### tlength

Calling tlength(nderiv) to calculate the length cost function w/o its derivatives on all degrees of freedom. When nderiv = 0, it only calculates the 0 - order length cost function, which is  $/tlength = \sum_{i=1,Ncoils} \frac{1}{2}(L_i - L_o^i)^2/$ . When nderiv = 0, it will calculate both the 0 - order and  $1^{st} - order$  derivatives in array t1L(1:Ncoils,0:Codf). When nderiv = 0, it will calculate all the 0 - order,  $1^{st} - order$  and  $2^{nd} - order$  derivatives t2L(1:Ncoils,0:Codf,1:Ncoils,0:Codf).

[called by: denergy.]

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# 1.1 Total length cost function

1. The length of each coils can be calculated through,

$$L_{i} = \int_{icoil} \sqrt{\dot{x}(t)^{2} + \dot{y}(t)^{2} + \dot{z}(t)^{2}} dt \approx \sum_{ksea = 0.Ndcoil - 1} \sqrt{xt(kseg)^{2} + yt(kseg)^{2} + zt(kseg)^{2}} \frac{2\pi}{NDcoil}$$
(1)

The results of user discretized method and NAG:D01EAF adaptive routine can be compared through subroutine descent.

2. And then the cost funtion on length is

$$ttlen = \sum_{i=1,Ncoils} \frac{1}{2} Lw_i (L_i - L_o^i)^2$$
(2)

where  $Lw_i$  is the weight of length of each coil, while there is another weight on the length cost function  $weight\_ttlen$ 

### 1.2 First dirivatives

Since the length of coils has no relationships with the current in the coil, the first derivatives of *ttlen* on currents are all zero. An the derivatives on the geometry variables can be represented as,

$$\frac{\partial ttlen}{\partial x_n^i} \equiv (L_i - L_o^i) \frac{\partial L_i}{\partial x_n^i} \tag{3}$$

Here i is denoted to the  $i^{th}$  coil and  $x_n$  means the  $n^{th}$  DoF. And

$$\frac{\partial L_i}{\partial x_n^i} \equiv \int_{icoil} \frac{\dot{x}}{\sqrt{\dot{x}(t)^2 + \dot{y}(t)^2 + \dot{z}(t)^2}} \frac{\partial \dot{x}}{\partial x_n^i} dt \tag{4}$$

## 1.3 Second derivatives

The second derivatives of length cost function are only related to geometry variables of the same coil. That is,

$$\frac{\partial^2 t t l e n}{\partial x_n^i \partial x_m^i} \equiv \frac{\partial L_i}{\partial x_m^i} \frac{\partial L_i}{\partial x_n^i} + (L_i - L_o^i) \frac{\partial^2 L_i}{\partial x_n^i \partial x_m^i} \equiv \int_{i coil} \frac{1}{\sqrt{\dot{x}(t)^2 + \dot{y}(t)^2 + \dot{z}(t)^2}} \frac{\partial \dot{x}}{\partial x_n^i} \frac{\partial \dot{x}}{\partial x_m^i} - \frac{\dot{x} \dot{x}}{(\sqrt{\dot{x}(t)^2 + \dot{y}(t)^2 + \dot{z}(t)^2})^3} dt$$
 (5)

### 1.4 Normalization

While normalizing length cost function, we should divide it with the target length of each coils. That is,

$$ttlen = \sum_{i=1,N_{coils}} \frac{1}{2} Lw_i \frac{(L_i - L_o^i)^2}{L_o^{i2}}$$
(6)

Since the target lengths are user specified constant, the normalization of length cost function derivatives can be implemented by dividing them with each coil's target length.

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Focus subroutines;