# QMCPACK Workshop 2021

#### **Molecular Calculations**

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https://github.com/QMCPACK/qmc\_workshop\_2021

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#### Important notes

• For full VMC and DMC background theory please refer to relevant literature and/or lecture from the week#2 of the workshop

https://github.com/QMCPACK/qmc\_workshop\_2021/blob/master/week2\_qmc\_introduction/week2\_qmc\_introduction.pdf

YouTube: <a href="https://www.youtube.com/channel/UCdca2X8NEbjX">https://www.youtube.com/channel/UCdca2X8NEbjX</a> oYv60vS4gA (QMCPACK Channel)

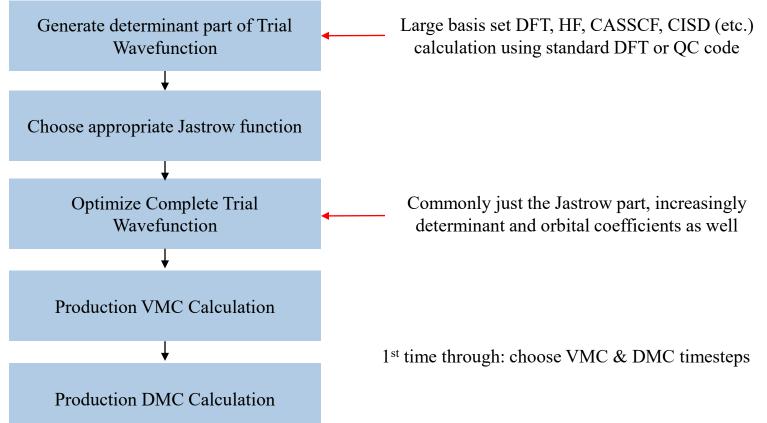
• For more details about Statistics and Nexus, refer to material from the week #3 of the workshop

https://github.com/QMCPACK/qmc workshop 2021/blob/master/week3 stats and nexus/week3 stats nexus vfinal.pdf

• For more details about QMCPACK, refer to the Manual!!!

https://qmcpack.readthedocs.io/en/develop/

# Target of the lab: Run through QMC workflow for molecules



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#### The Fixed-Node Diffusion Monte Carlo method

Projector Quantum Monte Carlo methods, such as DMC, are based on the time-dependent evolution of wavefunctions and the imaginary time Schrodinger equation. Any initial state  $|\psi\rangle$ , that is not orthogonal to the ground state  $|\phi_0\rangle$ , will evolve to the ground state in the long time limit

$$\frac{\partial |\psi\rangle}{\partial \tau} = -\widehat{H}|\psi\rangle, \qquad \qquad \lim_{\tau \to \infty} |\psi(\tau)\rangle = c_0 e^{-\epsilon_0 \tau} |\phi_0\rangle$$

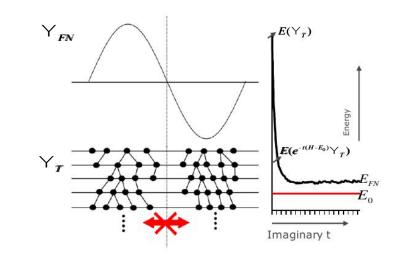
To avoid reaching the bosonic solution, we introduce a guiding/trial function  $\psi_G(\mathbf{R})$ , which closely approximates the ground state.

$$f(\mathbf{R}, \tau) = \psi_G(R)\psi(\mathbf{R}, \tau)$$

DMC is variational, and upper bound to the exact nodal surface

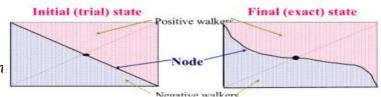
Diffusion Drift Branching
$$-\frac{\delta f(\mathbf{R}, \tau)}{\delta \tau} = \left[ \sum_{i=1}^{N} -\frac{1}{2} \nabla^{2}_{i} f(\mathbf{R}, \tau) \right] - \nabla \cdot \left[ \frac{\nabla \psi(\mathbf{R})}{\psi(\mathbf{R})} f(\mathbf{R}, \tau) \right] + (E_{L}(\mathbf{R}) - E_{T}) f(\mathbf{R}, \tau)$$

Quality of the calculation depends on the quality of nodal surface. Can be systematically improved (by increasing complexity of the guiding function)



#### Model fermion problem: Particle in a box

Symmetric potential:  $V(\mathbf{r}) = V(-\mathbf{r})$ Antisymmetric state:  $f(\mathbf{r}) = -f(-\mathbf{r})$ 



### Single Particle Orbitals

#### Linear Combination of Atomic Orbitals (LCAO)

Generate a trial Wavefunction (DFT, HF, MCSCF, CASSCF, sCI, etc..)

$$D_{k}^{S} = \left| \begin{array}{c} f_{1}(r_{1}) & \cdots & f_{1}(r_{N^{S}}) \\ \vdots & \ddots & \vdots \\ f_{N^{S}}(r_{1}) & \cdots & f_{N^{S}}(r_{N^{S}}) \end{array} \right| \left| \begin{array}{c} f_{i} = \overset{l=N_{b}}{\circ} C_{l}^{i} \mathsf{F}_{l} \\ \vdots & \vdots & \vdots \\ \text{Single-particle orbitals} \end{array} \right|$$

QMCPACK implements linear combination of atomic orbitals (LCAO) and Gaussian basis sets in (non)periodic boundary conditions.

$$\phi(\mathbf{r}) = R_l(r) Y_{lm}(\theta, \phi)$$

where  $Y_{lm}(\theta, \Phi)$  is a spherical harmonic, l and m are the angular momentum and its z component, and r,  $\theta$ ,  $\Phi$  are spherical coordinates.

Various codes are supported natively (through Nexus):

- PySCF, Gamess, Quantum Package, Quantum Espresso (Molecule in a box – but not LCAO)

Large number of codes supported through converters (molden2qmc: <a href="https://github.com/QMCPACK/molden2qmc">https://github.com/QMCPACK/molden2qmc</a>

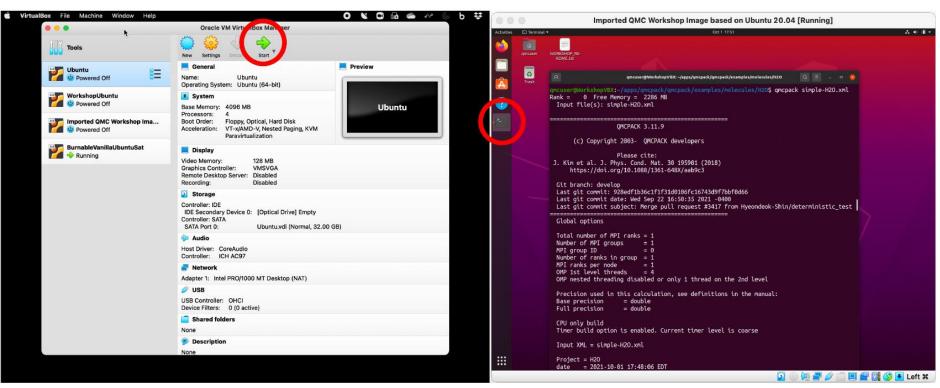
- TURBOMOLE, PSI4, CFOUR, ORCA, DALTON, MOLPRO, NWCHEM, QCHEM (generate a Molden output through this files, then calling molden2qmc as described in the tutorial)

Workshop Week 5: QMC for solids, Use of plane wave SPOs. Can also run "molecule in a box"

#### Starting the Lab: Virtual Machine

#### Start the Virtual Machine

#### Open a Terminal



# Starting the Lab: File Update & Navigation

#### Update workshop example files:

```
cd
$HOME/qmc_workshop_2021
git pull
```

#### Enter week 4 lab directory:

```
cd
$HOME/qmc_workshop_2021/week4_molecules
```

We will make intensive use of the Nexus framework. If you missed week3 tutorial, I recommend reviewing it on our YouTube channel, and running the lab before running this one!

