high-risk** despite its performance: one disk failure means total data loss.

#### Example 11: MTTF

If:

- Each disk has an MTTF of 1,000,000 hours.
- We have an array of 100 disks.

Then:

$$\text{MTTF}_{\text{array}} = \frac{1,000,000}{100} = 10,000 \text{ hours}$$

Without fault tolerance, our system is 100× more likely to fail than a single disk.

With RAID 5 or 6, the system can still work if one disk fails. However, **if another disk fails during the rebuild process, data is lost** in RAID 5 or **further degraded** in RAID 6. Therefore, the probability of data loss is approximately equal to the probability of a second failure occurring within the mean time to recovery (MTTR) window.

$$\text{MTTF}_{\text{RAID}} = \text{MTTF}_{\text{array}} \cdot \left( \frac{1}{\% \text{ of additional critical failures during MTTR}} \right) \quad (65)$$

The first part  $\text{MTTF}_{\text{array}}$  captures the **rate of first failures**. The second part **increases the effective MTTF depending on how likely we are to survive the rebuild window** (i.e., how unlikely a second failure is during MTTR). In other words, the **probability term** models the likelihood of **another failure occurring during a vulnerable period when the system is degraded** (e.g., during the process of rebuilding a RAID 5 array with one failed disk).

- The **Mean Time To Failure of each RAID level** (except the zero) is:

– **RAID 1** (page 64) employs **mirroring**: every disk has an exact replica. This means each piece of data is stored **twice**, on two separate drives. The system can tolerate **one drive failure per mirrored pair** without data loss. In theory:

✓ **Best case:** up to  $\frac{N}{2}$  drives can fail without affecting data (if each failed drive is from a different mirror).

✗ **Worst case:** system fails if both disks in any mirror pair fail before the array is rebuilt.

The formula used is:

$$\text{MTTF}_{\text{RAID } 1} = \text{MTTF}_{\text{array}} \cdot \left( \frac{1}{\% \text{ of 2nd critical failure during MTTR}} \right) \quad (66)$$

Where:

\*  $\text{MTTF}_{\text{array}} = \frac{\text{MTTF}_{\text{single disk}}}{\text{Number of Disks}}$

\* MTTR: Mean Time To Repair.

\* % of 2nd critical failure during MTTR:

$$\% \text{ of 2nd critical failure during MTTR} = \frac{1}{\text{MTTF}_{\text{disk}}} \cdot \text{MTTR} \quad (67)$$

Where:

·  $\frac{1}{\text{MTTF}_{\text{single disk}}}$  is the **failure rate** of a single disk.

· MTTR is the the **duration in which the system is in a degraded state**, i.e., vulnerable to a second failure.

This probability models the **chance that the mirror of a failed disk also fails during the rebuild window**. The extended version:

$$\text{MTTF}_{\text{RAID } 1} = \frac{\text{MTTF}_{\text{disk}}^2}{N \cdot \text{MTTR}} \quad (68)$$

– **RAID 0 + 1** (page 64) means **first striping** (RAID 0), then **mirroring** (RAID 1). The disks are divided into **stripe groups**, and then each group is mirrored. If any disk in a stripe group fails, **that whole group is lost**. The array can survive a **single group failure**, but not a second.

$$\text{MTTF}_{\text{RAID } 0+1} = \text{MTTF}_{\text{array}} \cdot \left( \frac{1}{\% \text{ of 2nd critical failure during MTTR}} \right) \quad (69)$$

Where:

- \*  $\text{MTTF}_{\text{array}} = \frac{\text{MTTF}_{\text{single disk}}}{\text{Number of Disks}}$
- \* MTTR is the mean time to repair (the vulnerable window).
- \* Despite the RAID 1, the **probability of a second critical failure during the mean time to repair (MTTR)** is:

$$\% \text{ of 2nd critical failure during MTTR} = \left( \frac{G}{\text{MTTF}_{\text{disk}}} \right) \cdot \text{MTTR} \quad (70)$$

Where  $G$  is the number of **disks in each stripe group**, and  $\frac{G}{\text{MTTF}_{\text{disk}}}$  is the **combined failure rate** of the  $G$  disks in the remaining group. Multiplying this by the MTTR gives the probability that the second group will fail during the rebuild.

Once a **disk** in one stripe group **fails**, the **entire group becomes inoperative**. To avoid total data loss, the **mirrored stripe group must not fail before rebuild completes**.

The extended version:

$$\text{MTTF}_{\text{RAID } 01} = \frac{\text{MTTF}_{\text{disk}}^2}{N \cdot G \cdot \text{MTTR}} \quad G = \text{disks per stripe group} \quad (71)$$

- **RAID 1 + 0** (page 65) combines **mirroring first** (RAID 1) then **striping** (RAID 0). Disks are organized into mirrored pairs. Then data is striped across the pairs. A disk can fail in any mirrored pair, the system remains operational. To cause data loss, **both disks in a mirrored pair must fail**. Thus, it **tolerates multiple disk failures** as long as no pair is entirely lost.

$$\text{MTTF}_{\text{RAID } 1+0} = \text{MTTF}_{\text{array}} \cdot \left( \frac{1}{\% \text{ of 2nd critical failure during MTTR}} \right) \quad (72)$$

Where:

- \*  $\text{MTTF}_{\text{array}} = \frac{\text{MTTF}_{\text{single disk}}}{\text{Number of Disks}}$
- \* MTTR is the mean time to repair (the vulnerable window).
- \* The probability of a second critical failure during the Mean Time To Repair (MTTR) is the same as for RAID 1 (see formula 67):

$$\% \text{ of 2nd critical failure during MTTR} = \frac{1}{\text{MTTF}_{\text{disk}}} \cdot \text{MTTR} \quad (73)$$

The system is only at risk if the **exact mirror** of the failed disk also fails during the rebuild. So, unlike RAID 0+1, the failure risk localized, not dependent on an entire group.

The extended version:

$$\text{MTTF}_{\text{RAID } 10} = \text{MTTF}_{\text{RAID } 1} = \frac{\text{MTTF}_{\text{disk}}^2}{N \cdot \text{MTTR}} \quad (74)$$

- **RAID 4** (page 68) is a block-level striping with a **dedicated parity disk**. All parity information is stored on **one disk**, creating a bottleneck on writes.
  - RAID 5** (page 72) is a block-level striping with **distributed parity**. Parity is **spread across all disks**, improving write performance and eliminating the RAID 4 bottleneck.
- Both RAID 4 and RAID 5 can **tolerate a single disk failure**. Data is reconstructed using parity. Failure occurs only if **a second disk fails before** the first one is rebuilt.

$$\text{MTTF}_{\text{RAID } 4, 5} = \text{MTTF}_{\text{array}} \cdot \left( \frac{1}{\% \text{ of 2nd failure during MTTR}} \right) \quad (75)$$

Where:

- \*  $\text{MTTF}_{\text{array}} = \frac{\text{MTTF}_{\text{single disk}}}{\text{Number of Disks}}$
- \* MTTR is the mean time to repair (the vulnerable window).
- \* The probability of a second critical failure during the Mean Time To Repair (MTTR) is:

$$\% \text{ of 2nd failure during MTTR} = \frac{N - 1}{\text{MTTF}_{\text{disk}}} \cdot \text{MTTR} \quad (76)$$

Where  $N$  is the number of disks in the array. The **first failure** does not cause data loss (covered by parity). The **second failure** is only dangerous **if it occurs during rebuild**. The probability considers all  $N - 1$  remaining disks and their individual failure rates.

They have the same formula because they both rely on **single-parity protection**. The **main difference** between them is their **performance** and **load balancing capabilities**, not their reliability! The extended version:

$$\text{MTTF}_{\text{RAID } 4} = \text{MTTF}_{\text{RAID } 5} = \frac{\text{MTTF}_{\text{disk}}^2}{N(N - 1) \cdot \text{MTTR}} \quad (77)$$

- **RAID 6** (page 76) is an extension of RAID 5 with **double parity**. It uses two independent parity blocks per stripe (commonly  $P$  and  $Q$ ). These allow the array to tolerate **two simultaneous disk failures**. The system only fails if **a third disk fails** during the time in which the two failed disks are being rebuilt.

$$\text{MTTF}_{\text{RAID } 6} = \text{MTTF}_{\text{array}} \cdot \frac{1}{\% \text{ 2nd failure} \cdot \% \text{ 3rd failure}} \quad (78)$$

Where:

- \*  $\text{MTTF}_{\text{array}} = \frac{\text{MTTF}_{\text{single disk}}}{\text{Number of Disks}}$
- \* MTTR is the mean time to repair (the vulnerable window).

- \* The probability of the second failure during MTTR:

$$\% \text{ 2nd failure} = \frac{N - 1}{\text{MTTF}_{\text{single disk}}} \cdot \text{MTTR} \quad (79)$$

It is the risk of a second failure while the first is being repaired.

- \* The probability of the third failure during MTTR:

$$\% \text{ 3rd failure} = \frac{N - 2}{\text{MTTF}_{\text{single disk}}} \cdot \frac{\text{MTTR}}{2} \quad (80)$$

It is the risk of a third failure during the overlapping time when **both first and second disks** are being rebuilt. The MTTR is divided by two because it **assumes** that both **disks are under recovery simultaneously (average time)**.

Unlike RAID 5, RAID 6 can still recover after a second disk fails. But during this dual-failure state, the system becomes vulnerable to a **third-failure**. That third failure is what RAID 6 models as catastrophic. The extended version:

$$\text{MTTF}_{\text{RAID } 6} = \frac{2}{N} \cdot \frac{\text{MTTF}_{\text{disk}}^3}{(N - 1) \cdot (N - 2) \cdot \text{MTTR}^2} \quad (81)$$

Metric	Tolerates
$\text{MTTF}_{\text{RAID } 0} = \frac{\text{MTTF}_{\text{single disk}}}{N}$	0 disk failures
$\text{MTTF}_{\text{RAID } 1+0} = \frac{(\text{MTTF}_{\text{single disk}})^2}{(N \times \text{MTTR})}$	Multiple failures (1 per mirror)
$\text{MTTF}_{\text{RAID } 0+1} = \frac{(\text{MTTF}_{\text{single disk}})^2}{(N \times G \times \text{MTTR})}$	1 full group
$\text{MTTF}_{\text{RAID } 4} = \frac{(\text{MTTF}_{\text{single disk}})^2}{(N \times N - 1 \times \text{MTTR})}$	1 disk
$\text{MTTF}_{\text{RAID } 5} = \frac{(\text{MTTF}_{\text{single disk}})^2}{(N \times N - 1 \times \text{MTTR})}$	1 disk
$\text{MTTF}_{\text{RAID } 6} = \frac{2 \times (\text{MTTF}_{\text{single disk}})^3}{(N \times N - 1 \times N - 2 \times \text{MTTR}^2)}$	2 disks

Table 12: MTTF summary RAID levels.

- RAID 0: No redundancy. Failure of any disk leads to total data loss.
- RAID 1+0: High reliability; localized failure risk; faster rebuilds.
- RAID 0+1: Less reliable than 1+0; entire group fails if any disk in it fails.

- RAID 4/5: Identical MTTF; RAID 5 distributes parity to avoid bottlenecks of RAID 4.
- RAID 6: Extremely high reliability; more complex failure modeling.

Last remarks:

- The increase in **exponential of MTTF<sub>disk</sub>** reflects higher redundancy (RAID 6 uses  $MTTF^3$ ).
- More complex RAID levels (1+0 or 6) handle multiple simultaneous failures much more gracefully.
- **Mean Time To Repair (MTTR)** plays a critical role: the longer the rebuild takes, the more likely a second or third failure occurs.

### 4.3 Scalability and performance of data centers

#### 4.3.1 Evaluate system quality

System quality information is critical from a cost and performance perspective. In this context, “*performance*” means the **overall effectiveness of a computer system in terms of throughput, response time, and availability**.

##### ⌚ So how do we evaluate system quality?

There are generally two approaches:

- **Intuition and trend extrapolation.** Obviously, those who possess these qualities in sufficient quantity are rare. The pros are speed and flexibility, but the cons are accuracy.
- **Experimental evaluation of alternatives.** As pro has excellent accuracy, but as con has laborious and flexible.

The techniques are represented in the following figure.

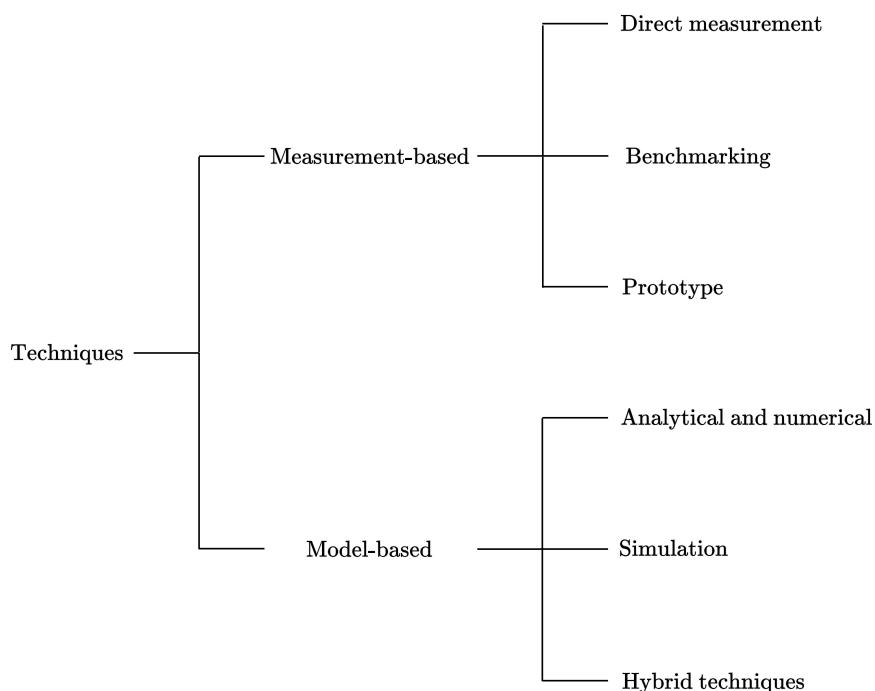


Figure 43: Quality Evaluation techniques.

The most common and useful solution to evaluate system quality is **model-based approach**. The systems are complex, so it is useful to create an **abstraction of the systems called models**. The model-based are divided into three groups:

- **Analytical and numerical techniques** are based on the **application of mathematical techniques**, which usually exploit results coming from the theory of probability and stochastic process.

✓ **Advantages**

- Most **efficient**.
- **Accurate**.

👎 **Disadvantages**

- Available only in very **limited cases**.

- **Simulation techniques** are based on the **reproduction of traces of the model**.

✓ **Advantages**

- Most **general**.

👎 **Disadvantages**

- May be **less accurate**, especially when considering cases where rare events may occur.
- **Solution time** can also be **very long** if high accuracy is desired.

- **Hybrid techniques** combine analytical/numerical methods with simulation.

### 4.3.2 Queueing Networks

#### 4.3.2.1 Definition

**Queueing Network Modeling** is a particular approach to computer system modeling in which the **computer system is represented as a network of queues**. A *network of queues* is a collection of **service centers**, which represent system **resources**, and **customers**, which represent **users or transactions**. [4]

Some **examples** of queues in computer systems are:

- CPU uses a time-sharing scheduler.
- A disk serves a queue of requests waiting to read or write blocks.
- A router on a network serves a queue of packets waiting to be routed.
- Databases have lock queues where transactions wait to acquire the lock on a record.

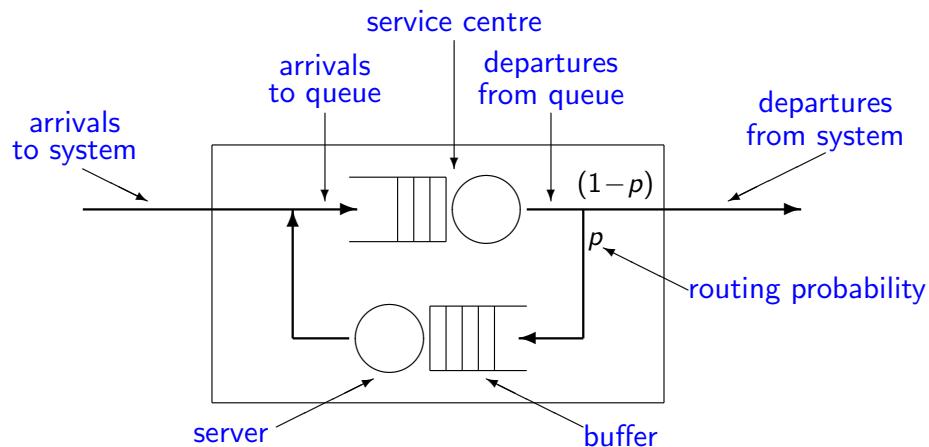


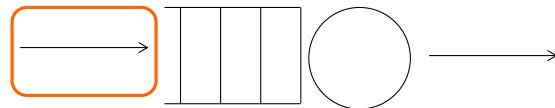
Figure 44: Queueing Network graphical representation.

#### 4.3.2.2 Characteristics

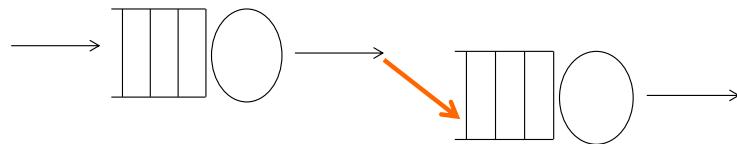
Queueing models are characterized by several aspects:

- **Arrival.** Arrivals represent orders coming into the system. They specify *how fast, how often, and what types of jobs* the station will service. **Arrivals can come from:**

1. An external source.



2. Another queue.



3. The same queue, through a loopback arc.

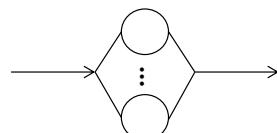


- **Service.** Service represents the time a job spends being served. The server does the job, but the number of servers can be different:

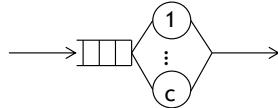
- **Single server.** It has the ability to serve one client at a time. Waiting customers remain in the buffer until they are selected for service. Finally, the next customer is selected depending on the service discipline.



- **Infinite servers.** There are always at least as many servers as there are customers, and each customer can have a dedicated server. As a consequence, there is no queuing (and no buffer).



- **Multiple servers.** There is a **fixed number of servers** ( $c$  in the figure below), each of which can **serve one customer at a time**.
  - \* Number of customers in the system  $\leq$  number of servers  
 $\Rightarrow$  **no queuing**.
  - \* Number of customers in the system  $>$  number of servers  
 $\Rightarrow$  the additional **customers must wait in the buffer**.



