QMC Workshop 2021

Observables Week 6 \\ November 9th

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https://github.com/QMCPACK/qmc_workshop_2021

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Outline

- Going beyond total energies
- The density estimator
 - VMC Case
 - DMC Case Mixed Estimator Bias
- Overview of lab material (Density of Water)

Next Week: QMC research presentations from guest lecturers

Going Beyond Total Energies

Other Scalar Quantities (QMCA Tool)

• The **scalar.dat** files of QMCPACK record numerous quantities per block (not just total energy and variance) :

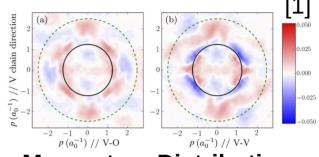
#	index	LocalEnergy	LocalEnergy sq	LocalPotential	Kinetic	ElecElec	IonIon	LocalECP	NonLocalECP	BlockWeight	BlockCPU	AcceptRatio
		-1.7180458115e+01		-2.8894295250e+01		1.6464087499e+01	7.0826301547e+00	-5.3568444419e+01	1.1274315161e+00		3.0608057500e-02	7.3708333333e-01
	1	-1.7255928686e+01	2.9807370888e+02	-3.0545955753e+01	1.3290027068e+01	1.6554259132e+01	7.0826301547e+00	-5.5022279869e+01	8.3943482873e-01	1.0000000000e+02	3.3220134000e-02	7.3958333333e-01
	2	-1.7097969016e+01	2.9278739997e+02	-3.2384941910e+01	1.5286972894e+01	1.7775718704e+01	7.0826301547e+00	-5.8416061607e+01	1.1727708382e+00	1.0000000000e+02	3.3500155500e-02	7.2041666667e-01
		-1.7172461800e+01	2.9515620642e+02	-2.9541109404e+01	1.2368647604e+01	1.6595669862e+01	7.0826301547e+00	-5.4050856627e+01	8.3144720570e-01	1.0000000000e+02	3.2998673250e-02	7.4583333333e-01
	4	-1.7099473131e+01	2.9254022396e+02	-3.0272376078e+01	1.3172902947e+01	1.6571567375e+01	7.0826301547e+00	-5.4723928360e+01	7.9735475121e-01	1.0000000000e+02	3.3510831500e-02	7.3166666667e-01
		-1.7252344308e+01	2.9787400431e+02	-3.1015931262e+01	1.3763586954e+01	1.6910836009e+01	7.0826301547e+00	-5.6527003242e+01	1.5176058162e+00		3.3724926250e-02	7.3291666667e-01
	6	-1.7293154972e+01	2.9952641814e+02	-3.3213203661e+01	1.5920048689e+01	1.7684759063e+01	7.0826301547e+00	-5.9978837616e+01	1.9982447375e+00	1.0000000000e+02	3.3212170000e-02	7.2666666667e-01
		-1.7224256691e+01	2.9684870264e+02	-3.2424089111e+01	1.5199832420e+01	1.7739088898e+01	7.0826301547e+00	-5.8140909144e+01	8.9510098024e-01	1.0000000000e+02	3.3245939000e-02	7.2125000000e-01
	8	-1.7113139061e+01	2.9314904854e+02	-3.0407538775e+01	1.3294399714e+01	1.7513443637e+01	7.0826301547e+00	-5.6512960662e+01	1.5093480948e+00	1.0000000000e+02	3.3479175750e-02	7.1541666667e-01