#### Questions we answer in this lab:

- How to choose a trial wavefunction/method
- How to choose a basis set
- How to choose/optimize the Jastrow function
- How to select and correct for time steps in DMC
- How to manage population bias in DMC
- How to reduce the error bar in DMC
- How to systematically reduce the fixed-node approximation

### Application example: Beryllium dimer

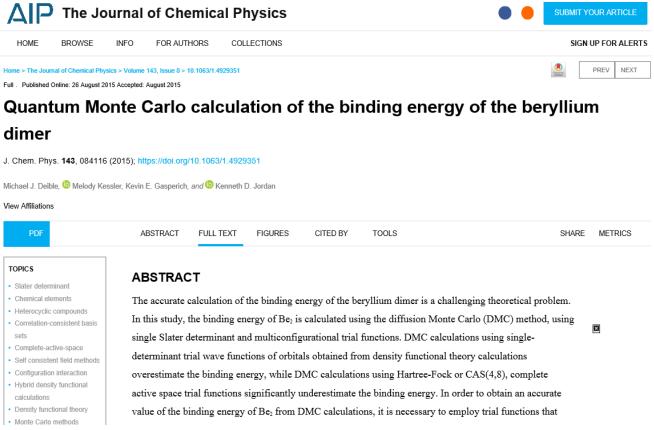


TABLE I. Total energies of Be and Be<sub>2</sub> and the Be<sub>2</sub> dissociation energy computed with DMC using various trial functions.

Trial function <sup>a</sup>	Total energy (a.u.)		
	Be <sup>b</sup>	Be <sub>2</sub>	$D_e (cm^{-1})$
HF/QZ-g	-14.657 30(4)	-29.317 89(6)	724(21)
LDA/QZ-g	-14.657 21(4)	-29.319 77(7)	1174(25)
PBE/QZ-g	-14.657 31(5)	-29.319 60(8)	1094(26)
BLYP/QZ-g	-14.657 25(4)	-29.319 56(8)	1113(26)
B3LYP/QZ-g	-14.657 27(3)	-29.319 46(8)	1079(23)
PBE0/QZ-g	-14.657 28(3)	-29.319 07(8)	992(21)
BH&HLYP/QZ-g	-14.657 26(5)	-29.318 91(7)	966(26)
BD/QZ-g	-14.657 18(4)	-29.318 72(7)	955(24)
$CAS(4,8)/QZ-fg^{c}$	-14.66723(1)	-29.337 07(3)	573(8)
CAS(4,16)/QZ-fg <sup>c</sup>	-14.667 30(1)	-29.338 32(3)	819(8)
Ext. CAS(4,16)/QZ-fg	-14.667 30(1)	-29.338 41(2)	838(7)
CAS(4,16)/QZ-g <sup>c</sup>	-14.667 27(2)	-29.338 38(3)	845(8)
Ext. CAS(4,16)/QZ-g	$-14.667\ 27(2)$	-29.338 45(2)	857(9)
CI/QZ-g <sup>c</sup>	-14.667 25(1)	-29.338 48(2)	873(6)
Ext. CI/QZ-g	-14.667 25(1)	-29.338 64(2)	908(6)
Experimental <sup>d</sup>	-14.667 356	-29.33897	934.9(4)

 $<sup>\</sup>overline{{}^{a}QZ}$  refers to the cc-pVQZ basis set. The "-g" and "-fg" indicate, respectively, that the g functions and f and g functions were omitted from the basis sets. Ext. refers to CAS and CI results extrapolated to the full configuration space for the active orbital list as described in the text.

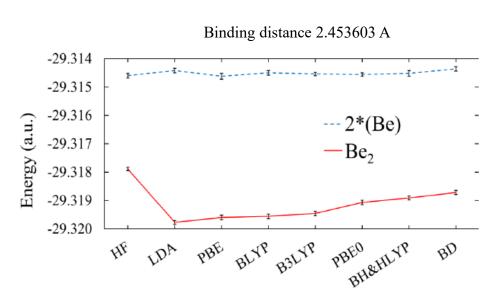


FIG. 3. DMC energies of twice the beryllium atom and the dimer for several single-determinant trial wave functions.

<sup>&</sup>lt;sup>b</sup>The DMC energies of the Be atom calculated using various single determinant trial functions should agree. The spread of the energies in the table is the result of statistical errors and the use of a finite (0.001 a.u.) time step.

<sup>&</sup>lt;sup>c</sup>0.001 threshold on CI coefficients for retained configurations.

<sup>&</sup>lt;sup>d</sup>The experimental D<sub>e</sub> value for Be<sub>2</sub> is from Ref. 5. The non-relativistic energy of the Be atom is from Ref. 60.

#### Outline

- I- Single determinant, all electrons calculations:
  - Setting up an all-electrons Calculation with Nexus (DFT)
    - Generating multiple Trial wavefunction (HF, DFT:LDA, GGA, Hybrids)
    - Effects of basis-sets on the trial wavefunction (cc-pcvXz | X=D,T,Q)
  - QMC Calculations
    - Wavefunction conversion
    - Cusp Correction
    - Jastrow Optimization
    - Effect of a Jastrow function on VMC and DMC calculation
  - Controlling the DMC approximations
    - Time-step Error
    - Population bias
    - Reducing error bars
  - Dependence of DMC to the trial wavefunction (SD-DMC)



Total 8e<sup>-</sup> (Be:4e<sup>-</sup>)

Experimental<sup>1</sup> total energy:-29.33897 Ha

Bond length<sup>1</sup>: 2.453603 Å

# Setting up an all-electrons Calculation with Nexus (DFT)

Varying the trial wavefunction (modifying the nodes – SCF study)

$$Y_T(R) = J(R)Y_{AS}(R) = e^{J_1 + J_2 + \cdots} \mathring{a}_k^M C_k D_k^-(f) D_k^-(f)$$
Nodes (HF, DFT, Basis-set etc..)

We will see how close to the exact solution, some mean-field solutions are:

- We will try HF, DFT {LDA, PBE, PBE0, SCAN}
- For each method/functional, we will use 4 basis-sets: cc-pvXz | X=d,t,q

### Using PySCF

- Using python3
- From PySCF Importing modules for density fitting (DF), self consistent calculations (SCF) and density Functional theory (DFT)
- Importing Gaussian type orbitals (GTO)
- Defining Atoms and coordinates (different ways to do)
- Defining a basis set, units, charge and spin.
- Defining the method:
  - RHF Restricted Hartree Fock
  - ROHF Restricted Open-shell Hartree Fock
  - UHF unrestricted Hartree Fock
  - RKS Restricted Kohn-Sham (DFT, requires specifying XC functional)
  - ROKS and UKS: Restricted Open-shell Kohn-Sham and Unrestricted Kohn-Sham (DFT, requires specifying XC functional)
- Running simulation (mf.kernel)
- Save to QMCPACK format:
  - Outside VM requires to add the location of QMCPACK script PyscfToQMCPACK.py to your PYTHONPATH
  - export PYTHONPATH=/mypath/qmcpack/src/QMCTools/:\$PYTHONPATH

File located in: ~/week4\_molecules/00\_dft/Be2.py

```
#! /usr/bin/env pvthon3
 mport numpy as np
 from numpy import array
### generated pyscfimport text ###
 from pyscf import df, scf, dft
### end generated pyscfimport text ###
### generated system text ###
 rom pyscf import gto as gto_loc
mol = gto_loc.Mole()
mol.verbose = 5
mol.atom
                    2.45360300
mol.basis
             = 'cc-pvtz'
mol.unit
mol.charge = 0
mol.spin
mol.symmetry = True
mol.build()
### end generated system text ###
### generated calculation text ###
mf = scf.ROHF(mol).density_fit()
mf.max_cycle=200
mf.level shift=0.0
mf.tol
               = '1e-10'
e scf = mf.kernel()
### end generated calculation text ###
### generated conversion text ###
  om PyscfToQmcpack import savetoqmcpack
savetoqmcpack(mol,mf,'scf')
### end generated conversion text ###
```

#### Using Nexus

- We need to import the module we will need for the simulation:
  - PySCF, physical system, multiple QMC sections we will need.

