

6.  $SD = 14$   
 $n = 169$   
 $\mu = 15$   
 $\bar{x} = 16$

- 1.
2.  $\alpha = 0.10$  (90%)
3. Calculate the  $z$  value.

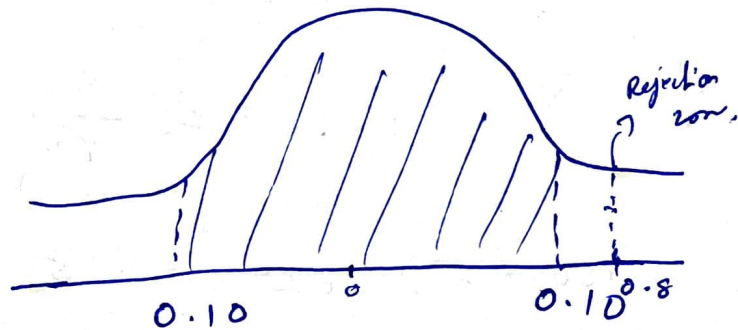
$$z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

$$= \frac{16 - 15}{14 / \sqrt{169}}$$

$$= \frac{1}{14 / 13}$$

$$= 1 / 1.076$$

$$z = 0.92$$



4.  $P$  value (from the  $z$  table)

$$P(z = 0.92) = 0.8212$$

$$\boxed{\alpha = 0.10}$$

$$P = 0.8212 > \alpha = 0.10$$

$P(z) < 0.10$ ; Reject the null hypothesis

$P(z) > 0.10$ ; Accept the  $H_0$  hypothesis

4 Perform t-test distribution

$$\text{Mean } \bar{x} = 100.8$$

$$SD = 1.85$$

$$n = 10$$

$$v = 10 - 1 = 9$$

$$95\% \text{ level } \alpha = 0.05 \quad \& \therefore \frac{\alpha}{2} = 0.025$$

$$t_{9, 0.025} = 2.262$$

$$\bar{x} - t_{n-1, \frac{\alpha}{2}} \frac{s}{\sqrt{n}} \leq \mu \leq \bar{x} + t_{n-1, \frac{\alpha}{2}} \frac{s}{\sqrt{n}}$$

$$100.8 - 2.262 * \frac{1.85}{\sqrt{10}} \leq \mu \leq 100.8 + 2.262 * \frac{1.85}{\sqrt{10}}$$

$$100.8 - 2.262 (0.585) \leq \mu \leq 100.8 + 2.262 (0.585)$$

$$100.8 - (1.323) \leq \mu \leq 100.8 + (1.323)$$

$$99.47 \leq \mu \leq 102.123$$

3. Ratio of Sample Variances

$$\begin{array}{l} S_1^2 = 0.893 \\ S_2^2 = 0.829 \end{array}$$

$$F = \frac{S_1^2}{S_2^2} = \frac{0.797}{0.687} = 1.160$$

$$H_0 = \sigma_1^2 = \sigma_2^2$$

$$H_A = \sigma_1^2 \neq \sigma_2^2$$

$$V_1 = 10 - 1 = 9$$

$$V_2 = 12 - 1 = 11$$

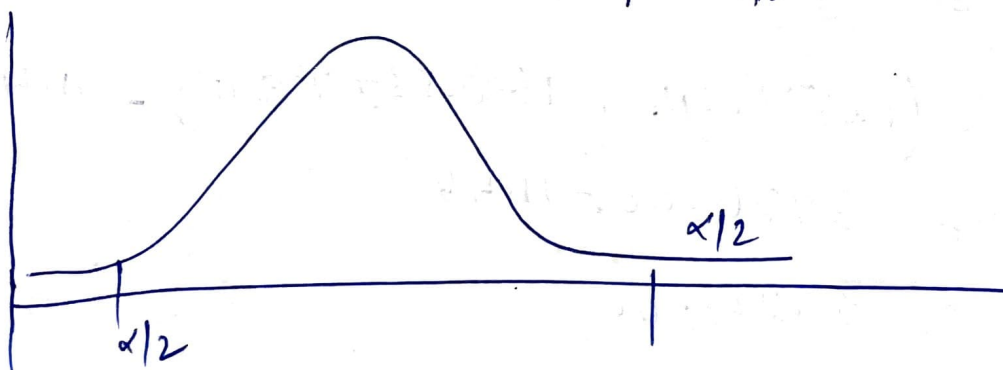
$$F_{0.025, 9, 11} = 3.5879$$

$$F_{0.975, 9, 11} = \frac{1}{F_{0.025, 9, 11}} = 0.2787$$

$$F_{0.025, 9, 11} = 3.5879, F_{0.975, 9, 11} = 0.2787;$$

$$F_{\text{observed}} = 1.160$$

Accept  $H_0$



## 2. ANOVA :

Financial :