• The means and error bars can be obtained with the *qmca* tool

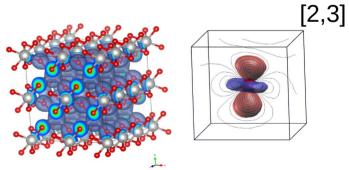
```
> gmca dmc.s000.scalar.dat
runs/H20/dmc J2/dmc series 0
                                   -17.1777 +/-
                                                          0.0044
 LocalEnergy
 Variance
                                      0.308 +/-
                                                           0.015
 Kinetic
                                    13.728 +/-
                                                           0.086
 LocalPotential
                                    -30.906 +/-
                                                           0.087
 ElecElec
                                     17.112 +/-
                                                           0.040
 LocalECP
                                     -56.36 +/-
                                                            0.12
 NonLocalECP
                                      1.265 +/-
                                                           0.034
                                                            0.00
 IonIon
                                      7.08 +/-
 LocalEnergy sg
                                     295.38 +/-
                                                            0.16
 BlockWeight
                                     100.00 +/-
                                                            0.00
 BlockCPU
                                    0.03402 +/-
                                                         0.00014
 AcceptRatio
                                    0.7234 +/-
                                                          0.0011
 Efficiency
                                  372472.44 +/-
                                                            0.00
                                                            0.00
                                       5.10 +/-
 TotalSamples
                                      15000 +/-
```

Beyond Energies

- QMCPACK is capable of calculating a broad range of observables (estimators), not just the total energy (e.g. the Chiesa KE correction shown last week).
- Others include:
 - Energy Density
 - One-body reduced Density Matrix
 - Spherically Averaged Pair-Correlation
 - Static Structure Factor
 - Forces
 - And More ...
- For a detailed list and their formal descriptions and implementation details, see the following:
 - https://qmcpack.readthedocs.io (Online Documentation)
 - https://doi.org/10.1088/1361-648X/aab9c3 (Citation Paper)
 - https://doi.org/10.1063/5.0004860 (QMCPACK Advances)



Momentum Distribution



Density and Spin-Density

[1] Phys. Rev. B 99, 075154 (2019)

[2] New J. Phys. 18 113049 (2016)

[3] cond-mat arXiv:2103.09809 (2021)

Notes on QMCPACK Estimators

• To calculate estimators, modifications to the QMCPACK input are generally minor, intuitive, and user friendly:

- Estimators can be evaluated during all chained QMC runs, for instance: VMC → DMC → DMC → ...
- However, the estimator elements can also be evaluated at specific QMC sections (i.e. for VMC only). The online documentation outlines precisely how this is specified.
- Generally not available (or needed) for optimizations.

The Density Estimator

The Density Estimator – VMC Case

• To calculate the density, the particle number density operator is used. And its form is given as:

$$\hat{n}_{ec{r}} = \sum_{i=1}^N \delta(ec{r} - ec{r_i})$$
 , Particle Number Density Operator

- Provides a count of the number of electrons at a point \vec{r} .
- In practice, QMCPACK must use a finite histogram grid, then average the number of particles in each grid cell over an ensemble of walkers distributed as $\Psi_T(\vec{R})^2$ to obtain the density $n(\vec{r})$:

$$n_c = \int d^3R |\Psi_T(\vec{R})|^2 \int_{\Omega_c} d^3r \sum_{i=1}^N \delta(\vec{r} - \vec{r_i})$$

$$\approx \frac{1}{M} \sum_{m=1}^M [\text{# of sample's electrons in cell, } c]$$

Note:

The **spin-density** is obtained similarly; up and down electrons are counted *separately* to generate up and down densities.

The Density Estimator – DMC Case

- First, let's briefly step back and look closely at how the energy is evaluated in DMC:
- Mixed-Estimator:

$$E = \lim_{\tau \to \infty} \frac{\langle e^{-\tau \hat{H}/2} \Psi_{T} | \hat{H} | e^{-\tau \hat{H}/2} \Psi_{T} \rangle}{\langle e^{-\tau \hat{H}/2} \Psi_{T} | e^{-\tau \hat{H}/2} \Psi_{T} \rangle}$$

$$= \lim_{\tau \to \infty} \frac{\langle e^{-\tau \hat{H}} \Psi_{T} | \hat{H} | \Psi_{T} \rangle}{\langle e^{-\tau \hat{H}} \Psi_{T} | \Psi_{T} \rangle} = \frac{\langle \Psi_{0} | \hat{H} | \Psi_{T} \rangle}{\langle \Psi_{0} | \Psi_{T} \rangle}$$

$$= \frac{\int d^{3}R \Psi_{0}(\vec{R}) \Psi_{T}(\vec{R}) E_{L}(\vec{R})}{\int d^{3}R \Psi_{0}(\vec{R}) \Psi_{T}(\vec{R})}$$

(1) Use commuting property

(2) "Mixed Estimator"

(3) Average of local energy over dist. $\Psi_0 \Psi_T$.

