

HASHMAP

- ① `HashMap<key, value>` is a part of Java Collection.
- ② This class is found in `java.util` package.
- ③ Hashmap is a datastructure which has an amazing property that most of the operations which we perform on it are done in $O(1)$ time complexity.

The data is stored in a hashmap in the form of key value pairs.

Country	Population (in Millions)
INDIA	1391
CHINA	1398
USA	329
INDONESIA	268

Population Map

∴ key : Country (String)
value : Population (Integer)

∴ Agar Hum Data Hashmap me store kروا رہے hai toh Data Key-value pair, ki form me store hoga!

Data Pair
→ Key ↗ Ek key aur ek value ko mila kr ek pair banta hai usse bolty hai Key-value Pair
→ value

- ④ Hashmap is a MAP : Map is a key-value mapping, which means every key is mapped to exactly 1 value and we can use the key to retrieve the corresponding value from a map.
- ⑤ Advantage of Hashmap is that time complexity to insert and retrieve a value is $O(1)$ on Average.

CREATING HASHMAP

It is compulsory to use Capital I's !

`HashMap<String, Integer> hm = new HashMap<>();`

key's
datatype

value's
datatype

name of
the hashmap

Like other DS, Hashmap is also created using new keyword.

{ } → This is what an empty hashmap looks like.
So, let's now try to insert some values into it and then displaying it.

PUT INTO HASHMAP → put(key, value) function can be used to put some values into the hashmap.

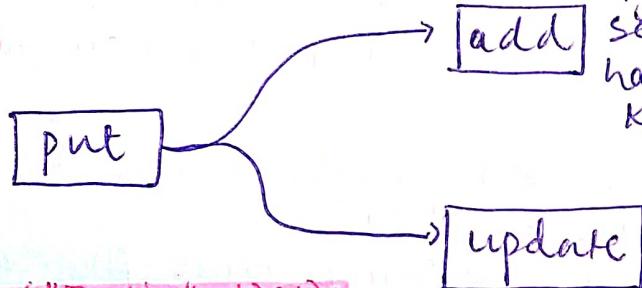
Time complexity → O(1)

There are 2 possible cases while we are using the put(key, value) function in a hashmap.

When the key is already present

If the key is already present, we cannot insert the same key again. (Warna humare paas duplicate ke hojayegi). (Aur hume isse duplicate key chahiye nahi).

→ Only the value of the existing key will get updated in the hashmap.



hm.put("India", 1391);
hm.put("China", 1398);
hm.put("USA", 329);
hm.put("Indonesia", 268);

System.out.println(hm);] → {USA:329, China:1398, India:1391, Indonesia:268}

hm.put("Indonesia", 270);

System.out.println(hm);]

→ {USA:329, China:1398, India:1391, Indonesia:270}

value updated.

* We must observe that the hashmap has changed the order in which the elements occur.

* So, this is something that we can not control in hashmap. We can not control the order of occurrence of elements in a hashmap.

Toh put function humare liye key add ka bhi kaam kar sakta hai aur key update bhi!

④ GET A VALUE IN HASHMAP → Time complexity : O(1)

The `get(key)` function in a `hashmap` is used to get the value corresponding to a particular key in the `hashmap`.

There are
2 possibilities

- Key existed → If the key exists, then we will get the value of that key by using the get() function.
- Key doesn't exist → If the key does not exist, then the `get(key)` function will return null.

`System.out.println(hm.get("India"));` → India: Key already exists in the hm hashmap with value = 139.

`System.out.println(hm.get("Utopia"));` → The key "Utopia" does not exist. So null value will be returned.

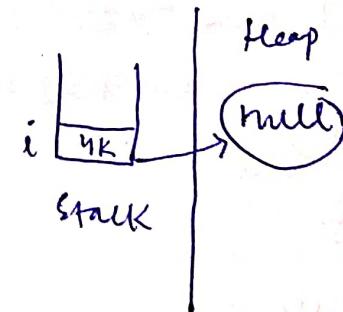
* We should get the values of a key only in the Integer.

Capital I Integer datatype can store null as

`Integer x = hm.get("Utopia");`
we can store null here returns null

`int x = hm.get("Utopia");`
int datatype returns null
can not store null so we
will get a null pointer exception. → Because int is a primitive datatype.

<u>Primitive Type</u>	<u>Wrapper Class</u>
byte	Byte
int	Integer
short	Short
long	Long
float	Float
double	Double
boolean	Boolean
char	Character



① CONTAINS KEY IN HASHMAP → Time complexity : O(1)

The ContainsKey() is a Boolean function.

We pass a particular key value as a parameter to this function. If the hashmap contains key, it returns true else return false.

System.out.println(hm.containsKey("China"));

→ TRUE

we get true for the key "China" as it exists in the

System.out.println(hm.containsKey("Pakistan"));

→ False

we get false for the key "Pakistan" as the hashmap does not consist the key.

② KEYSET IN HASHMAP

→ We know that we have key-value pairs in hashmap, we can get only the keys in hashmap by using the KeySet() function.

public static void main (String [] args) {

```
    Hashmap<String, Integer> hm = new Hashmap<>();  
    hm.put("India", 1391);  
    hm.put("China", 1398);  
    hm.put("USA", 329);  
    hm.put("Indonesia", 268);
```

Set<String> key = hm.keySet();

for (String key : keys) {

Integer val = hm.get(key);

System.out.println(key + ":" + val);

}

}

Output:

USA : 329

China : 1398

India : 1391

Indonesia : 268

↓
The Keyset() function returns the set of all the keys in hashmap

↓
we can store it in a Set Container.

Set<String> keys = hm.keySet();

System.out.println(keys);

Set ek essa collection hota hai, jisme hamneha unique values hogi! Jese hashmap me key hamse unique hoti hai!

HIGHEST FREQUENCY CHARACTER

Hume ek string given hogi, hume uss string me se maximum Occuring character ko print karna hai!

Hume I frequency map Banayengy

- Hoga character ki Frequency
- Key = character
- value = frequency

String : abbc babc dd dab b d a b b b

○ We iterate through every character of the string and then increase the count against that character.

APPROACH

① We create a new Hashmap of character, w/s integer, named hm

② We iterate through all the character of the string and check if the hashmap contains the given character. If it does, then, we get the frequency of that character & store in the old variable.

≡ Hum string ke saare characters par iterate krenge aur check krenge, kya hashmap me yeh character phle se exist krya hai?

≡ Agar hashmap me yeh character phle se exist krya hai toh hum old variable, me iss character ki frequency store krenge! → old variable ka naam hai jisme character ki existing frequency hum store krenge!

≡ Then, we increase it by 1 and store in the new. The 'new' gets inserted in hashmap against character.

new variable me old + 1 store krenge,

And then new gets inserted in the hashmap against the character.

③ Elseif, the hashmap does not contain that character then we add it to hashmap with its frequency 1.

string	
character	frequency
a	3
b	9
c	2
d	3

④ We initialize a variable "max" with the first character of the given string where "max" is the character with highest frequency!

```
char max = str.charAt(0);
```

⑤ We apply the for loop for every character of the hashmap. If the frequency of current character is greater than the frequency of "max", then that character gets stored in max.

⑥ We print the max. TIME COMPLEXITY $\rightarrow O(n) + O(n) = O(n)$

```
public static void main(String[] args) {  
    Scanner sc = new Scanner(System.in);  
    String str = sc.nextLine();  
    Map<Character, Integer> hm = new HashMap<>();  
  
    for (int i=0; i<str.length(); i++) {  
        char ch = str.charAt(i);  
        if (hm.containsKey(ch)) {  
            int old = hm.get(ch);  
            int new = old + 1;  
            hm.put(ch, new);  
        } else {  
            hm.put(ch, 1);  
        }  
        char max = str.charAt(0);  
  
        for (Character key : hm.keySet()) {  
            if (hm.get(key) > hm.get(max)) {  
                max = key;  
            }  
        }  
        System.out.println(max);  
    }  
}
```

Humne yeh naya hashmap Banaya hm naam ka!

String ke sabhi character's pe loop lagaya!

Agar string me vo char phle se hai toh uski value update hogi!

Agar vo character string me phle se exist nahi kta toh hum ek naya put karayengy ~~update usko~~ ~~update~~

char. ke liye value 1 ke saath usko hm hashmap me add dungy!

hm.keySet() se sabhi keys receive agar key ki value krenge!

max ki value se yada hai toh max me vo key daldo

last me max-frequency wali char. ko print kero!

NET COMMON ELEMENTS - I

Hume 2 array given hongay a_1 and a_2 !

$a_1 \rightarrow 1 1 2 2 2 3 5$	OUTPUT	$1 2 5$
$a_2 \rightarrow 1 1 1 2 2 4 5$		

We are required to print all the elements of a_2 which are also present in a_1 (in order of their occurrence in a_2)

Hume ek element 1 baar hi print karna hai!

Make sure not to print duplicate!

Toh phle hum array 1 ke sabhi elements ke liye ek hashmap Banayengy!

$a_1: 1 1 2 2 2 3 5$

$a_2: 1 1 1 2 2 4 5$

keys	values
1	x2
2	x23
3	1
4	
5	

∴ Aab hum array 2 ko traverse krenge, har element ko check krenge aur Agar vo element a_1 Ke Frequency map me present hogya toh hum uss element ko print krdengy!

Because it is present in freq. map of array 1 and array 2. So it is a common element.

Now, we will remove that element from the frequency map of array 1 if its present in map & array 2.

$a_2: 1 1 1 2 2 4 5$

1	x2
2	x23
3	1
5	1

Output: 1

Hum array 2 4 2 Travel krenge hume 1 mila, 1 is also present in the hashmap

$a_2: 1 1 1 2 2 4 5$

1	x2
2	x23
3	1
5	1

Output: 1 2

$a_2: 1 1 1 2 2 4 5$

3	1
5	1

Output: 1 2 5

```

public static void main (String [] args) {
    Scanner sc = new Scanner (System.in);
    int n1 = sc.nextInt();
    int [] arr1 = new int [n1];
    for (int i=0; i<arr1.length; i++) {
        arr1[i] = sc.nextInt();
    }
    int n2 = sc.nextInt();
    int [] arr2 = new int [n2];
    for (int i=0; i<arr2.length; i++) {
        arr2[i] = sc.nextInt();
    }
}

HashMap <Integer, Integer> fmap = new HashMap <>();
int (int val : arr1) { → array 1 ke liye frequency map banaya!
    if (!fmap.containsKey (val) == (false)) {
        fmap.put (val, 1);
    } else {
        int oldfreq = fmap.get (val);
        int newfreq = oldfreq + 1;
        fmap.put (val, nf);
    }
}
for (int val : arr2) {
    if (!fmap.containsKey (val) == (true)) {
        System.out.println (val);
        fmap.remove (val);
    }
}

```

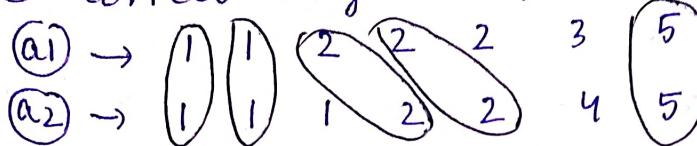
Hashmap Banaya!