- **Queue.** If jobs exceed the parallel processing capacity of the system, they are **forced to wait in a buffer**.

When the job currently in service leaves the system, one of the jobs in the queue can now enter the free service center. **Service Discipline/Queuing Policy** determines which of the jobs in the queue will be selected to start its service.

- **Population.** Ideally, members of the population are indistinguishable from one another. When this is not the case, we divide the population into **classes whose members all exhibit the same behavior**. Different classes differ in one or more characteristics, e.g. arrival rate, service demand. Identifying different classes is a task of workload characterization.
- **Routing.** For many systems, we can view the system as a collection of resources and devices, with customers or jobs circulating between them.

We can associate a service center with each resource in the system and then route customers between the service centers.

After being serviced at one service center, a customer can move on to other service centers, following a pre-defined pattern of behavior according to the customer's needs.

A queueing network can then be represented as a graph where the nodes represent the service centers  $k$  and the arcs represent the possible transitions of users from one service center to another. Nodes and arcs together define the network topology.

Whenever a job has several possible alternative routes after completing service at a station, an appropriate selection policy must be defined.

The policy is also called the **Routing Algorithm**. The most important routing algorithms are:

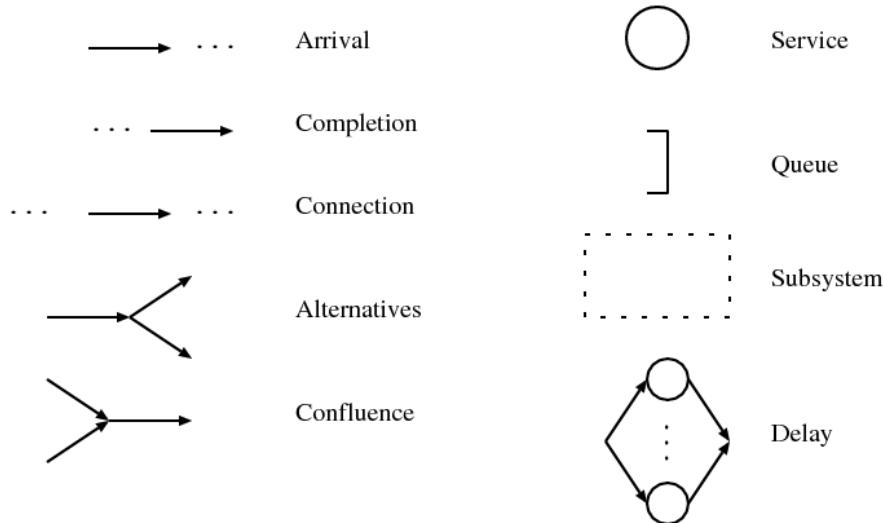
- **Probabilistic Routing Algorithm.** Each path is assigned a probability of being chosen by the job that left the station in question.
- **Round Robin Routing Algorithm.** The destination chosen by the job rotates among all possible existing destinations.

- **Join the shortest queue Routing Algorithm.** Jobs can query the queue length of the possible destinations and choose the one with the least number of jobs waiting to be served.

With important definition of routing, we can say that a **network** can be:

- **Open.** Customers can come from or go to any external environment.
- **Closed.** A fixed population of customers remains within the system.
- **Mixed.** There are classes of customers within the system that exhibit both open and closed patterns of behavior.

An additional graphical notation is:

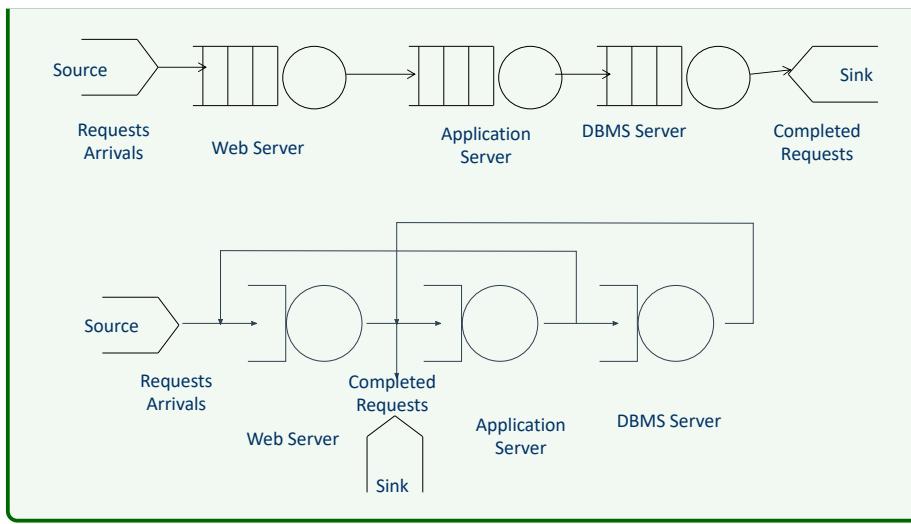


#### Example 12: Open Networks

A client server system, dealing with external arrivals (classical three tier architecture).

Provide a QN model of the system and evaluate the overall throughput considering that the network delay is negligible with respect to the other devices and two different cases:

1. The only thing we know is that each server should be visited by the application.
2. In the second case we know that the application **after visiting the web server** requires some operations at **the application server** and then **can go back to the web server** and leave the system **or** can require service at the **DMBS** and then **go back to the application server**.

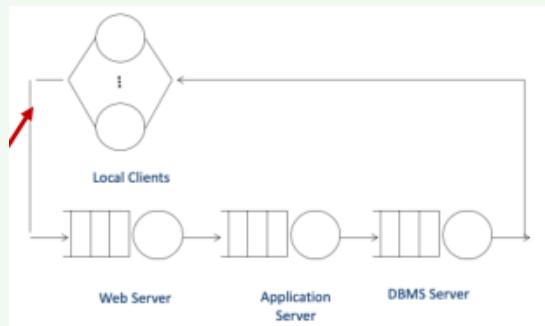


### Example 13: Closed Networks

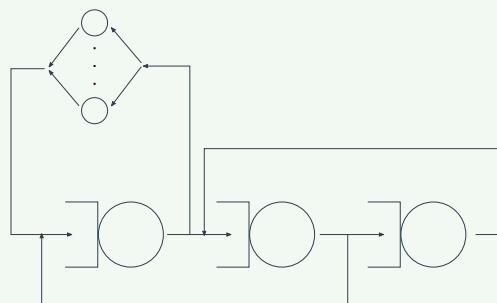
A client server system, **with a finite number of customers** (classical three tier architecture and not accessible from outside).

Provide a QN model of the system and evaluate the system throughput considering that Network delay is negligible with respect to the other devices. Model the two different cases previously described.

- First scenario



- Second scenario



### 4.3.3 Operational Laws

**Operational Laws** are simple equations that can be used as an abstract representation or model of the average behavior of almost any system.

#### ✓ Advantages

- The laws are very general and make almost no assumptions about the behavior of the random variables that characterize the system.
- **Simplicity:** they can be applied quickly and easily.

In the Computing Infrastructure course, then in this note, the operational laws are applied to the Queueing Network model (4.3.2, page 168).

Operational laws are based on **observable variables**, values that we can derive by observing a system over a finite period of time.

In general, we assume that the system receives requests from its environment. Each request creates a job or customer within the system. Finally, when a job has been processed, the system responds to the environment by completing the corresponding request.

---

#### 4.3.3.1 Basic measurements

From an abstract system we can derive the following quantities:

- **T**, the length of time we observe the system
- **A**, the number of request arrivals we observe
- **C**, the number of request completions we observe
- **B**, the total amount of time during which the system is busy ( $B \leq T$ )
- **N**, the average number of jobs in the system

From these values, we can derive the following four important **quantities**:

- **Arrival rate:**

$$\lambda = \frac{\text{number of request arrivals}}{\text{length of time we observe the system}} = \frac{A}{T} \quad (82)$$

- **Throughput or Completion rate:**

$$X = \frac{\text{number of request completions}}{\text{length of time we observe the system}} = \frac{C}{T} \quad (83)$$

- **Utilization:**

$$U = \frac{\text{total amount of time during which the system is busy}}{\text{length of time we observe the system}} = \frac{B}{T} \quad (84)$$

- **Mean service time** per completed job:

$$S = \frac{\text{total amount of time during which the system is busy}}{\text{number of request completions}} = \frac{B}{C} \quad (85)$$

We will assume that the **system is job-flow balanced**. Then the **number of arrivals is equal to the number of completions** during an observation period.

Note that if the system is job flow balanced, then the **arrival rate is equal to the completion rate (throughput)**:

$$\lambda = X$$

A **system** can be thought of as **consisting** of a number of devices or **resources**. Each of these can be treated as a **separate system** from the perspective of operational laws.

An **external request generates a job** within the system; this job may **then circulate among the resources** until all the necessary processing has been done; as it arrives at each resource, it is treated as a request, generating a job internal to that resource.

In this case, we have the following quantities:

- **T**, the **length of time** we observe the system
- **$A_k$** , the number of request **arrivals** we observe for resource  $k$
- **$C_k$** , the number of request **completions** we observe at resource  $k$
- **$B_k$** , the total amount of time during which the resource  $k$  is **busy** ( $B_k \leq T$ )
- **$N_k$** , the average **number of jobs** in the resource  $k$

And we can derive the following four quantities for resource  $k$ :

- **Arrival rate**:

$$\lambda_k = \frac{A_k}{T} \quad (86)$$

- **Throughput or Completion rate**:

$$X_k = \frac{C_k}{T} \quad (87)$$

- **Utilization**:

$$U_k = \frac{B_k}{T} \quad (88)$$

- **Mean service time** per completed job:

$$S_k = \frac{B_k}{C_k} \quad (89)$$

#### 4.3.3.2 Utilization Law

Using the formulas:

- Throughput:  $X_k = \frac{C_k}{T}$
- Mean service time:  $S_k = \frac{B_k}{C_k}$
- Utilization:  $U_k = \frac{B_k}{T}$

From:

$$X_k \cdot S_k = \frac{C_k}{T} \cdot \frac{B_k}{C_k} = \frac{B_k}{T} = U_k$$

We can derive the **Utilization Law**:

$$U_k = X_k \cdot S_k \quad (90)$$

#### 4.3.3.3 Little's Law

The **Little's Law** is:

$$N = X \cdot R \quad (91)$$

In other words,  $N$  is equal to the **number of requests in the system**. Little's Law can be applied to the entire system as well as to some subsystems.

If the system throughput is  $X$  requests/sec, and each request remains in the system on average for  $R$  seconds, then for each unit of time, we can observe on average  $XR$  requests in the system.

#### Example 14

Consider a disk that serves 40 requests/seconds ( $X = 40$  req/s) and suppose that on average there are 4 requests ( $N = 4$ ) present in the disk system (waiting to be served or in service).

Little's Law tell that  $N = XR \Rightarrow R = \frac{N}{X}$ , so the average time spent at the disk by a request must be  $\frac{4}{40} = 0.1$ .

If we know  $S$  (e.g.) each request requires 0.0225 seconds of disk service and we can then deduce that the average waiting time (time in the queue) is 0.0775 seconds.

The value of Little's Law changes depending on the application:

- Service level.

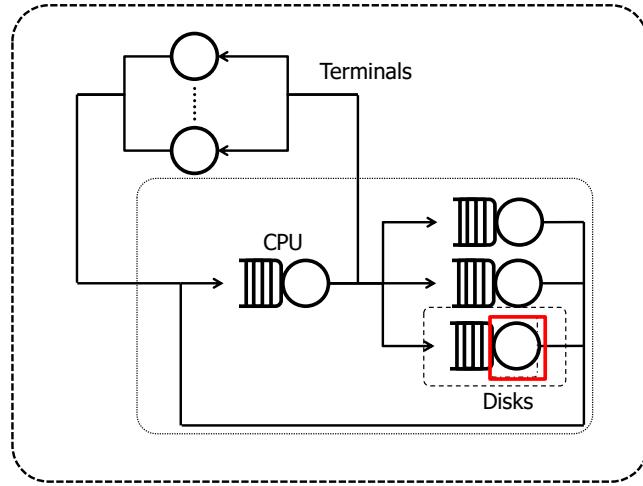
– The service time is:

$$R = S$$

Where  $R$  is the average of each request remaining in the system.

– The utilization is:

$$N = X \cdot R = X \cdot S = U$$



- Service and Queue level.

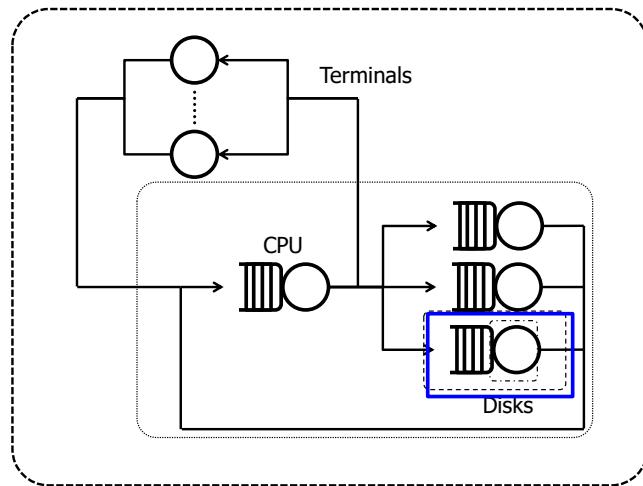
- The service time is:

$$R = S$$

Where  $R$  is the average of each request remaining in the system.

- The utilization is:

$$N = \text{Flying requests} \Rightarrow \frac{N}{X} = R = (S + T_{\text{queue}})$$



- Subsystem level.

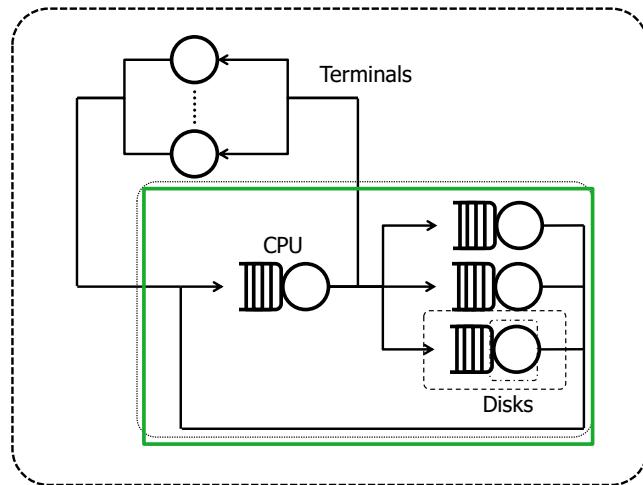
- The service time is:

$$R = \text{Residence Time}$$

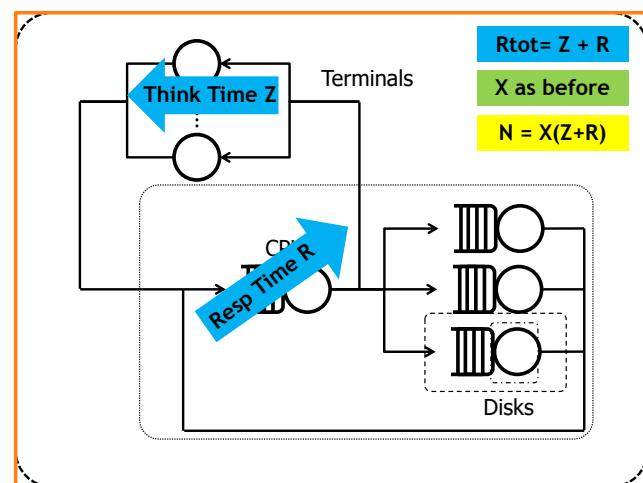
Residence time corresponds to our conventional notion of response time: the period of time from when a user submits a request until that user's response is returned.

- The utilization is:

$$N = \text{Flying requests} \Rightarrow \frac{N}{X} = R$$



- System level.



#### 4.3.3.4 Interactive Response Time Law

The **Interactive Response Time Law** is:

$$R = \frac{N}{X} - Z \quad (92)$$

The response time in an interactive system is the **residence time minus the think time**. Note that if the think time is zero ( $Z = 0$ ) and  $R = \frac{N}{X}$ , then the **interactive response time law simply becomes Little's Law**.

##### Example 15

Suppose that the library catalogue system has **64 interactive users** connected via Browsers, the average **think time is 30 seconds**, and that system **throughput is 2 interactions/second**. What is the response time?

The interactive response time law tell us that the response time must be  $\frac{64}{2} - 30 = 2$  seconds.

#### 4.3.3.5 Visit count

In an observation interval we can count not only completions external to the system, but also the number of completions at each resource within the system. We denote  $C_k$  by the **number of completions at resource  $k$** . We define the **Visit Count**:

$$V_k = \frac{C_k}{C} \quad (93)$$

It is the ratio of the number of completions at the  $k$ -th resource to the number of system completions.

##### Example 16

If, during an observation interval, we measure **10 system completions** and **150 completions at a specific disk**, then on average each system-level request requires **15 disk operations**.

Note that:

- If  $C_k > C$ , resource  $k$  is **visited several times** (on average) during each system level request. This happens when there are **loops in the model**.
- If  $C_k < C$ , resource  $k$  **might not be visited** during each system level request. This can happen if there are **alternatives** (e.g. caching of disks).
- If  $C_k = C$ , resource  $k$  is **visited** (on average) **exactly once every request**.

#### 4.3.3.6 Forced Flow Law

The **Forced Flow Law** captures the relationship between the different components within a system. It states that the throughputs, or flows, in all parts of a system must be proportional to each other.

$$X_k = V_k \cdot X \quad (94)$$

The throughput at the  $k$ -th resource is equal to the product of the throughput of the system and the visit count at that resource.

Rewriting  $C_k = V_k \cdot C$  and applying  $X_k = \frac{C_k}{T}$ , we can derive the forced flow law:

$$C_k = V_k \cdot C \Rightarrow \frac{C_k}{T} = \frac{V_k \cdot C}{T} \Rightarrow X_k = V_k \cdot X$$


---

#### 4.3.3.7 Utilization Law with Service Demand

If we know the amount of processing each job requires at a resource then we can calculate the utilization of the resource.

Let us assume that each time a job visits the  $k$ -th resource, the amount of processing or service time it requires is  $S_k$ .

Note that **service time is not the same as the residence time** of the job at that resource. In general a job might have to **wait** for some time **before processing** being.