#### - Settings:

- Path for the result
- Seconds to sleep before checking if job is completed
- Machine: type of workstation (Nexus can submit jobs to HPC platforms such as Theta at ANL or Summit at ORNL)

#### - Physical system:

- Can read geometry from: xyz file, CIF file, raw coordinates, POSCAR file, etc..
- SCF run:
  - Recognizes all methods and "most" pyscf parameters. (please contact developers if a parameter is missing)
  - Note that the results will be written in the *path* section

grep "converged SCF energy =" runs/Be2/cc-pvtz/HF/SCF/scf.out converged SCF energy = -29.1338009143752 Ha

File located in: week4\_molecules/00\_dft/nx\_Be2\_scf.py

```
#! /usr/bin/env pvthon3
from nexus import settings, job, run_project, obj
from nexus import generate_physical_system
from nexus import generate_pyscf
# Obtain the core count of the local machine (lab only)
import os
cores = os.cpu_count()
settings(
    results
    sleep
               = 3.
    machine
               = 'ws'+str(cores),
system = generate_physical_system(
                                      # Be2 geometry located in the Be2.xyz file
    structure = 'Be2.xyz',
# perform Hartree Fock in all electron and a cc-pvtz basis set
scf = generate_pyscf(
    identifier = 'scf',
                                                 # log output goes to scf.out
               = 'Be2/cc-pvtz/HF/SCF',
                                                 # directory to run in
               = job(serial=True,app='python3'), # pyscf must run serially
    system
               = system,
                                                 # used to make Mole() inputs
               = obj(
        basis = 'cc-pvtz',
        symmetry = True,
        verbose = 5.
    calculation = obi(
                                                 # Restricted Orbital Hartree Fock
                    = 'ROHF',
                                                 # Density fitting
        df_fitting = True,
                                                 # Max SCF cycles
        max cycle = 200,
                                                 # Mixing orbitals for convergence
        level\_shift = 0.0,
                    = '1e-10'.
                                                 # Accuracy needed for convergence
   save_qmc = True ,
                                                 # Save the orbital to QMCPACK format
run_project()
```

# Plotting/analyzing your data (gnuplot)

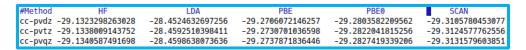
We will use a simple script to extract the energies from the output files using the qmca binary and plot them using gnuplot

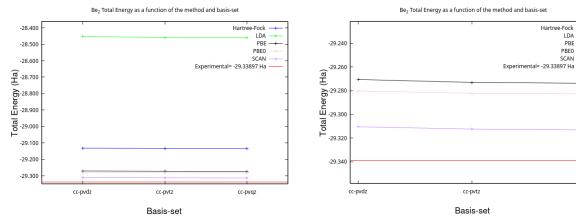
SCAN

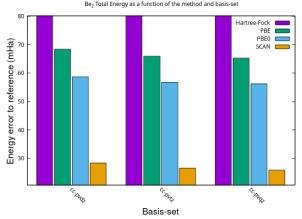
cc-pvqz

- Script name is Extract data scf.sh (will parse the output and put the energies in a correct format
- Type:

```
sh Extract data scf.sh
gnuplot Be2 TotEnergy SCF.gp; gnuplot Be2 EnergyDiff SCF.gp
```







- Large dependence on the functional

- SCAN particularly good but still not exact (25mHa)

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1- Choice of an Anti Symmetric wavefunction

$$Y_T(R) = J(R)Y_{AS}(R) = e^{J_1 + J_2 + \dots} \mathring{a}_k^M C_k D_k^-(f) D_k^-(f)$$

- 2- Converting/extracting QMC data from PYSCF output
- 3- Correcting orbitals for electron-nuclei cusp (all electron calculations only): Variance analysis
- 4- Adding 1 body (electron-ion), 2 body(electron-electron) and 3 body (electron-electron-ion) Jastrow functions: **Variance Analysis**
- 5- Run Diffusion Monte Carlo
  - Correct for time-step error
  - Control population bias
  - Reducing error bars

1- Choice of an Anti Symmetric wavefunction

$$Y_T(R) = J(R)Y_{AS}(R) = e^{J_1 + J_2 + \frac{1}{2}} \partial_k^M C_k D_k^{-}(f) D_k^{-}(f)$$

Nexus will check the directory path; if data is available and status is successful, the module will be skipped

This will generate an HDF5 file containing all data needed by QMCPACK

#### File located in: week4 molecules/01 qmc SD/nx Be2 qmc0.py

```
#! /usr/bin/env python3
from nexus import settings, job, run_project, obj
from nexus import ppset
from nexus import generate_physical_system
 rom nexus import generate pyscf
from nexus import generate_convert4qmc
from nexus import generate cusp correction
from nexus import generate_gmcpack
# Obtain the core count of the local machine (lab only)
cores = os.cpu count()
settings(
              = ''',
    results
               = 3,
    machine = 'ws'+str(cores),
system = generate_physical_system(
                                      # Be2 geometry located in the Be2.xvz file
    structure = 'Be2.xvz'.
XC=["SCAN"]
                                                        #Loop around multiple XC functionals
MyBasis=["cc-pvtz"]
                                                        #Loop around multiple basis sets
for x in XC:
    for y in MyBasis:
       # perform DFT
        scf = generate_pyscf(
            identifier = 'scf'.
                                                        # log output goes to scf.out
                       = 'Be2/'+y+'/'+x+'/SCF',
                                                        # directory to run in
                       = iob(serial=True.app='pvthon3'),# pvscf must run serially
            system
                      = system,
                      = obi(
                                                        # used to make Mole() inputs
                basis = v.
                symmetry = True,
                verbose = 5,
            calculation = obi(
                                                        # Restricted Orbital Kohn Sham
                                                        # Density fitting
                df_fitting = True,
                \max cycle = 200,
                                                        # Max SCF cycles
                level shift = 0.0.
                                                        # Mixing orbitals for convergence
                            = '1e-10',
                                                        # Accuracy needed for convergence
                                                        # Exchange and correlation functional
            save_qmc = True ,
                                                        # Save the orbital to OMCPACK format
```

File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc0.py

- 1- Choice of an Anti Symmetric wavefunction
- 2- Converting/extracting QMC data from PySCF output

- Nexus needs to know that it is an all electron calculation and we will want to correct for the electron-nuclei cusp, and where are the orbitals (scf tag).

```
# convert orbitals to QMCPACK format
c4q = generate_convert4qmc(
  identifier = 'c4q',
  path = 'Be2/'+y+'/'+x+'/SCF',  # directory to run in
  job = job(cores=1),
  add_cusp = True,  # Make sure to add Cusp Correction scheme
  dependencies = (scf,'orbitals'),  # Create a dependency to DFT success
)
```

File located in: week4 molecules/01 qmc SD/nx Be2 qmc0.py

- 1- Choice of an Anti Symmetric wavefunction
- 2- Converting/extracting QMC data from PySCF output

```
# calculate cusp correction
cc = generate_cusp_correction(
               = 'cusp',
               = 'Be2/'+v+'/'+x+'/SCF',
                                                 # directory to run in
  iob
               = job(cores=cores),
               = system.
 system
 dependencies = (c4q, 'orbitals'),
                                                 #Create dependency to converter
```

#### 3- Correcting orbitals for electron-nuclei cusp (all electron calculations only)

- At the nuclei, Gaussian basis sets are unable to describe the cusps in the single-particle orbitals (zero gradient at the nuclei on which they are centered).
- In VMC/DMC, the potential energy contribution to  $E_{\rm I}$  diverges as -Z/r when r~0. We need equal and opposite divergence in local kinetic energy.
- Using Gaussian Basis set, the kinetic energy is finite at the nucleus and E<sub>L</sub> diverges.
- The solution is to modify each molecular orbitals to obey the cusp condition at each nucleus; replacement of the orbital inside some small radius by a wellbehaved form.

