

## ② INTRODUCTION TO 2D-ARRAY

Code View

```

P C M {
    P S V M(S[J] a) {
        int [] arr = new int[3][4];
        arr[0][0] = 11;
        arr[0][1] = 12;
        arr[0][2] = 13;
        arr[0][3] = 14;
        arr[1][0] = 21;
        arr[1][1] = 22;
        arr[1][2] = 23;
        arr[1][3] = 24;
        arr[2][0] = 31;
        arr[2][1] = 32;
        arr[2][2] = 33;
        arr[2][3] = 34;
    }
}
    
```

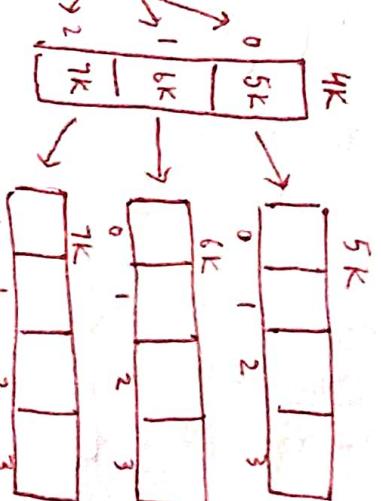
Abstract View

0	1	2	3
11	12	13	14
21	22	23	24
31	32	33	34

0	1	2	3
5K	5K	5K	5K
6K	6K	6K	6K
7K	7K	7K	7K

NO. OF ROWS = arr.length  
NO. OF COLUMNS = arr[0].length

Memory View



```

scanned s = new Scanner
int n = s.nextInt();
int m = s.nextInt();
int arr = new int[n][m];
for (int i = 0; i < arr.length; i++) {
    for (int j = 0; j < arr[i].length; j++) {
        arr[i][j] = s.nextInt();
    }
}
    
```

Code for  
2D ARRAY Demo

QUESTION

3

## MATRIX MULTIPLICATION

$$\begin{array}{c}
 \begin{array}{|c|c|c|} \hline 0 & 1 & 2 \\ \hline a_{00} & a_{01} & a_{02} \\ \hline a_{10} & a_{11} & a_{12} \\ \hline \end{array} \times \begin{array}{|c|c|c|c|} \hline 0 & 1 & 2 & 3 \\ \hline b_{00} & b_{01} & b_{02} & b_{03} \\ \hline b_{10} & b_{11} & b_{12} & b_{13} \\ \hline b_{20} & b_{21} & b_{22} & b_{23} \\ \hline \end{array} = \begin{array}{|c|c|c|c|} \hline 0 & 1 & 2 & 3 \\ \hline p_{00} & p_{01} & p_{02} & p_{03} \\ \hline p_{10} & p_{11} & p_{12} & p_{13} \\ \hline \end{array} \\
 \text{A } (2 \times 3) \quad \text{SAMT} \quad \text{B } (3 \times 4) \quad \text{P } (2 \times 4)
 \end{array}$$

$$P_{ij} = a_{i0} b_{0j} + a_{i1} b_{1j} + \dots + a_{i(n-1)} b_{(n-1)j}$$

$$= \sum_{k=0}^{n-1} a_{ik} b_{kj}$$

$$\therefore P_{01} = a_{00} * b_{01} + a_{01} * b_{11} + a_{02} * b_{21}$$

= EK SPOT FILL KRNE KE LIYE 1<sup>ST</sup> MATRIX KI ROW.

JO ISS SPOT KI ROW HAI WOH REHTI HAI 1<sup>ST</sup> MATRIX KI ROW.

JO ISS SPOT KA COLUMN HAI WOH REHTA HAI 2<sup>ND</sup> MATRIX KA COLUMN.

ISSME COLUMNS CHANGE HOTY HAT!

ISSME ROWS CHANGE HOTI HAI!

= (a) me ROW SAME HAI ; COLUMNS CHANGE HUYA!

= (b) me ROW CHANGE HUI ; COLUMNS SAME RAHEY!

### APPROACH

- (1) PHELE 1<sup>ST</sup> MATRIX KA INPUT LOO... → [row, column, array]
- (2) FIR 2<sup>ND</sup> MATRIX KA INPUT LOO... → [row, column, array]
- (3) CONDITION FOR INVALID INPUT →  $\rightarrow G1 != 82$
- (4) NOW, PRODUCT KI MATRIX BANEGI! →  $\rightarrow int[ ][ ] prod = new int[m][n]$
- (5) LOOP CHALEGA PRODUCT MATRIX PE!
  - PHELA LOOP → matrix banake print krne ke liye!
  - DUSRA LOOP → print krne ke liye!

INPUT ARRAYS IN 2D-ARRAY  
 P S V M(S[]a) {  
 Scanner s = new Scanner (System.in);  
 int r1 = s.nextInt(); → ROW  
 int c1 = s.nextInt(); → COLUMN  
 int [][] arr1 = new int [r1][c1];  
 for(int i=0; i < r1; i++) {  
 for(int j=0; j < c1; j++) {  
 arr1[i][j] = s.nextInt();
 }
 }  
 int r2 = s.nextInt(); → ROW  
 int c2 = s.nextInt(); → COLUMN  
 int [][] arr2 = new int [r2][c2];  
 for(int i=0; i < r2; i++) {  
 for(int j=0; j < c2; j++) {  
 arr2[i][j] = s.nextInt();
 }
 }  
 if (c1 != r2) {  
 System.out.print("INVALID INPUT");  
 return;
 }  
 int [][] prod = new int [r1][c2];  
 for(int i=0; i < r1; i++) {  
 for(int j=0; j < c2; j++) {  
 for(int k=0; k < r1; k++) {  
 prod[i][j] += (arr1[i][k] \* arr2[k][j]);
 }
 }
 }  
 for(int i=0; i < r1; i++) {  
 for(int j=0; j < c2; j++) {  
 System.out.print(prod[i][j] + " ");
 }
 System.out.println();
 }
}

### FIRST ARRAY

Time complexity  
 $O(n^3)$   
 3 nested loops are used. Cubic

### SECOND ARRAY

SPACE complexity  
 $O(n^2)$   
 As 2D arrays are used to store numbers.  
 ∴ Space complexity is Quadratic

### CONDITION FOR INVALID INPUT

### NEW PRODUCT MATRIX ARRAY CREATION

PRINTING PRODUCT MATRIX

## ② THE STATE OF WAKANDA - I

The historic state of Wakanda has various monuments and souvenirs which are visited by many travelers every day. The guides follow a prescribed route of visiting the monuments which improve their understanding of the relevance of each monument.