Agar val phle se fmap me hai toh old freq. + 1 krdo, value aur new freq. hojayega freq. map me update!

Agar array 2 ki element (val) hume freq. map me nilega toh uss value (element) ko print krdo aur val ko a fmap se remove krdo!

GET COMMON ELEMENTS 2

Humne correct Integration print kreni hai!



Output: 1 1 2 2 5

character	Freq.
1	X 2
2	X X 3
3	1
5	1

= Phete (a1) ki freq. map banao

Humne hashmap Banalisa (a1) ke liye →

= Aab humne (a2) per travel kreni hai!

Aur agar (a2) ka koi bhi element freq. map me mila aur uss key ki value > 0 hai toh usse print kro aur uss key ki value me se 1 minus kro!

character	Freq
1	0 X X
2	1 X X
3	1
5	0 X

Output

1 1 2 2 5

```

public static void main (String args) {
    Scanner sc = new Scanner (System.in);
    int n1 = sc.nextInt();
    int arr1[] = new int [n1];
    for (int i=0; i<arr1.length; i++) {
        arr1[i] = sc.nextInt();
    }
    int n2 = sc.nextInt();
    int arr2[] = new int [n2];
    for (int i=0; i<arr2.length; i++) {
        arr2[i] = sc.nextInt();
    }
    HashMap <Integer, Integer> fmap = new HashMap <> ();
    for (int val : arr1) {
        if (fmap.containsKey (val) == false) {
            fmap.put (val, 1);
        } else {
            int oldfreq = fmap.get (val);
            int newfreq = oldfreq + 1;
            fmap.put (val, newfreq);
        }
    }
}

```

```

for (int val : arr2) {
    if (fmap.containsKey (val) == true && fmap.get (val) > 0) {
}

```

```

System.out.println (val);
int oldfreq = fmap.get (val);
int newfreq = oldfreq - 1;
fmap.put (val, newfreq);
}
}

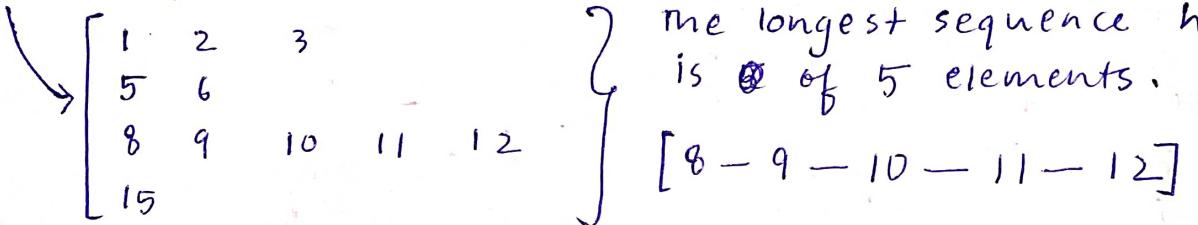
```

LONGEST CONSECUTIVE SUBSEQUENCE

Hume array given hoga!

example: [10 5 9 1 11 8 6 15 3 12 2]

The following consecutive sequence can be formed from the given array



APPROACH

Hum ek hashmap Banayengy (Integer V/s Boolean) for all the elements of the array and store "TRUE" against them all initially!

10 5 9 1 11 8 6 15 3 12 2

keys (Integer)	values (Boolean)
10	TRUE F
5	TRUE
9	TRUE F
1	TRUE
11	TRUE F
8	TRUE
6	TRUE F
15	TRUE
3	TRUE F
12	TRUE F
2	TRUE F

- = The true here represents that its corresponding element is the starting element of the desired sequence.
- = Ek loop lagaya array ke upper aur sabki elements ko hashmap me store krdia as keys and unne sabki values TRUE daal di!
- = Aab Hum pure ko iterate krenge loop lagake and we will check whether a number 1 less than that element is present in the hashmap or not. If the element is not present, then we do nothing. And if that element is present then that will be the starting element of sequence.
- = After iterating on all the elements of array, now, the values of keys are updated in Hashmap.

= For every TRUE value, we find the consecutive elements in the hashmap. Humare pass 2 variables hongay:

* m_sp = max starting point

for the starting point of sequence of maximum length

* rlen = max length

for the length of sequence of max. length.

$\Rightarrow 5 \rightarrow$ is have true as it's value in the hashmap.
 $\therefore 5-6 \rightarrow$ The consecutive sequence of 5 becomes (5-6).
Size of this sequence is 2.

$$\begin{array}{|l|} \hline \text{mlen} = 2 \\ \text{msp} = 5 \\ \hline \end{array}$$

\Rightarrow Now, the next sequence with '1' as the starting element is 1-2-3
length of this sequence = 3 \rightarrow it is greater than mlen

$$\begin{array}{|l|} \hline \text{mlen} = 3 \\ \text{msp} = 1 \\ \hline \end{array} \rightarrow \text{updated}$$

\Rightarrow This will go until we find the max length out of all sequences.

$\therefore [8-9-10-11-12] \rightarrow$ this is our max sequence

$$\begin{array}{|l|} \hline \text{mlen} = 5 \\ \text{msp} > 8 \\ \hline \end{array} \rightarrow \text{Aab hum point krdengy!}$$

public static void main (String [] args) {

Scanner sc = new Scanner (System . in);

int n = sc.nextInt(); \rightarrow size of array as input

int arr [] = new int [n];

for (int i = 0 ; i < arr.length ; i ++) { \rightarrow array fill kiya
arr [i] = sc.nextInt(); } elements se

} \rightarrow ek naya hashmap banaya jisme keys aur uski values daali

HashMap < Integer , Boolean > map = new HashMap < > ();

for (int val : arr) { \rightarrow sathe keys ki values
map.put (val , true); \rightarrow ko initially TRUE
kra }

for (int val : arr) { \rightarrow agar vo element se previous element
if (map.containsKey (val - 1) == true) { present hai toh uss
map.put (val , false); elements / key ki value FALSE Kardo }

int msp = 0; \rightarrow maximum starting point

int mlen = 0; \rightarrow maximum length

for (int val : arr) { \rightarrow ~~for~~ Array ke sabhi elements pe loop lagega
if (map.get (val) == true) { \rightarrow aur vo element select hogा jo
TRUE hai hashmap me!
int tsp = val; \rightarrow temporary starting point
int tlen = 1; \rightarrow temporary length

```
while (map.containsKey(tsp + tlen) == true) {  
    tlen++; }  
if (tlen > mlen) {  
    msp = tsp;  
    mlen = tlen; }  
  
for (int i=0; i<mlen; i++) {  
    System.out.println(msp + i); }
```

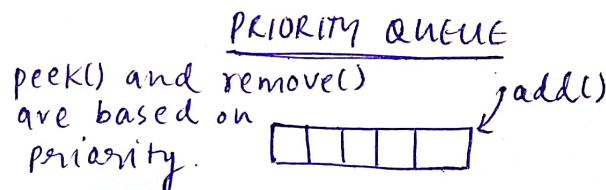
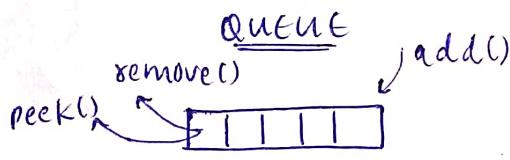
→ hum har element ka length aur temporary length ko increase krdy chalengy.

→ tlen is greater than mlen then update the values of msp and mlen.

→ Now, msp aur uske next elements ko print krdy !

PRIORITY QUEUE / HEAP

- It is an Abstract Data Type.
- In Priority Queue, har element ki kuch property hoti hai.
- It is very similar to Queue.
- The Priority of the elements in a Priority Queue determines the order in which elements are removed from the Priority Queue.
- ∴ All the elements are arranged in Ascending or Descending Order.
- PRIORITY QUEUE is an EXTENSION of the Queue with following properties:
 - * Every Queue has a PRIORITY associated with it.
 - * An element with higher priority is dequeued before an element with lower priority.
 - * If two elements have the same priority, they are served according to their ~~order~~ ^{first} order of occurrence in the queue.
- impl * The elements from Priority Queue are retrieved in sorted order.
- * The Priority Queue class has the same structure and function as that of Queue.



* Time Complexity of functions of Priority Queue.

add() $\rightarrow O(\log n)$

remove() $\rightarrow O(\log n)$

peek() $\rightarrow O(1)$

Structure Same

* Similarities B/w PQ and Queue

same Functions

* Differences B/w PQ and Queue

We can set priority according our needs!

Ascending Order

Highest Rank Order Priority: (smaller no. ko jyada Priority)

Highest Score Order Priority: (greater no. ko jyada Priority)

Descending order

CREATING A PRIORITY QUEUE

* Priority Set To Smaller Values

PriorityQueue<Integer> pq = new PriorityQueue<>();

↓
datatype
of
Element

name of priority queue

* By default, the priority will be set
of smaller values (Highest Rank Order)
Ascending Order (SORTED)

* Priority Set To Greater Values

PriorityQueue<Integer> pq = new PriorityQueue<>(Collections.reverseOrder());

PriorityQueue<Integer> pq = new PriorityQueue<>(reverse
order());

* greater value elements will be
given more priority.

reverse order means
elements remove
wrong!

HEAP SORT

Hume ek array given hoga. This array will be unsorted.

* Approach for getting all elements in Ascending Order

= make a priority queue, priority will be set as default.

= loop laga kar array ke sabhi elements ko PQ me add kardo!