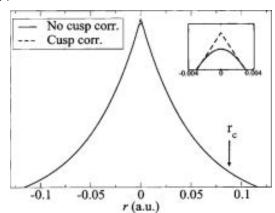
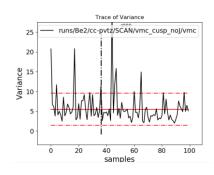


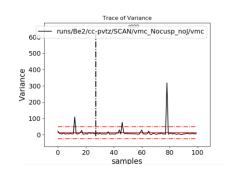
FIG.1 The 1s orbital of the Ne atom expanded in a Gaussian basis set with and without the cusp correction

File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc0.py

3- Correcting orbitals for electron-nuclei cusp (all electron calculations only)

Effect of Cusp correction can be seen by running both  $nx_Be2_qmc0.py$  and  $nx_Be2_qmc0_NoCusp.py$  files





```
# run VMC with cusp Correction and no Jastrow function
        qmc = generate_qmcpack(
          identifier
                       = 'Be2/'+y+'/'+x+'/vmc cusp noJ',# directory to run in
          path
          job
                       = iob(cores=cores),
                       = system.
          svstem
          iastrows
                       = 'vmc',
                                                         # vmc run
                                                         # equilibration steps
          warmupsteps
          blocks
                       = 100.
                                                         # number of blocks
                                                         # number of steps to avoid autocorellation
          steps
          timestep
                       = 0.1.
                                                         # timestep
          dependencies = orbdeps,
run_project()
```

gmca -g ev runs/Be2/cc-pvtz/SCAN/vmc Nocusp noJ/\*scalar.dat runs/Be2/cc-pvtz/SCAN/vmc cusp noJ/\*.scalar.dat

LocalEnergy Variance ratio
runs/Be2/cc-pvtz/SCAN/vmc\_Nocusp\_noJ/vmc series 0 -29.129717 +/- 0.048947
runs/Be2/cc-pvtz/SCAN/vmc\_cusp\_noJ/vmc series 0 -29.105796 +/- 0.031162

Variance ratio
0.4185
5.519650 +/- 0.■03832
0.1896

File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc0.py

- 1- Choice of an Anti Symmetric wavefunction
- 2- Converting/extracting QMC data from PySCF output
- 3- Correcting orbitals for electron-nuclei cusp (all electron calculations only)
- \*- Intermediate step

All non-QMC dependencies are now known to nexus and will be carried through various nexus blocks through the tag *orbdeps* 

- 4- Adding 1 body (electron-ion), 2 body(electron-electron) and 3 body (electron-electron-ion) Jastrow functions

$$Y_{T}(R) = J(R) Y_{AS}(R) = e^{J_{1}+J_{2}} \tilde{A}_{k}^{M} C_{k} D_{k}^{-}(f) D_{k}^{-}(f)$$

$$J_{1} = \int_{I}^{ion0} \sum_{i}^{e} u_{ab}(|r_{i} - R_{I}|) \qquad J_{2} = \sum_{i}^{e} \sum_{j>i}^{e} u_{ab}(|r_{i} - r_{j}|)$$

$$egin{aligned} u_{\sigma\sigma'I}(r_{\sigma I}, r_{\sigma'I}, r_{\sigma\sigma'}) &= \sum_{\ell=0}^{M_{eI}} \sum_{m=0}^{M_{eI}} \sum_{n=0}^{M_{ec}} \gamma_{\ell m n} r_{\sigma I}^{\ell} r_{\sigma'I}^{m} r_{\sigma\sigma'}^{n} \\ & imes \left(r_{\sigma I} - rac{r_c}{2}
ight)^3 \Theta\left(r_{\sigma I} - rac{r_c}{2}
ight) \\ & imes \left(r_{\sigma'I} - rac{r_c}{2}
ight)^3 \Theta\left(r_{\sigma'I} - rac{r_c}{2}
ight) \end{aligned}$$

- u<sub>ab</sub> is an interpolating 1D B-spline (tricubic spline in a linear grid) between zero distance and r<sub>cut</sub>.
- The cusp condition as  $r_i$  approaches  $r_i$  is set by the relative spin of the electrons
- MeI and Mee are the maximum polynomial orders of the electron-ion and electron-electron distances, respecttively, {Y<sub>imn</sub>} are the optimizable parameters (modulo constraints), r<sub>c</sub> is a cutoff radius, and r<sub>cut</sub> are the distances between electrons or ions a and b. i.e. The correlation function is only a function of the interparticle distances and not a more complex function of the particle positions, r. As indicated by the  $\Theta$  functions, correlations are set to zero beyond a distance of r./2 in either of the electron-ion distances and the largest meaningful electron-electron distance QMC Workshop 2021

- 4- Adding 1 body (electron-ion), 2 body(electron-electron) and 3 body (electron-electron-ion) Jastrow functions
  - We optimize the J1 and J2 parameters

```
# optimize 2-body Jastrow
optJ2 = generate gmcpack(
  identifier
                    = 'opt'.
                    = 'Be2/'+y+'/'+x+'/optJ2',
                                                        # directory to run in
  path
                    = job(cores=cores),
  iob
  system
                    = system.
  J2
                    = True,
                                    # 2-body B-spline Jastrow
  J1 rcut
                    = 6.0,
                                    # 6 Bohr cutoff for J1
                                    # 8 Bohr cutoff for J2
  J2 rcut
                    = 8.0.
  seed
                    = 42,
                                    # Fix the seed (lab only)
                    = 'opt',
                                    # Wavefunction optimization run
                    = 'oneshift'.
                                    # Energy minimization
  minmethod
  init cycles
                                    # 4 iterations allowing larger parameter changes
  cycles
                                    # 8 production iterations
                    = 8,
  warmupsteps
                    = 10.
  blocks
                    = 20.
                    = 3,
  steps
  timestep
                    = 0.1.
  init minwalkers
                    = 0.1,
  minwalkers
                    = 0.5,
                                    # VMC samples per iteration
  samples
                    = 25600.
  dependencies
                    = orbdeps.
```

#### runs/Be2/cc-pvtz/SCAN/optJ2/opt.in.xml

```
<jastrow type="One-Body" name="J1" function="bspline" source="ion0" print="yes">
           <correlation elementType="Be" size="12" rcut="6.0" cusp="0.0">
              <coefficients id="eBe" type="Array">
0 0 0 0 0 0 0 0 0 0 0
              </coefficients>
           </correlation>
        </jastrow>
        <jastrow type="Two-Body" name="J2" function="bspline" print="yes">
           <correlation speciesA="u" speciesB="u" size="16" rcut="8.0">
              <coefficients id="uu" type="Array">
              </coefficients>
           </correlation>
           <correlation speciesA="u" speciesB="d" size="16" rcut="8.0">
              <coefficients id="ud" type="Array">
              </coefficients>
           </correlation>
        </jastrow>
```