The route of the monument is fixed and expressed in a 2-d matrix where the travelers visit the prescribed next monument.

For example : ∵ The prescribed route and the visitors travel

1	2	3
4	5	6
7	8	9

this path :  
1 → 2 → 3 → 4 → 5 → 6 → 7 → 8 → 9

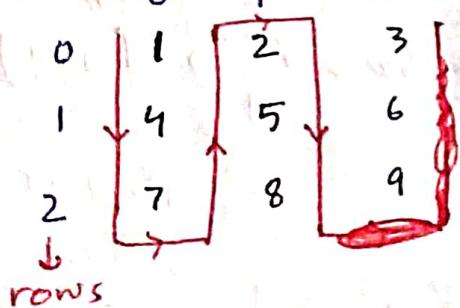
However, a certain visitor decides to ~~not~~ travel a different path as follows :

- ① He first travels southwards till no further south places are available.
- ② He then moves only 1 place eastwards.
- ③ He starts to move again towards north till any further north moves are available.

This continues till all the places are covered.

Path followed by this traveler :

1 → 4 → 7 → 8 → 5 → 2 → 3 → 6 → 9  
0      1      2      3  
        ↓      ↓      ↓      ↓  
        4      5      6      7



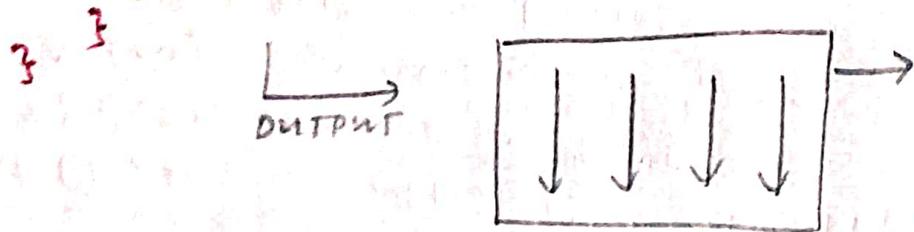
## WAVE DISPLAY / TRAVERSAL

```
p s v m(s [] a) {  
    Scanner s = new Scanner(System.in);  
    int r = s.nextInt();  
    int c = s.nextInt();  
    int [][] arr = new int [r] [c];  
    for (int i = 0; i < arr.length; i++) {  
        for (int j = 0; j < arr[0].length; j++) {  
            arr[i][j] = s.nextInt();  
        }  
    }
```

```

for (int j=0; j < arr[0].length; j++) {
    for (int i=0; i<arr.length; i++) {
        System.out.print(arr[i][j]);
    }
}

```



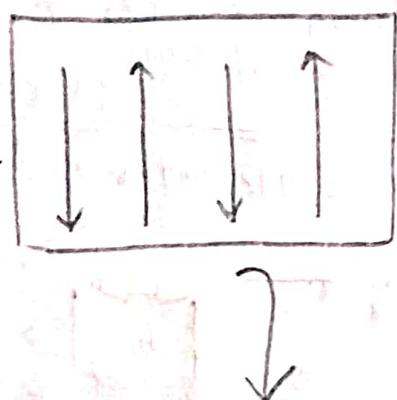
we need ↴

even-columns ↴

niche ki trah ↴

odd-columns ↴

upper ki trah ↴



```

for (int j=0; j < arr[0].length; j++) {
}

```

~~#~~ if ( $j \% 2 == 0$ ) { EVEN }

```

for (int i=0; i < arr.length; i++) {
    System.out.print(arr[i][j]);
}

```

~~#~~ else { ODD }

```

for (int i=arr.length-1; i>=0; i--) {
    System.out.print(arr[i][j]);
}

```

~~#~~ // Bhar columns ka loop hai!

~~=~~ Ander rows ka loop!

~~=~~ Agar even columns hai toh sidha loop print hoga!

~~=~~ Agar odd columns hai toh ulta loop print hoga!

~~=~~ Hamesha last wala element (arr.length-1) hoga hai!

j=0	1	2	3	4
i=0 → 11	12	13	14	
1 → 21	22	23	24	
2 → 31	32	33	34	

Time complexity

$$\underline{\underline{O(n^2)}}$$

As there is nested loop and the outer for loop runs n times. There are two inner for loops.

making the time complexity:

