Jawahar Education Societys Annasaheb Chudaman Patil College of Engineering, Kharghar, Navi Mumbai

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SUBJECT: Analysis of Algorithms Lab

Implement a C program for Graph Colouring using Backtracking Approach.

EXPERMINT: 09

DATE.: / / 20

Experiment No-09

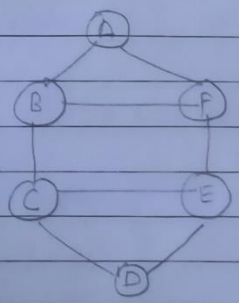
- **Aim:-** To implement Graph coloring using Backtracking
- **Objective :-** To implement complexity of Graph coloring
- **Outcomes :-** Students will be able to compute the complexity of Graph Coloring problem
- **Hardware/Software Required:** TURBO C
- **Problem Definition:**

Let G be the Graph and m be the given positive value integer. The problem is to find whether the nodes of G can be colored in such a way that no two adjacent nodes have the same color yet only m colors are used. Solution vector x is n tuple such that $x = (x_1, x_2, \ldots, x_n)$ where x_i is color of node i and $x_i <= m$.

- **Theory :-**

Backtracking is the refinement of the brute force approach, which systematically searches for solution to a problem among all available options. It does so by assuming that the solution are represented by vector $(V_1, V_2, \ldots, V_m)$ of value and by traversing the domains of vectors until the solution are found.

Ex



Teachers Signature

Implement a C program for Graph Colouring using Backtracking Approach.

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Solution vector x = {1, 2, 3, 3, 2, 3}

The idea is to assign colors one by one to different vertices, starting from the vertex 0. Before assigning a color, we check for the safety by considering already assigned color to the adjacent vertices. If we find a color assignment which is safe, we mark the color assignment as part of solution. In backtracking we can represent solution space for the program using state space tree.

· Algorithm:-

```
Algorithm Graphcoloring (k)
1. while (true)
2  Nextcolor (k);                    // assign a color to k
3. if (x[k] = 0), then return;       // color insufficient
4. if (k == n) then                  // print solution
5.     print x[1..n];
6  else
7  Graphcoloring (k+1)
```

· Algorithm:-Nextcolor (k)

```
1) while (true)
2) x[k] = (x[k]+1) mod (m+1);        // next highest color
3) if x[k]=0 then return             // all colors used
4) for j=1 to n do
5) break; if (G[k,j] !=0 AND (x[k] == x[j]) // same color
6) break;
7) if (j=n+1) then return;           // distinct color.
```

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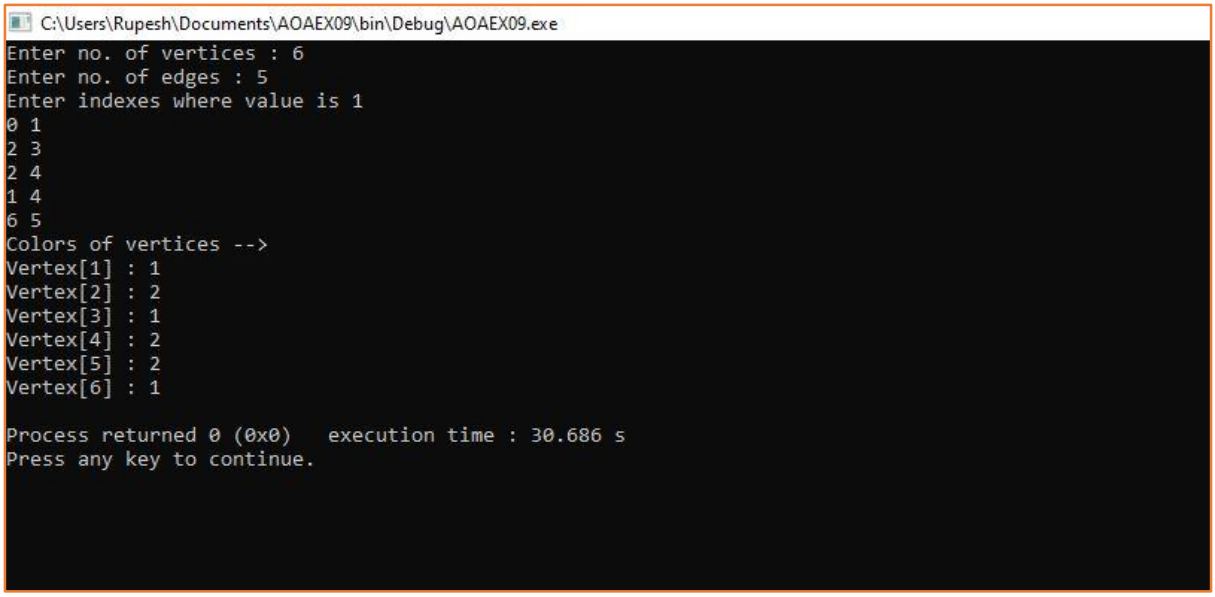
Implement a C program for Graph Colouring using Backtracking Approach.

Input:

```c
#include<stdio.h>
int G[50][50],x[50]; //G:adjacency matrix,x:colors
void next_color(int k){
int i,j;
x[k]=1; //coloring vertex with color1
for(i=0;i<k;i++){ //checking all
if(G[i][k]!=0 && x[k]==x[i])
x[k]=x[i]+1; //assign higher color than x[i]
}
}
int main(){
int n,e,i,j,k,l;
printf("Enter no. of vertices : ");
scanf("%d",&n); //total vertices
printf("Enter no. of edges : ");
scanf("%d",&e); //total edges
for(i=0;i<n;i++)
for(j=0;j<n;j++)
G[i][j]=0; //assign 0 to all index of adjacency matrix
printf("Enter indexes where value is 1");
for(i=0;i<e;i++)
{
scanf("%d %d",&k,&l);
G[k][l]=1;
G[l][k]=1;
}
for(i=0;i<n;i++)
next_color(i); //coloring each vertex
printf("Colors of vertices -->\n");
for(i=0;i<n;i++) //displaying color of each vertex
printf("Vertex[%d] : %d\n",i+1,x[i]);
return 0;
}
```

Implement a C program for Graph Colouring using Backtracking Approach.

Output:



Conclusion: Thus it is observed that the Complexity **of Colouring using Backtracking Approach** Problem is **$O(m^V)$.**