File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc1.py

- 4- Adding 1 body (electron-ion), 2 body(electron-electron) and 3 body (electron-electron-ion) Jastrow functions
- We optimize the J1 and J2 parameters (stochastic optimization via VMC; lower energy/variance means better parameters)

```
cd runs/Be2/cc-pvtz/SCAN/optJ2/
qmca -q ev *.scalar.dat | sort -k4
```

```
LocalEnergy
                                               Variance
                                                                  ratio
opt series 0 -29.152415 +/- 0.009964
                                         2.094150 +/- 0.020768
                                                                 0.0718
    series 2 -29.253657 +/- 0.004868
                                         0.413195 +/- 0.005872
                                                                 0.0141
    series 1 -29.259555 +/- 0.007212
                                         0.375314 +/- 0.006928
                                                                 0.0128
     series 5 -29.264656 +/- 0.006250
                                         0.461682 +/- 0.006575
                                                                 0.0158
    series 6 -29.265019 +/- 0.004714
                                         0.463221 +/- 0.008596
                                                                 0.0158
    series 9 -29.266346 +/- 0.008183
                                         0.492715 +/- 0.005705
                                                                 0.0168
    series 11 -29.267270 +/- 0.004427
                                         0.494253 +/- 0.004432
                                                                 0.0169
    series 8 -29.267562 +/- 0.005051
                                         0.503567 +/- 0.007467
                                                                 0.0172
    series 3 -29.268296 +/- 0.006235
                                         0.446392 +/- 0.005157
                                                                 0.0153
    series 4 -29.268767 +/- 0.006669
                                                                 0.0156
                                         0.457073 +/- 0.007368
     series 7 -29.270653 +/- 0.004499
                                         0.481380 +/- 0.004861
                                                                 0.0164
    series 10 -29.271025 +/- 0.004992
                                          0.497263 + / - 0.005199
                                                                 0.0170
```

```
<wavefunction name="psi0" target="e">
         <determinantset type="MolecularOrbital" href="../SCF/scf.h5" source="ion0" transform="yes" name="LCAOBSet" cuspCorrection="yes">
            <slaterdeterminant>
               <determinant id="updet" size="4" cuspInfo="../SCF/updet.cuspInfo.xml">
                  <occupation mode="ground">
                                                                                                 </occupation>
                  <coefficient size="60" spindataset="0">
                                                                                                              </coefficient>
               </determinant>
               <determinant id="downdet" size="4" cuspInfo="../SCF/downdet.cuspInfo.xml">
                  <occupation mode="ground">
                                                                                                 </occupation>
                  <coefficient size="60" spindataset="0">
                                                                                                              </coefficient>
        <iastrow type="One-Body" name="J1" function="bspline" source="ion0" print="yes">
            <correlation elementType="Be" size="12" rcut="6.0" cusp="0.0">
              <coefficients id="eBe" type="Array"> -1.036692517 -0.9491756812 -0.85382965 -0.7409253541 -0.639286145 -0.5468855822 -0.457551058
-0.3672189612 -0.2742578036 -0.1941760504 -0.1200012388 -0.06098051466</coefficients>
        <jastrow type="Two-Body" name="J2" function="bspline" print="yes">
            <correlation speciesA="u" speciesB="u" size="16" rcut="8.0">
               <col>
    id="uu" type="Array"> 0.286494837 0.2002724141 0.155101472 0.1186741914 0.09128333231 0.07007304412 0.05148561169 0
03365197704 0.01551622838 -0.000369036969 -0.01378501028 -0.02668143697 -0.03437087653 -0.0273251815 -0.0193908639 -0.01321158763</coefficients>
            </correlation>
            <correlation speciesA="u" speciesB="d" size="16" rcut="8.0">
              <coefficients id="ud" type="Array"> 0.6973392418 0.5437740857 0.4535660295 0.3935979623 0.3382767646 0.2900516436 0.2437848858 0.
993285683 0.1571844165 0.1192336806 0.08739279614 0.05667843986 0.03326895371 0.02371499997 0.0157137336 0.009161590998</coefficients>
         </jastrow>
     </wavefunction>
```

- Lowest energy achieved at series 010, best parameters optimized in iteration 009: opt.s009.opt.xml
- Note the reduction of he variance as the energy goes down.
- Ratio variance/energy gives good judgment on the variance (lower than 0.02 is a very good ratio)

File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc1.py

- 4- Adding 1 body (electron-ion), 2 body(electron-electron) and 3 body (electron-electron-ion) Jastrow functions
  - We optimize the J3 parameters after J1 and J2 are optimized

```
# optimize 3-body Jastrow
optJ3 = generate gmcpack(
  identifier
                    = 'opt'.
                    = 'Be2/'+v+'/'+x+'/optJ3'.
                                                       # directory to run in
  path
                    = iob(cores=cores).
  iob
  svstem
                    = svstem.
                                    # 3-body B-spline Jastrow
  J3
                    = True.
                                    # Fix the seed (lab only)
  seed
                    = 42,
                    = 'opt',
                                    # Wavefunction optimization run
  qmc
                    = 'oneshift', # Energy minimization
  minmethod
                                    # 4 iterations allowing larger parameter changes
  init cycles
  cycles
                                    # 8 production iterations
  warmupsteps
  blocks
                    = 20.
  steps
                    = 5.
  timestep
                    = 0.1.
  init_minwalkers
                    = 0.1.
  minwalkers
                    = 0.5,
  samples
                    = 25600.
                                    # VMC samples per iteration
  dependencies
                    = orbdeps+[(optJ2, 'jastrow')],
```

#### runs/Be2/cc-pvtz/SCAN/optJ3/opt.in.xml

```
<iastrow type="One-Body" name="J1" function="bspline" source="ion0" print="yes">
            <correlation elementType="Be" size="12" rcut="6.0" cusp="0.0">
              <coefficients id="eBe" type="Array">
-1.036692517 -0.9491756812 -0.85382965 -0.7409253541 -0.639286145 -0.5468855822
-0.4575510581 -0.3672189612 -0.2742578036 -0.1941760504 -0.1200012388 -0.06098051466
              </coefficients>
            </correlation>
         </iastrow>
         <jastrow type="Two-Body" name="J2" function="bspline" print="yes">
            <correlation speciesA="u" speciesB="u" size="16" rcut="8.0">
              <coefficients id="uu" type="Array">
0.286494837 0.2002724141 0.155101472 0.1186741914 0.09128333231 0.07007304412
0.05148561169 0.03365197704 0.01551622838 -0.000369036969 -0.01378501028
-0.02668143697 -0.03437087653 -0.0273251815 -0.0193908639 -0.01321158763
              </coefficients>
            </correlation>
            <correlation speciesA="u" speciesB="d" size="16" rcut="8.0">
              <coefficients id="ud" type="Array">
0.6973392418 0.5437740857 0.4535660295 0.3935979623 0.3382767646 0.2900516436
0.2437848858 0.1993285683 0.1571844165 0.1192336806 0.08739279614 0.05667843986
0.03326895371 0.02371499997 0.0157137336 0.009161590998
              </coefficients>
            </correlation>
         </jastrow>
         <jastrow type="eeI" name="J3" function="polynomial" print="yes" source="ion0">
            <correlation ispecies="Be" especies1="u" especies2="u" isize="3" esize="3" rcut="5.0">
              <coefficients id="uuBe" type="Array" optimize="yes"/>
            </correlation>
            <correlation ispecies="Be" especies1="u" especies2="d" isize="3" esize="3" rcut="5.0">
              <coefficients id="udBe" type="Array" optimize="yes"/>
            </correlation>
         </iastrow>
      </wavefunction>
```

File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc1.py

4- Adding 1 body (electron-ion), 2 body(electron-electron) and 3 body (electron-electron-ion) Jastrow functions