	$x^2$
10.76	115.77
15.05	226.50
17.01	289.34
5.07	25.70
14.5	380.25
8.16	66.58
10.38	107.74
6.75	45.56
92.68	1257.44

Energy

	$x^2$
12.72	161.79
13.91	193.48
6.43	41.34
11.19	125.21
18.79	353.06
20.73	429.73
9.6	92.16
17.4	302.76
110.67	1699.53

Utilities

	$x^2$
11.88	141.13
5.86	34.33
13.46	181.17
9.9	98.01
3.95	15.60
3.44	11.83
7.11	50.55
15.7	246.49
71.3	779.11

Correction Term :

$$C_x = \frac{\sum (x)^2}{N}$$

$$= \frac{(92.68 + 110.67 + 71.3)}{24}$$

$$= 274.65 / 24$$

$$= 11.44$$

(1) Sum of square total :

$$SS1 = \sum x^2 - C_x$$

$$= (1257.44 + 1699.53 + 779.11) - 11.44$$

$$= 3736.08 - 11.44$$

$$= 3724.68$$

[2] Sum of Square among group

3

$$SS_A = \frac{(\sum x^2)}{n} - C_x$$

$$= \left( \frac{92.68^2}{8} + \frac{110.67^2}{8} + \frac{71.3^2}{8} \right) - C_x$$

$$= (1073.69 + 1530.98 + 635.49) - 11.44$$

$$= (3240.16) - 11.44$$

$$= 3228.72.$$

[3] Sum of Squares within the group.

$$SS_W = SS_T - SS_A$$

$$= 3724.68 - 3228.72$$

$$= 495.96$$

[4] Mean of Sum of Squares among the group.

$$M_{SSA} = \frac{SS_A}{k-1}$$

$$k=3$$

$$= \frac{3228.72}{3-1} = 1614.36.$$



(5) Mean of sum of squares within the group.

$$\begin{aligned}
 M_{SSW} &= \frac{SSW}{n-k} \\
 &= \frac{495.96}{24 - 3} \\
 &= \frac{495.96}{21} \\
 &= \cancel{23.61} \quad \cancel{23.61} \quad 23.61
 \end{aligned}$$

F-Ratio:

$$\begin{aligned}
 &= \frac{M_{SSA}}{M_{SSW}} = \frac{1614.36}{\cancel{23.61} \quad \cancel{23.61} \quad 23.61} \\
 &= \cancel{68.37} \quad \cancel{52.00} \quad 68.37
 \end{aligned}$$

Compare F-Ratio (calculated F value)

Source of variance	df	SS	MSS	F Ratio
Among group	k-1 (3-1)	3228	1614	68.37
within group	n-k (24-3) ↳ 21	495	23.61	

$$df (21, 2) = 3.466$$

$$F_c \Rightarrow 68.37, F_t = 3.466$$

$$\begin{aligned}
 F_{ratio} &> F_{table} \\
 68.37 &> 3.466
 \end{aligned}$$

Reject  $H_0$  hypothesis.

Yes, there is a difference in the rate of solvent for any of the industries.

5.

$$1. \mu = 105 \rightarrow H_0$$

$$\mu > 105 \rightarrow H_A$$

$$2. \bar{x} = 125$$

$$\mu = 105$$

$$SD = 14$$

$$n = 25$$

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$$

$$t = \frac{125 - 105}{14/\sqrt{25}}$$

$$= \frac{20}{2.8} = 7.14$$

$$3. \alpha = 5\%$$

$$df = 25 - 1 = 24$$

$$t_{table} = 1.711$$

$$t_{table} < t_{observed}$$

$$1.711 < 7.14$$

Reject  $H_0$

Mean sales is greater & enhancement worked.