= Now, PQ se ab hum elements ko retrieve krenge toh elements will be in sorted order (ASCENDING ORDER)

10	11	33	44	56	57	98
----	----	----	----	----	----	----

import java.util.*;

public class FirstPriorityQueue

{

 public static void main(String[] args) {

 int[] arr = {40, 90, 20, 14, 33};

 PriorityQueue<Integer> pq = new PriorityQueue<>();

$O(n \log n)$

for (int val : arr) {	→ one for loop has $O(n)$
pq.add(val);	→ add() function of PQ has $O(\log n)$
}	

$O(n \log n)$

while (pq.size() > 0) {	→ while loop has $O(n)$
{	
System.out.println(pq.remove());	→ remove() function of PQ has $O(\log n)$
}	
}	

∴ OUTPUT

14	20	30	40	90
----	----	----	----	----

∴ Time complexity: $O(n \log n) + O(n \log n)$

$$= 2 O(n \log n)$$

$$= O(n \log n)$$

Heap Sort
Are of

2 Types

The one with Space → $O(n)$
complexity

Another one where constant space is used.

* Approach for getting all elements in Descending Order

10	57	33	44	56	11	98
----	----	----	----	----	----	----

make a (pq), priority will be given more to greater elements

```
import java.util.*;
public class FirstPriorityQueue {
    public static void main (String [] args) {
        int [] arr = {40, 90, 20, 14, 33};
        Priority Queue <Integer> pq = new Priority Queue <>
            (Collections.reverseOrder());
        for (int val : arr) {
            pq.add (val);
        }
        while (pq.size > 0) {
            System.out.println (pq.remove () + " ");
        }
    }
}
```

$\Theta(n \log n)$ highest score priority order.

Output:

90	55	40	33	20	14
----	----	----	----	----	----

K - Largest Element

Hume ek array given hogi aur ek K given hogi! Unhe array me se K^{th} no. wala largest element print krdengy!

INPUT
10 19 3 74 86 57 24 5 11

$\therefore K = 3 \quad \text{OUTPUT} \Rightarrow 74, 86, 57$

APPROACH 1 \leftarrow Time complexity = $O(n \log n)$

Space complexity = $O(n)$

\Leftarrow Phle ek (PQ) Banayengy where priority will be given more to greater elements. Usse (PQ) me array ke saare elements daal denge! \leftarrow Time complexity = $O(n \log n)$
Space complexity = $O(n)$

\Leftarrow Fir K -times uss (PQ) me se elements ko remove karayengy toh humare paas K -largest element sethne hongy!
 \leftarrow Time complexity = $O(K \log n)$ \rightarrow no. of elements removed.
Space complexity = $O(n)$ \rightarrow remove() func

\therefore Overall Time complexity $\Rightarrow O(n \log n) + O(K \log n)$
 $\Rightarrow O((n+K) \log n) \Rightarrow O(n \log n)$

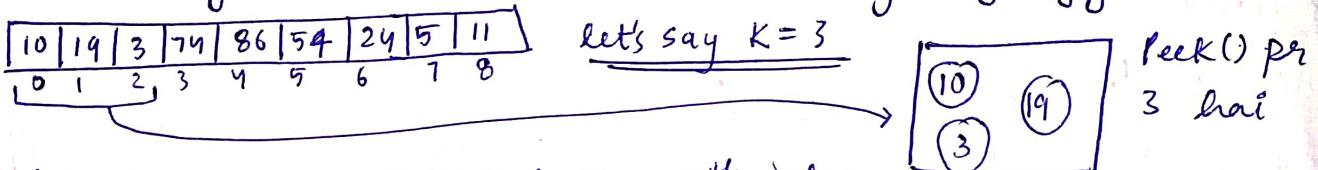
Overall Space complexity $\Rightarrow O(n)$

```
public static void main (String [] args) {
    Scanner sc = new Scanner (System.in);
    int n = sc.nextInt();
    int arr [] = new int [n];
    for (int i = 0; i < n; i++) {
        arr [i] = sc.nextInt();
    }
    int K = sc.nextInt();
```

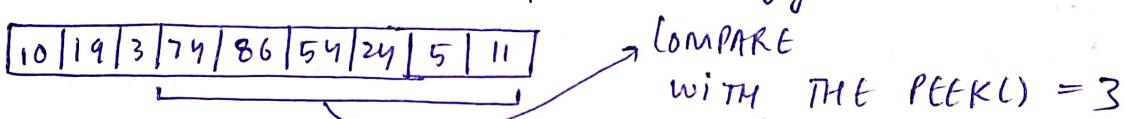
```
PriorityQueue < Integer > pq = new PriorityQueue < > (Collections.reverseOrder());
for (int val : arr) {
    pq.add (val);
}
for (int i = 0; i < K; i++) {
    int val = pq.peek();
    pq.remove();
    System.out.println (val);
```

APPROACH 2 Time Complexity $\rightarrow O(n \log n)$ Highest Rank
 Space Complexity $\rightarrow O(K)$ Priority Order

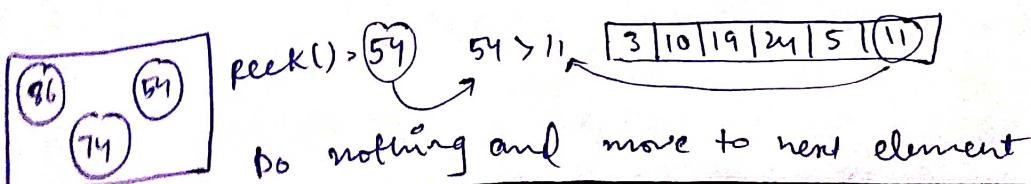
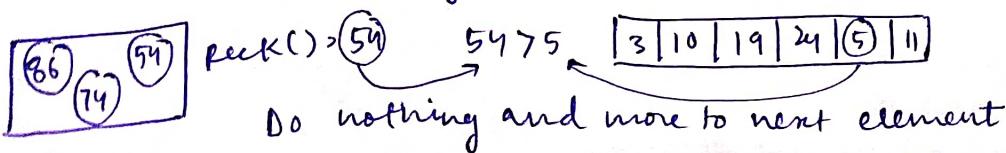
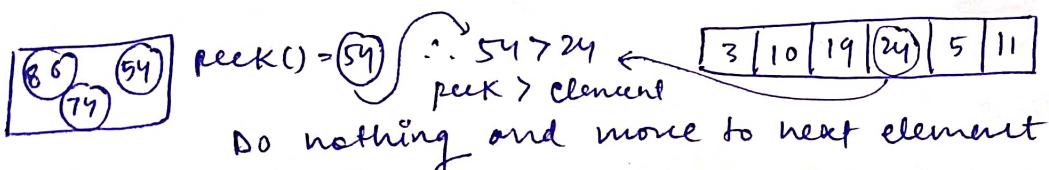
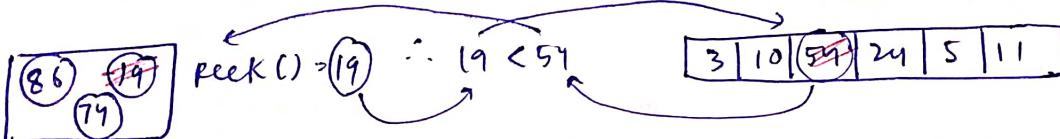
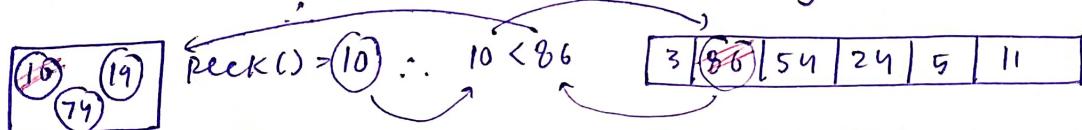
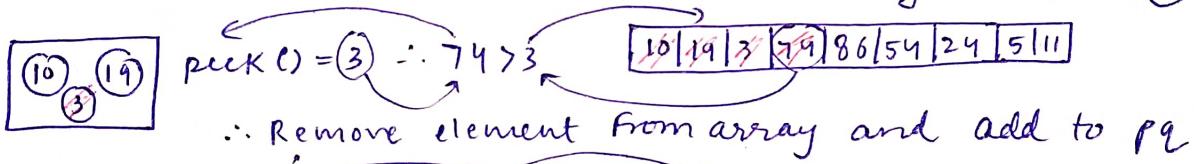
- = Hum (pq) barayengy where the priority is set as default.
- = (pq) me array ke K^{th} elements hi add krey jayengy.



- = Aab array par ek loop lagega K^{th} index wale element se array ke last element tak aur hum saare elements ko peek se compare kreyengy!



- = If the element in the array is less than peek(), then do nothing
- = But if the element in the array is greater than peek of (pq) then,
 - We will remove that element from (pq).
 - Add the element ~~from~~ in the array. & in the (pq)



Now we will print and remove K elements from the PQ.
We are left with 3 largest elements in PQ.

```
public static void main (String [] args) {
```

```
    Scanner sc = new Scanner (System.in);
```

```
    int n = sc.nextInt();
```

```
    int arr [] = new int [n];
```

```
    for (int i=0; i<n; i++) {
```

```
        arr[i] = sc.nextInt();
```

```
}
```

```
    int K = sc.nextInt();
```

```
PriorityQueue<Integer> pq = new PriorityQueue<>();
```

```
    for (int i=0; i<K; i++) {
```

```
        pq.add (arr[i]);
```

```
}
```

```
    for (int i=K; i<arr.length; i++) {
```

```
        int val = arr[i];
```

```
        if (val > pq.peek()) {
```

```
            pq.remove();
```

```
            pq.add (val);
```

```
}
```

```
4
```

```
    while (pq.size() > 0) {
```

```
        System.out.println (pq.peek());
```

```
        pq.remove();
```

```
3
```

```
2
```

MERGE K-SORTED LISTS

[LIST = ArrayList]

Hume k-sorted list given hogे, hume un k-sorted lists ko merge krke 1 sorted list banani hai.

$$TC \rightarrow O(n \log n) \quad SC \rightarrow O(k)$$

Approach 1

Phle saari list ke sabhi elements (PQ) me daal do aur unhe (PQ) se remove krke (AL) me daaldo.

Pn jaha space complexity bahut high hojayegi!

Approach 2

Hume k-sorted list given hai!

Hum (PQ) Banayegi aur usme har list ka phela element daaldengy aur is (PQ) me humne priority di hai smaller elements ko!

Toh humare pass (PQ) me k elements hai because of k no. of lists.

Now, we will remove the element with highest priority and add 1 element in the (PQ) (from the same ArrayList to which the remove element belong).

This will be done in loop unless the (PQ) becomes empty.

In this way we will get our sorted ArrayList and we will point the resultant ArrayList.