- We optimize the **J1**, **J2 AND J3** parameters

```
cd runs/Be2/cc-pvtz/SCAN/optJ3/
qmca -q ev *.scalar.dat | sort -k4
```

```
LocalEnergy
                                              Variance
                                                                 ratio
opt series 3 -29.268254 +/- 0.007506
                                        0.244048 + / - 0.003614
                                                                0.0083
opt series 0 -29.269403 +/- 0.004200
                                        0.494745 +/- 0.005474
                                                                0.0169
                                         0.267680 +/- 0.004092
    series 11 -29.276331 +/- 0.004007
                                                                 0.0091
    series 8 -29.277155 +/- 0.005009
                                        0.264350 +/- 0.004955
                                                                0.0090
    series 9 -29.279309 +/- 0.004174
                                        0.268449 +/- 0.008893
                                                                0.0092
    series 2 -29.281779 +/- 0.004483
                                        0.246311 +/- 0.003313
                                                                0.0084
    series 4 -29.282044 +/- 0.004457
                                        0.252980 +/- 0.003455
                                                                0.0086
    series 1 -29.284109 +/- 0.005932
                                        0.234446 +/- 0.005228
                                                                0.0080
    series 6 -29.285399 +/- 0.009696
                                        0.262893 +/- 0.008862
                                                                0.0090
    series 10 -29.286640 +/- 0.003885
                                         0.263126 +/- 0.002738
                                                                 0.0090
    series 7 -29.287853 +/- 0.003120
                                        0.254136 +/- 0.004671
                                                                0.0087
opt series 5 -29.288128 +/- 0.004488
                                        0.247736 +/- 0.003564
                                                                0.0085
```

- Lowest energy achieved at series 005, best parameters optimized in iteration 004: **opt.s004.opt.xml**
- Some of the electron correlation effects in J1 and J2 are affected by J3, hence full reoptimization of J1 and J2 is needed

```
?xml version="1.0"?>
 <wavefunction name="psi0" target="e">
         <determinantset type="MolecularOrbital" href=".../SCF/scf.h5" source="ion0" transform="yes" name="LCAOBSet" cuspCorrection=</pre>
            <slaterdeterminant>
              <determinant id="updet" size="4" cuspInfo="../SCF/updet.cuspInfo.xml">
                 <occupation mode="ground">
                                                                                                 </occupation>
                  <coefficient size="60" spindataset="0">
                                                                                                              </coefficient>
              <determinant id="downdet" size="4" cuspInfo="../SCF/downdet.cuspInfo.xml">
                 <occupation mode="ground">
                                                                                                 </occupation>
                 <coefficient size="60" spindataset="0">
                                                                                                              </coefficient>
              </determinant>
            </slaterdeterminant>
        </determinantset>
        <iastrow type="One-Body" name="J1" function="bspline" source="ion0" print="yes">
            <correlation elementType="Be" size="12" rcut="6.0" cusp="0.0">
              <coefficients id="eBe" type="Array"> -1.299983246 -1.183412295 -1.009573911 -0.8924886749 -0.7590911094 -0.539570117
 -0.4614140423 -0.3606319321 -0.2747886299 -0.1932344795 -0.1203174429 -0.06144056575</coefficients>
        <jastrow type="Two-Body" name="J2" function="bspline" print="yes">
           <correlation speciesA="u" speciesB="u" size="16" rcut="8.0">
              <coefficients id="uu" type="Array"> 0.3142959259 0.2371252083 0.1776026558 0.1338254218 0.1022842678 0.08005437084
.06236689886 0.0446936029 0.02761499316 0.01192522851 -0.001028569266 -0.01398351476 -0.02222915965 -0.01730293957 -0.0124356745 -
.008510647734</coefficients>
           </correlation>
           <correlation speciesA="u" speciesB="d" size="16" rcut="8.0">
              <coefficients id="ud" type="Array"> 0.9597802065 0.7517309829 0.5699293731 0.4339576349 0.3350611863 0.2820777488 0.
2423013536 0.2002422849 0.160596697 0.124562161 0.09420381054 0.06560106389 0.04332410727 0.03395272133 0.02342932223 0.01493720409
        </jastrow>
        <iastrow type="eeI" name="J3" function="polynomial" print="yes" source="ion0">
            <correlation ispecies="Be" especies1="u" especies2="u" isize="3" esize="3" rcut="5.0">
              <coefficients id="uuBe" type="Array" optimize="yes"> -0.004206845037 -1.500259898e-06 0.01424943211 0.001271344092
.004010698539 0.000290233957 0.006468551918 0.001398783433 0.01788778613 -0.001625400806 0.001264699615 -0.01196958723 -0.00632652
5316 0.0009183695881 0.002194130537 0.0008426467211 0.0005102280408 -0.002346602199 0.0003363102911 0.004200270529 0.002520303643
.004729355109 -0.002514671044 -0.0008406753613 -0.003043595073 0.001623060765</coefficients>
           <correlation ispecies="Be" especies1="u" especies2="d" isize="3" esize="3" rcut="5.0">
              <coefficients id="udBe" type="Array" optimize="yes"> -0.001276239878 -0.002606274218 0.01349269463 -0.002045781279
.002332224448 -0.0002758375536 -0.001211862742 -0.003148054288 0.0293132779 0.002642747618 0.002991168074 -0.01866694899 -0.01686
94921 -0.0004313174292 0.01136595659 0.001804653231 -0.001181381798 0.007250084821 0.01486076966 0.008665070969 -0.00827841117 -0.0
002539213093 -0.001825210376 0.009459478566 -0.004456789435 0.00103412212</coefficients>
        </jastrow>
     </wavefunction>
</amcsvstem>
```

File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc1.py

- 4- Adding 1 body (electron-ion), 2 body(electron-electron) and 3 body (electron-electron-ion) Jastrow functions
  - We compare energies from VMC\_NoJ, VMC\_2J, VMC\_3J

```
LocalEnergy Variance ratio runs/Be2/cc-pvtz/SCAN/vmc_NoJ/vmc series 0 -29.122630 +/- 0.008140 6.293397 +/- 0.650270 0.2161 runs/Be2/cc-pvtz/SCAN/vmc_2J/vmc series 0 -29.264403 +/- 0.002655 0.497976 +/- 0.002821 0.0170 runs/Be2/cc-pvtz/SCAN/vmc_3J/vmc ■series 0 -29.281952 +/- 0.002211 0.262596 +/- 0.002101 0.0090
```

- Significant improvement of <u>the variance</u> and energy (better trial wavefunction) when using 1, 2 and 3 body Jastrow function
- Better trial wavefunction => **lower variance** => lower error bar (error bar ~4x smaller => needs 16x more CPU time to reach similar accuracy)

File located in: week4 molecules/01 qmc SD/nx Be2 qmc1.py

- 4- Adding 1 body (electron-ion), 2 body(electron-electron) and 3 body (electron-electron-ion) Jastrow functions
  - We compare energies from DMC NoJ, DMC 2J, DMC 3J

```
LocalEnergy
                                                                            Variance
                                                                                               ratio
runs/Be2/cc-pvtz/SCAN/dmc_NoJ/dmc series 1 -29.322531 +/- 0.002778
                                                                      5.032637 +/- 0.029377
                                                                                               0.1716
runs/Be2/cc-pvtz/SCAN/dmc 2J/dmc
                                   series 1 -29.319212 +/- 0.000941
                                                                      0.492822 +/- 0.001771
                                                                                               0.0168
runs/Be2/cc-pvtz/SCAN/dmc 3J/dmc
                                   series 1 -29.318362 +/- 0.000797
                                                                      0.258312 +/- 0.001667
                                                                                               0.0088
```

In All electron calculations, adding a Jastrow function improves significantly the variance, but eventually energies converges to the same value

> Speedup of ~8X 20X better variance

Keep in mind!!: Difference of energy between J2 and J3 is : 0.4 +/-1.33 mHa Same energies!!! Difference of energy between NoJ and J3 is: 4.1 +/- 2.9mHa within 2 sigma

Questions?