The **total amount of service that a system job generates at the  $k$ -th resource** is called the **Service Demand  $D_k$** :

$$D_k = S_k \cdot V_k \quad (95)$$

Using the service demand, we can rewrite the **Utilization Law**:

$$U_k = X_k \cdot S_k = (X \cdot V_k) \cdot S_k = D_k \cdot X \quad (96)$$

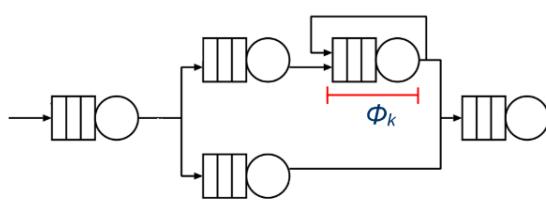
The utilization of a resource is denoted  $U_k$  and it is the percentage of time that the  $k$ -th resource is in use processing a job. It is also equal to the product of:

- The throughput of that resource and the average service time at that resource;
- The throughput at system level and the average service demand at that resource.

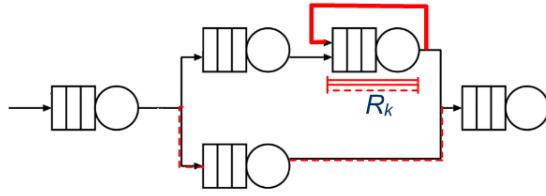
#### 4.3.3.8 Response and Residence Times

When considering nodes characterized by visits different from one, we can define two permanence times: Response Time and Residence Time.

The **Response Time**  $\tilde{R}_k$  (or  $\Phi_k$ ) accounts for the **average time spent in station  $k$** , when the **job enters the corresponding node** (i.e. time for the single interaction, disk request):



The **Residence Time**  $R_k$  accounts instead for the **average time spent by a job at station  $k$  during the staying in the system**: it can be greater or smaller than the response time depending on the number of visits.



Note that there is the same relation between Residence Time and Response Time as the one between **Demand Time** and **Service Time**:

$$\begin{aligned} D_k &= v_k \cdot S_k \\ R_k &= v_k \cdot \tilde{R}_k \end{aligned} \tag{97}$$

Also note that for **single queue open system**, or *tandem models*,  $v_k = 1$ . This implies that **average service time and service demand are equal, and response time and residence time are identical**.

$$v_k = 1 \Rightarrow \begin{aligned} D_k &= S_k \\ R_k &= \tilde{R}_k \end{aligned}$$

#### 4.3.4 Bounding Analysis

##### 4.3.4.1 Introduction

The simplest useful approach to computer system analysis using queueing network models is **Bounding Analysis**. With very little computation it is possible to determine upper and lower bounds on system throughput and response time as functions of the system workload intensity (number of arrival rate of customers).

##### Advantages

- **Highlight** and **quantify** the critical influence of the system **bottleneck**<sup>11</sup>.
- Can be **computed quickly**, even by hand.
- Useful in **System Sizing**.
- Useful for **System Upgrades**.

The notation used is:

- **K**, the **number of service centers**.
- **D**, the **sum of the service demands at the centers**, so:

$$D = \sum_k D_k \quad (98)$$

- **D<sub>max</sub>**, the **largest service demand at any single center**.
- **Z**, the **average think time**, for interactive systems.

And the following **performance quantities** are considered:

- **X**, the **system throughput**.
- **R**, the **system response time**.

---

<sup>11</sup>The resource within a system which has the greatest service demand is known as the **bottleneck resource** or **bottleneck device**, and its service demand is  $\max_k \{D_k\}$ , denoted  $D_{\max}$ .

The bottleneck resource is important because it limits the possible performance of the system. This will be the resource which has the highest utilization in the system.

#### 4.3.4.2 Asymptotic bounds

The **Asymptotic Bounds** are derived by considering the (asymptotically) extreme conditions of light and heavy loads. There are two possible views:

- **Optimistic**

- Upper bound: *system throughput*
- Lower bound: *system response time*

- **Pessimistic**

- Upper bound: *system response time*
- Lower bound: *system throughput*

The **extreme conditions** used are:

- Light load.
- Heavy load.

The bounding analysis **assumes** that a customer's service **demand** at a center **does not depend on how many other customers are currently in the system or in which service centers they are located**.

#### Open Models

An **Open Model** has **jobs** (or operations) **arriving freely** from the outside, at a given arrival rate  $\lambda$ . For example, web servers receive requests from many different users with no fixed limit, so new requests can arrive at any time. For the **open models**, the  $X$  (*system throughput*) bound is equal to the **maximum arrival rate** that the system can handle.

If the  $\lambda$  (arrival rate, page 173) is greater than the  $X$  (*system throughput*)  $\lambda > X$ , then the **system is saturated**. This situation **causes new jobs to wait indefinitely**.

The  $X$  (*system throughput*) bound is calculated as:

$$\lambda_{\text{sat}} = \frac{1}{D_{\max}} \quad (99)$$

The  $R$  (*system response time*) bound is equal to the largest and smallest possible system response time experienced at a given arrival rate ( $\lambda$ ), which is only examined if  $\lambda < \lambda_{\text{sat}}$ . If the condition is **not satisfied**, then the **system is unstable**.

With the open models, there are two **extreme situations** to consider:

- If **no customers interferes with any other**, so **no queue time**, then the system response time is equal to the sum of the service demands at the centers  $\mathbf{R} = \mathbf{D}$ , with  $D = \sum_k D_k$ .

- If  $n$  customers arrive together every  $\frac{n}{\lambda}$  time units, there is **no pessimistic bound** on  $R$  (system response time).

Customers at the end of the batch are forced to queue for customers at the front of the batch, and thus experience large response times. The **batch can be extremely long**  $N \rightarrow \infty$ .

**There is no pessimistic bound on response times, regardless of how small the arrival rate  $\lambda$  might be.**

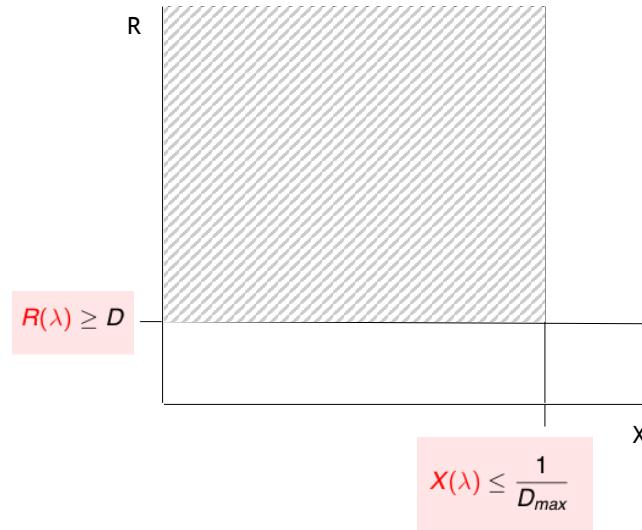
The bounding analysis for open models gives the following formulas:

- Bound for  $X(\lambda)$ :

$$X(\lambda) \leq \frac{1}{D_{\max}} \quad (100)$$

- Bound for  $R(\lambda)$ :

$$R(\lambda) \geq D_{\max} \quad (101)$$



### Closed Models

A **Closed Model** has a **fixed number of users** (or jobs) circulating between **thinking** and **requesting service**. For example, consider an interactive terminal in a university lab where 20 users log in. Each user submits a job and waits for a response. Then, they think and finally submit another job. Here the population  $N$  is fixed, and users “*think*”, so we introduce the **think time**  $Z$ .

Bounding Analysis depends on the situation:

- **Light Load** situation.
  - **Lower bounds:**
  - \* **1 customer** case:

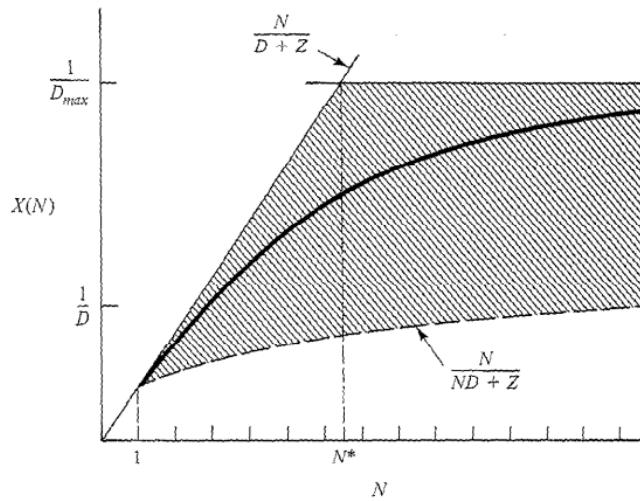
$$\begin{aligned} N &= X \cdot (R + Z) \\ 1 &= X \cdot (D + Z) \\ X &= \frac{1}{(D + Z)} \end{aligned} \tag{102}$$

- \* **Adding customers:** smallest  $X$  (*system throughput*) obtained with largest  $R$  (*system response time*), i.e., new jobs queue behind others already in the system.

Remember: in closed models, the highest possible system response time occurs when each job, at each station, found all the other  $N - 1$  costumers in front of it, then  $R = N \cdot D$ .

In this case  $R = N \cdot D$  and  $X$  is:

$$\begin{aligned} X &= \frac{N}{(N \cdot D + Z)} \\ \lim_{N \rightarrow \infty} \frac{N}{(N \cdot D + Z)} &= \frac{1}{D} \end{aligned} \tag{103}$$



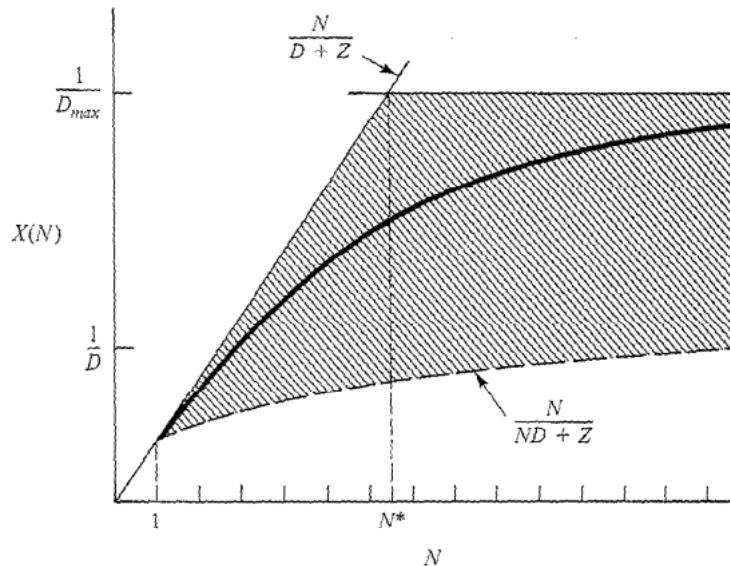
– **Upper bounds:**

\* **Adding customers:** largest  $X$  (*system throughput*) obtained with the lowest response time  $R$  (*system response time*, i.e. no conflicts).

Remember: in closed models, the lowest response time can be obtained if a job always finds the queue empty and always starts being served immediately.

In this case  $R = D$  and  $X$  is:

$$X = \frac{N}{(D + Z)} \quad (104)$$



• **Heavy Load** situation.

– **Upper bound:**

$$U_k(N) = X(N) D_k \leq 1 \quad (105)$$

Since the first to saturate is the **bottleneck** (max):

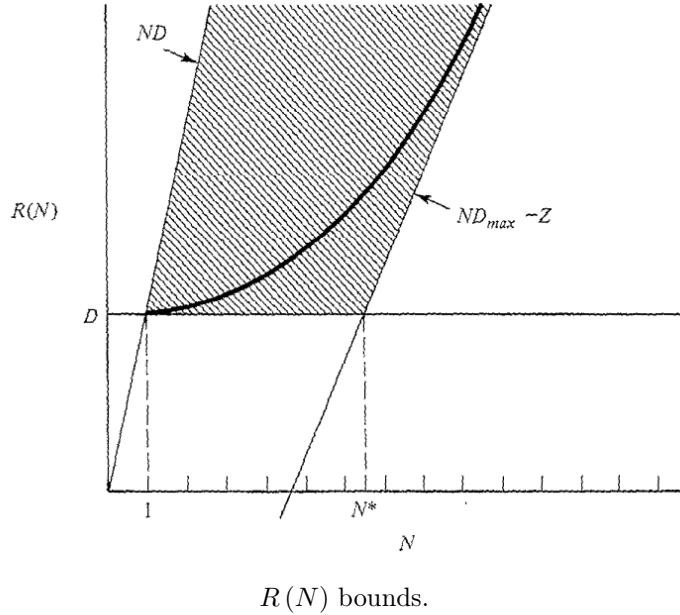
$$X(N) \leq \frac{1}{D_{\max}} \quad (106)$$

The  $X(N)$  bounds is:

$$\frac{N}{N \cdot D + Z} \leq X(N) \leq \min \left( \frac{1}{D_{\max}}, \frac{N}{D + Z} \right) \quad (107)$$

The  $R(N)$  bounds is:

$$\max(D, N \cdot D_{\max} - Z) \leq R(N) \leq N \cdot D \quad (108)$$



\*  $N^*$  case: particular population size determining if the light or heavy load optimistic bound is to be applied:

$$N^* = \frac{D + Z}{D_{\max}} \quad (109)$$

- If  $N < N^*$ : use light load bound ( $Z$  matters). The population is too small to fully load the bottleneck, then throughput limited by think time.

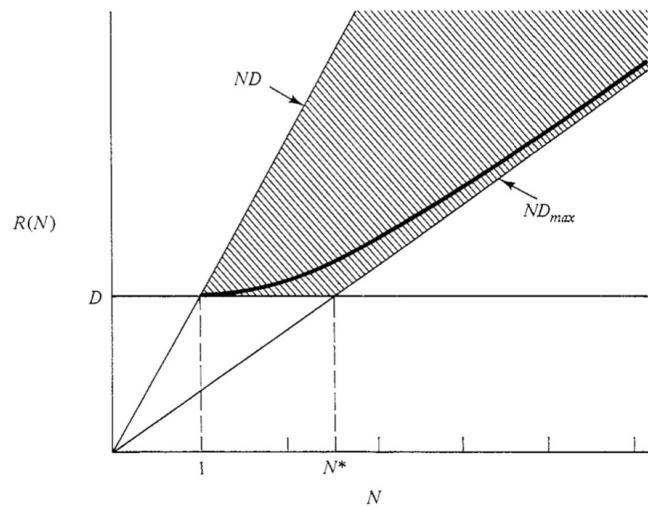
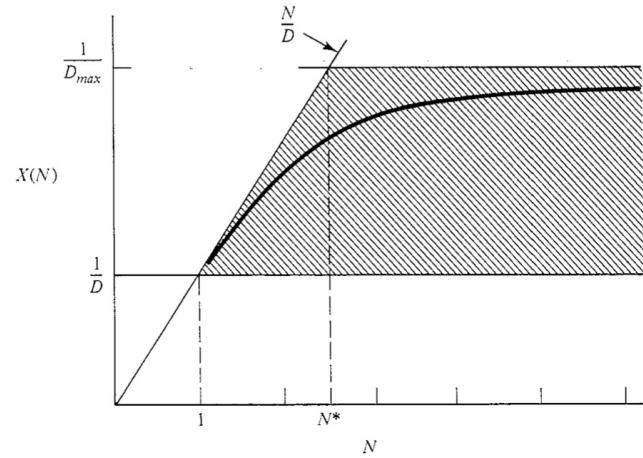
Here,  $D$  is the total resource consumption (sum over parallel branches). Throughput is limited by total work done, not wall-clock.

- If  $N > N^*$ : use heavy load bound ( $Z$  irrelevant, bottleneck only). The population is big enough to saturate the bottleneck, then throughput capped by hardware,  $Z$  doesn't matter anymore.

Here,  $D_{\text{critical}}$  is the critical-path time (max over parallel branches). Only the slowest resource matters as load grows.

We always calculate  $N^*$  using the parallel (critical path) version of  $D$ ; whereas the light-load throughput requires the full sequential (total work)  $D$ .

Without thinking time we have the following limits:



## 5 Exams

### 5.1 2025

#### 5.1.1 February 3

##### True (✓) false (✗) questions

1. ✓ Data centers require specialized fire suppression systems.
2. ✗ In current datacenters, east-west traffic is typically less bandwidth-intensive than north-south traffic.
3. ✓ Cloud computing does not require the user to manage the underlying hardware infrastructure, instead relying on the cloud provider to manage it.
4. ✗ RAID 6 offers better random read performance than RAID 5.
5. ✓ Cloud architectures can help reduce the cost of IT infrastructure by enabling pay-as-you-go pricing.
6. ✓ In-rack cooling involves placing cooling units directly in the server racks.
7. ✗ RAID 5 has a higher storage overhead than RAID 4.
8. ✗ Oversubscription is not used in TOR switches
9. ✗ A three-tier network architecture is never used in leaf-spine architectures
10. ✓ Raised floor systems in data centers help with cable management and airflow distribution.

##### Exercises

11. Let us consider a set of requests in the disk queue referring to the following cylinders of the disk: 65, 23, 50, 8, 39. Consider the initial position of the disk head at cylinder 52 and it is moving from inside (lower cylinder number) to outside (higher cylinder number). If no further requests arrive, write the order of the served requests (from the first to the last) if the disk head scheduling algorithm adopted is SCAN? Use the cylinder number to refer to the request.

**Answer:** SCAN (Elevator Algorithm) is a disk scheduling algorithm (see page 43). In this algorithm, the head moves in one direction (like an elevator), serving all requests in that direction. When it reaches the end, it reverses direction.

The exercise text gives us a hint about the original movement: “[...] from inside (lower cylinder number) to outside (higher cylinder number) [...]”. Therefore, we know that the next value will be 65, and then it will return since it is the highest value (end).

$$(52 \rightarrow 65 \xrightarrow{\text{end reached, moving inside...}} 50 \rightarrow 39 \rightarrow 23 \rightarrow 8)$$

12. A company uses a computing system composed of three servers: one front-end server and two back-end servers. The system remains operational even if one of the two back-end servers fails. In all other cases, the system is considered offline. All servers have a Mean Time To Failure (MTTF) of 8 months. (i) Compute the probability that at least one of the three servers fails within the first 40 days, and (ii) compute the overall reliability of the computing system after 40 days. *Notes: Use at least 4 decimal places for each intermediate calculation.*

**Answer:** The system works if the front-end works **AND** at least 1 back-end works. So only 1 back-end can fail. The system is down if both fails or if front-end fails.