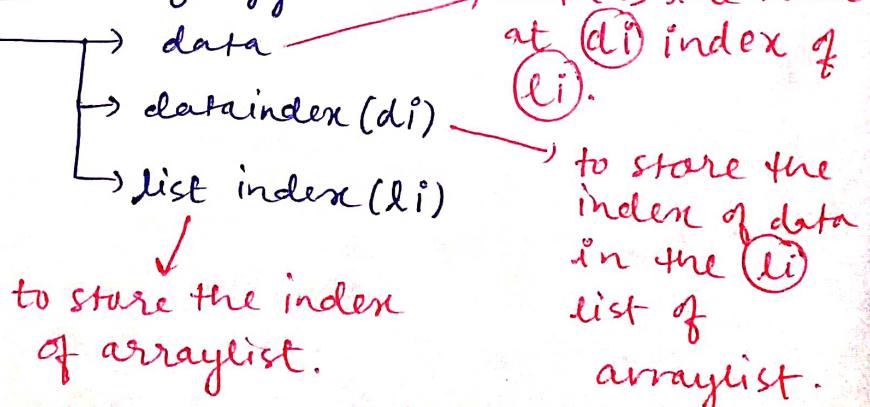
NOTE

Hume har element ke sath yeh track rakhna hai ki vo konsi ArrayList ke data hai aur kya vo ArrayList ka last index hai? (For resolving null pointer exception)

Inn sab baato ka track rakhna jaruri hai!

Issliye Hum ek Pair class Banayengy

Pair class consist of



APPROACH

① Hum ek Pair Class Banayengy!

li	di	0	1	2	3	4	5	6
0	0	10	20	30	40	50	60	
1	1	5	7	9	11	19	55	57
2	2	1	2	3				
3	3	32	39					

list index (li)

data index (di)

data

data index represent the index of data in the list index of arraylist

→ K list are provided in ArrayList. So list index will store the index of li(th) list of arraylist. And ∵ it helps us to keep track of the position in the arraylist.

② Hum ek Pair banayengy of Pair class (type), aur Pair me pair class ke objects dalengy, But Pair me hume essa data dalana hoga hai jiski priority Pair ko pata chal sakey!
∴ By default the smallest element is given more priority in Pair.

Now, Pair ko kaise pata chalega ki smallest pair konsa hai?
Toh hume compare kerna hai pair class ke objects ko,
Toh yeh kرنے ke liye hume pair class me comparable implement kerna hoga,
Taki pair class ka har object ka data dusre object ke data se hume compare kr paye!

static class Pair implements Comparable<Pair>

{
int li;
int di;
int data;

Agar hum kisi class me comparable implement krti hai toh waha compareTo function ana hi chahiye!

public int compareTo (Pair o)

o means other objects of class Pair

{
return this.data - o.data;

Agar yeh difference (+ve) mila toh this is Bigger!

Agar (-ve) mila toh this is smaller!

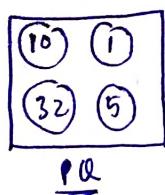
Agar 0 toh this and other are equal.

this.data - o.data → Highest Rank Priority

o.data - this.data → Highest Score Priority

Mtlab smaller elements / Pairs are give more Priority

③ So, first of all we will create a PQ. Assume har list ke First element ke liye Pair Banake PQ me dalengy!

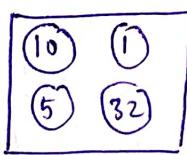


Peek() = 1

Toh humne har element ke liye Pair banaya where the list index will be the index of list to which the element belong.

④ Now, we will create a Resultant ArrayList, Ab hum PQ me ek element remove krenge aur ek new element PQ me dalengy (From the same list ~~to~~ to which element is removed)

DRY RUN



Peek() = 1

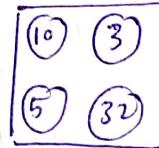
PQ

Resultant ArrayList (RA) = -



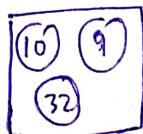
Peek() = 2

RA = 1



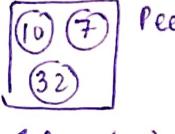
Peek() = 3

RA = 1 2



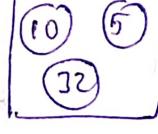
Peek = 9

RA = 1 2 3 5 7



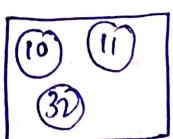
Peek = 7

RA = 1 2 3 5

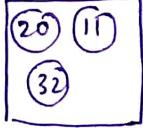


Peek() = 5

RA = 1 2 3



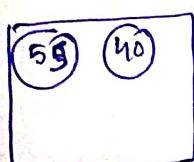
Peek() = 10
RA = 1 2 3 5 7 9



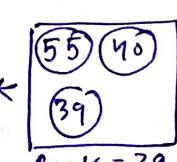
Peek = 11
RA = 1 2 3 5 7 9 10



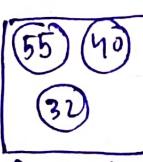
Peek = 19
RA = 1 2 3 5 7 9 10 11



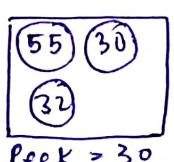
Peek > 40
RA = 1 2 3 5 7 9 10 11 19 20 30 32



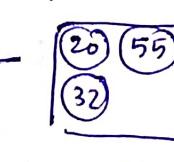
Peek = 39
RA = 1 2 3 5 7 9 10 11 19 20 30 32



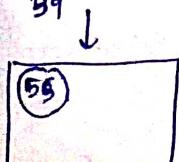
Peek > 32
RA = 1 2 3 5 7 9 10 11 19 20 30



Peek = 30
RA = 1 2 3 5 7 9 10 11 19 20



Peek = 20
RA = 1 2 3 5 7 9 10 11 19 20



Peek = 55

RA = 1 2 3 5 7 9 10 11 19 20 30 32 39 40



Peek = 57

RA = 1 2 3 5 7 9 10 11 19 20 30 32 39 40 55



PQ

∴ RA = 1 2 3 5 7 9 10 11 19
20 30 32 39 40
55 57

```
public class Pair implements Comparable {
```

```
    int data;
```

```
    int di;
```

```
    int li;
```

```
    public int compareTo(Pair o) {
```

```
        return this.data - o.data;
```

```
}
```

```
}
```

```
public static ArrayList<Integer> mergeKSortedLists(ArrayList<ArrayList<Integer>><lists>) {
```

```
    ArrayList<Integer> resultAL = new ArrayList<>();
```

```
    PriorityQueue<Pair> pq = new PriorityQueue<>();
```

```
    for (int li = 0; li < lists.size(); li++) {
```

```
        Pair p = new Pair();
```

```
        p.li = li;
```

```
        p.di = 0;
```

```
        p.data = list.get(li).get(0);
```

```
        pq.add(p);
```

```
}
```

```
    while (pq.size() > 0) {
```

```
        Pair removedPair = pq.peek();
```

```
        pq.remove();
```

```
        resultAL.add(removedPair.data);
```

```
        removedPair.dit++;
```

```
        if (removedPair.di < list.get(removedPair.li).size()) {
```

```
            removedPair.data = list.get(removedPair.li).get(removedPair.di);
```

```
            pq.add(removedPair);
```

```
}
```

```
}
```

```
return resultAL;
```

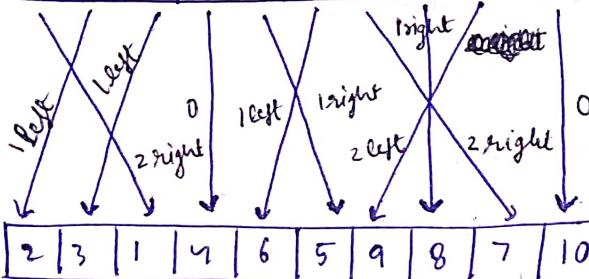
```
}
```

SORTED K-SORTED ARRAY

Hume ek array given hoga, aur ek integer K given hoga!

The integer K denotes that the array is a K-sorted array.

+2	-1	-1	0	+1	-1	+2	+1	-2	0
1	2	3	4	5	6	7	8	9	10



SORTED ARRAY

K-SORTED ARRAY

∴ Hume ek K-sorted array given hoga! K-sorted array me har element apni position se (0 to K) k-position left \nexists right par move ho sakte hai!

if $K=2 \rightarrow$ Har element ko 1 \nexists 2 position left \nexists right move kr sakte hai!

It is also possible that element does not move!

∴ We can only move 0/1/2 positions if $K=2$ smaller

APPROACH

- = Hum ek Pa banayengy of size $K+1$
- = Now, Hum ek element remove kengy (Pa) se $\xrightarrow{\text{Highest Rank Priority Order}}$
- = unless removed element ko print kradya!
- Aab Humare pass K elements hai (Pa) me!
- So, we insert next element in the (Pa) and size again becomes $K+1$, we keep on doing this unless (Pa) becomes empty, we keep on removing 1 of the element from (Pa) and adding the next element of the array (unless we have no next element in the array to be added in the (Pa)).
- If the array is completely visited & some elements are left in the (Pa), we empty the (Pa) completely and print the removed element, and then this procedure stops here.

DRY RUN

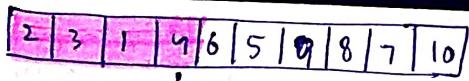
2	3	1	4	6	5	9	8	7	10
---	---	---	---	---	---	---	---	---	----

Added $K+1$ elements in (Pa)

$\text{peek}() = 1$

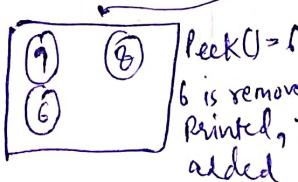
$\therefore 1$ is removed & printed
and next element 4 is added in (Pa)

①

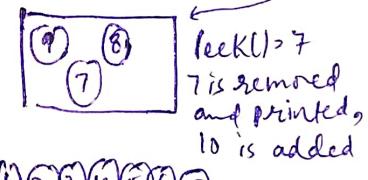


`peek() = 9`
2 is removed and printed,
next element 6 is added

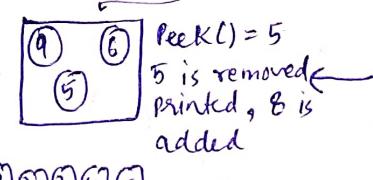
① ②



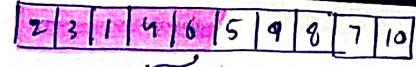
① ② ③ ④ ⑤ ⑥



① ② ③ ④ ⑤ ⑥ ⑦

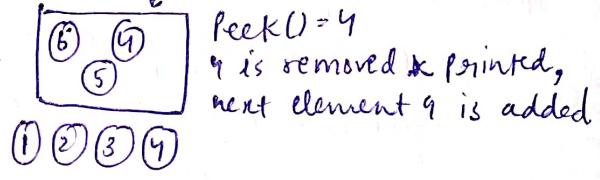


① ② ③ ④ ⑤ ⑥

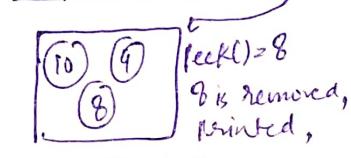
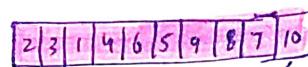