Doesn't work for observables that do not commute with H

The Density Estimator – DMC Case

- If we evaluate an observable, O, that does not commute with H in the same way as the energy, an error is incurred $\mathcal{O}[(\Psi_0 \Psi_T)]$.
- For this reason, in practice a combination of the mixed estimator (DMC) and the variational estimator (VMC) is used:

$$|<\Psi_0|\mathcal{O}|\Psi_0>\approx 2<\Psi_0|\mathcal{O}|\Psi_T>-<\Psi_T|\mathcal{O}|\Psi_T> \\ \text{(DMC)} \qquad \text{(VMC)} |$$

- Notice that the accuracy of the extrapolated estimator depends on the quality of the trial wave function. Its error now $\mathcal{O}[(\Psi_0 \Psi_T)^2]$.
- An alternate approach to get around this problem is to use a method known as "forward walking" which enables one to sample the pure distribution $<\Psi_0|\Psi_0>$. This is beyond the scope of this talk, though the method is implemented in QMCPACK and details can be found in the online manual:

https://qmcpack.readthedocs.io/en/develop/hamiltonianobservable.html#forward-walking-estimators

Notes:

• When calculating the density for systems with open boundaries, the user must specify the cell that will be used to evaluate the density – best to center the molecule in the desired cell. For periodic boundaries, the supercell is used by default.

Be sure that when estimating any observable, if it does not commute with H
then you should use an extrapolated estimate (KE, Potential Energy, etc.)

Questions?

Overview of Lab Material:

Calculating and analyzing the density of water

- Step 0: git pull inside ~/qmc_workshop_2021 and ~/apps/qmcpack/qmcpack
- **Step 1:** Orbital and wave function generation using PySCF and QMCPACK
- Step 2: Calculating and storing VMC and DMC charge density
- **Step 3:** Using **qdens** tool to generate .xsf file for visualization in VESTA
- **Step 4:** Using **qdens-radial** tool to estimate atomic occupations (with an extrapolated estimate and resampled error bars)

Step 1: Orbital and wave function generation using PySCF and QMCPACK

- Material located at: ./qmc_workshop_2021/week6_observables/01_density_water
- Nexus work flow file: h2o_workflow.py
- Define the pseudopotentials and structure

```
ppset(
    label = 'ccecp',
    qmcpack = ['H.ccECP.xml','0.ccECP.xml'],
)

system = generate_physical_system(
    structure = 'H20.xyz', # H20 atomic structure
    H = 1, # H pseudo Zeff
    0 = 6, # 0 pseudo Zeff
)
```

Step 1: Orbital and wave function generation using PySCF and QMCPACK

Hartree-Fock (HF) and Orbital Conversion

```
# perform Hartree-Fock
scf = generate pvscf(
   identifier = 'scf',
   path = 'H2O/hf', # directory to run in
job = job(serial=True,app='python3'),
   template = './scf template.py', # pyscf template file
   system = system,
                                    # used to make Mole() inputs
   mole = obi(
       ecp = 'ccecp',
       basis = 'ccecp-ccpvqz',
       symmetry = True,
   save gmc = True, # save wfn data for gmcpack
# convert orbitals to OMCPACK format
c4q = generate convert4qmc(
   identifier = 'c4g',
   path = \frac{H20}{hf'},
   job
              = job(cores=1),
   no jastrow = True,
   dependencies = (scf, 'orbitals'),
```