- (a) First of all, we compute **single server reliability**. We use the reliability exponential function (see page 136):

$$R(t) = e^{-\lambda t} \quad \text{where } \lambda = \frac{1}{\text{MTTF}}$$

We convert MTTF to days:  $8 \times 30 = 240$ . Then:

$$\lambda = \frac{1}{240} = 0.004166667$$

The reliability is:

$$\begin{aligned} R(t) &= e^{-0.004166667 \times 40} \\ &= e^{-0.16666667} \\ &= \frac{1}{e^{0.16666667}} \\ &= \frac{1}{1.181360413} \\ &= 0.846481725 \end{aligned}$$

So probability of failure in 40 days (using unreliability function, see page 133):

$$Q(t) = 1 - R(t) = 1 - 0.846481725 = 0.153518275$$

- (b) Part (i) - **Probability that at least one of the 3 servers fails.**  
All 3 must work to have no failures. So:

$$\begin{aligned} P(\text{at least 1 fails}) &= 1 - R^3 \\ &= 1 - (0.846481725)^3 \\ &= 1 - 0.60653066 \\ &= 0.39346934 \end{aligned}$$

- (c) Part (ii) - **Compute system reliability.**

- Front-end must work, so the probability is  $R$ .
- About back-end, at least 1 must work. So the formula is:  $1 - \text{both fail}$ . The probability both back-ends fail (unreliability) is:

$$Q^2 = 0.153518275^2 = 0.023567861$$

So, the probability at least 1 back-end works:

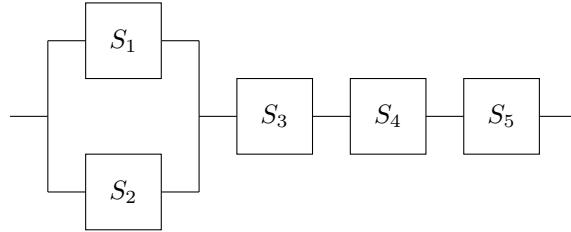
$$\begin{aligned} P(\text{at least 1 back-end works}) &= 1 - Q^2 \\ &= 1 - 0.023567861 \\ &= 0.976432139 \end{aligned}$$

So final system reliability:

$$\begin{aligned} R_{\text{system}} &= R_{\text{FE}} \times R_{\text{BE}} \\ &= 0.846481725 \times 0.976432139 \\ &= \mathbf{0.826531961} \end{aligned}$$

13. A company uses a distributed data storage system composed of five storage units, organized in a *primary* and *secondary* storage groups, according to the following scheme: (i) Two redundant *primary* storage units ( $S_1$  and  $S_2$ ), meaning that the system continues to work as long as at least one of the two remains operational; (ii) Three *secondary* storage units ( $S_3$ ,  $S_4$ , and  $S_5$ ) in a configuration that requires that all three secondary units must be operational to have the data storage system working. Each storage unit has the following parameters: Mean Time To Failure (MTTF) = 8 months; Mean Time To Repair (MTTR) = 5 day. Compute the overall availability of the system. *Notes: Use at least 5 decimal places for each intermediate calculation.*

**Answer:** The problem is one of availability. The text here describes the schema.



The overall availability of the system is given by the availability of the parallel group times the availability of the series group.

- **Availability of each component.** Since the availability of each component is the same throughout the system, this value is pre-computed (see page 144).

$$A = \frac{\text{MTTF}}{\text{MTTF} + \text{MTTR}} = \frac{240}{240 + 5} = 0.979591837$$

Note: we have converted MTTF from months to days ( $8 \times 30 = 240$ ).

- **Availability Parallel Group.** Since all components have the same availability value, we are using the simplified version (see page 144):

$$\begin{aligned} A_p &= 1 - (1 - A)^n \\ &= 1 - (1 - 0.979591837)^2 \\ &= 1 - (0.020408163)^2 \\ &= 1 - 0.000416493 \\ &= 0.999583507 \end{aligned}$$

- **Availability Series Group.** Since all components have the same availability value, we are using the simplified version (see page 143):

$$A_s = A^n = (0.979591837)^3 = 0.94001649$$

- **Overall System Availability:**

$$A_{\text{system}} = A_p \times A_s = 0.999583507 \times 0.94001649 = \mathbf{0.93962498}$$

14. You have been assigned the responsibility of optimizing the web server of your company. Through the analysis of your system logs, you have collected the following data (assume that this data is gathered during the peak hour, i.e.,  $T = 1\text{h}$ , on a representative business day).

- Number of completed requests  $C = 10000$
- Average system utilization  $U = 0.5$

What is the system throughput  $X$  and the requests service demand  $D$ ?

**Answer:** Throughput is calculated by dividing the number of completed requests by the length of time the system is observed. The exercise gives us a time of 1 hour and 10,000 requests. Therefore, the throughput is (see page 173):

$$X = \frac{10'000}{1 \text{ hour}} = \frac{10'000}{60 \text{ minutes}} = \frac{10'000}{(60 \cdot 60) \text{ seconds}} = 2.777777778 \text{ req/sec}$$

The Service Demand can be obtained using the Utilization Law because we already have the average system utilization and system throughput (see page 179):

$$\begin{aligned} U &= D \cdot X \\ 0.5 &= D \cdot 2.777777778 \\ D &= \frac{0.5}{2.777777778} \\ D &= 0.18 \text{ sec} \\ D &= 180 \text{ ms} \end{aligned}$$

15. Considering the system described in Question 14, what is the maximum throughput that the system can achieve?

**Answer:** The maximum throughput is achieved at 100% utilization. Then, apply the Utilization Law:

$$\begin{aligned} U &= D \cdot X \\ 1 &= 180 \text{ ms} \cdot X_{\max} \\ X_{\max} &= \frac{1 \text{ req}}{180 \text{ ms}} \\ X_{\max} &= 0.005555556 \\ X_{\max} &= 5.555556 \text{ req/sec} \end{aligned}$$

16. Given the system described in Question 14, assume an expected peak workload growth of 4x (i.e. four times more requests within the same time interval). Determine the minimum number of additional servers required to ensure that the system utilization does not exceed 60%. Assume that all new servers have the same configuration as the existing ones and that the incoming requests are evenly distributed across all servers. The answer should include the total number of servers required, including the original one.

**Answer:** System utilization must be 60%, so  $U = 0.6$ .

Since the peak growth is 4x, we can increase the number of completed requests from 10,000 to 40,000.

Since each server cannot exceed 60% utilization, we can use the utilization law to determine how many requests each server can handle.

$$\begin{aligned} U &= D \cdot X \\ 0.6 &= 180 \text{ ms} \cdot X_{\max} \\ X_{\max} &= \frac{0.6}{180 \text{ ms}} \\ X_{\max} &= 0.00333333 \text{ req/ms} \\ X_{\max} &= 3.333333 \text{ req/s} \\ X_{\max} &= (3.333333 \cdot 60 \cdot 60) \text{ req/hour} \\ X_{\max} &\approx 12'000 \text{ req/hour} \end{aligned}$$

If a server can handle a maximum throughput of 12,000 requests per hour, then we need 4 servers:

$$\text{Required Servers} = \frac{40,000}{12,000} = 3.333 \approx 4$$

### Open Questions

17. Explain the concept of Wear Leveling in the context of SSD.

**Answer:** Flash memory has a limited number of erase/write cycles for each block. To avoid uneven usage of specific blocks, wear leveling techniques spread erase/write operations across all blocks. On the hardware side, this is implemented using a flash translation layer (FTL) that monitors erase/write cycles per block, identifies cold blocks, and periodically reads valid data from cold blocks. The FTL then moves the data to fresher blocks, erases the original blocks, and reuses them.

18. Discuss the concept of Datacenter Availability, and define what are the differences among the Tier Levels established by the Uptime Institute.

**Answer:** Data Center availability is defined by in four different tier level:

- (a) Tier 1: Single path, no redundancy, 99.671% uptime.
- (b) Tier 2: Single path, redundancy, 99.741% uptime.
- (c) Tier 3: Multiple paths, concurrently maintainable, 99.982% uptime.
- (d) Tier 4: Fault-tolerant, fully redundant, multiple independent systems, 99.995% uptime.

### 5.1.2 January 13

#### True (✓) false (✗) questions

1. ✓ SANs are primarily used for block-level access to data, while NAS devices provide file-level access.
2. ✓ RAID can be used with both hardware and software implementations.
3. ✗ GPUs (Graphics Processing Units) are primarily used in datacenters for accelerating graphical applications and gaming.
4. ✗ Cloud computing applications do not require any server to run.
5. ✗ Availability zones within a Compute Region can have a roundtrip time larger than few milliseconds.
6. ✓ Edge computing is a distributed computing paradigm that brings computation and data storage closer to the location where it is needed.
7. ✗ The power consumption of an average datacenter is in the order of a few GigaWatts.
8. ✗ Leaf-spine topologies are more suitable for small-scale datacenter deployments with limited server connections.
9. ✓ Warehouse-scale computers are typically composed of a large set of homogeneous servers.
10. ✓ Virtualization can help simplify IT management by reducing the number of physical machines that need to be managed.

### Exercises

11. A scientific computation that needs to be carried out within the PoliMi data center uses a server composed of 2 CPUs and 4 GPUs. Knowing that:

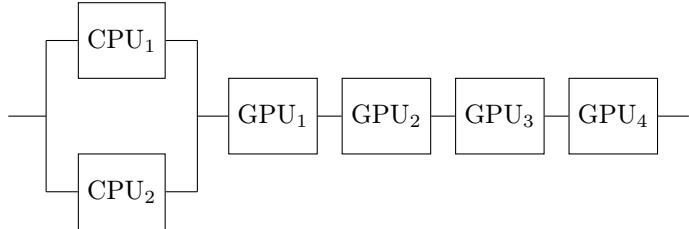
- The computation takes 8 days to complete,
- The computation requires at least one CPU and all GPUs within the server to be operational to complete successfully;
- MTTF<sub>CPU</sub> = 180 days and MTTF<sub>GPU</sub> = 120 days.

How many parallel instances of the computation must be launched to ensure a probability higher than 98% that at least one computation produces results successfully? Notes: (i) Use at least 4 decimal places for all intermediate calculations. (ii) All other components of the server can be considered ideal.

**Answer:** Each instance has some chance of *surviving* 8 days:

- If we run  $n$  instances, the probability that *all fail* is  $P_{\text{fail}}^n$ .
- So:  $P_{\text{success, total}} = 1 - P_{\text{fail}}^n$ .
- Require:  $1 - P_{\text{fail}}^n \geq 0.98 \Rightarrow 1 - (P_{\text{fail 1 job}})^n \geq 0.98$

We can retrieve the RBD from the system:



- (a) **Probability CPUs survive.** A single CPU survives 8 days with probability (see page 136):

$$P_{\text{CPU, survive}} = R(t) = e^{-t\lambda} = e^{-\frac{8}{180}}$$

Where  $\lambda = \frac{1}{\text{MTTF}}$ . So, the probability that the system fails when the last component fails is (see page 142), then the probability that everything works:

$$\begin{aligned}
 R_S(t) &= 1 - \prod_{i=1}^{n=2} \left[ 1 - e^{-\frac{8}{180}} \right] \\
 &= 1 - \left( 1 - e^{-\frac{8}{180}} \right)^2 \\
 &= 1 - (1 - 0.956528739)^2 \\
 &= 1 - (0.043471261)^2 \\
 &= 1 - 0.001889751 \\
 &= 0.998110249
 \end{aligned}$$

(b) **Probability GPUs survive.** GPUs have the survival probability:

$$P_{\text{GPU, survive}} = R(t) = e^{-t\lambda} = e^{-\frac{8}{120}}$$

So, the system failure is determined by the failure of the first component (see page 141), then the probability that everything works:

$$\begin{aligned} R_S(t) &= \prod_{i=1}^{n=4} e^{-\frac{8}{120}} \\ &= \left(e^{-\frac{8}{120}}\right)^4 \\ &= (0.935506985)^4 \\ &= 0.765928338 \end{aligned}$$

(c) **Probability that one job fail.** We calculate the probability of a system failure by starting with the system's overall reliability.:

$$\begin{aligned} P_{\text{fail, 1 job}} &= 1 - (0.998110249 \cdot 0.765928338) \\ &= 1 - 0.764480924 \\ &= 0.235519076 \end{aligned}$$

(d) **Calculate the number of parallel instances.** Now that we have the probability of one job failing, we can substitute this value into the requirements formula to find the  $n$  variable:

$$\begin{aligned} 1 - P_{\text{fail}}^n &\geq 0.98 \\ 1 - (P_{\text{fail 1 job}})^n &\geq 0.98 \\ -(0.235519076)^n &\geq 0.98 - 1 \\ (0.235519076)^n &\leq 0.02 \\ \ln((0.235519076)^n) &\leq \ln(0.02) \\ n \cdot \ln(0.235519076) &\leq \ln(0.02) \\ \downarrow &\leq \text{flips because } \ln(0.235519076) < 0 \\ n &\geq \frac{\ln(0.02)}{\ln(0.235519076)} \\ n &\geq \frac{-3.912023005}{-1.445963367} \\ n &\geq 2.705478641 \end{aligned}$$

Therefore,  $n$  must be greater than 2.71 to achieve a reliability greater than 98%. We round up to  $n = 3$  because we are talking about real-world components.

12. If the time required to recover and replace a component of the server described in the previous exercise (whether it is a CPU or a GPU) is equal to 24 days, what is the total availability of the server? Notes: (i) Use at least 5 decimal places for all intermediate calculations. (ii) All other components of the server can be considered ideal.

**Answer:** The exercise provides the Mean Time To Repair (MTTR), which is 24 days. With the help of the Reliability Block Diagram (RBD), we can easily determine which availability formula to use:

- **Availability of each CPU component** (see page 144):

$$A_{\text{CPU}} = \frac{\text{MTTF}}{\text{MTTF} + \text{MTTR}} = \frac{180}{180 + 24} = 0.882352941$$

- **Availability of each GPU component** (see page 144):

$$A_{\text{GPU}} = \frac{\text{MTTF}}{\text{MTTF} + \text{MTTR}} = \frac{120}{120 + 24} = 0.833333333$$

- **Availability CPU (parallel) group** (see page 144):

$$\begin{aligned} A_{\text{CPUs}} &= 1 - (1 - A_{\text{CPU}})^n \\ &= 1 - (1 - 0.882352941)^2 \\ &= 1 - (0.117647059)^2 \\ &= 1 - 0.01384083 \\ &= 0.98615917 \end{aligned}$$

- **Availability GPU (series) group** (see page 143):

$$\begin{aligned} A_{\text{GPUs}} &= A_{\text{GPU}}^n \\ &= (0.833333333)^4 \\ &= 0.482253086 \end{aligned}$$

- **Overall System Availability:**

$$A_{\text{system}} = A_{\text{CPUs}} \cdot A_{\text{GPUs}} = 0.98615917 \cdot 0.482253086 = \mathbf{0.475578303}$$

- **Availability if we use 3 parallel instances.** The previous availability was achieved with a single server instance. If we follow the previous solution's suggestion and run 3 instances of the same server to achieve 98% reliability, the system's availability will be (use parallel formula, see page 144):

$$\begin{aligned} A_{\text{system with 3 instances}} &= 1 - (1 - A_{\text{system}})^n \\ &= 1 - (1 - 0.475578303)^3 \\ &= 1 - (0.524421697)^3 \\ &= 1 - 0.144225467 \\ &= \mathbf{0.855774533} \end{aligned}$$

13. A company is planning to use a RAID 5 array composed of 8 disks for critical data storage. The desired Mean Time To Failure for the entire RAID system ( $\text{MTTF}_{\text{RAID}5}$ ) is 16 years. Each disk in the array has a MTTF disk equal to 500 days. What should be the MTTR required *in hours* to meet the target RAID MTTF<sub>RAID5</sub> .

**Answer:** We know that the MTTF of the RAID 5 is (see page 75):

$$\text{MTTF}_{\text{RAID}5} = \frac{\text{MTTF}_{\text{disk}}^2}{G \cdot (G - 1) \cdot \text{MTTR}}$$

We can substitute the known values into the formula (where 16 years are 5840 days):

$$\begin{aligned}\text{MTTF}_{\text{RAID}5} &= \frac{\text{MTTF}_{\text{disk}}^2}{G \cdot (G - 1) \cdot \text{MTTR}} \\ 5840 &= \frac{(500)^2}{8 \cdot (8 - 1) \cdot \text{MTTR}} \\ 5840 &= \frac{250'000}{56 \cdot \text{MTTR}} \\ 5840 \cdot \text{MTTR} &= \frac{250'000}{56 \cdot \text{MTTR}} \cdot \text{MTTR} \\ \frac{1}{5840} \cdot 5840 \cdot \text{MTTR} &= \frac{250'000}{56} \cdot \frac{1}{5840} \\ \text{MTTR} &= \frac{250'000}{327'040} \\ \text{MTTR} &= 0.764432485 \text{ days} \\ \text{MTTR} &= 0.764432485 \text{ days} \cdot 24 \text{ hours} \\ \text{MTTR} &= 18.346379648 \text{ hours}\end{aligned}$$

14. Consider a system composed of three stations: the CPU that is characterized by  $V_{\text{CPU}} = 100$  visits and an average service time of  $S_{\text{CPU}} = 10\text{ms}$ ; the disk, characterized by a throughput of 12 IOPS, and a demand of  $D_{\text{DISK}} = 150\text{ms}$ ; and the GPU whose demand is  $D_{\text{GPU}} = 40\text{s}$  and the number of visits  $V_{\text{GPU}} = 10$ . Finally, the system throughput is  $X = 20$  jobs/min while the response time when there are  $N = 20$  end-users in the system is  $R = 55\text{s}$ . Compute the CPU demand and the GPU throughput. Write in the answer sheet:  $D_{\text{CPU}} = \dots$ ;  $X_{\text{GPU}} = \dots$

**Answer:** First, we clarify the data we have.

- CPU:
  - $V_{\text{CPU}} = 100$  visits
  - $S_{\text{CPU}} = 10\text{ms}$
- Disk:
  - Throughput of 12 IOPS
  - $D_{\text{DISK}} = 150\text{ms}$
- GPU:
  - $D_{\text{GPU}} = 40\text{s}$
  - $V_{\text{GPU}} = 10$  visits
- System:
  - $X = 20$  jobs/min
  - If  $N = 20$  end-users, then  $R = 55\text{s}$

The **CPU demand** is (see page 179):

$$D_{\text{CPU}} = S_{\text{CPU}} \cdot V_{\text{CPU}} = 10 \cdot 100 = 1000 \text{ ms} = \mathbf{1 \text{ sec}}$$

The **GPU throughput** is (see the Forced Flow Law, page 179):

$$X_{\text{GPU}} = V_{\text{GPU}} \cdot X = 10 \cdot 20 \text{ jobs/sec} = \mathbf{200 \text{ GPU ops/min}}$$

15. Considering the system described in Question 14, what is the users' think time  $Z$ ?

**Answer:** We use the Interactive Response Time Law (see page 178):

$$\begin{aligned} R &= \frac{N}{X} - Z \\ 55 \text{ sec} &= \frac{20}{(20 \div 60) \text{ jobs/sec}} - Z \\ 55 \text{ sec} &= \frac{20}{0.333333333 \text{ jobs/sec}} - Z \\ 55 \text{ sec} &= \underline{60.00000006}^{\approx 60} - Z \\ -5 \text{ sec} &= -Z \\ Z &= \mathbf{5 \text{ sec}} \end{aligned}$$

16. Based on the system in Question 14, the number of end users is predicted to reach 40 in one month. Considering the response time lower bound, which option is better?
- Upgrade the system by adding one more GPU (you can assume the new GPU is equal to the one initially available and to balance evenly the GPU processing).
  - Replace the GPU with one 2.5 times faster than the original one.