`peek() = 3`
3 is removed and printed, next element 5 is added

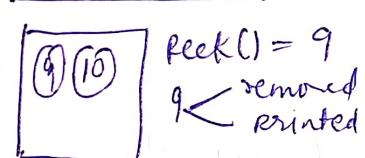
① ② ③



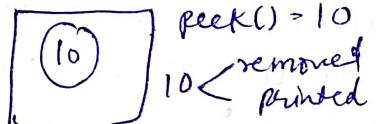
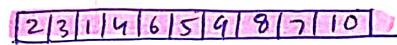
① ② ③ ④



① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨



① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨



`peek() = 10`

10 removed, printed

`public static void main (String [] args) {`

`Scanner sc = new Scanner (System.in);`

`int n = sc.nextInt();`

`int arr [] = new int [n];`

`for (int i=0; i<n; i++) {`

`arr[i] = sc.nextInt();`

`}`

`int K = sc.nextInt();` → K ki value input li

`PriorityQueue <Integer> pq = new PriorityQueue <>();` → EK Priority Queue Banai

`for (int i=0; i<=K; i++) {`

`pq.add (arr[i]);`

`}`

Humne K-sorted array
input liye

array ke
K+1 elements
pq me dale!

```

for (int i = k+1; i < arr.length; i++) {
    int val = pq.peek(); → peek kro jo
    System.out.println(val); → print kro
    pq.remove(); → remove kro
    pq.add(arr[i]); → next element
    add kro!
}

```

Jab tak array ke kache huye elements (pq) me na daal jaye tab tak loop chalga

```

while (pq.size() > 0) { → Agar (pq) me ab bhi kuch elements
    int val = pq.peek(); → bache hai toh print kardo aur
    System.out.println(val); → unhe (pq) me se remove
    pq.remove(); → kardo!
}

```

Time Complexity

$$O(n) + O(\log k)$$

this is because we are traversing the entire array

removing the elements from (pq) since the size of (pq) is $O(k)$

$$O(n \log k)$$

Space Complexity = $O(k)$

(Q) MEDIAN PRIORITY QUEUE

Hume apni ek (PQ) Banani hai yeh normal (PQ) nahi hai yeh
hai MEDIAN PRIORITY QUEUE.

Iss (PQ) me MEDIAN Ko sabse jyda priority milogi!

Har baar remaining elements ka median hi return krenge!

10	20	30	40	50
----	----	----	----	----

Normal (PQ)

(smaller priority)

peek() → 10

remove() → 10

Normal (PQ)

(larger priority)

peek() → 50

Remove() → 50

Median (PQ)

(median priority)

peek() → 30

remove() → 30

30 is median
of all elements
in (PQ).

APPROACH

① Median Priority Queue

∴ left (PQ) right (PQ)
 n n left
 peek $\begin{bmatrix} n \\ n+1 \\ n \end{bmatrix}$ n left
 n+1 n+1 right

Max Priority Queue

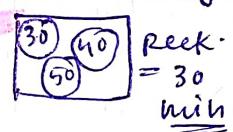
left (PQ) stores the first (smaller)
half of queue



peek = 20
max

Min Priority Queue

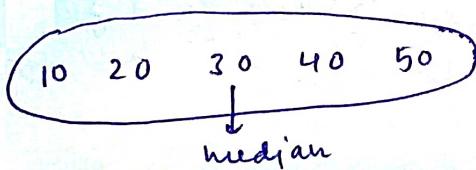
right (PQ) stores the greater half
of the element.



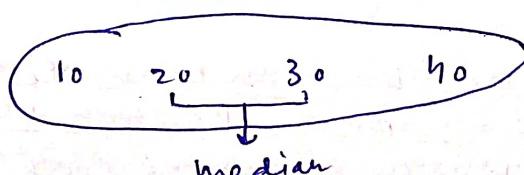
min

⇒ If the median queue has even no. of element i.e. If both left (PQ) & right (PQ) has equal size. left (PQ) me se element remove hogा and that element will be printed as a median.

⇒ If there are odd number of elements in the (PQ) if the left priority /right priority queue has n+1 elements & the other priority queue right/left (PQ) has n elements, then in this case, the (PQ) with n+1 element will remove an element.

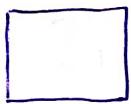


odd no. of elements in
a median Priority
Queue

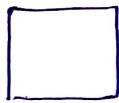


Even no. of elements in a
median priority
Queue

DRY RUN



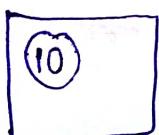
peek() = -



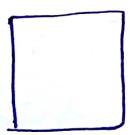
peekL() = -

∴ Our (MPQ) is empty
(Initially)

∴ Add(10)

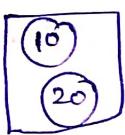


peek() = 10

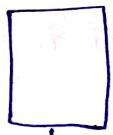


peek() = -

Add(20)



peekL() = 20



peekL() By default,
= - element is
inserted in
left PQ.

By Default, an element
is inserted in the left
PQ.

Rule 1



peekL() = 10



peek = 20

Now size of left and right PQ
is equal.

Rule 2

But, if the difference of size of left and
right PQ should be 1.

∴ But here difference becomes 2. So,
remove 1 element from PQ having
more element & put it in another.

RULE 3

when the element being added
is greater than peek() of right
PQ, then the element will get
inserted in right PQ.

element > right.peek() → inserted
in right PQ

when the element being added is
smaller than the peek() of left PQ
then the element will be inserted
in left PQ.

element < left.peek() → inserted
in left PQ.

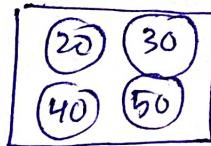
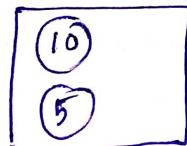
After inserting we need to check whether the left and right PQ
is balanced.

If size difference is ~~greater~~ or greater than 1 then use

RULE 2

If the [element < right.peek()] & [element > left.peek()] both by default,
use element to left PQ we add lenqy! Then we will check if
the PQ has [size difference < -1].

Add(30) \rightarrow 30 > right.peek() \rightarrow inserted in right PQ
 Add(5) \rightarrow 5 < left.peek() \rightarrow inserted in left PQ
 Add(40) \rightarrow 40 > right.peek() \rightarrow inserted in right PQ



peek() = 10
(Max. PQ)

peek() = 20
(Min. PQ)

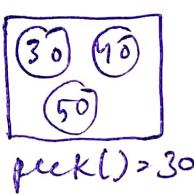
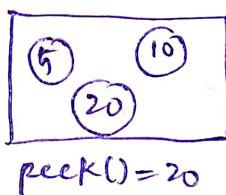
Add(50) \rightarrow 50 > right.peek() \rightarrow inserted in right PQ.

Remove one element from RPQ
 and add to LPQ.

USE
RULE 2

There isn't
 balance in
 size

size diff. = 2



MedianPQ.remove()

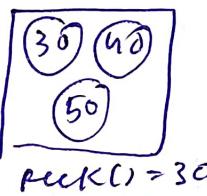
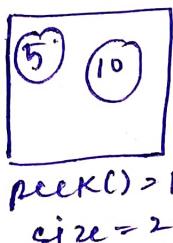
Now,

MedianPQ.peek()

20 \rightarrow WHY?

The median is the peek of PQ with more elements in total. But if, in total there are even no. of elements, then median is the peek of left PQ.

equal no. of element in left PQ and right PQ and even no. of elements in total, we will remove the element from left PQ.



size = 2

size = 3

5 elements in Total

\therefore when the size is Odd (when size of left PQ and right PQ is unequal)

then remove the element from PQ having more elements.

right PQ > left PQ
 size size

Remove element
 from right PQ

Order of Removal of element from median PQ's.

$20 \rightarrow 30 \rightarrow 10 \rightarrow 40 \rightarrow 5 \rightarrow 50$

In this question, we have to write following functions

- 1) Add() $\rightarrow O(\log n)$
- 2) Peek() $\rightarrow O(\log n)$
- 3) Remove() $\rightarrow O(1)$
- 4) size() $\rightarrow O(1)$

Similar to normal PQ

Space complexity $\rightarrow O(1)$

public static class MedianPriorityQueue

```
PriorityQueue<Integer> left; → yeh left PQ banaya (Max Priority)
PriorityQueue<Integer> right; → yeh right PQ banaya (Min Priority)
public MedianPriorityQueue() → constructor of median PQ
    { left = new PriorityQueue<>(Collections.reverseOrder()); → left PQ
      right = new PriorityQueue<>(); → right PQ (min) (max)
        add func of median PQ
    public void add (int val)
        if (right.size() > 0 && val > right.peek())
            right.add (val);
        else
            left.add (val);
            handleCap();
        }
    private void handleCap()
        if (left.size() - right.size() == 2)
            int val = left.remove();
            right.add (val)
        else if (right.size() - left.size() == 2)
            int val = right.remove();
            left.add (val);
        }
    public int remove()
        if (this.size() == 0)
            System.out.println ("Underflow");
            return -1;
        if (left.size() >= right.size())
            return left.remove();
        else
            return right.remove();
        }
```

Agar left aur right PQ ka size diff.
1 se jyada hua toh hum balance
kerna padega!

```

public int peek()
{
    if (this.size() == 0)
    {
        System.out.println("Underflow");
        return -1;
    }
    if (left.size() >= right.size())
    {
        return left.peek();
    }
    else
    {
        return right.peek();
    }
}

public int size()
{
    return left.size() + right.size();
}

public static void main (String [] args)
{
    BufferedReader br = new BufferedReader (new InputStreamReader
                                         (System.in));
    MedianPriorityQueue queue = new MedianPriorityQueue(); Humne median PQ class ka ek object banaya
    String str = br.readLine();
    while (str.equals("quit") == false)
    {
        if (str.startsWith("add"))
        {
            int val = Integer.parseInt (str.split (" ") [1]);
            queue.add (val); Object pe add func call kiya
        }
        else if (str.startsWith("remove"))
        {
            int val = queue.remove();
            if (val != -1)
            {
                System.out.println (val);
            }
        }
        else if (str.startsWith("peek"))
        {
            int val = queue.remove();
            if (val != -1)
            {
                System.out.println (val);
            }
        }
    }
}

```

else if (str.startsWith ("size"))

{

 System.out.println (queue.size ());

}

str = br.readLine ();

}

}

PRIORITY QUEUE USING HEAP

Hume apni kudki
 PQ class banani
 hai which will
 have following

- = add()
- = peek()
- = remove()
- = size()

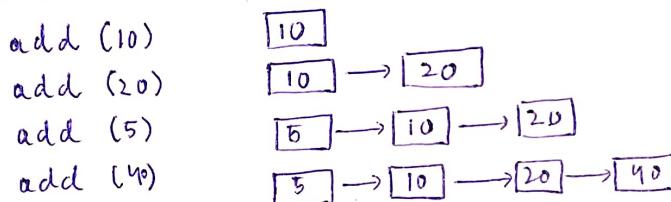
Heap is a
 Data Structure
 which is based
 on BINARY TREE

(Priority Queue ek class
 hai, jo Heap Data
 structure use karke
 Banani gayi hai)

Priority Queue Banane ke liye humare
 pass 3 Tarike hai!