$$O(n) * (O(n/2) + O(n/2)) = \underline{\underline{O(n^2)}}$$

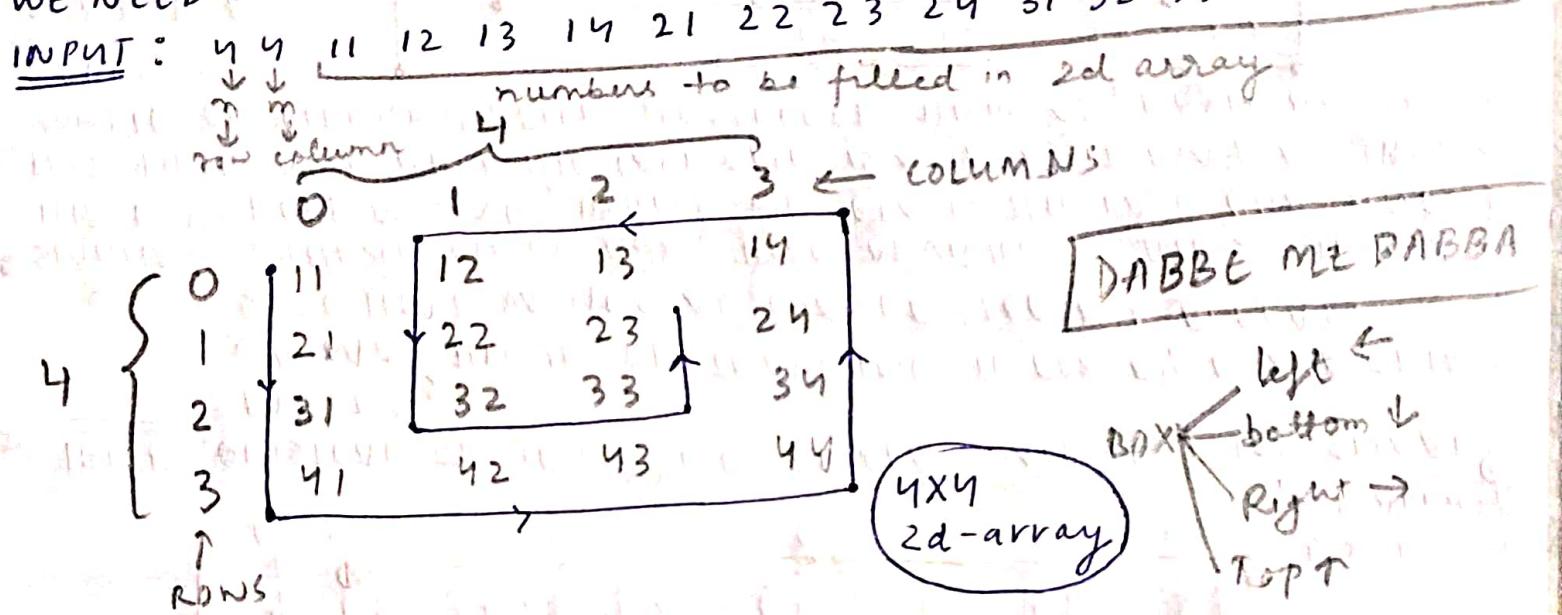
Space complexity

$$\underline{\underline{O(1)}}$$

## Spiral Display:

You will be given a number ( $n$ ), representing the number of rows, then a number ( $m$ ), representing the number of columns. After that we ~~will~~ will be given  $(n \times m)$  numbers, representing 2D array.

We need to traverse this input 2D array, in a spiral pattern.



→ 5 7 min < row column

	11	12	13	14	15	16	17
0	21	22	23	24	25	26	27
1	31	32	33	34	35	36	37
2	41	42	43	44	45	46	47
3	51	52	53	54	55	56	57
4							
	0	1	2	3	4	5	6

max < row column

1EK BOX PURA KARNE KE LIYE, 4 WALL HONHI. 4 FOR LOOP LAGENGIY.

[ left wall ] column → fixed → min  
row → varies → min → max

[ bottom wall ] column → varies → min → max  
row → fixed → max

[ right wall ] column → fixed → max  
row → varies → max → min

[ Top wall ] column → varies → max → min

## APPROACH

```

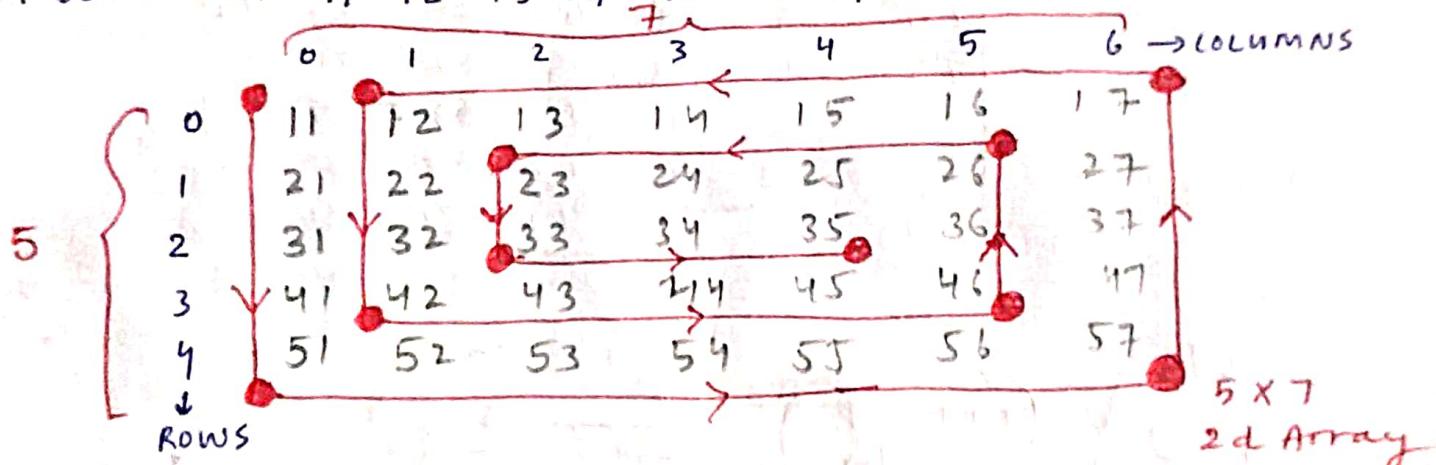
    ps.v.m(s, a) {
        Scanner s = new Scanner(System.in);
        int n = s.nextInt();
        int m = s.nextInt();
        int [][] arr = new int [n][m];
        for (int i=0; i<arr.length; i++) {
            for (int j=0; j<arr[0].length; j++) {
                arr[i][j] = s.nextInt();
            }
        }
    }

```

ARRAY  
BANANA  
AWK  
FILL  
KRAI

= LET'S ASSUME INPUT IS :