converged SCF energy = -16.9177692534032

Step 1: Orbital and wave function generation using PySCF and QMCPACK

Two-body Jastrow optimization

```
# optimize 2-body Jastrow
optJ2 = generate gmcpack(
    identifier = 'opt',
   job = job(cores=cores),

system = system,

pseudos = 'ccecp'.
    path = 'H20/optJ2',
    J2
                   = True.
   J2_rcut = 8.0,
qmc = 'opt'
|minmethod = 'ones
                             # use opt defaults
                   = 'opt',
                   = 'oneshiftonly', # adjust for oneshift
    init cycles
    init minwalkers = 0.1.
    cycles
                   = 25600.
    samples
                   = [(c4q,'particles'),(c4q,'orbitals')],
    dependencies
```

In this case, HF leads to a wave function with a variance-to-energy ratio of ~0.02 Ha.

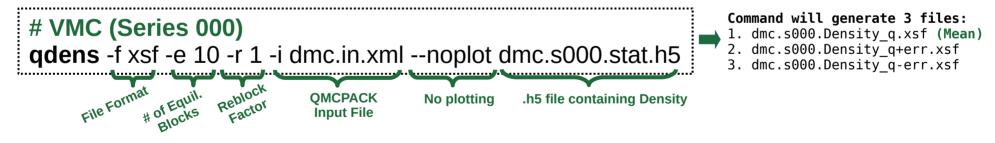
Step 2: Calculating and storing VMC and DMC charge density

Defining the QMC runs with density estimator:

```
from qmcpack input import density
# run DMC with Slater-Jastrow wavefunction
gmc = generate gmcpack(
    identifier = 'dmc',
   path
                = 'H20/dmc J2',
                = job(cores=cores),
    iob
                = system,
    system
    pseudos
    iastrows
                 = [].
    estimators = [\text{density}(\text{delta}=(0.02,0.02,0.02), \text{x min}=0, \text{x max}=8, \text{y min}=0, \text{y max}=8, \text{z min}=0, \text{z max}=8)], # Grid spacing in bohr
    seed
                             # DMC run
    amc
                             # DMC walker population sampled from VMC
    vmc samples = 1024,
    vmc blocks = 150,
    vmc steps
    vmc timestep = 0.3,
   eg dmc
                             # Add DMC equilibration
                 = True,
                              # Use a small number of blocks
    eq blocks
                 = 30.
    eg steps
    eq timestep = 0.02,
                            # Use a larger timestep
                 = 500, # Large number of blocks for production
    blocks
                 = 25, # 10 steps/block averages out some autocorr time
    steps
                            # Smaller production timestep
    timestep
                              # Use T-moves scheme w/ non-local pseudopotentials
    nonlocalmoves = True,
    dependencies = orbdeps+[(optJ2,'jastrow')],
```

Step 3: Using **qdens** tool to generate .xsf file for visualization in VESTA

- After the QMC runs complete, the density for each block will be located in the dmc.s*.stat.h5 files.
- We use the qdens for two reasons: (1) average density over all the blocks and store the average density in a format suitable for visualization and/or analysis.
- Note: Use qmca first to determine equilibration and auto-correlation lengths



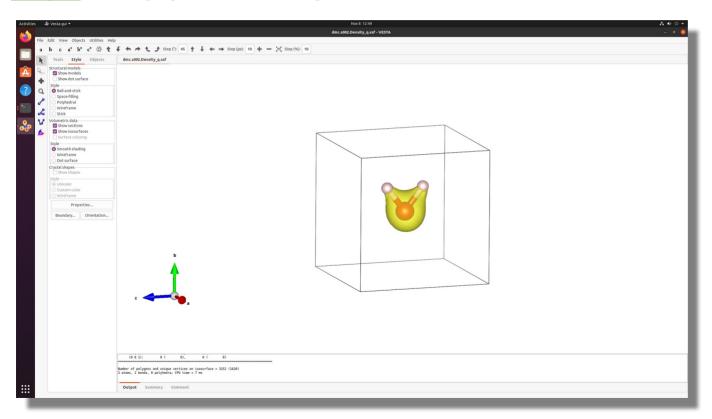
DMC (Series 002)

qdens -f xsf -e 25 -r 3 -i dmc.in.xml --noplot dmc.s002.stat.h5

Command will generate 3 files:

- dmc.s002.Density_q.xsf (Mean)
- 2. dmc.s002.Density_q+err.xsf
- 3. dmc.s002.Density_q-err.xsf

Step 3: Using **qdens** tool to generate .xsf file for visualization in VESTA



To visualize: \$ VESTA

Then import .xsf file:
File > Open > dmc.s002.Density_q.xsf

VESTA Manual: https://jp-minerals.org/vesta/en/doc.html

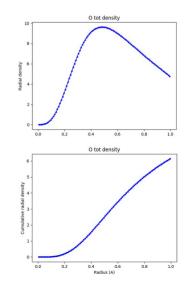
Step 4: Using **qdens-radial** tool to estimate atomic occupations

- Once we have the *Density*.xsf files from qdens, we can use another QMCPACK tool, **qdens-radial**, to calculate on-site populations.
- How does this work: given a set of species and radii (in Angstroms), the tool will generate a radial density angular average around the atomic sites out to the specified radius
- The radial density can be chosen to be non-cumulative or cumulative (integrated).

Example 1: Plot DMC non-cumulative radial density of O. qdens-radial -p -s O -r 1 dmc.s002.Density_q.xsf

Plot Species Radii (A) .xsf file containing Density

Example 2: Plot DMC cumulative radial density of O. qdens-radial -p -s O -r 1 -c dmc.s002.Density_q.xsf



Step 4: Using qdens-radial tool to estimate atomic occupations

• For the cumulative case, **qdens-radial** will also print the cumulative value at the specified radius, i.e., an estimate of the atomic occupation

Example 3: Estimate of the DMC atomic occupation qdens-radial -p -s O -r 1.1 -c dmc.s002.Density_q.xsf

Output:

Cumulative Value of O Species at Cutoff 1.0 is: 6.55517033828574

 We can also get an extrapolated estimate (mixed-estimator bias) for this quantity by providing a VMC .xsf file:

Example 4: Estimate of the extrapolated atomic occupation qdens-radial -p -s O -r 1.1 -c --vmc=dmc.s000.Density_q.xsf dmc.s002.Density_q.xsf

Output:

Extrapolating from VMC and DMC densities...

Cumulative Value of O Species at Cutoff 1.1 is: 6.576918233167152

Step 4: Using qdens-radial tool to estimate atomic occupations

- What about error bars?
- We can "resample" the density at each grid point:
- Recipe:
 - 1. Use error bars from *.Density_q+err.xsf file, draw samples from a Gaussian distribution with standard deviation that matches error bar.
 - 2. Calculate occupations with resampled data and calculate standard deviation to obtain the error bar on the occupation
 - 3. Make sure number of samples is converged

Example 5: Estimate DMC atomic occupation with error bar qdens-radial -p -s O -r 1.1 -c -n 20 --dmcerr=dmc.s002.Density_q+err.xsf dmc.s002.Density_q.xsf

Output:

Resampling to obtain error bar (NOTE: This can be slow)... Will compute 20 samples...

...

Cumulative Value of O Species at Cutoff 1.1 is: 6.55517033828574+/-0.001558553749396279

Notes:

• The same tools (**qdens** and **qdens-radial**) can be used for periodic systems and for the **SpinDensity** estimator – and twist averaging can be performed when generating the converted files from qdens.

 For SpinDensities, qdens will generate a collection of .xsf files containing up, down, up+down, and up-down densities. These can also be easily visualized in VESTA and qdens-radial can be used to estimate populations (using up+down density) or local magnetic moments (using up-down density).

Questions?