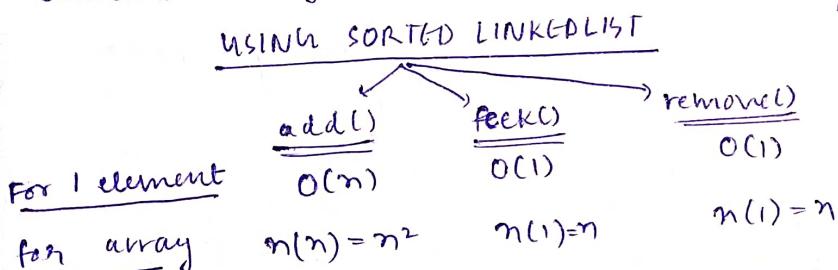
WAY 1 Priority Queue using a Sorted Linked List

works but the time complexity is not
 good.



n^2 time chalga loop array ke sabhi
 elements ke liye! (add ke liye)

add function: me hume puri
 linked list ko travel krna pad raha
 hai tab jake correct position pe add
 hoga $\rightarrow O(n)$ $\rightarrow O(1)$
 peek() gives us the smallest element
 by default. linkedlist is
 sorted. \therefore smallest element
 is head of linkedlist
 remove() returns and remove the smallest
 element of linkedlist.

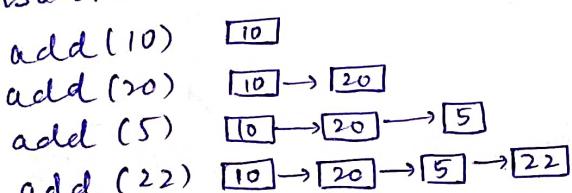


NOTE

Hume,
 add() $\rightarrow O(\log n)$ Change
 remove() $\rightarrow O(1)$ hume
 peek() $\rightarrow O(1)$ yah

WAY 2 USING UNSORTED LINKED LIST

Elements ko randomly tail pe add krya chalo, toh humare paas
 unsorted linkedlist banti jayegi!



add(): Hume bs TAIL per next element ko
 add krna hogya and that element will be
 the next Tail. $\therefore O(1)$

remove()
 In PQ, we remove the smallest element, because the priority is given to
 the smallest by default,
 lekin humare linkedlist unsorted hai, toh smallest remove krne ke liye
 hume puri linkedlist ko travel krna hogya! $\rightarrow O(n)$

peek()
 Similar to remove() function:
 $O(n)$

USING UNSORTED LINKEDLIST

add \downarrow remove \downarrow peek \downarrow
 $O(1)$ $O(n)$ $O(n)$

n time me add $\rightarrow n(1) \rightarrow n$
 n time me remove $\rightarrow n(n) \rightarrow n^2$
 [for array ke sabhi elements ke liye]

Here also time complexity are not the desired one.

WAY 3 USING ARRAYLIST LIKE HEAP DATA STRUCTURE

Isse use kme se,

(PQ) me \leftarrow add() $\rightarrow O(\log n)$] For Single Element
 remove() $\rightarrow O(\log n)$
 peek() $\rightarrow O(1)$

= pure array ~~me~~ ko (PQ) me add krne ke liye TC
 $= O(n \text{ element} \times \log n)$ TC of 1 element

- pure array ke sabhi element ko (PQ) me se remove krne ke liye TC $\rightarrow O(n \log n)$
- pure array ke sabhi elements ke liye peek() ki TC
 $= n \times 1 = O(n)$

WHAT IS HEAP ? Hum Heap ka use kya karey hai !

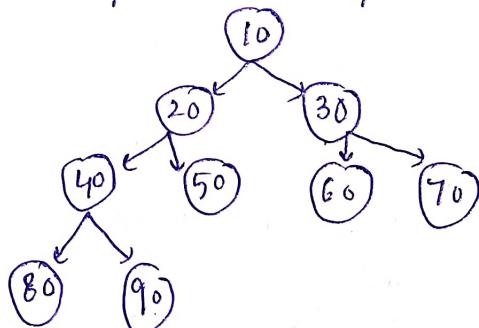
Heap is a Binary Tree having 2 Special Properties !

- * Complete Binary Tree (CBT)
- * Heap Order Property (HOP)

Hum ArrayList ko Heap ki

graph use kya karey hai !

Taki \leftarrow add $\rightarrow \log(n)$
 remove $\rightarrow \log(n)$] hojaye !
 peek $\rightarrow O(1)$



(hamesha)

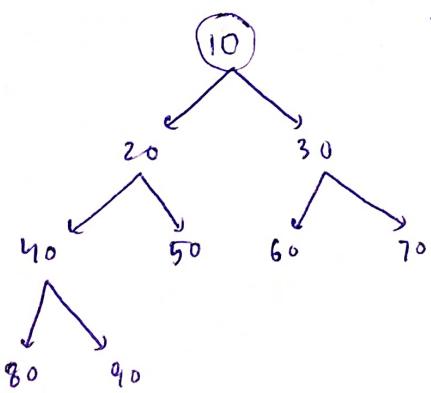
Heap Order Property

parent ki priority dono children se kadi hoti hai !
 parent ki value hamesha children ki value se] \leftarrow mat lab
 choti hogi

left aur right ki priority me koi relation nahi
 hai koi bhi bada losakta hai !
 And to be specific the priority of any child is not
 pre-decided. This property helps to achieve the TC of peek() = O(1)

Hume Heap Order Property use kar kri?

peek() \rightarrow T.C = $O(1)$ \rightarrow Kuki Hume bas ROOT return krna hogea kuki parent uske dono children se jyda priority hogya!



this tree is a Binary Tree (every node has 2 child)
this tree follows Heap Order Property kuki har parent node ki priority uske children se jyda hai

HOW?

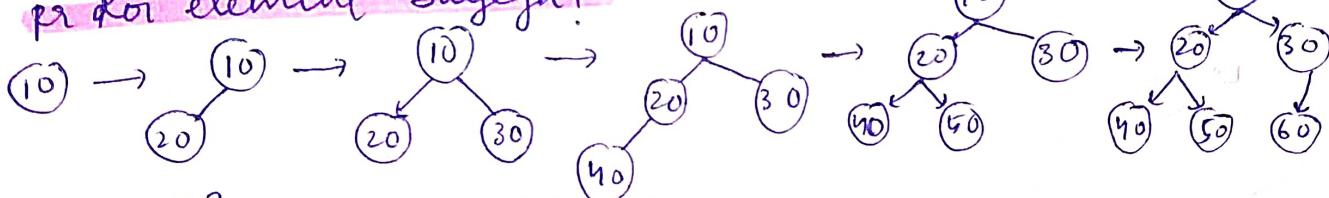
- = Toh sabse jyada priority hogi Root node ki!
- = So peek() func will simply return root.
- \therefore T.C of peek() $\rightarrow O(1)$ due to HOP.

(*) COMPLETE BINARY TREE

Let suppose the height of the tree is h , then according to this property atleast $(h-1)$ levels should be completely filled, and the last (h^{th}) level should be filled from left to right.

= Har Parent ka right child attach karne se phle left child attach karna hogta!

= Phle wale level ko pura fill karay ke bad hi next level par koi element jayega!

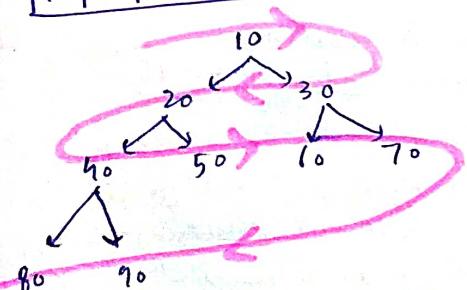


WHY CBT?

add()
remove()

\rightarrow T.C = $O(\log n)$ \rightarrow KESÉ?
ek array / ArrayList se represent krsaktey hai

0	1	2	3	4	5	6	7	8
10	20	30	40	50	60	70	80	90

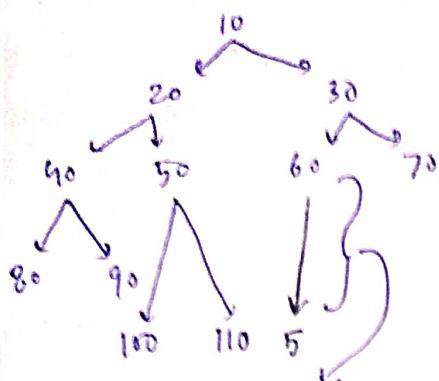


iss ArrayList ko tree ki form me bana dia!

Agar ArrayList me element sarey jayengy toh tree me left to right vo element lagaty jayengy aur jab yeh level full ho jayega toh next level me left to right yeh element lagaty jayengy!

So, this CBT is our Priority Queue. This CBT is actually a ~~arraylist~~ behind the scene.

This arraylist also follows the HOP!



peek(): peek() gives the root $\therefore O(1)$
Root \rightarrow list.get(0); $\rightarrow 10$

add(): add() func will add the data in the end of arraylist.