Provide the estimated bounds in the two scenarios to motivate your answer. Write in the answer sheet:  $A$  or  $B$ ;  $R_{\text{LOW}}^A = \dots$ ;  $R_{\text{LOW}}^B = \dots$

**Answer:** Here is a recap of our dependability:

- CPU demand: 1 sec
- Disk demand: 150 ms
- GPU demand: 40 sec

Number of users grows from 20 to 40. We know that, in closed systems (systems where  $N$  is fixed), response time depends on:

- How many users are circulating (our case  $20 \rightarrow 40$ ),
- How busy the bottleneck is.

When the system gets heavily loaded ( $N$  is big), the **bottleneck station** (the slowest resource, here GPU) **determines the lower limit for response time**, because jobs pile up there.

The lower bound for heavy load is asymptotically (see page ??):

$$R = N \cdot D_{\max}$$

However, we also need to remove the think time:

$$R = N \cdot D_{\max} - Z$$

- **Option A - Add 1 more GPU.** Now there are 2 identical GPUs. The load can be split **evenly**, so the service demand at the GPU station halves:

$$D_{2 \text{ GPUs}} = \frac{D_{1 \text{ GPU}}}{2} = \frac{40 \text{ sec}}{2} = 20 \text{ sec}$$

The lower bound is:

$$R_{\min}^A = N \cdot D_{\max} - Z = 40 \cdot 20 - 5 = \mathbf{795 \text{ sec}}$$

- **Option B - Replace GPU with one 2.5× faster.** A GPU that is 2.5 times faster is like adding another GPU and half of another. Therefore, the new service demand increases:

$$D_{\text{GPU 2.5 faster}} = \frac{D_{1 \text{ GPU}}}{2.5} = \frac{40 \text{ sec}}{2.5} = 16 \text{ sec}$$

The lower bound is:

$$R_{\min}^B = N \cdot D_{\max} - Z = 40 \cdot 16 - 5 = \mathbf{635 \text{ sec}}$$

Finally, the best option is the option  $B$ , with  $R_{\min}^B = 635$  seconds.

### Open Questions

17. What are the advantages and disadvantages of using Type 1 hypervisors versus Type 2 hypervisors in a virtualized environment?

**Answer:** Type 1 hypervisors allow you to manage resources more effectively because there is no operating system between the virtualized software and the hardware. Also, performance is better than with Type 2. On the other hand, Type 1 can be difficult to set up because Type 2 is easier to interact with since it already has an installed OS. In summary, Type 1 offers better performance and isolation but may require specific drivers to run. In contrast, Type 2 is more user-friendly and easier to manage but uses more resources than Type 1.

18. What are the implications of hardware heterogeneity on software stack development in datacenters?

**Answer:** In a heterogeneous datacenter, we have different hardware configurations: different CPU models, different GPU types, different amounts of RAM, specialized storage (SSD vs HDD), specialized network cards.

Software stack development is clearly affected by these scenarios. Developers need to test their software on different platforms. They must also guarantee that there will be no overflows or unexpected behaviors when using different storage types (HDD or SSD). If the software uses different GPU frameworks, such as CUDA, developers must guarantee that it will work with other technologies, as the node where it will be deployed may use a different GPU architecture (e.g., AMD instead of NVIDIA). Performance aspects are also fundamental because the software must be optimized for various CPUs. Finally, each of these aspects implies that the software requires careful testing (which is unfortunately not always guaranteed in the real world).

## 5.2 2024

### 5.2.1 September 5

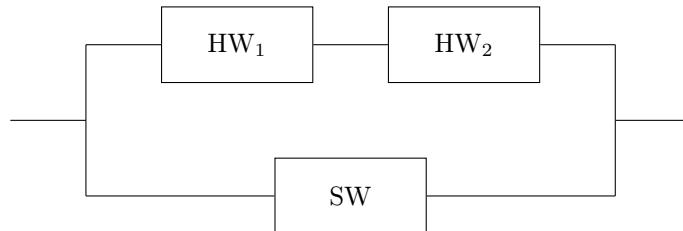
#### True (✓) false (✗) questions

1. ✗ Warehouse-scale computers are primarily used in small businesses with limited computing needs.
2. ✗ Given their efficiency, accelerators like GPUs and TPUs have no impact on the cooling requirements of datacenters.
3. ✗ Hypervisors can only be used to run virtual machines with the same amount of memory as the physical machine on which they are hosted.
4. ✗ Leaf-spine topologies are not suitable for highly virtualized environments with a large number of virtual machines.
5. ✗ GPUs in datacenters are primarily used for accelerating graphics rendering and video processing tasks.
6. ✓ RAID 10 provides better random write performance than RAID 6.
7. ✓ Virtualization can reduce costs by enabling the sharing of hardware resources between virtual machines.
8. ✗ RAID architectures are used to substitute regular backups.
9. ✓ A UPS provides backup power to equipment during a power outage.
10. ✗ Cooling towers are not suitable for high-density datacenters.

### Exercises

11. A monitoring system for a rack inside a data center is designed to be composed of 2 hardware sensors ( $M_{HW}$ ), all necessary to extract information on the use of each blade. Each of the sensors is characterized by a MTTF of 27 days and a MTTR of 1 day. If the monitoring system were to be updated to include a purely software system ( $M_{SW}$ ), from which it would be possible to extract the same usage information obtained with the HW sensors, what would be the availability of the entire blade-usage monitoring system ( $M_{HW} + M_{SW}$ ) if the availability of the software system (M-SW) was 96%? Use always at least 5 decimal digits for each calculation.

**Answer:** We can draw the RBD where the hardware sensors are sequential and the software is inserted in parallel with the hardware components:



- The **availability of the series group** can be calculated using the product of the availability of each component (see page 143):

$$A_{HW} = \prod_{i=1}^{n=2} A_i$$

The availability of each component is as follows:

$$A_i = \frac{MTTF_i}{MTTF_i + MTTR_i} = \frac{27}{27+1} = \frac{27}{28} = 0.964285714$$

The series group is available as follows:

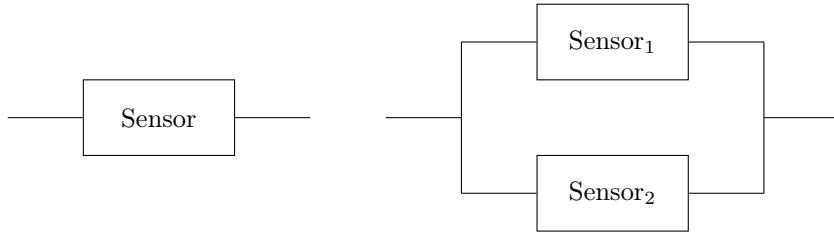
$$A_{HW} = 0.964285714 \cdot 0.964285714 = 0.929846938$$

- We calculate the **system's overall availability** with the parallel formula (see page 144) since the hardware and parallel groups are in parallel. We have everything necessary to calculate it:

$$\begin{aligned}
A_{\text{system}} &= 1 - \prod_{i=1}^{n=2} (1 - A_i) \\
&= 1 - [(1 - A_{HW}) \cdot (1 - A_{SW})] \\
&= 1 - [(1 - 0.929846938) \cdot (1 - 0.96)] \\
&= 1 - [0.070153062 \cdot 0.04] \\
&= 1 - 0.002806122 \\
&= \mathbf{0.997193878}
\end{aligned}$$

12. A company uses a temperature sensor to monitor a critical environment within an industrial plant. The sensor has a MTTF (Mean Time To Failure) of 4000 hours. If the company decides to replace the original sensor with a redundant version consisting of two sensors like the previous one, what is the overall reliability of the monitoring system after 2000 hours? Use always at least 4 decimal digits for each calculation.

**Answer:** A system composed of only one sensor becomes a system composed of two sensors in parallel because they substitute for one another. The Reliability Block Diagram is:



- The **system's reliability** when **only one sensor is used** is as follows:

$$R(t) = e^{-\lambda t} \quad \text{where } \lambda = \frac{1}{\text{MTTF}}$$

$$\begin{aligned} R(2000 \text{ hours}) &= e^{-\frac{1}{4000} \cdot 2000} \\ &= e^{-0.5} \\ &= 0.60653066 \end{aligned}$$

- The **reliability** of the system when **two parallel sensors** are added is given by the formula (see page 142):

$$\begin{aligned} R(t) &= 1 - \prod_{i=1}^{n=2} (1 - R_i(t)) \\ R(2000 \text{ hours}) &= 1 - \prod_{i=1}^{n=2} (1 - R_i(2000)) \\ &= 1 - [(1 - 0.60653066) \cdot (1 - 0.60653066)] \\ &= 1 - [0.39346934 \cdot 0.39346934] \\ &= 1 - 0.154818122 \\ &= \mathbf{0.845181878} \end{aligned}$$

13. Consider the following RAID 1 + 0 setup composed of 6 disks, each one with an MTTF equal to 410 days and an MTTR equal to 2 days, and a single mirror case for the RAID 1 part. What is the MTTF of the storage infrastructure?

**Answer:** We use the Mean Time To Failure of RAID 10 (see page 162):

$$\begin{aligned}
 \text{MTTF}_{\text{RAID 10}} &= \frac{\text{MTTF}_{\text{disk}}^2}{N \cdot \text{MTTR}} \\
 &= \frac{(410)^2}{6 \cdot 2} \\
 &= \frac{168'100}{12} \\
 &= 14008.333333333 \\
 &\approx \mathbf{14008 \text{ days}}
 \end{aligned}$$

14. You are tasked with performing capacity planning for an application cluster. Your system can be modeled using a closed model. On average, there are  $N = 30$  users logged into the system, with a think time of  $Z = 10$  seconds. Your objective is to determine whether it is more efficient to introduce:

- 10 servers, **each** with a service demand of  $D_{10} = 10$  seconds, or
- A single server that is 10 times faster than each server in the previous case, with a service demand of  $D_1 = 0.1$  seconds.

Calculate the lower bound on response time for both scenarios.

**Answer:**

- **Option A - 10 servers.** In order to determine which formula to apply, we must first establish whether the situation is light or heavy. To determine this, we use the  $N^*$ :

$$N^* = \frac{D + Z}{D_{\max}} = \frac{D + Z}{\frac{D_{\text{server}}}{m}} = \frac{10 + 10}{\frac{10}{10}} = \frac{20}{1} = 20$$

Since the number of logged users is greater than  $N^*$ , we are in a **heavy situation**. It means that the response time is:

$$R_{\min} = \max \left( D, N \cdot \frac{D_{\max}}{m} - Z \right) = \max \left( 10, 30 \cdot \frac{10}{10} - 10 \right) = 20 \text{ s}$$

Where  $m$  is the number of servers:  $\frac{D_{\text{server}}}{m}$ . The heavy-load limit is about how *fast* the system can drain all users, so we divide by  $m$  to get the effective bottleneck demand for the whole system.

- **Option B - 1 server.** In this case, the  $N^*$  is:

$$N^* = \frac{D + Z}{D_{\max}} = \frac{0.1 + 10}{0.1} = 101$$

Since the number of logged users is less than  $N^*$ , we are in a **light situation**. This means that the response time equals the demand service  $D$ :  $R_{\min} = D = 0.1$  s.

For 30 users, **option B is the most efficient method**, with a response time of 0.1 seconds.

15. Based on the system described in question 14, calculate the upper bound on throughput for both scenarios.

*Answer:*

- **Option A - 10 servers.** In this context, we are in a **heavy situation**, and the throughput is as follows:

$$\begin{aligned} X &= \min \left( \frac{1}{D_{\max}}, \frac{N}{D + Z} \right) \\ &= \min \left( \frac{1}{\frac{10}{10}}, \frac{30}{10 + 10} \right) \\ &= \min (1, 1.5) \\ &= 1 \text{ req/sec} \end{aligned}$$

Where  $D_{\max} = \frac{D_{\text{server}}}{m}$ .

- **Option B - 1 server.** In this context, we are in a **light situation**, and the throughput is as follows:

$$\begin{aligned} X &= \frac{N}{D + Z} \\ &= \frac{30}{0.1 + 10} \\ &= 2.97029703 \text{ req/sec} \end{aligned}$$

16. Considering the system in question 14, compute the number of users  $N^*$  that determines whether the system should be analyzed using the light load or heavy load optimistic bounds.

*Answer:*

- **Option A - 10 servers**, where  $D_{\max} = \frac{D_{\text{server}}}{m}$ .

$$N^* = \frac{D + Z}{D_{\max}} = \frac{D + Z}{\frac{D_{\text{server}}}{m}} = \frac{10 + 10}{\frac{10}{10}} = \frac{20}{1} = 20$$

- **Option B - 1 server.**

$$N^* = \frac{D + Z}{D_{\max}} = \frac{0.1 + 10}{0.1} = 101$$

## Open Questions

17. Describe characteristics, advantages, and disadvantages of Direct Attached Storage (DAS), Network Attached Storage (NAS) and Storage Area Networks (SAN).

*Answer:*

- **Direct Attached Storage (DAS).** Storage directly connected to a single host (server or PC). The main advantages are high performance for local workloads (low latency), low cost, simple to deploy, and good for dedicated single-server applications. The main disadvantages are not shareable over a network by default, is hard to scale beyond the local bus, poor resource utilization when multiple servers need the same data, and limited redundancy features compared to shared storage.
- **Network Attached Storage (NAS).** A dedicated file server, a storage accessible over a TCP/IP network using file-level protocols. The main advantages are centralized file sharing across multiple hosts, simple network setup, flexible because any client with network access can mount shares, and good for collaborative environments. The main disadvantages are file protocol overhead, ethernet can be a performance bottleneck for I/O-intensive applications, file-level permissions add complexity, and is not ideal for very high throughput or database block workloads.
- **Storage Area Network (SAN).** A dedicated high-speed network providing block-level storage to multiple servers. Hosts see remote storage as local disks, the OS mounts volumes just like DAS. The main advantages are high-performance, low latency, block-level access (flexible for filesystems), highly scalable (allocates volumes dynamically), and high availability (e.g., RAID). The main disadvantages are higher cost, more complex to deploy and administer than DAS/NAS, requires specialized skills for setup and maintenance, and misconfigurations can affect multiple servers.

18. Describe, comment, and contextualize the four main types of Clouds.

*Answer:*

- **Public Cloud.** A public cloud is a shared, multi-tenant environment operated by a third-party provider (e.g., AWS, Azure, Google Cloud). The physical infrastructure (data centers, networks, storage) is owned and managed by the provider. Users rent virtualized resources on demand via the internet.

This is the most common cloud model for startups, developers, and businesses who want to avoid large upfront infrastructure investments. Public clouds provide elasticity, pay-as-you-go pricing, and massive scale.

So it is quick to deploy, scalable, cost-effective, but we have less control over underlying hardware.

- **Private Cloud.** A private cloud is a **single-tenant environment** dedicated to one organization. It can be hosted on-premises (in the company's own data center) or by a third-party provider, but the key point is that the resources are **not shared** with other tenants.

It is often chosen by large enterprises and regulated sectors, such as finance, healthcare, and the public sector, that require strong governance, data sovereignty, and full control over security policies.

The main advantages are full control, customizable security, and can leverage existing investments. But the main disadvantages are higher cost, less elastic than public clouds, requires in-house expertise for management and updates.

- **Hybrid Cloud.** A hybrid cloud combines **two or more clouds** (private and public) connected via standardized or proprietary technology. This allows workloads to **move or burst** between environments as needed.

Typical for enterprises that want to keep sensitive data in a private environment while using the public cloud for flexible capacity (e.g., handling seasonal peaks).

The main advantages are flexibility to optimize cost, performance, and compliance; supports gradual migration to the cloud. But the disadvantages are complex integration; needs careful governance to avoid shadow IT or misconfigurations.

- **Community Cloud.** A community cloud is **shared by several organizations** with a common concern (e.g., same compliance requirements, mission, or industry standards). The infrastructure is jointly owned or managed by the community or a third party.

Used in sectors like government agencies, research institutions, or collaborative industries that benefit from a shared infrastructure but want more control than the public cloud.

The main advantages are shared costs, tailored policies, and collaboration within a trusted group. However, the disadvantages are less common than with other models. Governance and funding models can be complex, and scalability is more limited than with large public clouds.

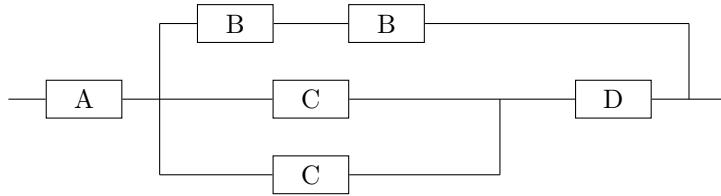
### 5.2.2 June 12

#### True (✓) false (✗) questions

1. ✓ Virtualization can reduce costs by enabling the sharing of hardware resources between virtual machines.
2. ✓ In-row cooling systems allow for higher server densities and increased rack power densities in datacenters.
3. ✗ RAID 6 offers better random and sequential write performance than RAID 5.
4. ✓ The computing continuum refers to the idea that computing devices exist on a spectrum, from small, low-power devices to large, high-performance machines.
5. ✓ In-row cooling involves placing cooling units between server racks.
6. ✗ Full virtualization can run on a wider range of hardware than paravirtualization.
7. ✗ In current datacenters east-west traffic typically involves lower data volumes compared to north-south traffic.
8. ✓ TPUs are more power-efficient and offer higher performance compared to GPUs in deep learning tasks.
9. ✗ DAS devices connect directly to a network and are accessed over the network by clients.
10. ✓ Controlling humidity levels in a datacenter is important for preventing equipment failures.

### Exercises

11. Suppose we have a computer system composed of 6 different components, and designed to have an RBD as shown in the image below. The four types of components (A, B, C, and D) have different reliability characteristics. We know that after 2 years the reliability of components B, C, and D are respectively  $R_B(2y) = 0.8$ ,  $R_C(2y) = 0.6$ , and  $R_D(2y) = 0.9$ . What should be the MTTF for component A, if we want to have a Reliability of the whole system after 2 years equal to  $R_{sys}(2y) = 0.82$ ? Use always at least 3 decimal digits for each calculation.