(5) 7 11 12 13 14 15 16 17 21 22 23 24 25 26 27 31 32 33  
34 35 36 37 41 42 43 44 45 46 47 51 52 53 54 55 56 57



5x7  
2d Array

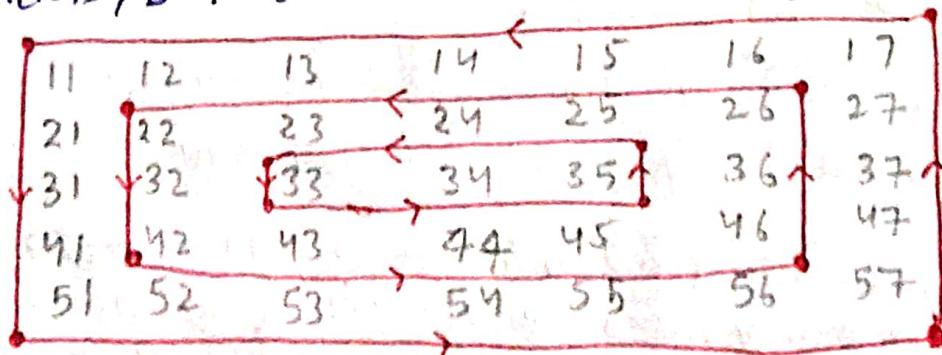
= TRICK : INSTEAD OF TRAVELING 2D-ARRAY ACTUALLY IN SPIRAL PATTERN,  
WE MAY THINK OF TRAVELING IT BOX BY BOX MAKING SURE THAT VALUES AT CORNER DOESN'T REPEAT.

• STARTING WITH AN OUTER BOX, THEN MOVING TO THE SMALLER ONE. THIS WAY KEEP MOVING, UNLESS WE REACH THE LAST BOX. AND IT'S NOT NECESSARY THAT THE LAST ONE IS A BOX, IT MAY BE JUST A COUPLE OF ELEMENTS, BUT CONSIDERED THEM AS BOXES AS SHOWN BELOW:

DABBE

ME

DABBBA



```

int minr = 0; // mini. row
int minc = 0; // mini. column
int maxr = arr.length - 1; // max. row
int maxc = arr[0].length - 1; // max. column
    ] IN 4 VARIABLES
    ] SE SUBST OUTER
    ] MOST BOX DEFINE
    ] HOWA!

```

```
int tne = n * m; // total no. of elements
```

```
int count = 0; // for keeping count of elements printed
```

```
while (count < tne) {
```

```
if (minc > maxc || i > maxr) break; // EXIT // LEFT WALL
    ] column → fix
    ] row → vary
    ] min → max

```

```
for (int i = minr, j = minc; i <= minr && count < tne; i++) {
    System.out.println(arr[i][j]);
    count++; // counter is incremented by 1
}
```

}

```
minc++; // updating minimum column
```

```
// BOTTOM WALL <-----> column → vary → min to max
for (int i = maxr, j = minc; j <= maxc && count < tne; j++) {
    System.out.println(arr[i][j]);
    count++; // counter is incremented by 1
}
```

}

```
maxr--; // updating maximum row
```

```
// RIGHT WALL <-----> row → vary → max to min
for (int i = maxr, j = maxc; i >= minr && count < tne; i--) {
    System.out.println(arr[i][j]);
    count++; // counter is incremented by 1
}
```

}

```
maxc--; // updating maximum column
```

```
// TOP WALL <-----> column → vary → max to min
for (int i = maxr, j = maxc; j >= minc && count < tne; j--) {
    System.out.println(arr[i][j]);
    count++; // counter is incremented by 1
}
```

}

```
minr++; // updating minimum row
```

}

}

```

if (count < tne) {
    for (int i = minr; i <= maxr; i++) {
        Syso(arr[i][minc]);
        count++;
    }
}

```

SAME

```

for (int i = minr; i <= maxr; i++)
    count < tne; i++)
    Syso(arr[i][minc]);
    count++;
}

```

### TIME COMPLEXITY

$O(n^2)$  → As there is nested ~~for~~ for loop and the outer for loop runs  $n$  times.  
 There are two inner for loop.  
 Either ① will run in each iteration.

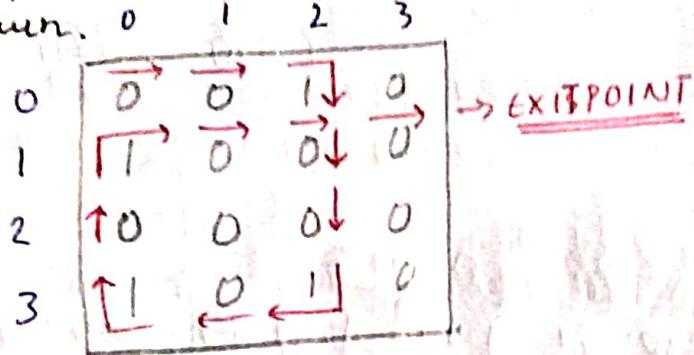
making the time :  $O(n) * O(m) = O(n*m)$

### SPACE COMPLEXITY

$O(1)$  → we are not using any auxiliary space and hence the space complexity is  $O(1)$ .

## EXIT POINT OF A MATRIX

The problem states that we have a matrix or a 2-d array that has only 1's and 0's as the values inside it. If we encounter a 0 in the matrix we have to keep moving in the direction that we are moving, otherwise, when we encounter 1, we will take a 90° right turn.