### Break

How to set up time step, number of blocks, number of steps and number of walkers

- Extrapolate the time-step
- Control population bias
  - Reducing error bars

File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc2.py

Goal: Extrapolate the time-step

```
Change of file
```

```
#### DMC BLOCKS FOR TIME STEP EXTRAPOLATION
       # run DMC with cusp Correction and 1,2 and 3 Body Jastrow function
       qmc = generate_qmcpack(
          identifier
                         = 'dmc',
          seed
                         = 'Be2/'+y+'/'+x+'/dmc_tstep',
                                                              # directory to run in
          path
                                                               # Submit with the number of cores available
          job
                         = job(cores=cores),
          system
                          = system,
                         = [].
          iastrows
                         = 'dmc',
         vmc_samples
                                                               # Number of Samples (selected from a VMC step)
                          = 4096.
                                                               # Number of Equilibration steps
         warmupsteps
                          = 50,
         vmc blocks
                         = 200,
                                                               # Number of VMC blocks (To generate the DMC samples)
                                                               # Number of VMC steps (To generate DMC samples)
          vmc steps
                          = 20.
                                                               # VMC Timestep (To Generate DMC samples)
          vmc timestep
                         = 0.3.
                                                               # DMC timestep
          timestep
                          = 0.01.
         timestep_factor = 0.5,
                                                               # Reduce by 1/2
         ntimesteps
                         = 4,
                                                               # 4 times, i.e. [0.01, 0.005, 0.0025, 0.00125] timesteps
                                                               # start with small number for large timesteps [autocorrelation]
                          = 20.
          steps
                                                               # Number of DMC blocks
          blocks
                         = 400.
                                                               # Dependece (1B and 2B Jastrows)
          dependencies
                         = orbdeps+[(optJ3, 'jastrow')],
run_project()
```

File located in: week4 molecules/01 qmc SD/nx Be2 qmc2.py

Extrapolate Time Step

We evaluate autocorrelation times for each time step

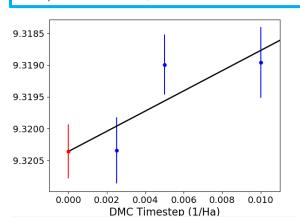
```
qmca -q e *s00{1,2,3,4}*.scalar.dat --sac

dmc series 1 LocalEnergy = -29.319165 +/- 0.000422 2.7
dmc series 2 LocalEnergy = -29.319135 +/- 0.000471 4.3
dmc series 3 LocalEnergy = -29.320283 +/- 0.000544 4.7
dmc series 4 LocalEnergy = -29.319607 +/- 0.000396 3.3
```

qmc-fit ts -e 20 -b '2 4 4 ' -t '0.01 0.005 0.0025' \*s00{1,2,3}\*scalar\*

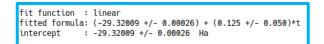
qmc-fit ts -e 20 -b '2 4 4 3' -t '0.01 0.005 0.0025 0.00125' \*s00{1,2,3,4}\*scalar\*

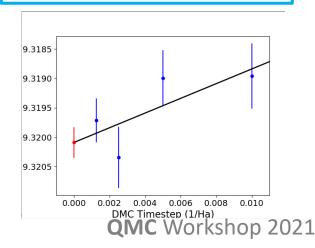
```
fit function : linear
fitted formula: (-29.32036 +/- 0.00043) + (0.159 +/- 0.066)*t
intercept : -29.32036 +/- 0.00043 Ha
```



The extrapolation is performed by resampling the data at each timestep (jackknife resampling), making a fit to each resampled mean, and then observing the distribution of extrapolated zero time intercepts. We have reblocked the data by a factor of 8 (averaged 8 blocks into single new blocks) to remove autocorrelation.

```
Time steps=0.0025 Ha<sup>-1</sup>
Steps =80
```





File located in: week4\_molecules/01\_qmc\_SD/nx\_Be2\_qmc3.py

Goal: Population bias

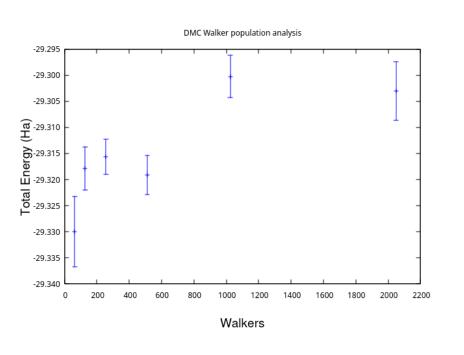
```
Change of file
```

```
#### DMC BLOCKS FOR POPULATION BIAS ANALYSIS
       # run DMC with cusp Correction and 1.2 and 3 Body Jastrow function
        pop=64
       while pop<2049:
          qmc = generate qmcpack(
                             = 'dmc pop'+str(pop),
             identifier
             seed
             path
                             = 'Be2/'+y+'/'+x+'/dmc_pop',
                                                                  # directory to run in
             iob
                                                                  # Submit with the number of cores available
                             = iob(cores=cores),
             system
                             = system,
                             = [],
             iastrows
                             = 'dmc',
                                                                  # Number of Samples (selected from a VMC step)
            vmc_samples
                             = pop,
            warmupsteps
                             = 0,
                                                                  # Number of Equilibration steps
            vmc blocks
                                                                  # Number of VMC blocks (To generate the DMC samples)
                             = 10,
                                                                  # Number of VMC steps (To generate DMC samples)
                             = 1,
             vmc steps
                                                                  # VMC Timestep (To Generate DMC samples)
             vmc timestep
                             = 0.3,
             timestep
                             = 0.01.
                                                                  # DMC timestep
                                                                  # number of step*population maintained constant to maintain error bar
             steps
                             = 20480//pop.
                                                                  # Number of DMC blocks
             blocks
                             = 10.
                                                                  # Dependece (1B and 2B Jastrows)
                             = orbdeps+[(optJ3, 'jastrow')],
             dependencies
           pop=pop*2
run_project()
```

We avoid equilibration time in DMC to show the population bias and loop through multiple walker configurations

File located in: week4 molecules/01 qmc SD/nx Be2 qmc3.py

#### Goal: Population bias



- We will use a simple script to extract the dmc energies from each run with increased population and plot them using gnuplot
- Script name is Extract\_data\_qmc\_Pop.sh (will parse the output and put the energies in a correct format)
- Type: sh Extract data qmc Pop.sh
- You can look at the script to generate the plots by typing:

```
cat Be2_dmc_pop_bias.gp
gnuplot Be2 dmc pop bias.gp
```

Using a population of 1024 seem to be enough to converge the energy Using 512 walkers would introduce a ~20mHa bias in the energy

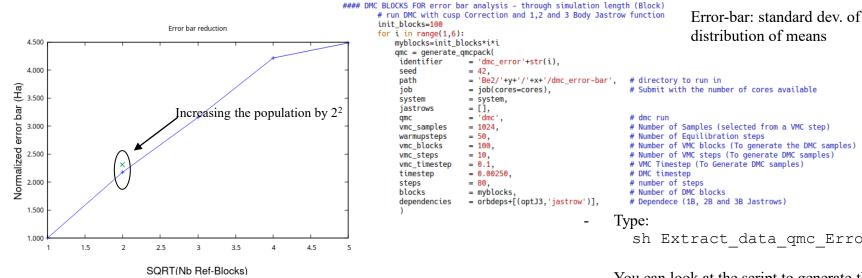
File located in:

week4 molecules/01 qmc SD/nx Be2 qmc4.py



#### Goal: Reducing the error bars

To reduce the error bar by a factor N, multiply the population or the number of blocks by  $N^2$ 



# Number of VMC blocks (To generate the DMC samples)

sh Extract data qmc Error-bar.sh

You can look at the script to generate the plots by typing:

```
cat Be2 dmc pop bias.gp
gnuplot Be2 dmc pop bias.gp
```

Small computer -> reduce population and run longer

Large computer -> increase population and run shorter

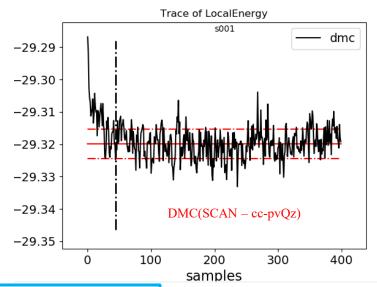
QMC Workshop 2021

#### Running a DMC Calculation

File located in: week4 molecules/01 qmc SD/nx Be2 qmc5.py

```
Change of file
```