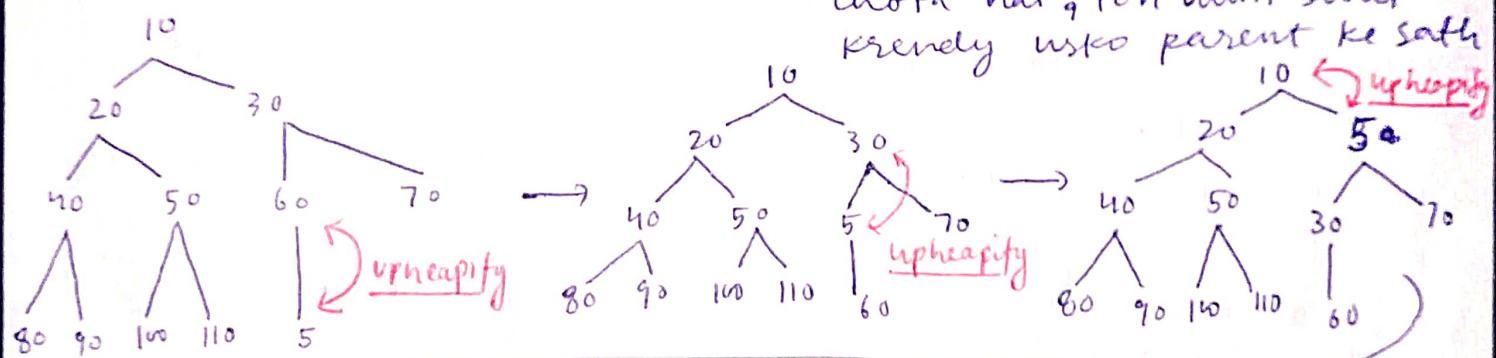
[10 20 30 40 50 60 70 80 90 100 110 5]
--

5 is added here!

Aab hum UPHEAPIFY() func ka use krengy aur 5 ko uske parent se swap krengy yeh tab tak krengy jab tak 5 chota rahega apne parents.

5 is added here
UPHEAPIFY()

node agar uske parent se chota hai, toh hum swap krengy usko parent ke sath

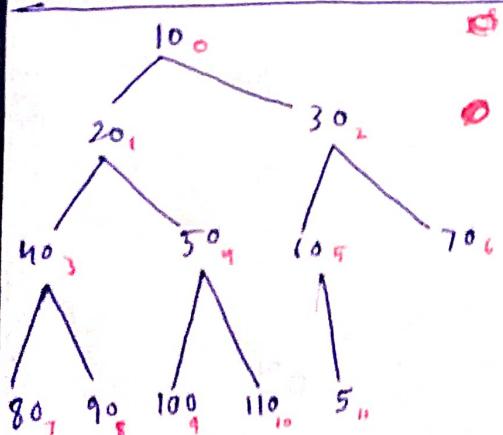


\therefore we have upheapified 3 times (loop 3 baar chalega!)

$$\text{height} = \text{no. of edges} = 3$$

height ki $T.C = O(\log n)$ hoti hai

inta time Lagega upheapify ke loop me!



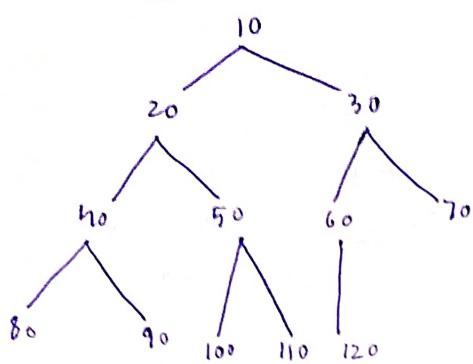
2° ArrayList se tree banane ke Benefits?

Hum har node se uska Parent index find kr sakte hai!

= Hume konse spot pe 5 add karna hai
yeh arraylist se pata chalega ki 11 index pe karna hai!

= Lekin, Agar hum Tree use kry CBT banane ke liye, toh hum pura Euler Tree Traverse krengy aur pata chalega ki 60 ko child hai 5.

remove() → Humne highest priority ko remove karna hai!

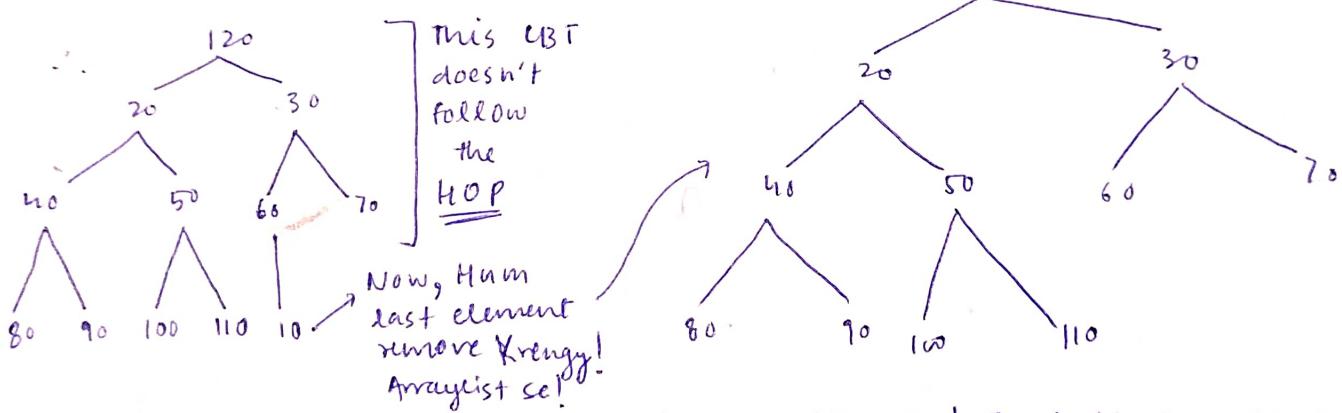
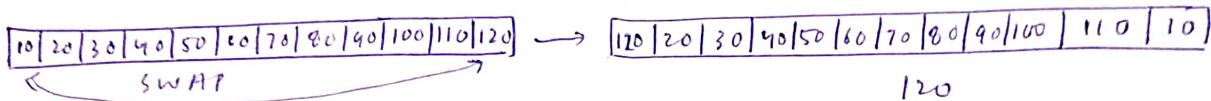


0	1	2	3	4	5	6	7	8	9	10	11
10	20	30	40	50	60	70	80	90	100	110	120

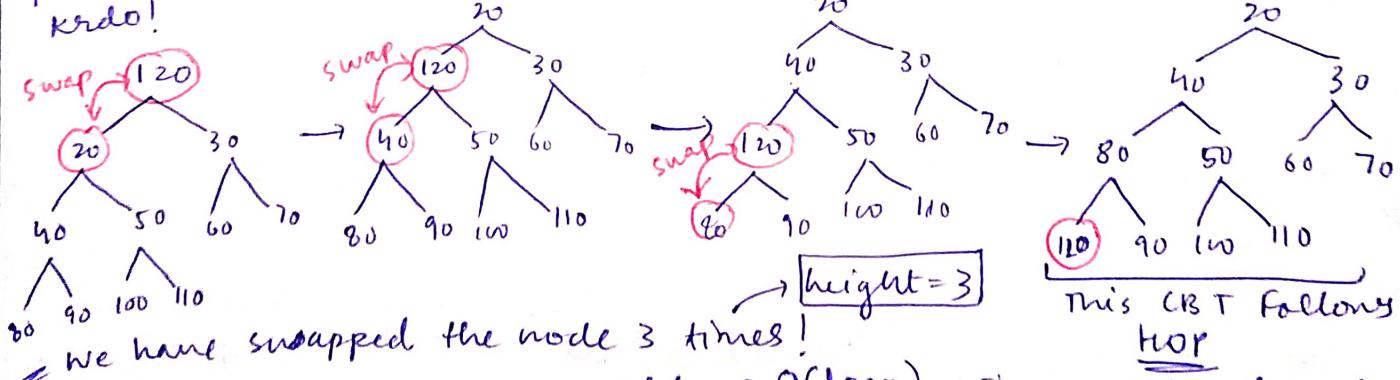
ArrayList me smallest element ko remove karna hai!

0th index wala element remove kرنے ke liye arraylist ki [T.C → O(n)] hoti hai Kuki sabhi elements ko 1 index aage shift kरna padega!

Toh sabse phle ArrayList ke 1st aur last element ko swap krenge



Aab Hum DOWNHEAPIFY() function use krenge! Root ko compare krenge left, right child ke sath aur agar kisi node ki value parent node se ~~greater~~ ^{smaller} hai toh uss child se parent ko swap krdo!



PRIORITY QUEUE
USING
ARRAYLIST AS A HEAP

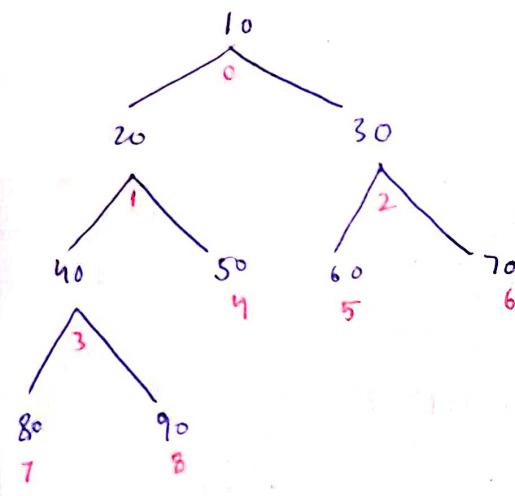
add → $O(\log n)$ → First add the element in arraylist, then upheapify

remove → $O(\log n)$ → first swap first, last element of arraylist, remove the last, and now downheapify.

peek → $O(1)$

Just return the first element of ArrayList

IMPLEMENTATION



Data structure used for storage by heap is ArrayList.