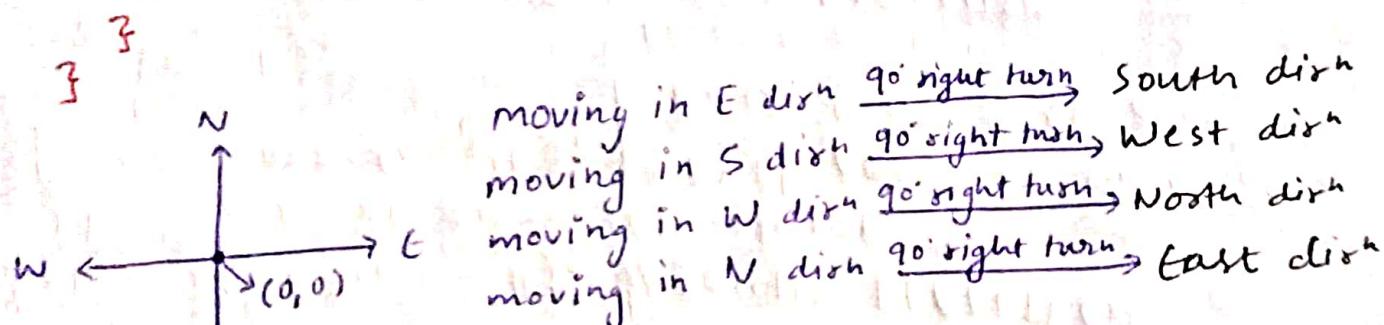
0 → pe sidha chalega  
 1 → pe 90° ka right turn lelega

## APPROACH

```

P s r m (s [J]a) {
    Scanner s = new Scanner (System.in);
    int r = s.nextInt();
    int c = _____;
    int [][] arr = new int [r][c];
    for (int i=0; i<arr.length; i++) {
        arr[i][j] = s.nextInt();
    }
}
    
```

ARRAY  
 BANAYA  
 AUR  
 USSE  
 FILL  
 KRA



i = row  
 j = column

moving in East direction ( $\rightarrow$ )  $j++$   
 SOUTH  $\rightarrow$  ( $\downarrow$ )  $i++$   
 WEST  $\rightarrow$  ( $\leftarrow$ )  $j--$   
 NORTH  $\rightarrow$  ( $\uparrow$ )  $i--$

```

int i = 0;
int j = 0;
int dir = 0; // East=0 ; South=1 ; West=2 ; North=3
while(true) {
    dir = (dir + arr[i][j]) % 4; // To keep the values b/w 0 and 3
    if (dir == 0) { // EAST DIRECTION
        j++; // move in the same row
        if (j == arr[0].length) { } // exit point is on column back (in last column)
            j--;
            break;
    }
    else if (dir == 1) { // SOUTH DIRECTION
        i++; // move down the column
        if (i == arr.length) { } // exit point is one row back (in last row)
            i--;
            break;
    }
    else if (dir == 2) { // WEST DIRECTION
        j--; // move backwards in the row
        if (j == -1) { } // exit point is one column ahead (in 0th column)
            j++;
            break;
    }
    else { // NORTH DIRECTION
        i--; // move up in the column
        if (i == -1) { } // exit point is one row ahead (in 0th row)
            i++;
            break;
    }
}

```

TIME complexity :  $O(n^2)$

SPACE complexity :  $O(1)$

ROTATE BY 90 DEGREE  
 WE ARE GIVEN A SQUARE MATRIX AND WE HAVE TO ROTATE IT BY  
 90° DEGREE.

$$n=m \rightarrow \text{Input}$$

	0	1	2	3
0	11	12	13	14
1	21	22	23	24
2	31	32	33	34
3	41	42	43	44

AFTER  
  
 90°  
 ROTATION

	0	1	2	3
0	41	31	21	11
1	42	32	22	12
2	43	33	23	13
3	44	34	24	14

- = FIRST ROW → LAST COLUMN
- = SECOND ROW → SECOND LAST COLUMN
- = THIRD ROW → THIRD LAST COLUMN / SECOND COLUMN
- = FOURTH ROW → FIRST COLUMN

$$\begin{matrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{matrix}$$

→ 90° rotate

$$\begin{matrix} m & i & e & a \\ n & j & f & b \\ o & k & g & c \\ p & l & h & d \end{matrix}$$

TRANSPOSE

1<sup>st</sup> R → 1<sup>st</sup> C  
 2<sup>nd</sup> R → 2<sup>nd</sup> C  
 3<sup>rd</sup> R → 3<sup>rd</sup> C  
 4<sup>th</sup> R → 4<sup>th</sup> C

$$\begin{matrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{matrix}$$

REVERSE COLUMNS

→ ROW BY ROW  
 REVERSE  
 ↓  
 SAARE COLUMNS  
 REVERSE HAJAHENG

```

p c m {
    p s v m (s[j]a) {
        Scanner s = new Scanner (System.in);
        int n = s.nextInt();
        int [ ] arr = new int [n][n];
        for (int i=0; i<arr.length; i++) {
            for (int j=0; j<arr[0].length; j++) {
                arr[i][j] = s.nextInt();
            }
        }
        rotateby90 (arr);
        display (arr);
    }
}
    
```

INPUT FROM  
 USER

AND  
 DIMENSIONS  
 ARRAY  
CREATION

	0	1	2	3
0	11	12	13	14
1	21	22	23	24
2	31	32	33	34
3	41	42	43	44

TRAVERSE ONLY THIS PART FOR TRANSPOSE. IT WILL PROVIDE THE RIGHT PATTERN.