**Answer:** We have 4 groups here:

Group 1. The two C components are **parallel**. The reliability of C is 0.6, so:

$$\begin{aligned}
 R_{\text{Group 1}} &= 1 - \prod_{i=1}^{n=2} (1 - R_{C_i}) \\
 &= 1 - [(1 - 0.6) \cdot (1 - 0.6)] \\
 &= 1 - 0.16 \\
 &= 0.84
 \end{aligned}$$

Group 2. Group 1 and component D are **sequential**. The reliability of D is 0.9, and the reliability of group 1 is 0.84, so:

$$R_{\text{Group 2}} = \prod_{i=1}^{n=2} R_i = 0.9 \cdot 0.84 = 0.756$$

Group 3. The two B components are **sequential**. The reliability of B is 0.8, so:

$$R_{\text{Group 3}} = \prod_{i=1}^{n=2} R_{B_i} = 0.8 \cdot 0.8 = 0.64$$

Group 4. Groups 3 and 2 are **parallel**. The reliability of the group 2 is 0.756 and the reliability of the group 3 is 0.64, so:

$$\begin{aligned}
 R_{\text{Group 4}} &= 1 - \prod_{i=1}^{n=2} (1 - R_i) \\
 &= 1 - [(1 - 0.756) \cdot (1 - 0.64)] \\
 &= 1 - [0.244 \cdot 0.36] \\
 &= 1 - 0.08784 \\
 &= 0.91216
 \end{aligned}$$

Group 5. Finally, component A is **sequential** with group 4. The reliability of Group 4 is 0.91216, but the reliability of A is unknown. In this case, we use the desired system reliability to find A:

$$\begin{aligned} R_{\text{sys}}(2y) &= \prod_{i=1}^{n=2} R_i \\ 0.82 &= 0.91216 \cdot R_A(2y) \\ \frac{1}{0.91216} \cdot 0.82 &= \frac{1}{0.91216} \cdot R_A(2y) \cdot \frac{1}{0.91216} \\ R_A(2y) &= 0.898965094 \end{aligned}$$

We use the reliability formula to find the Mean Time To Failure (MTTF):

$$\begin{aligned} R_A(t) &= e^{-\lambda t} \\ R_A(2y) &= e^{-\lambda 2} \\ 0.898965094 &= e^{-\lambda 2} \\ \ln(0.898965094) &= -\frac{1}{\text{MTTF}} \cdot 2 \\ -0.106511073 &= -\frac{2}{\text{MTTF}} \\ \text{MTTF} \cdot 0.106511073 &= \frac{2}{\text{MTTF}} \cdot \text{MTTF} \\ \frac{1}{0.106511073} \cdot 0.106511073 \cdot \text{MTTF} &= 2 \cdot \frac{1}{0.106511073} \\ \text{MTTF} &= \mathbf{18.777390403 \text{ years}} \end{aligned}$$

12. We have to design a RAID 0 + 1 storage architecture composed of an array of 8 disks. Knowing that each disk has a MTTF equal to 450 days and that we would like to have a MTTF for the storage infrastructure ( $\text{MTTF}_{\text{RAID } 01}$ ) higher than 7 years, what is the maximum MTTR that we have to consider to satisfy the requirement? Consider all the disks with the same characteristics and a single mirror case for the RAID 1 part.

**Answer:** The Mean Time To Failure formula for RAID 0 + 1 is (see page 162):

$$\begin{aligned}\text{MTTF}_{\text{RAID } 01} &= \frac{\text{MTTF}_{\text{disk}}^2}{N \cdot G \cdot \text{MTTR}} \\ (7 \cdot 365) \text{ days} &= \frac{(450)^2}{8 \cdot 4 \cdot \text{MTTR}} \\ 2555 &= \frac{202'500}{32 \cdot \text{MTTR}} \\ \text{MTTR} \cdot 2555 &= \frac{202'500}{32 \cdot \text{MTTR}} \cdot \text{MTTR} \\ \text{MTTR} \cdot 2555 &= \frac{202'500}{32} \\ \frac{1}{2555} \cdot \text{MTTR} \cdot 2555 &= \frac{202'500}{32} \cdot \frac{1}{2555} \\ \text{MTTR} &= \frac{202'500}{81'760} \\ &= 2.476761252 \text{ days} \\ &= \mathbf{2.4768 \text{ days}}\end{aligned}$$

13. Let us consider a set of requests in the disk queue referring to the following cylinders of the disk: 22, 40, 27, 82, 16. Consider the initial position of the disk head at cylinder 20 and moving from inside (lower cylinder number) to outside (higher cylinder number). Writes the order of the served requests (from the first to the last) if the disk head scheduling algorithm adopted is C-SCAN (Circular SCAN)? Use the cylinder number to refer to the request.

**Answer:** The Circular SCAN algorithm is similar to the SCAN algorithm, but it returns to the starting point once it reaches the end. We are at position 20, and the movement is from the inside to the outside. The chain is:

$$(20 \rightarrow) \mathbf{22} \rightarrow \mathbf{27} \rightarrow \mathbf{40} \rightarrow \mathbf{82} \xrightarrow{\text{end reached, jump back}} (\rightarrow 0) \rightarrow \mathbf{16}$$

14. Consider a closed system composed of three stations:

- the CPU that is characterized by  $V_{CPU} = 3$  visits and an average service time of  $S_{CPU} = 10\text{ms}$ ;
- the disk is characterized by a throughput of  $X_{DISK} = 12$  I/O-operations per seconds, and a demand of  $D_{DISK} = 350\text{ms}$ ;
- the network whose demand is  $D_{NET} = 4\text{ms}$ , and throughput is  $X_{NET} = 20$  packet/s.

When there are  $N = 25$  end-users in the system, the system throughput is  $X = 1.85$  job/s, and the response time is  $R = 0.8\text{s}$ . Compute the CPU demand and the network number of visits.

**Answer:** The exercise is easier than it looks.

- **CPU Demand**  $D_{CPU}$ . We use the service demand formula, which is easier and cleaner (see page 179):

$$D_{CPU} = S_{CPU} \cdot V_{CPU} = 10 \cdot 3 = 30\text{ ms} = \mathbf{0.03\text{ sec}}$$

- **Network number of visits**  $V_{NET}$ . We would like to use the service demand formula again, but there are too many unknowns:

$$\begin{aligned} D_{NET} &= S_{NET} \cdot V_{NET} \\ 4 &= \underbrace{S_{NET}}_{\text{unknown}} \cdot \underbrace{V_{NET}}_{\text{goal}} \end{aligned}$$

We have the throughput of both the system and the component. We can use the visit count formula to our advantage (see page 178):

$$V_{NET} = \frac{X_{NET}}{X} = \frac{20}{1.85} = \mathbf{10.810810811}$$

15. Considering the same system as in Questions 14, what is the users' think time Z?

**Answer:** We use the Interactive Response Time Law to calculate Z, the think time (see page 178):

$$\begin{aligned} R &= \frac{N}{X} - Z \\ 0.8 &= \frac{25}{1.85} - Z \\ Z &= 13.513513514 - 0.8 \\ Z &= \mathbf{12.713513514\text{ sec}} \end{aligned}$$

16. Considering the same system as in *Questions 14 and 15*, and that the number of end-users reaches  $N = 50$  in one month. What will be the response time lower bound if you upgrade your system by adding three more disks? You can assume that the new disk is equal to the one initially available and that the original accesses to the disk are now uniformly spread on the set of available disks.

**Answer:** Before calculating the lower bound of response time, we must first determine whether the situation is light or heavy in order to select the appropriate formula.

- **Determine  $N^*$ .** First, the system's service demand is calculated based on the added parallel disks:

$$D = \underbrace{0.03}_{\text{CPU}} + \underbrace{\frac{0.35}{4}}_{\text{Disks}} + \underbrace{0.004}_{\text{NET}} = \underbrace{0.03}_{\text{CPU}} + \underbrace{0.0875}_{\text{Disks}} + \underbrace{0.004}_{\text{NET}} = 0.1215$$

The bottleneck here is still the disk components  $D_{\max} = 0.0875$ . We now have everything we need to calculate  $N^*$ :

$$N^* = \frac{D + Z}{D_{\max}} = \frac{0.1215 + 12.713513514}{0.0875} = 146.685868731$$

Since  $N^*$  is **greater** than  $N$ , the number of end users, we are in a **light situation**.

- **Calculate the lower bound of the response time.** Since we are in a light situation, the system isn't saturated and jobs flow freely without waiting. Throughput is limited by total resource consumption rather than maximum latency. In our case, 4 disks (each working 0.0875 seconds) results in 0.35 seconds of lost disk time per job, even though the work is done in parallel. Therefore, we sum all resource times to reflect the true workload capacity needed:

$$D = 0.03 + 0.35 + 0.004 = 0.384$$

Also, since we are in the light situation, the minimum response time is the service demand:

$$R_{\min} = D = \mathbf{0.384 \text{ seconds}}$$

## Open Questions

17. Explain and compare virtualization and containerization, discussing their key differences. Highlight the advantages and disadvantages of each approach.

**Answer:** **Virtualization** runs multiple virtual machines on a host by emulating full hardware and OS. Each VM has its own OS and kernel, giving strong isolation but with more overhead.

**Containerization** runs applications in isolated user spaces that share the host OS kernel. Containers (e.g., Docker) are lighter, faster to start, and use fewer resources.

### Key differences

- VMs = full OS + strong isolation + more overhead.
- Containers = same OS kernel + faster + lighter but weaker isolation.

### Pros

- Virtualization: strong isolation, runs any OS.
- Containerization: fast, efficient, easy to deploy at scale.

### Cons

- Virtualization: heavier, slower.
- Containers: less secure if misconfigured (shared kernel).

18. Discuss the role of networking in GPU-based systems within data centers. How does networking impact the performance, scalability, and efficiency of these systems?

**Answer:** **Networking is critical in GPU-based datacenters**, particularly for large-scale AI workloads such as LLM training. Since GPUs often work in parallel across many nodes, high bisection bandwidth, low latency, and high throughput are essential to avoid bottlenecks when exchanging massive amounts of data.

Poor networking can limit performance and scalability because GPUs may wait idly for data. Data centers use advanced topologies, such as Spine-Leaf or hypercube (D-Cube) networks, to efficiently balance East-West traffic.

However, adding more switches increases costs, energy usage, and cooling needs. Therefore, network design must balance performance and efficiency.

### 5.2.3 February 7

#### True (✓) false (✗) questions

1. ✓ RAID 5 can handle sequential reads and writes better than RAID 10 with the same amount of disks.
2. ✓ Monolithic hypervisors are better suited for high-performance computing than microkernel hypervisors.

#### Deepening: *Why is this True?*

- In the **monolithic hypervisor** (like VMware ESXi, Xen in monolithic mode, KVM's kernel module), the device drivers run within the hypervisor.
- In the **microkernel hypervisor** (like early Xen's microkernel style or L4-based designs), the device drivers run within a service virtual machine.

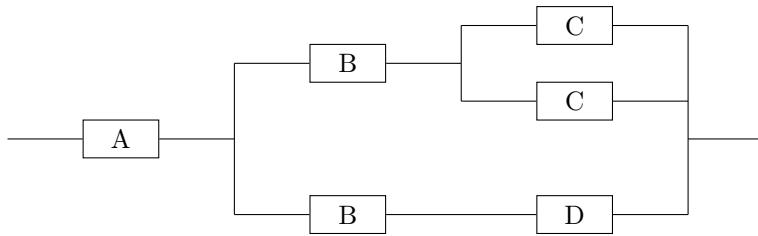
Monolithic hypervisors deliver **lower overhead and faster context switching** because they handle virtual machine (VM) operations in the same kernel address space as device drivers and the scheduler.

Microkernel hypervisors **add extra isolation** (good for security or fault tolerance) but this comes with **higher overhead**, so we lose raw performance.

3. ✓ Virtualization can help reduce the need for physical space and infrastructure by consolidating multiple servers onto a single physical machine.
4. ✓ A PUE of 1.0 means that all of the power consumed by a data center is being used by the IT equipment.
5. ✓ GPUs require specialized software and programming frameworks to fully leverage their parallel processing capabilities.
6. ✓ Warehouse-scale computers require specialized cooling and power management systems.
7. ✗ Hot/cold aisle containment reduces the efficiency of the cooling method for data-centers.
8. ✗ SSDs use spinning disks to store data.
9. ✓ In a leaf-spine topology, adding or removing a leaf switch does not impact the connectivity of other switches in the network.
10. ✗ POD, Virtual-Chassis, DCell and BCube models are all evolutions of the leaf-spine network architectures.

### Exercises

11. Suppose we have a computer system composed of 6 different components, and designed to have an RBD as shown in the image below. The four types of components (A, B, C, and D) have different reliability characteristics. We know that after 2 years the reliability of components B, C, and D are respectively  $R_B(2y) = 0.8$ ,  $R_C(2y) = 0.75$ , and  $R_D(2y) = 0.9$ . What should be the MTTF for component A, if we want to have a Reliability of the whole system after 2 years equal to  $R_{sys}(2y) = 0.85$ ?



**Answer:** We have 5 groups here:

Group 1. The two C components are **parallel**. The reliability of C is 0.75, so:

$$\begin{aligned}
 R_{\text{Group 1}} &= 1 - \prod_{i=1}^{n=2} (1 - R_{C_i}) \\
 &= 1 - [(1 - 0.75) \cdot (1 - 0.75)] \\
 &= 1 - [0.25 \cdot 0.25] \\
 &= 1 - 0.0625 \\
 &= 0.9375
 \end{aligned}$$

Group 2. Group 1 and Component B are in **series**. Group 1 has a reliability of 0.9375 and component B has a reliability of 0.8.

$$R_{\text{Group 2}} = \prod_{i=1}^{n=2} R_i = 0.9375 \cdot 0.8 = 0.75$$

Group 3. Components B and D are in **series**. If Component B has a reliability of 0.8 and Component D has a reliability of 0.9, then the reliability of this group is:

$$R_{\text{Group 3}} = \prod_{i=1}^{n=2} R_i = 0.8 \cdot 0.9 = 0.72$$

Group 4. Groups 2 and 3 are calculated in **parallel**. If Group 2 has a reliability of 0.75 and Group 3 has a reliability of 0.72, then:

$$\begin{aligned}
 R_{\text{Group 4}} &= 1 - \prod_{i=1}^{n=2} (1 - R_i) \\
 &= 1 - [(1 - 0.75) \cdot (1 - 0.72)] \\
 &= 1 - [0.25 \cdot 0.28] \\
 &= 1 - 0.07 \\
 &= 0.93
 \end{aligned}$$

Group 5. Groups 4 and A are calculated in **series**. Here, we don't have the reliability of Component A; however, we can easily find it since we have the reliability of the system:

$$\begin{aligned}
 R_{\text{Group 5}} &= \prod_{i=1}^{n=2} R_i \\
 0.85 &= 0.93 \cdot R_A(2y) \\
 R_A(2y) &= 0.85 \cdot \frac{1}{0.93} \\
 &= 0.913978495
 \end{aligned}$$

Now that we have the reliability value of component A, we can use the reliability formula with the Euler number exponent to find the mean time to failure (MTTF):

$$\begin{aligned}
 R_A(t) &= e^{-\lambda t} \\
 R_A(2y) &= e^{-\lambda 2} \\
 0.913978495 &= e^{-\lambda 2} \\
 \ln(0.913978495) &= -\lambda 2 \\
 -0.089948236 &= -\lambda 2 \\
 0.089948236 &= \frac{1}{\text{MTTF}} \cdot 2 \\
 \text{MTTF} \cdot 0.089948236 &= \frac{2}{\text{MTTF}} \cdot \text{MTTF} \\
 \frac{1}{0.089948236} \cdot \text{MTTF} \cdot \underline{0.089948236} &= 2 \cdot \frac{1}{0.089948236} \\
 \text{MTTF} &= \mathbf{22.235010812 \text{ years}}
 \end{aligned}$$

12. We have to design a RAID 5 storage architecture composed of an array of 7 disks. Knowing that each disk has a MTTF equal to 415 days and that we would like to have a MTTF for the storage infrastructure ( $MTTF_{RAID5}$ ) higher than 15 years, what is the maximum MTTR that we have to consider to satisfy the requirement? Consider all the disks with the same characteristics.

**Answer:** We use the Mean Time To Failure formula for RAID 5 (see page 75):

$$\begin{aligned}
 MTTF_{RAID\ 5} &= \frac{MTTF_{disk}^2}{G(G-1) \cdot MTTR} \\
 (15 \cdot 365) \text{ days} &= \frac{(415)^2}{7(7-1) \cdot MTTR} \\
 5475 \text{ days} &= \frac{172'225}{42 \cdot MTTR} \\
 MTTR \cdot 5475 &= \frac{172'225}{42 \cdot MTTR} \\
 \frac{1}{5475} \cdot MTTR \cdot 5475 &= \frac{172'225}{42} \cdot \frac{1}{5475} \\
 MTTR &= \frac{172'225}{42} \cdot \frac{1}{5475} \\
 &= \frac{172'225}{229'950} \\
 &= 0.748967167 \text{ days} \\
 &\approx \mathbf{0.75 \text{ days}}
 \end{aligned}$$

13. Consider an HDD with a data transfer rate of 10 MB/s, a rotation speed of 12000 RPM, a mean seek time of 4 ms, and a negligible overhead controller. What is the minimum locality required to achieve a mean I/O service time of 1.25 ms to transfer a sector of 4 KB?

**Answer:** We can use the average I/O time formula (see page 157) to find the data locality:

$$T_{I/O\ Avg} = (1 - DL)(T_{seek} + T_{rotation}) + T_{transfer} + T_{controller\ overhead}$$

In our case, the only well-known parts of this formula are the I/O average time and seek time. The controller overhead is negligible, so we can consider it zero. However, the rotation and transfer times are easy to obtain since we have all the necessary data!