FORMULAS

$$\text{left child} = 2[\text{Parent Index}] + 1$$

$$\text{right child} = 2[\text{Parent Index}] + 2$$

parent

left child

right child

0

1

2

1

2

3

$$2 \times 0 + 1 = 1$$

$$2 \times 0 + 2 = 2$$

$$2 \times 1 + 1 = 2$$

$$2 \times 1 + 2 = 3$$

For left child $\rightarrow \frac{2-1}{2} = \frac{1}{2} \approx 1$

for right child $\rightarrow \frac{3-1}{2} = \frac{2}{2} = 1$

CODE

```

public static class PriorityQueue {
    ArrayList<Integer> data;
    public PriorityQueue() {
        data = new ArrayList<>();
    }
    public void add(int val) {
        data.add(val);
        upheapify(data.size() - 1);
    }
    void upheapify(int i) {
        if (i == 0) {
            return;
        }
        int pi = (i - 1) / 2;
        if (data.get(pi) > data.get(i)) {
            swap(pi, i);
            upheapify(pi);
        }
    }
}
  
```

Humne ek ArrayList ko declare kرا
Constructor of Priority Queue Class
data = new ArrayList<>(); → data ArrayList ko initialized kرا
as arraylist works as a heap
add function
adding data at the last of arraylist
upheapify(data.size() - 1); → upheapify the data at the last of the arraylist
upheapify function
parent index
find kرا
Agar parent index ki value jyada hai toh swap kardo
aur fir recursive call lagado!

```
public int remove() { → remove function
    if (data.size() == 0) {
        System.out.println("Underflow");
        return -1;
    } → phle AL ke 1st aur last element swap kro!
    swap(0, data.size() - 1); → fir last element ko remove kardo!
    int val = data.remove(data.size() - 1);
    downheapify(0); → fir 1st element pe downheapify call kardo!
    return val;
}
```

```
void downheapify(int i) { → downheapify function
    int mini = i; → mini ko parent index dia!
    int lci = 2 * i + 1;
    int rci = 2 * i + 2;
    if (lci < data.size() && data.get(lci) < data.get(mini))
        mini = lci; Agar kisi bhi child ki value parent index se
    } → kam hai toh parent index ko uska child banardo
    if (rci < data.size() && data.get(rci) < data.get(mini))
        mini = rci;
    } → Agar mini aur parent index same nahi
    if (mini != i) { → hai toh matlab (pi) ki value change hui
        swap(mini, i); → diai, aur hum recursive call lagani
        downheapify(mini); → diai!
    }
}
```

```
public void swap(int i, int j) {
    int ith = data.get(i);
    int jth = data.get(j);
    data.set(i, jth);
    data.set(j, ith);
}
```

```
public int peek() {
    if (data.size() == 0) {
        System.out.println("Underflow");
        return -1;
    }
    return data.get(0);
}
```

```
public int size() { return data.size(); }
```

```
public static void main (String [] args) {
    BufferedReader br = new BufferedReader (new InputStreamReader
        (System.in));
    PriorityQueue qu = new PriorityQueue ();
    String str = br.readLine();
    while (str.equals ("quit") == false) {
        if (str.startsWith ("add")) {
            int val = Integer.parseInt (str.split (" ")[1]);
            qu.add (val);
        }
        else if (str.startsWith ("remove")) {
            int val = queue.remove ();
            if (val != -1) {
                System.out.println (val);
            }
        }
        else if (str.startsWith ("peek")) {
            int val = queue.peek ();
            if (val != -1) {
                System.out.println (val);
            }
        }
        else if (str.startsWith ("size")) {
            System.out.println (qu.size ());
        }
        str = br.readLine();
    }
}
```

Efficient Heap CONSTRUCTOR

```
public MyPriorityQueue (int []arr) {
    data = new ArrayList<>();
    for (int val : arr) {
        add (val);
    }
}
```

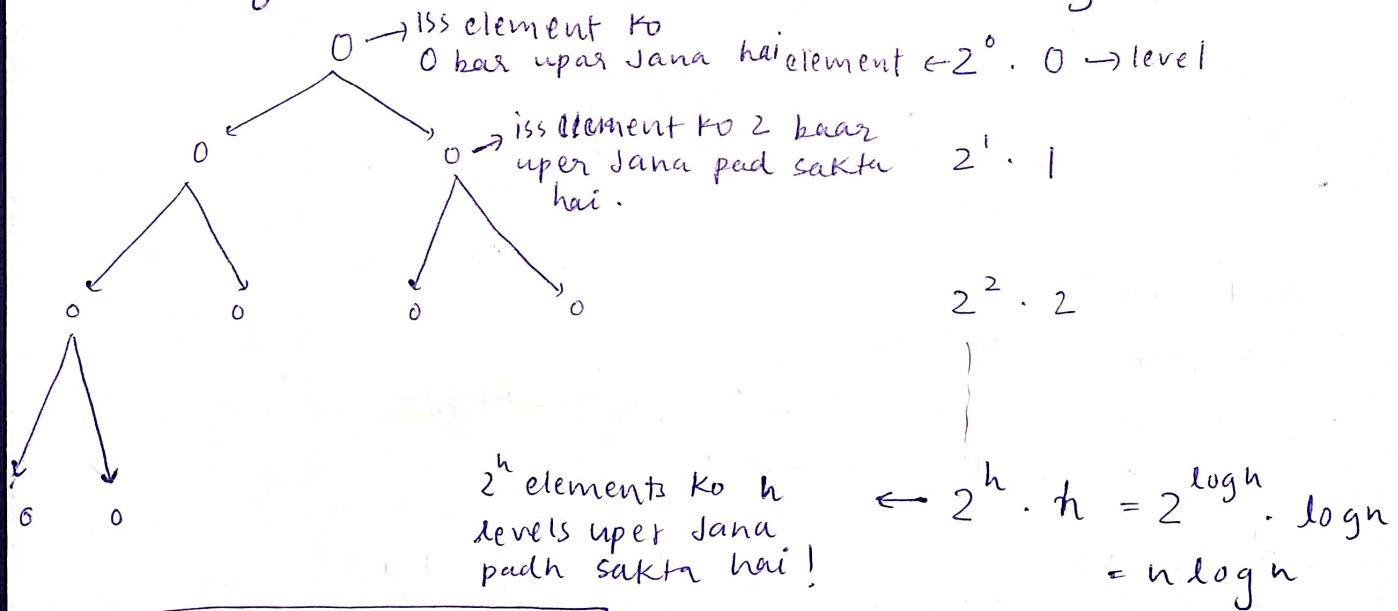
Jo Heap constructor humare pass tha ! usme agar humari array me n elements given hai, toh PQ me T.C = $O(n \log n)$ hai.

Toh array ke sabhi elements par for loop lagake agar hum PQ me add krya hai toh,

for loop ki T.C = $O(n)$

1 element ki PQ me add ki T.C = $O(\log n)$

\therefore T.C of add n elements in PQ = $O(n \log n)$



$$\boxed{n = 2^0 + 2^1 + 2^2 + \dots + 2^h} \rightarrow \text{No. of Total terms} = h+1$$

$$\therefore \text{sum} = \frac{a(r^n - 1)}{r - 1} = \frac{2^0 (2^{h+1} - 1)}{2 - 1}$$

$$n = \frac{1 (2^{h+1} - 1)}{1} = \frac{2^{h+1} - 1}{1} \Rightarrow n = 2^{h+1} - 1 \Rightarrow n+1 = 2^{h+1}$$

taking log both side

$$h+1 = \log_2(n+1) \Rightarrow h = \log_2(n+1)+1 \Rightarrow \boxed{h \approx \log n} \text{ Hence proved}$$

$$a = 2^1 \\ a = 1 = 2^0 \\ n = h+1$$

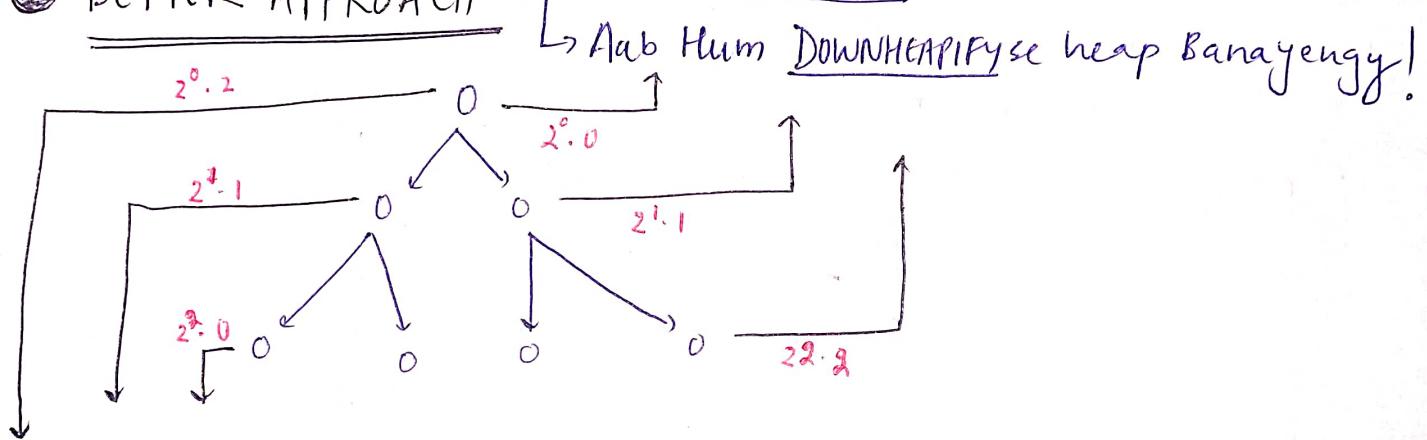
$T.C = \underbrace{2^0 \cdot 0 + 2^1 \cdot 1 + 2^2 \cdot 2 + \dots + 2^h \cdot h}_{\text{IGNORED}}$ \rightarrow $T.C$ to add n element in PQ and then upheapify.

$$= \underbrace{2^0 \cdot 0 + 2^1 \cdot 1 + 2^2 \cdot 2 + \dots}_{\text{IGNORED}} \underbrace{2^h \cdot h}_{\star} \rightarrow 2^h \cdot h = 2^{\log n} \cdot \log n$$

$$\therefore T.C = \underbrace{2^{\log n}}_n \cdot \underbrace{\log n}_{\log n} = n \log n$$

• Sabse jyada elements last level pe hongy (2^h) toh sabse jyada kaam bhi (upheapify) hume last level pe kerna hogya!

② BETTER APPROACH \rightarrow Hum UPHEAPIFY se heap nahi Banayengy



$$2^0 \cdot h + 2^1 \cdot h + \dots + 2^h \cdot h = T(n) \quad (1)$$

multiplying both sides by 2

$$2^1(h) + 2^2(h-1) + \dots + 2^{h+1}(0) = 2T(n) \quad (2)$$

subtract (2) from (1)

$$-2^h - 2^1(h-1) - \dots - 2^1 = -T(n)$$

$$T(n) = 2^h + 2^{h-1} + 2^{h-2} + \dots + 2^1 - 2^0(h) = \frac{2(2^h - 1)}{1} = h$$

$$\therefore T(n) = 2n - 2 - \log n$$

$$\boxed{T(n) \propto n}$$

phle sabhi elements ko PQ me add kro aur fir,

$(\frac{n}{2} - 1)$ index se (0) index tak downheapify function call kedo!

```
public MinPriorityQueue<int> arr)
{
    data = new ArrayList<>();
}
```

```
for (int val : arr)
{
    data.add(val);
}

for (int i = data.size() / 2 - 1; i >= 0; i--)
{
    downHeapify(i);
}
```

Now the $T \cdot C \cdot O$ add all elements of array in PQ will be $O(n)$.