BUT IF WE TRAVERSE COMPLETE ARRAY THEN MANY PLACES WILL BE REMAINED UNCHANGED AND ANSWER WILL BE DIFFERENT.

ps v rotateby90 (int [][] arr) {

for (int i=0; i < arr.length; i++) {

for (int j=0; j < arr[0].length; j++) {

int temp = arr[i][j];  
 arr[i][j] = arr[j][i];  
 arr[j][i] = temp;

}

}

TRANSPOSE  
OF  
MATRIX

	0	1	2	3
0	11	21	31	41
1	12	22	32	42
2	13	23	33	43
3	14	24	34	44

REVERSING  
EACH  
ROW

	0	1	2	3
0	41	31	21	11
1	42	32	22	12
2	43	33	23	13
3	44	34	24	14

	0	1	2	3
0	11	21	31	41
1	11	31	21	11

SIMILARLY  
REVERSING  
EACH ROW

for (int i=0; i < arr.length; i++) {  
 int li = 0; // LEFT INDEX  
 int ri = arr[0].length - 1; // RIGHT INDEX  
 while (li <= ri) {  
 int temp = arr[i][li];  
 arr[i][li] = arr[i][ri];  
 arr[i][ri] = temp;  
 li++;  
 ri--;
 }
}

REVERSE  
COLUMNS,  
ROW BY ROW  
ELEMENTS  
REVERSE

QUESTION

```

    public void display (int [][] arr) {
        for (int i = 0; i < arr.length; i++) {
            for (int j = 0; j < arr[0].length; j++) {
                System.out.print (arr[i][j] + " ");
            }
            System.out.println ();
        }
    }
}

```

DISPLAY  
 FUNCTION  
 TO DISPLAY  
 THE FINAL  
 MATRIX  
 ARRAY

### TIME COMPLEXITY

THE TIME COMPLEXITY FOR ROTATING THE MATRIX BY THIS PROCEDURE IS  $O(n^2)$ .

AS FOR TRANSPOSING WE ARE TRAVERSING THE UPPER TRIANGLE. i.e. WE ARE TRAVERSING  $(n^2/2)$  ELEMENTS AND THEN REVERSING TAKES  $O(n)$  time. AND WE HAVE

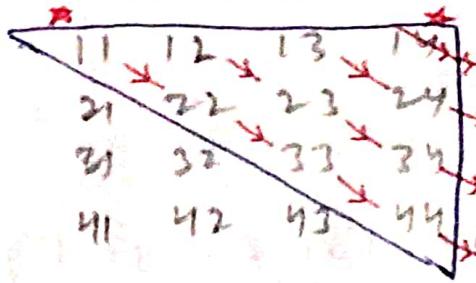
TO REVERSE  $n$  ROWS.  
SO IT BECOMES  $O(n^2 + \frac{n^2}{2})$   
WHICH IS  $O(n^2)$ .

### SPACE COMPLEXITY

THE SPACE COMPLEXITY IS  $O(1)$  AS WE ARE TRANSPOSING AND THEN REVERSING IN-PLACE AND WE ARE NOT CONSUMING ANY AUXILIARY MEMORY.

## ④ THE STATE OF WAKANDA - 2 (DIAGONAL TRAVERSAL)

WE NEED TO PRINT UPPER DIAGONAL OF THE MATRIX



∴ IT IS A SQUARE MATRIX  
 $\Downarrow n = m$   
 row                      column

`p c m {`

```

    p s v m (s[j] a) {
        scanner s = new scanner (System.in);
        int n = s.nextInt();
        int [][] arr = new int [n] [n];
        for (int i = 0; i < arr.length; i++) {
            for (int j = 0; j < arr[0].length; j++) {
                arr[i][j] = s.nextInt();
            }
        }
    }
}
```

INPUT AND  
ARRAY  
CREATION

SABSE PHELE 0<sup>th</sup> DIAGONAL PRINT HOGA  
 FIR 1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>.

HAR DIAGONAL KI SHURUWAT ( $i=0$ ) HOTI HAI,

AUR ( $j = \text{gap}$ )

CONDITION  $\rightarrow j < n$  HAR DIAGONAL KE LIYE!

```
for (int g = 0; g < arr.length; g++) {
```

```
    for (int i = 0; j = g; j < arr.length; i++, j++) {
```

`System.out.println(arr[i][j]);`

loop for  
printing  
upper  
diagonal  
of  
matrix.

Time Complexity

WHEN  $\text{gap} = 0$ , inner loop runs  $n$  times  
 $\text{gap} = 1$ ,  $n-1$   
 $\text{gap} = 2$ ,  $n-2$

$n + (n-1) + (n-2) + (n-3) + \dots$  times

$$= \frac{n * (n+1)}{2} \approx O(n^2)$$

Space Complexity

we are not using any auxiliary space and hence the space complexity  $O(1)$ .

## ③ RING ROTATE OR SHELL ROTATE

WE HAVE A  $[n \times m]$  MATRIX WHERE  $n$  IS THE NUMBER OF ROWS AND  $m$  IS THE NUMBER OF COLUMNS. WE WILL BE GIVEN A RING NUMBER  $s$  REPRESENTING THE RING OF THE MATRIX.

1	12	13	14	15	16
2	22	23	24	25	26
3	32	33	34	35	36
4	42	43	44	45	46
5	52	53	54	55	56
6	62	63	64	65	66

WE WILL BE GIVEN A NUMBER  $s$  REPRESENTING THE NUMBER OF ROTATIONS IN AN ANTI-CLOCKWISE MANNER OF THE SPECIFIED RING. WE ARE REQUIRED TO ROTATE THE  $(s^{th})$  RING BY  $s$  ROTATIONS AND DISPLAY THE ROTATED MATRIX  $\xrightarrow{\text{SHELL convert} \rightarrow 1-D}$

- = SHELL KE DATA KO 1-D ARRAY ME BHAR LENGY,
- = 1-D ARRAY ROTATE KRENYY,  $\xrightarrow{\text{ROTATE 1-D Array}}$
- = ROTATED 1-D ARRAY KO WAPIS SHELL KO BHAR DENNY.  
 $\boxed{\text{ROTATED 1-D ARRAY} \xrightarrow{\text{convert}} \text{SHELL}}$

## ④ PSEUDOCODE

```
oned = fillOneDFromShell(arr, s);
rotate(oned, r);
fillShellFromOneD(arr, s, oned);

P C m {
    P S V m(S[] a) {
        Scanner s = new Scanner(System.in);
        int n = s.nextInt();
        int m = s.nextInt();
        int [][] arr = new int[n][m];
        for (int i=0; i<arr.length; i++) {
            for (int j=0; j<arr[0].length; j++) {
                arr[i][j] = s.nextInt();
            }
        }
    }
}
```