- **Rotation Time.** We determine the rotation using two formulas: the full rotation delay and the total rotation average, which is what we are looking for.

$$R = \frac{1}{\text{RPM}} = \frac{1}{12'000} = 0.000083333 \cdot 60 = 0.005 \text{ sec}$$

$$T_{\text{rotation}} = \frac{R}{2} = \frac{0.005}{2} = 0.0025 \text{ sec} = 2.5 \text{ ms}$$

- **Transfer Time.** The transfer time can be easily calculated by dividing the read/write speed of a sector by the data transfer rate:

$$\begin{aligned} T_{\text{transfer}} &= \frac{\text{R/W sector}}{\text{Data Transfer Rate}} \\ &= \frac{4}{(10 \cdot 1024) \text{ KB/s}} \\ &= \frac{4}{10'240} \\ &= 0.000390625 \text{ sec} \\ &= 0.390625 \text{ ms} \end{aligned}$$

We now have all the necessary ingredients to calculate the desired data locality:

$$\begin{aligned} T_{\text{I/O Avg}} &= (1 - DL)(T_{\text{seek}} + T_{\text{rotation}}) + T_{\text{transfer}} + T_{\text{controller}} \\ 1.25 &= (1 - DL)(4 + 2.5) + 0.390625 + 0 \\ 1.25 &= 4 + 2.5 - 4DL - 2.5DL + 0.390625 \\ 0 &= -6.5DL + 6.890625 - 1.25 \\ 6.5DL &= 5.640625 \\ DL &= \frac{5.640625}{6.5} \\ &= 0.867788462 \\ &\approx \mathbf{86.78 \%} \end{aligned}$$

14. A company wants to evaluate the performance of the services provided to its users. The computer system includes two servers  $S_1$  and  $S_2$ . The system is initially considered as an open queue network model and the following measurements were obtained during 20-minute monitoring:

- Number of requests served at the system level:  $C = 300$
- Number of requests served by  $S_1$ :  $C_{S1} = 600$
- Number of requests served by  $S_2$ :  $C_{S2} = 100$
- Busy time  $S_1$ :  $B_{S1} = 350$  sec
- Busy time  $S_2$ :  $B_{S2} = 200$  sec

What are the service demand for  $S_1$  and  $S_2$  ( $D_{S1}$  and  $D_{S2}$ ) and their utilization ( $U_{S1}$  and  $U_{S2}$ )?

**Answer:** This exercise is not complicated, but it does require knowledge of basic formulas before delving deeper.

- **Service Demand.** The formula for service demand  $D$  is:

$$D_k = V_k \cdot S_k$$

What is missing here are the number of visitors and the mean service time.

- **Number of visitors**  $V_k$ . The number of visitors is easy to determine:

$$\begin{aligned} V_k &= \frac{C_k}{C} \\ V_{S1} &= \frac{600}{300} = 2 \\ V_{S2} &= \frac{100}{300} = 0.333333333 \end{aligned}$$

- **Mean service time**  $S_k$ . The mean service time is calculated using the busy time for each component and the number of requests:

$$\begin{aligned} S_k &= \frac{B_k}{C_k} \\ S_{S1} &= \frac{350}{600} = 0.583333333 \\ S_{S2} &= \frac{200}{100} = 2 \end{aligned}$$

We are now ready to calculate the service demand for each component:

$$\begin{aligned} D_k &= V_k \cdot S_k \\ D_{S1} &= 2 \cdot 0.583333333 = \mathbf{1.166666666 \text{ sec}} \\ D_{S2} &= 0.333333333 \cdot 2 = \mathbf{0.666666666 \text{ sec}} \end{aligned}$$

- **Utilization.** The formula for utilization  $U$  is:

$$U_k = X_k \cdot S_k$$

The only thing missing here is the throughput of each component. We could use the basic formula with the number of requests and the observation time:

$$\begin{aligned} X_k &= \frac{C_k}{T} \\ X_{S1} &= \frac{600}{(20 \cdot 60) \text{ sec}} = 0.5 \\ X_{S2} &= \frac{100}{(20 \cdot 60) \text{ sec}} = 0.083333333 \end{aligned}$$

So, the utilization is as follows:

$$\begin{aligned} U_k &= X_k \cdot S_k \\ U_{S1} &= 0.5 \cdot 0.583333333 = 0.291666667 \approx \mathbf{29.17\%} \\ U_{S2} &= 0.083333333 \cdot 2 = 0.166666666 \approx \mathbf{16.67\%} \end{aligned}$$

15. Consider now the same system presented in *Questions 14* as a closed model with a think time  $Z = 18$  sec, and the same values for the demand  $D_{S1}$  and  $D_{S2}$  calculated in the previous question (open model version). In the context of the asymptotic bounds, what is the system throughput upper bound for  $N = 30$  users?

**Answer:** We analyze the situation (heavy or light) before calculating the throughput:

$$N^* = \frac{D + Z}{D_{\max}} = \frac{(1.16 + 0.66) + 18}{1.16} = 17.086206897$$

Since the number of users exceeds  $N^*$  ( $N > N^*$ ), the situation is **heavy**. Therefore, the throughput bounds are:

$$\begin{aligned} \frac{N}{N \cdot D + Z} \leq X &\leq \min \left( \frac{1}{D_{\max}}, \frac{N}{D + Z} \right) \\ \max(D, N \cdot D - Z) \leq R &\leq N \cdot D \end{aligned}$$

Therefore, the maximum throughput is:

$$\begin{aligned} X_{\max} &= \min \left( \frac{1}{D_{\max}}, \frac{N}{D + Z} \right) \\ &= \min \left( \frac{1}{1.16}, \frac{30}{1.82 + 18} \right) \\ &= \min(0.862068966, 1.513622603) \\ &= 0.862068966 \text{ jobs/sec} \end{aligned}$$

It may not be the same as the professor's solution, but it depends on how many values we take as precise.

16. Considering the same system as in *Questions 14 and 15*, if you consider to add another instance of  $S_1$  in the system that equally splits the number of visits with the other  $S_1$  instance, how do the bounds change?

**Answer:** Adding another instance for  $S_1$  changes the system's service demand:

$$D = \frac{1.16}{2} + 0.66 = 0.58 + 0.66 = 1.24$$

However, the situation remains **heavy** even if we add another instance. Clearly, the bottleneck is now  $S_2$ .

$$N^* = \frac{D + Z}{D_{\max}} = \frac{1.24 + 18}{0.66} = 29.15151515$$

The maximum throughput is:

$$\begin{aligned} X_{\max} &= \min \left( \frac{1}{D_{\max}}, \frac{N}{D + Z} \right) \\ &= \min \left( \frac{1}{0.66}, \frac{30}{1.24 + 18} \right) \\ &= \min (1.515151515, 1.559251559) \\ &= \mathbf{1.515151515} \end{aligned}$$

### Open Questions

17. In the context of Virtualization, describe a Type 2 hypervisor providing also advantages and drawbacks?

**Answer:** Hosted Hypervisors run within the operating system of the host machine. Although hosted hypervisors run within the OS, additional operating systems can be installed on top of it. Hosted hypervisors have higher latency than bare metal hypervisors (type 1) because requests between the hardware and the hypervisor must pass through the extra layer of the OS.

Its advantages are its simplicity of use and flexibility in terms of underlying hardware. However, its main disadvantage is its high resource consumption.

18. Provide the definition of *Geographic Areas*, *Compute Regions*, and *Availability Zones* in the context of data centers. What are the advantages and drawbacks of placing all compute instances for my service within a single availability zone?

**Answer:**

- Geographic Areas are the highest level of the organization, defined by geopolitical boundaries or country-specific regulations. For example North America, Europe, Asia.
- Compute Regions are a finer granularity within geographic areas, representing large-scale infrastructure within a geographic region. Each

Geographic Area contains at least two Computing Regions for redundancy. For example, AWS has US-East-1 and US-West-1, which refer to different regions.

- Availability Zones are within a Compute Region, and physically separate datacenters within a region, each with redundant power, cooling and network.

The advantages of placing all compute instances for my service within a single availability zone are:

- **Low Latency, High Bandwidth.** All instances are physically close, so we get minimal network latency and maximum intra-AZ bandwidth.
- **Simpler Design & Management.**
- **Cost Efficiency.** By staying within one AZ, we save on inter-AZ data transfer costs (eventually fees to pay).

However, the drawbacks are very risky:

- **Single Point of Failure.** If the AZ has an outage (power, network, disaster), our entire service is down.
- **Limited Fault Tolerance.** We're exposed to hardware, network, or maintenance failures that can't be mitigated by simply moving load elsewhere.
- **Scalability Limits.** One AZ has finite capacity. Spreading across AZs allows us to tap larger total capacity.
- **No Geo-Redundancy.** In public cloud, AZs are designed to be isolated failure domains, not using them means we're ignoring built-in resilience.

### 5.3 2023

#### 5.3.1 July 7

##### True (✓) false (✗) questions

1. ✗ Hot/cold aisle containment reduces the efficiency of the cooling method for datacenters.
2. ✓ Edge computing is not a suitable alternative to cloud computing for applications that require large-scale data processing.

##### Deepening: *Why is this True?*

**Edge computing** pushes computation *closer* to the data source, like IoT devices, local gateways, smart sensors. The main goals are **low latency, reduced bandwidth usage, and local immediate processing**.

BUT edge devices are resource-constrained: limited CPU, memory, storage. **Large-scale data processing** (like training huge ML models, massive search indexing, or large analytics) **needs the aggregated compute power** of datacenter-scale clusters, which edge nodes alone cannot deliver efficiently.

So, if our workload is **heavy data crunching**, we still need **cloud computing / warehouse-scale computing**, with big clusters, specialized accelerators (GPUs, TPUs), high-throughput storage, large memory pools.

3. ✓ RAID 0 provides the best read and write performance of any RAID level composed of the same amount of disks.
4. ✗ Datacenters within the same Geographic Areas share the same power and network infrastructure.

##### Deepening: *Why is this False?*

Main rule:

Physically Nearby ≠ Operationally Linked

Just because two datacenters are in the same city or region doesn't mean they literally share the same power grid **distribution** or the same **network backbone** *inside* the facility.

The isolation is intentional. Large operators (Google, AWS, Azure) deliberately design datacenters with **redundancy** and **fault domains**:

- Different substations.
- Independent fiber routes.

- Diverse network peers.
- Separate cooling & power feeds.

If one power supply or fiber route fails, the other datacenter is unaffected, this **improves availability** and disaster tolerance.

Another important main rule:

Geo-Redundancy  $\neq$  Shared Infrastructure

Multiple datacenters in a region might be *replicas* for lower latency or local failover, but they are separate buildings with separate utility connections to avoid **single points of failure**.

5. ✗ TOR switches are typically used in small-scale datacenter deployments and are not suitable for larger networks.
6. ✓ Virtualization can help reduce energy consumption by consolidating multiple physical machines into fewer physical ones.
7. ✗ POD, Virtual-Chassis, DCell and BCube models are all evolutions of the leaf-spine network architectures.

#### Deepening: *Why is this False?*

Because DCCell and BCube are **not** evolutions of leaf-spine, they are fundamentally **different architectural families**:

- (base) **Leaf-Spine** is a two-level hierarchical system.
  - **Leaf (access)** switches connect servers.
  - **Spine (aggregation/core)** switches connect all leafs.
- Any leaf can reach any other leaf with equal cost. It is simple, flat, and have an high bisection bandwidth. Typical for modern cloud datacenters and big clusters.
- (correct ✓) **POD**: for example, in traditional Cisco architectures, a “POD” is a *modular block* that *can* be built with Leaf-Spine. So PODs can align with Leaf-Spine.
- (correct ✓) **Virtual-Chassis**: Vendor feature, where multiple switches act like one logical switch, it fits within Leaf-Spine designs for scaling port counts and management.
- (incorrect ✗) **DCell** and **BCube**. Here’s why the answer is incorrect. These come from Microsoft Research (and Huawei) for *modular, server-centric* topologies.
  - **DCell**: Recursive server-based hierarchy. Servers act as mini-switches → multi-hop paths → scalable, fault-tolerant.

- **BCube:** Server-centric, designed for modular containers. Each server has multiple NICs and connects to multiple mini-switches → many alternative paths.

So both break the typical Leaf-Spine model, instead of a simple two-level switch hierarchy, they *distribute* switching responsibilities to servers and small switches. They're *peer-to-peer inspired*, not classic core/aggregation.

8. ✗ Type 2 hypervisors run on top of a guest operating system that provides indirect access to hardware resources.

#### Deepening: Why is this False?

The confusion is about host OS vs guest OS. A **Type 2 hypervisor** is called hosted because it runs *on top of an existing Host Operating System* (e.g., Oracle VirtualBox). The **host OS** is the **real operating system installed on the physical machine** (Windows, Linux, macOS). The **Type 2 hypervisor** is just an application running on that host OS, it uses the host OS's drivers to access CPU, memory, disk, network. Then the hypervisor runs **guest OSes** inside virtual machines, then the VMs see *virtual hardware*.

Physical hardware → Host OS → Type 2 hypervisor → Guest OS

So the hypervisor runs **on the host OS**, not on a guest OS. The **guest OS** runs inside the hypervisor.

9. ✓ In-row cooling systems allow for higher server densities and increased rack power densities in datacenters.
10. ✗ DAS (Direct Attached Storage) is a storage system directly attached to the datacenter network.

#### Deepening: Why is this False?

Because DAS is not connected to the datacenter network, it's **directly attached to a specific server** (see page 80). DAS (Direct Attached Storage) means the storage (HDDs, SSDs) is connected **directly to a single server**, through SATA, SAS, PICe, or other local buses. There's **no network in between**, no shared storage fabric (like SAN or NAS). Other servers cannot directly access that storage unless the host server exports it via network protocols.

Instead, NAS (Network Attached Storage) is a storage connected to the datacenter network via Ethernet, clients access files via NFS/SMB. Finally, SAN (Storage Area Network) is a dedicated network for block storage (e.g., Fibre Channel).

### Exercises

11. Let us consider a set of requests in the disk queue referring to the following cylinders of the disk: 57, 32, 46, 83, 12. Consider the initial position of the disk head at cylinder 54 and moving from inside (lower cylinder number) to outside (higher cylinder number). Writes the order of the served requests (from the first to the last) if the disk head scheduling algorithm adopted is C-SCAN (Circular SCAN)? Use the cylinder number to refer to the request.

**Answer:** C-SCAN (Circular SCAN) is a disk scheduling algorithm (see page 44). It works like the SCAN, but when it reaches the end, it jumps back to the beginning, like a circular elevator.

The exercise text gives us a hint about the original movement: “[...] from inside (lower cylinder number) to outside (higher cylinder number) [...].” Therefore, we know that the next value will be 57:

$$(54 \rightarrow) \mathbf{57} \rightarrow \mathbf{83} \xrightarrow{\text{end reached, jump back}} (\rightarrow 0) \rightarrow \mathbf{12} \rightarrow \mathbf{32} \rightarrow \mathbf{46}$$

12. We have to design a RAID 5 storage architecture composed of an array of 8 disks. Knowing that we cannot guarantee an average MTTR lower than 6 hours and that we would like to have a MTTF for the storage infrastructure ( $\text{MTTF}_{\text{RAID}5}$ ) higher than 15 years, what is the minimum MTTF that we should consider for each disk? Consider all the disks with the same characteristics.

**Answer:** We can calculate the desired MTTF for each disk using the MTTF of the RAID 5 (see page 75):

$$\begin{aligned} \text{MTTF}_{\text{RAID}5} &= \frac{\text{MTTF}_{\text{disk}}^2}{G(G-1) \cdot \text{MTTR}} \\ (15 \times 365 \times 24) \text{ hours} &= \frac{\text{MTTF}_{\text{disk}}^2}{8(8-1) \cdot 6 \text{ hours}} \\ 131'400 \text{ hours} &= \frac{\text{MTTF}_{\text{disk}}^2}{56 \cdot 6 \text{ hours}} \\ 336 \text{ hours} \cdot 131'400 \text{ hours} &= \frac{\text{MTTF}_{\text{disk}}^2}{\cancel{336 \text{ hours}}} \cdot \cancel{336 \text{ hours}} \\ 44'150'400 \text{ hours} &= \text{MTTF}_{\text{disk}}^2 \\ \text{MTTF}_{\text{disk}} &= \sqrt{44'150'400 \text{ hours}} \\ &= 6644.576735955 \text{ hours} \\ &= (6644.576735955 \div 24) \text{ days} \\ &= \mathbf{276.857363998} \text{ days} \end{aligned}$$

13. A sensing system demonstrates an average availability equal to 0.98. The system is composed of a single device that needs to be substituted when fails. Knowing that its MTTR is equal to 3 hours, what will be the reliability of a new deployed device after 4 days?

**Answer:** Here is a recap of the data provided by the exercise:

- Availability  $A = 0.98$
- Mean Time To Repair MTTR = 3 hours
- Time  $t = 4$  days = 96 hours

The reliability formula is:

$$R(t) = e^{-\lambda t} \quad \text{where } \lambda = \frac{1}{\text{MTTF}}$$

So, we need to find the Mean Time To Failure (MTTF). We can use the Availability formula as a little trick to find the unknown variable, MTTF:

$$\begin{aligned} A &= \frac{\text{MTTF}}{\text{MTTF} + \text{MTTR}} \\ (\text{MTTF} + 3) \cdot 0.98 &= \frac{\text{MTTF}}{\text{MTTF} + 3} \cdot \frac{(\text{MTTF} + 3)}{(\text{MTTF} + 3)} \\ 0.98 \text{MTTF} + 2.94 &= \text{MTTF} \\ 0.98 \text{MTTF} - \text{MTTF} &= -2.94 \\ \text{MTTF} \cdot (0.98 - 1) &= -2.94 \\ \frac{1}{(0.98 - 1)} \cdot \text{MTTF} \cdot \frac{(0.98 - 1)}{(0.98 - 1)} &= -2.94 \cdot \frac{1}{(0.98 - 1)} \\ \text{MTTF} &= \frac{-2.94}{-0.02} \\ &= \frac{2.94}{0.02} \\ &= 147 \text{ hours} \end{aligned}$$

Thanks to MTTF, we have all the information necessary to calculate reliability:

$$\begin{aligned} R(t) &= e^{-\lambda t} \\ R(96) &= e^{-\frac{1}{147} \cdot 96} \\ &= e^{-0.653061224} \\ &= \mathbf{0.520450121} \end{aligned}$$

So the probability that a new deployed device *does not fail* in 4 days is about  $\approx 52\%$ .

14. Consider a queuing system with two stations. We have the following information about the system:

- station 1 response time: 5 s
- station 2 response time: 3 s
- station 1 throughput: 3 transactions/s
- station 2 throughput: 7 transactions/s
- system throughput: 4 transactions/s

Which is the average response time of the system?

**Answer:** Jobs flow through the system. Each job visits each station some average number of times. The total response time is the sum of all the time spent at all the stations per job. But, we don't have the **visit counts** directly, instead we have each station's throughput  $X_i$  and the system throughput  $X$ . And that tells us how many times a job on average goes through each station.

The visit ratio for station  $i$  is (see page 178):

$$V_i = \frac{X_i}{X}$$

This tells us, on average, each job causes how many operations at that station.