INPUT FROM  
USER  
AND  
ARRAY  
CREATION

```
int s = s.nextInt(); // SHELL
int r = s.nextInt(); // ROTATION
rotateShell(arr, s, r);
display(arr);
```

```
}
```

P S V rotatedShell (int [][] arr, int s, int r) { // To rotate  
 int [] onesd = fillOnedFromShell (arr, s); the particular  
 rotate (onesd, r);  
 shell  
 fillShellFromOned (arr, s, onesd);

}

P S V rotate (int [] onesd, int r) { // rotate function  
 r = r % arr.length;  
 if (r < 0) {  
 r = r + arr.length;

To rotate the ~~function~~ onesd array by  $\textcircled{r}$  given by user

}  
 reverse (onesd, 0, onesd.length - r - 1);  
 reverse (onesd, onesd.length - r, onesd.length - 1);  
 reverse (onesd, 0, onesd.length - 1);

}  
 → // Reverse function → To reverse the onesd.

P S V reverse (int [] onesd, int li, int ri) {

while (li < ri) {

int temp = onesd[li];  
 onesd[li] = onesd[ri];  
 onesd[ri] = temp;

li++;  
 ri--;

shift = 3  
 1, 2, 3, 4, 5, 6, 7

↓ reverse  
 4, 3, 2, 1, 5, 6, 7

↓ reverse  
 4, 3, 2, 1, 7, 6, 5

↓ reverse  
 5, 6, 7, 1, 2, 3, 4

}

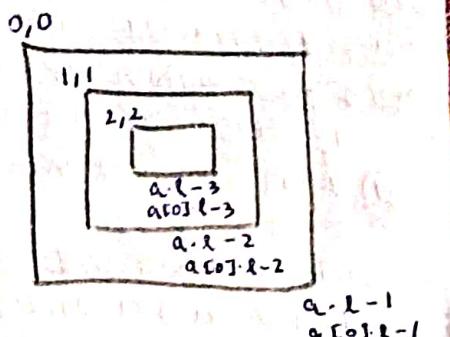
P S int [] fillOnedFromShell (int [][] arr, int s) {

JO SHELL KOTA HAI  $s=3$ ,  
 TOP LEFT CORNER WO HONA  $(s-1, s-1)$

BOTTOM RIGHT CORNER WO HONA  $(a.length-s, a[0].length-s)$

YEH HAR JAAM HONA

HAR SHELL KE LIYE,



```

int minr = s-1;
int minc = s-1;
int maxr = arr.length - s;
int maxc = arr[0].length - s;
// int sz = dw + bw + rw + tw - 4;
    same same

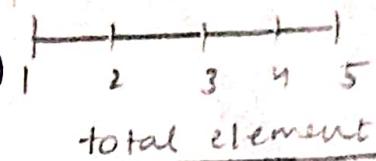
```

// int sz = 2\*(maxr-minr+1) + 2\*(maxc-minc+1) - 4;

int sz = 2\*(maxr-minr+1) + 2\*(maxc-minc+1) - 4;

ONE-D ARRAY KO SIZE  
KITNA HONA?

LSHELL KE SIARE ELEMENT  
HONGY PAR CORNERS DO  
BAAK LENA NAHI!



total element

$$\begin{aligned} & \text{high low} + 1 \\ & = 5 - 1 + 1 \\ & = 4 + 1 \\ & = 5 \end{aligned}$$

int sz = 2\*(maxr-minr+1) + 2\*(maxc-minc+1) - 4;

int [] oned = new int [sz];

int idx = 0;

for (int i = minr, j = minc; i <= maxr; i++) {  
 oned[idx] = arr[i][j];  
 idx++;  
}

left wall  
row → increase → minr → maxr  
col. → stay at minc

for (int i = maxr, j = minc + 1; j <= maxc; j++) {  
 oned[idx] = arr[i][j];  
 idx++;  
}

bottom wall  
row → stays at maxr  
col. → ↑ → minc to maxc

for (int i = maxr - 1, j = maxc; i >= minr; i++) {  
 oned[idx] = arr[i][j];  
 idx++;  
}

right wall  
row → ↓ → maxr to minr  
col. → stay at maxc

for (int i = minr, j = maxc - 1; j >= minc + 1; j--) {  
 oned[idx] = arr[i][j];  
 idx++;  
}

top wall  
row → stay at minr  
col. → ↓ → maxc to minc

return oned;

```

P S V fillShellFromOneD (int [][] arr, int s, int [] oneD) {
    int minR = s - 1;
    int minC = s - 1;
    int maxR = arr.length - s;
    int maxC = arr[0].length - s;
    int idx = 0;
    for (int i = minR, j = minC; i <= maxR; i++) { } "left
        arr[i][j] = oneD[idx];
        idx++;
    }
    for (int i = maxR, j = minC + 1; j <= maxC; j++) { } "bottom
        arr[i][j] = oneD[idx];
        idx++;
    }
    for (int i = maxR - 1, j = maxC; i >= minR; i--) { } "Right
        arr[i][j] = oneD[idx];
        idx++;
    }
    for (int i = minR, j = maxC - 1; j >= minC; j--) { } "Top Wall
        arr[i][j] = oneD[idx];
        idx++;
    }
}

P S V display (int [][] arr) {           // display function
    for (int i = 0; i < arr.length; i++) { } To display the
        for (int j = 0; j < arr[0].length; j++) { } Ring rotated
            System.out.print (arr[i][j] + " "); array !
    }
    System.out.println ();
}

```

Time complexity  $\rightarrow O(n+m)$

Space complexity  $\rightarrow O(n+m)$

SADDLE PRICE → (POINT)

YOU ARE GIVEN A SQUARE MATRIX OF SIZE  $n$ . YOU ARE GIVEN

$[n \times n]$  ELEMENTS OF THE SQUARE MATRIX.

YOU ARE REQUIRED TO FIND THE SADDLE PRICE OF THE GIVEN MATRIX AND PRINT THE SADDLE PRICE.

THE SADDLE PRICE IS DEFINED AS THE LEAST PRICE IN THE ROW BUT THE MAXIMUM PRICE IN THE COLUMN OF THE MATRIX.

2. SADDLE POINT'S NAHI HO SAKTY!

SADDLE POINT → TESSA NO. JO APNI ROW ME MIN. (CHOTA) HO!

AUR APNE COLUMN ME MAX. (BADA) HO!

a	b	c	d
e	f*	g	h
i	j	k	l*
m	n	o	p

Let us say  $f$  and  $l$  are Saddle points  
Agar  $f$  saddle point hai toh apni row ke least hai toh vo certainly  $l$  se chota hogा!  
Aur apne column ka max hai toh  $l$  se bada hogा!

An  $l$  bhi saddle point hai toh vo apni row me least hai toh  $l$  se chota hogा!

column me max hai toh

$l$  se bada hogा!

$$j < f < h \rightarrow l$$

↳ This line states that

$$\{ j < h \}$$

↳ This is not possible  $\{ h < j \}$  abhi.

$$h < l < j \rightarrow l$$

↳ This line states that

11	12	13	14
21	22	23	24
31	32	33	34
41*	42	43	44

SADDLE POINT → Apni row ke least Apni column ke max

Phle pure row ko travel krenge use useka least dhundhe legay!  
toh hame potential saddle point milega!

↳ hum potential saddle point ko check krenge kya tu apne column me max hai: toh tu?

Potentially se Saddle point hojayaga!

Isse har row ko travel krenay aur check krenay!

ESSA ho sakte hai ki ek bhi saddle point na mile!  $\rightarrow$  YES  
Is Point invalid input

PC m {

ps v m (s [ ] a) + t {

Scanner s = new Scanner (System.in);

Code written with  
green color is

int n = s.nextInt();

Correct Code

int [ ] [ ] arr = new int [n] [n];

with all test  
cases pass.

for (int i = 0; i < arr.length; i++) {

for (int j = 0; j < arr[0].length; j++) {

arr [i] [j] = s.nextInt();

Time Complexity

In worst case, we might need to  
travel all the elements in the  
matrix.  $\therefore O(n^2)$

// Saari rows me loop lagya!

for (int i = 0; i < arr.length; i++) { Space Complexity : O(1)

// mujhe per row ka mini chahiye!

// fir usse check kera hai ki column max. hai ki nahi!

int lci = 0;  $\xrightarrow{\text{smallest value (j) (svj)}}$

int min = arr [i] [0];

for (int j = 1; j < arr[0].length; j++) {

if (arr [i] [j] < arr [i] [lci]) {

lci = j;

min

$\downarrow \min = arr [i] [j]$ ,

}  $\oplus$  boolean flag = true; chalre hai!

// Aab mujhe uss column check kera hai ki yeh max hai  
ya nahi? Subara loop lagana hai

for (int k = 0; k < arr.length; k++) {

if (arr [k] [lci] > arr [i] [lci]) {

flag = false;

min

break;

}

if (flag == true) { // Agar flag true raha toh

System.out.println (arr [i] [lci]); array print krenge

return;

// Saddle point

System.out.println ("INVALID INPUT"); // waisa yeh print hoga!

}



## SEARCH IN A SORTED 2-D ARRAY

CHUME EK ARRAY MILA HAI! sorted hai (row + columns).

11	12	13	14	x
21	22	23	24	
31	32	33	34	
41	42	43	44	

let find (32)

Binary Search jaisa kuch lagyengy!

42  $\Rightarrow$  FIND  $\Rightarrow$  ?

40  $\rightarrow$  INVALID

x = ?

P cm {  
P s. r m [s[] a) + & {

Scanner s = new Scanner (System.in);

int n = s.nextInt();

int [] [] arr = new int [n][n];

for (int i = 0; i < arr.length; i++) {  
 for (int j = 0; j < arr[0].length; j++) {  
 arr[i][j] = s.nextInt();  
 }  
}

}; data

int x = s.nextInt();  $\rightarrow$  Jo search karna hai uska input

#Aab humne chej dikhni hai!

row  $\leftarrow$  int i = 0;  
column  $\leftarrow$  int j = arr[0].length - 1;  $\rightarrow$  corner milgaya!

(1)  $\rightarrow$  Right-top-most column.

while (i < arr.length & & j >= 0) {

if (x == arr[i][j]) {

data  $\rightarrow$  System.out.println (i);

j  $\rightarrow$  return;

} else if (x < arr[i][j]) {

j - -;

} else {

i + +;

}

} System.out.println ("NOT FOUND");

}

## Approach

2 <sub>00</sub>	3 <sub>01</sub>	5 <sub>02</sub>	8 <sub>03</sub>
6 <sub>10</sub>	9 <sub>11</sub>	12 <sub>12</sub>	18 <sub>13</sub>
11 <sub>20</sub>	15 <sub>21</sub>	20 <sub>22</sub>	25 <sub>23</sub>
23 <sub>30</sub>	30 <sub>31</sub>	40 <sub>32</sub>	50 <sub>33</sub>

To be Found

$$\text{Data} = x = 12$$

- = Can enter from 4 corners
- = move along the rows and columns not diagonals.

Let say we have to

$$\text{Find } \boxed{\text{Data} = 15}$$

TO BE FOUND

## Entry Point

### Decision

2	3	5	(8)
6	9	12	18
11	15	20	25
23	30	40	50

Entry Point

2	3	5	(8)
6	9	12	(18)
11	15	20	25
23	30	40	50

2	3	5	(8)
6	9	(12)	(18)
11	(15)	(20)	25
23	30	40	50

2	3	5	(8)
6	9	(12)	(18)
11	15	20	25
23	30	40	50

Time Complexity: Drops from  $O(m \times n)$  to  $O(m+n)$

Space Complexity:  $O(1)$