The time *per visit* is given (5s, 3s). So, the total time spent at that station per job is:

$$\text{Total time at station } i = V_i \times R_i$$

So:

$$\begin{aligned} R &= \sum_{i=1}^{n=2} R_i \cdot \frac{X_i}{X} \\ &= \underbrace{5 \cdot \frac{3}{4}}_{\text{station 1}} + \underbrace{3 \cdot \frac{7}{4}}_{\text{station 2}} \\ &= 3.75 + 5.25 \\ &= 9 \text{ seconds} \end{aligned}$$

15. Your data science team develops deep learning models by relying on a server including 8 CPUs, one GPU, and one SSD disk. Your team includes  $N = 10$  users who submit training jobs with a Think Time  $Z = 1$  hour. Every job uses all the available CPUs. Assuming that your server demands are the following:

- $D_{\text{CPU}^i} = 2 \text{ min } \forall i \in \{1 \dots 8\}$ . i.e. each CPU has a service demand equal to 2 min.
- $D_{\text{GPU}} = 12 \text{ min}$
- $D_{\text{Disk}} = 3 \text{ min}$

In the context of the asymptotic bounds, what is the system throughput upper bound and response time lower bound?

**Answer:** The data of the exercises are:

- $D_{\text{CPU}^i} = 2 \text{ min}$
- $D_{\text{GPU}} = 12 \text{ min}$
- $D_{\text{Disk}} = 3 \text{ min}$
- Think time  $Z = 1 \text{ hour} = 60 \text{ min}$

Before applying the throughput formula, it is necessary to understand whether the system has a heavy or light load in order to apply an optimistic or pessimistic view. We use  $N^*$  to determine whether to use the light load bound ( $N < N^*$ ) or the heavy load bound ( $N > N^*$ , see page 186):

$$N^* = \frac{D + Z}{D_{\max}} = \frac{17 + 60}{12} = 6.416666667 \approx 6.42$$

Where  $D$  is the total service demand per cycle:

$$D = \sum_{k=1}^K D_k = D_{\text{CPU}} + D_{\text{GPU}} + D_{\text{Disk}}$$

And the  $D_{\max}$  is the  $D_{\text{GPU}}$ . We use the critical path (parallel) to calculate  $N^*$ , because  $N^*$  identifies which single resource becomes saturated first. This occurs along the longest delay path in the network, which is the real elapsed time it takes one job to pass through all necessary stages while taking full parallelism into account.

$$N > N^* \Rightarrow 10 > 6.42 \Rightarrow \text{use heavy load bound}$$

In a **heavy load situation**, we use the critical path as  $D$  because we're analyzing which resource will saturate first under high load. So, the throughput bound is (see page 185):

$$\frac{N}{N \cdot D + Z} \leq X(N) \leq \min \left( \frac{1}{D_{\max}}, \frac{N}{D + Z} \right)$$

Since we are searching for the upper bound:

$$\begin{aligned}
 X_{\max} &= \min \left( \frac{1}{D_{\max}}, \frac{N}{D+Z} \right) \\
 &= \min \left( \frac{1}{12}, \frac{10}{17+60} \right) \\
 &= \min (0.083333333, 0.12987013) \\
 &= 0.083333333 \text{ min} \\
 &= (0.083333333 \cdot 60) \text{ jobs/hour} \\
 &= \mathbf{5 \text{ jobs/hour}}
 \end{aligned}$$

Where:

- $D_{\max} = D_{\text{GPU}}$
- $D$  is the total service demand per cycle:

$$D = D_{\text{CPU}} + D_{\text{GPU}} + D_{\text{Disk}} = 2 + 12 + 3 = 17 \text{ min}$$

Finally, when under a **heavy load situation**, the response time is (see page 185):

$$\max(D, N \cdot D_{\max} - Z) \leq R(N) \leq N \cdot D$$

Since we are searching for the lower bound:

$$\begin{aligned}
 R_{\min} &= \max(D, N \cdot D_{\max} - Z) \\
 &= \max(17, 10 \cdot 12 - 60) \\
 &= \max(17, 60) \\
 &= \mathbf{60 \text{ min}}
 \end{aligned}$$

16. If in the previous system (Question 15) you add 3 more GPUs (having hence 4 GPUs overall), what is the system throughput upper bound and response time lower bound? Consider that the original workload is evenly split across the entire set of GPUs.

**Answer:** Adding three more GPUs would split the service demand, meaning the original workload would be evenly split across the entire set of GPUs. This would greatly change the problem!

We move from a heavy load to a light load because  $N < N^*$ :

$$\begin{aligned}
 D &= D_{\text{CPU}} + D_{\text{GPU}} + D_{\text{Disk}} \\
 &= 2 + \frac{12}{4} + 3 \\
 &= 2 + 3 + 3 \\
 &= 8 \text{ min} \\
 N^* &= \frac{D+Z}{D_{\max}} \\
 &= \frac{8+60}{3} = 22.666666667
 \end{aligned}$$

With a **light load situation**:

- For each formula, we need to use the  $D$  value as the **total resource consumption** because throughput is limited by the total amount of work done, not wall-clock. This means that each task cannot be counted as parallel but rather sequential. Therefore:

$$\begin{aligned} D &= \sum_{i=1}^{n=8} D_{\text{CPU}_i} + \sum_{j=1}^{k=4} D_{\text{GPU}_j} + D_{\text{Disk}} \\ &= 16 + 12 + 3 \\ &= 31 \end{aligned}$$

Simply put, when the load is light, the system isn't saturated and jobs flow freely without waiting. Throughput is limited by total resource consumption rather than maximum latency. In our case, 8 CPUs (each working 2 minutes) results in 16 minutes of lost CPU time per job, even though the work is done in parallel. Therefore, we sum all resource times to reflect the true workload capacity needed.

- The **throughput** is (see page 185):

$$\begin{aligned} X_{\max} &= \frac{N}{(D + Z)} \\ &= \frac{10}{(31 + 60)} \\ &= \frac{10}{(91)} \\ &= 0.10989011 \text{ jobs/min} \\ &= (0.10989011 \times 60) \text{ jobs/hour} \\ &= 6.593406593 \approx \mathbf{6.6 \text{ jobs/hour}} \end{aligned}$$

- The **response time** is:

$$R_{\min} = D = \mathbf{31 \text{ min}}$$

### Open Questions

17. Discuss the main differences between para-virtualization and full-virtualization.

**Answer:** Full virtualization is a technique that provides a complete simulation of the underlying hardware. In contrast, para-virtualization modifies the operating system (OS) to use hypercalls instead of certain instructions. This is the main difference. For this reason, paravirtualization performs better than full virtualization. However, full virtualization provides complete isolation, though it is not permitted on all architectures. Finally, para-virtualization requires modification of the guest OS.

The trade-off is that para-virtualization needs guest OS source code access, which is possible for open-source OSes (like Linux), but not for proprietary ones (like Windows). Also, full virtualization typically provides stronger isolation and can run a wider range of unmodified operating systems.

18. What are the adopted strategies for efficient cooling of data center infrastructures targeting highly computational demanding applications, such as HPC and deep-learning workloads?

**Answer:** During the CI course, we studied three main cooling strategies.

- (a) **Hot/Cold Aisle Containment** is a physical containment of airflow to separate cold supply and hot exhaust air, maximizing cooling efficiency for dense racks.
- (b) **In-Rack and In-Row Cooling** are local cooling solutions that remove heat close to the servers, reducing recirculation and hotspots, used especially for high-density or high-performance clusters.
- (c) **Liquid Cooling** is a direct liquid cooling of servers/components (e.g., cold plates for CPUs/GPUs, or immersion cooling). It is essential when air cooling is no longer enough for extreme heat loads like dense GPUs for AI training.

## References

- [1] Mohammad Al-Fares, Alexander Loukissas, and Amin Vahdat. A scalable, commodity data center network architecture. *ACM SIGCOMM computer communication review*, 38(4):63–74, 2008.
- [2] L.A. Barroso, U. Hölzle, and P. Ranganathan. *The Datacenter as a Computer: Designing Warehouse-Scale Machines, Third Edition*. Synthesis Lectures on Computer Architecture. Springer International Publishing, 2022.
- [3] Shantanu Bhattacharya and Lipika Bhattacharya. *XaaS: Everything-As-A-Service: the lean and agile approach to business growth*. World Scientific, 2022.
- [4] E.D. Lazowska. *Quantitative System Performance: Computer System Analysis Using Queueing Network Models*. Prentice-Hall, 1984.
- [5] NIST. 8.1.8.4. R out of N model - itl.nist.gov. <https://www.itl.nist.gov/div898/handbook/apr/section1/apr184.htm>. [Accessed 14-08-2024].
- [6] Gianluca Palermo. Computing infrastructures. Slides from the HPC-E master's degree course on Politecnico di Milano, 2024.
- [7] Gianluca Palermo. Lesson 1, computing infrastructures. Slides from the HPC-E master's degree course on Politecnico di Milano, 2024.
- [8] David A. Patterson, Garth A. Gibson, and Randy H. Katz. A case for redundant arrays of inexpensive disks (raid). Technical Report UCB/CSD-87-391, Berkeley, Dec 1987.
- [9] Jiang Wu, Zhou Lei, Shengbo Chen, and Wenfeng Shen. An access control model for preventing virtual machine escape attack. *Future Internet*, 9(2):20, 2017.

# Index

## A

Actual Data Transfer Time	63
actual size on the disk $a$	36
Analytical and numerical techniques	167
Application Binary Interface (ABI)	111
Application-level virtualization	113
Arrival rate	173, 174
Artificial Neural Networks (ANNs)	31
as-a-Service	123
Asymptotic Bounds	182
Availability	21, 134
Availability of Parallel System	144
Availability of Series System	143
Availability Zones (AZs)	20
Average Service Time	157

## B

Bare Metal Hypervisor	114
BCube	98
Bisection Bandwidth	83
Blade Server	25, 30
Block	45
Block-Level Mapping	53
bottleneck device	181
bottleneck resource	181
Bounding Analysis	181

## C

C-LOOK	44
cache	42
CamCube	96
Cell	45
Chunk Size	62
Circular SCAN (C-SCAN)	44
Clos network	88
Clos network rearrangeably non-blocking condition	89
Clos network strictly non-blocking condition	90
Closed Model	184
Closed-Loop systems	104
Cloud Application Layer	124
Cloud Computing	122, 123
Cloud Software Environment Layer	124
Cloud Software Infrastructure Layer	124
Community Cloud	126
Completion rate	173, 174
Computing Continuum	6
Computing Infrastructure	5
Computing Regions (CRs)	20

Consolidation Management	122
Container	120
Controller Overhead	41
CRAC (computer room air conditioning)	104
<b>D</b>	
Data Center	5
Data Center Infrastructure Efficiency (DCiE)	107
Data Center Network (DCN)	84
Data Duplication (Mirroring)	59
Data Locality $DL$	157
Data Striping	59
DCell	97
DCN Hybrid architectures	84
DCN Server-centric architectures	84
DCN Switch-centric architectures	84
Demand Time	180
Demand-based FTL (DFTL)	55
Dependability	127
Development-Time Failures	129
Direct Attached Storage (DAS)	80
Disk Arrays	57
<b>E</b>	
Edge Computing	11
Edge Locations	20
Embedded System	10
Empirical Reliability Function	137
Endurance rating: Terabytes Written (TBW)	56
EoR (End-of-Row) architecture	86
Erase/Write Cycle Counter	56
external fragmentation	37
<b>F</b>	
Failure Avoidance	131
Failure in Time (FIT)	143
Failure Rate $\lambda$	136
Failure Tolerance	131
Failures In Time (FIT)	136
Fat-Tree (or 3-stage Clos)	92
Fault Hierarchy	140
Field-Programmable Gate Arrays (FPGAs)	32
First Come, First Serve (FCFC)	43
Flash Translation Layer (FTL)	48, 53
Flash-Based Caching	42
Fog Computing	11
Forced Flow Law	179
Full Rotation Delay	155
Full virtualization	117

**G**

Galois Fields (GF)	76
Garbage Collection (GC)	50
Geographic Areas (GAs)	19
Graphics Processing Units (GPUs)	32

**H**

Hard Disk Drive (HDD)	34, 39
Hardware RAID	79
Hardware-level virtualization	113
Hosted Hypervisor	116
Hot Spare Disk	78
Hot/Cold Aisle Containment	234
Hybrid Cloud	126
Hybrid FTL	54
Hybrid techniques	167
Hypervisor	114

**I**

In-Rack cooler	106
In-Row cooling	106
Interactive Response Time Law	178
internal fragmentation	36
Internet of Things (IoT)	10

**J**

JBOD (Just a Bunch Of Disks)	57
Join the shortest queue Routing Algorithm	171

**L**

LBA (Logical Block Address)	35
Leaf Bandwidth	83
Leaf switches	88
Leaf-Spine Architecture	88
Liquid cooling	106
Little's Law	175
Logical Block Address (LBA)	45, 46

**M**

Machine Learning (ML)	31
Mean service time	174
Mean Time Between Failures (MTBF)	136
Mean Time To Failure (MTTF)	136, 143, 144
Microkernel architecture	115
Mission-Critical Systems	130
Modular Datacenter Cube (MDCube)	100
Monolithic architecture	115
Motherboard	26
MTTF (Mean Time To Failure)	160
MTTF of RAID 01 $MTTF_{RAID\ 0+1}$	161
MTTF of RAID 10 $MTTF_{RAID\ 1+0}$	162

MTTF of RAID 1	MTTF <sub>RAID 1</sub>	161
MTTF of RAID 4	MTTF <sub>RAID 4</sub>	163
MTTF of RAID 5	MTTF <sub>RAID 5</sub>	163
MTTF of RAID 6	MTTF <sub>RAID 6</sub>	163
MTTF of TMR system		151
Multiple Independent I/O Requests		59
<b>N</b>		
Native Hypervisor		114
Network Attached Storage (NAS)		80
Network Interface Cards (NICs)		84
Non-Volatile Memory express (NVMe)		34
<b>O</b>		
Open Model		182
Open-Loop systems		104
Operation-Time Failures		130
Operational Laws		173
<b>P</b>		
Packet forwarding		84
Page		45
Page mapping plus caching		55
Page-Level Mapping		54
Paravirtualization		118
Parity-Based Redundancy		59
PCIe (peripheral component interconnect express)		34
PoD (Point of Delivery)		93
Power Usage Effectiveness (PUE)		107
Private Cloud		126
Probabilistic Routing Algorithm		170
Process Virtual Machine		111
Public Cloud		126
<b>Q</b>		
Queueing Network Modeling		168
Queuing Policy		170
<b>R</b>		
Rack Server		25, 28
Rack Unit		28
RAID 0 + 1 - MTTF		162
RAID 1 + 0 - MTTF		162
RAID (Redundant Array of Independent Disks)		58
RAID 0		61
RAID 0 + 1		64
RAID 0 - MTTF		160
RAID 0 - Total Random Throughput		63
RAID 0 - Total Sequential Throughput		63
RAID 1		64
RAID 1 + 0		65

RAID 1 - Capacity	66
RAID 1 - MTTF	161
RAID 1 - Random Read	67
RAID 1 - Random Write	67
RAID 1 - Sequential Read	67
RAID 1 - Sequential Write	66
RAID 4	68
RAID 4 - Additive Parity	69
RAID 4 - Capacity	71
RAID 4 - MTTF	163
RAID 4 - Random Read	71
RAID 4 - Random Write	71
RAID 4 - Reliability	71
RAID 4 - Sequential Read	71
RAID 4 - Sequential Write	71
RAID 4 - Subtractive Parity	69
RAID 5	72
RAID 5 - Capacity	73
RAID 5 - MTTF	75, 163
RAID 5 - Random Read	73
RAID 5 - Random Write	73
RAID 5 - Reliability	73
RAID 5 - Sequential Read	73
RAID 5 - Sequential Write	73
RAID 5 - Throughput	73
RAID 6	76
RAID 6 - MTTF	164
RAID level	60
Read Caching	42
Redundancy	59
Reed-Solomon	76
Reliability	133
Reliability Block Diagram (RBD)	141
Reliability Block Diagrams	138
Reliability Function of Parallel Systems	144
Reliability Function of Series Systems as one Exponential Component $\lambda_S$	143
Reliability Terminology - Error	139
Reliability Terminology - Failure	139
Reliability Terminology - Fault	139
Reliability Terminology - Non-Activated Fault	139
Reliability Terminology - Non-Propagated (Absorbed) Error	139
Residence Time $R_k$	180
Response Time	155
Response Time $\tilde{R}_k$	180
Revolutions Per Minute (RPM)	39
RooN ( $r$ out of $n$ )	149
Rotary UPS system	103
Rotational Delay	41
Rotational Latency	41
Round Robin Routing Algorithm	170

Routing Algorithm	170
<b>S</b>	
Safety-Critical Systems	130
SCAN (Elevator Algorithm)	43
seek average	155
Seek Delay	41
Seek Time	155
Server	25
Server Consolidation	122
Service Demand $D_k$	179
Service Discipline	170
Service Level Agreement (SLA)	21, 127
Service Time	155, 180
Shortest Seek Time First (SSTF)	43
Simulation techniques	167
Single Multiple-Block I/O Request	59
Software RAID	79
Solid-State Drive (SSD)	34, 45
Spine switches	88
Standby redundancy	153
Storage Area Networks (SAN)	80
Stripe Unit	59, 62
Stripe Width	59
System Virtual Machine	112
System-level virtualization	113
<b>T</b>	
Tensor Processing Units (TPUs)	32
Three Layer architecture	85
Three-Tier architecture	85
Throughput	173, 174
TMR Reliability $R_{TMR}$	150
Top-of-Rack switch (ToR switch)	86
ToR (Top-of-Rack) architecture	86
torn write	39
Total Facility Power	107
total rotation average	155
Tower Server	25, 27
track buffer	42
Transfer time	41, 155
Triple Modular Redundancy (TMR)	150
Type 1 Hypervisor	114
Type 2 Hypervisor	116
<b>U</b>	
Unavailability	134
Unrecoverable Bit Error Ratio (UBER)	56
Unreliability	133
UPS (uninterruptible power supply or source)	103

Utilization	173, 174
Utilization Law	175, 179
<b>V</b>	
Virtual Machine (VM)	109
Virtual Machine Manager (VMM)	114
Virtual Machine Monitor	114
Virtual Machine Monitor (VMM)	112
Visit Count	178
<b>W</b>	
Warehouse-Scale Computers (WSCs)	16
wasted disk space $w$	36
Write Amplification	46
Write Caching	42
Write-Ahead Log (WAL)	67
Write-Back Cache	42
Write-Through Cache	42
<b>X</b>	
X as a service	123