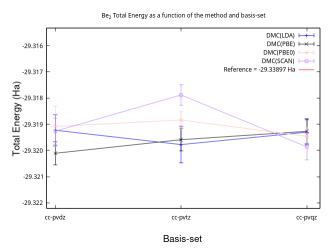
```
XC=["LDA","PBE","PBE0","SCAN"]
MyBasis=["cc-pvdz","cc-pvtz","cc-pvqz"]
for x in XC:
     for y in MyBasis:
          # perform DFT
 # run DMC with cusp Correction and 1,2 and 3 Body Jastrow function
 qmc = generate_qmcpack(
   identifier
                  = 'dmc',
   seed
                  = 42.
                  = 'Be2/'+y+'/'+x+'/dmc',
   path
                                                       # directory to run in
   iob
                  = job(cores=cores),
                                                       # Submit with the number of cores available
   system
                  = system,
   jastrows
                  = [],
                  = 'dmc'
   vmc samples
                  = 4096
                                                        # Number of Samples (selected from a VMC step)
   warmupsteps
                  = 100.
                                                        # Number of Equilibration steps
   vmc blocks
                  = 100.
                                                        # Number of VMC blocks (To generate the DMC samples)
   vmc steps
                  = 10.
                                                        # Number of VMC steps (To generate DMC samples)
   vmc_timestep
                  = 0.3.
                                                        # VMC Timestep (To Generate DMC samples)
   timestep
                  = 0.00250,
                                                        # DMC timestep
                  = 80.
                                                        # number of steps
   steps
                                                        # Number of DMC blocks
   blocks
                  = 400.
   dependencies
                  = orbdeps+[(optJ3,'jastrow')],
                                                        # Dependece (1B and 2B Jastrows)
```



```
qmca -q ev runs/Be2/cc-pvqz/SCAN/dmc/*.s001.scalar.dat
LocalEnergy Variance ratio
runs/Be2/cc-pvqz/SCAN/dmc/dmc series 1 -29.319851 +/- 0.000505 0.215959 +/- 0.000217 0.0074
```

### Plotting/analyzing your data (gnuplot)

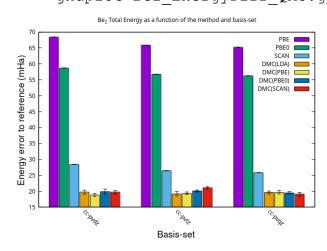
- We will use a simple script to extract the energies from the output files and plot them using gnuplot
- Script name is Extract\_data\_qmc.sh (will parse the output and put the energies in a correct format
- Type:
  sh Extract data qmc.sh



All DMC energies within each other's error bar (almost no dependence to basis-set or starting point)

You can generate the plot by typing:

gnuplot Be2\_TotEnergy\_QMC.gp
gnuplot Be2 EnergyDiff QMC.gp



Systematic improvement of DMC over DFT

Questions?

### Setting up an ECP DMC Calculation

#### Application to Be2 molecule

The use of ECPs reduces the number of electrons to be evaluated explicitly

Same steps as all electron calculations but we need to redo study for:

How to set up time step, number of blocks, number of steps and number of walkers

- Extrapolate the time-step
- Control population bias
  - Reducing error bars

pseudo\_dir = 'pseudopotentials',
 results = '',
 sleep = 3,
 machine = 'ws'+str(cores),
 )

ppset(
 label = 'ccecp',
 qmcpack = ['Be.ccECP.xml'],
 )

system = generate\_physical\_system(
 structure = 'Be2.xyz',
 Be=2,
 )

-ECP and all

Worth spending a few minutes on pointing out the difference between cc-ECP and all electron calculations

#### Setting up a DMC Calculation

File located in: week4 molecules/02 qmc ccECP/nx Be2 qmc0.py

Effect of Jastrows on VMC and DMC energy and variance



#### All electrons VMC

		LocalEnergy	Variance	ratio
runs/Be2/cc-pvtz/SCAN/vmc_NoJ/vmc	series 0	-29.122630 +/- 0.008140	6.293397 +/- 0.650270	0.2161
runs/Be2/cc-pvtz/SCAN/vmc_2J/vmc	series 0	-29.264403 +/- 0.002655	0.497976 +/- 0.002821	0.0170
runs/Be2/cc-pvtz/SCAN/vmc_3J/vmc	series 0	-29.281952 +/- 0.002211	0.262596 +/- 0.002101	0.0090

#### All electrons DMC

1			LocalEnergy	Variance	ratio
	runs/Be2/cc-pvtz/SCAN/dmc_NoJ/dmc runs/Be2/cc-pvtz/SCAN/dmc_2J/dmc runs/Be2/cc-pvtz/SCAN/dmc_3J/dmc	series 1	-29.312531 +/- 0.002778 -29.319212 +/- 0.000941 -29.318362 +/- 0.000797		0.1716 0.0168 0.0088

$$\widehat{H} = -\frac{1}{2}\nabla^2 + V_{ee} + V_{eI} + V_{II} + V_{FN} + (\Psi_T^{-1}V_{eI}\Psi_T - V_{eI})$$

Fixed node constraint

Pseudopotential localization

#### ccECP VMC

		LocalEnergy	Variance	ratio
runs/Be2/Calibration/vmc_NoJ/vmc	series 0	-1.906315 +/- 0.002627	0.141744 +/- 0.005848	0.0744
runs/Be2/Calibration/vmc_2J/vmc	series 0	-1.995480 +/- 0.001028	0.037666 +/- 0.001119	0.0189
runs/Be2/Calibration/vmc_3J/vmc	series 0	-1.999279 +/- 0.001005	0.042458 +/- 0.001270	0.0212

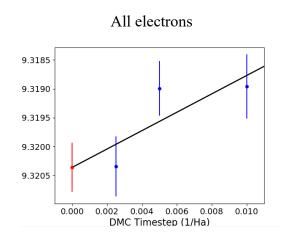
#### ccECP DMC

		LocalEnergy	Variance	ratio
runs/Be2/Calibration/dmc_NoJ/dmc	series 1	-2.000624 +/- 0.002397	0.085552 +/- 0.001534	0.0428
runs/Be2/Calibration/dmc_2J/dmc	series 1	-2.010426 +/- 0.000499	0.036481 +/- 0.000387	0.0181
runs/Be2/Calibration/dmc_3J/dmc	series 1	-2.012832 +/- 0.000589	0.043121 +/- 0.001206	0.0214

- The Jastrow will act on the local part of the pseudopodential (More details in lecture #6 of the Workshop) *e.g* DMC with and without Jastrows will not necessarily converge to the same energy.
- VMC and DMC calculations speed up by the use of Jastrows

### Setting up a DMC Calculation

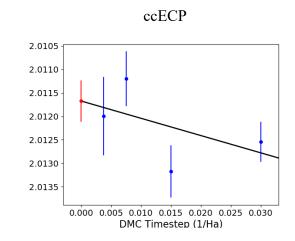
Time step study



```
fit function : linear
fitted formula: (-29.32036 +/- 0.00043) + (0.159 +/- 0.066)*t
intercept : -29.32036 +/- 0.00043 Ha
```

File located in: week4 molecules/02 qmc ccECP/nx Be2 qmc1.py





```
fit function : linear
fitted formula: (-2.01167 +/- 0.00044) + (-0.037 +/- 0.021)*t
intercept : -2.01167 +/- 0.00044 Ha
```

- When using ECPs, DMC is significantly less sensitive to the time step error (compared to all electrons calculations)
- The time step error is likely to benefit from cancellation of error when calculating energy differences

#### **Atomization Energy**

All electrons

Experimental: -4.26mHA

ccECP

Single Atom reference:

DFT-SCAN = -14.649312 Ha

DMC-SCAN = -14.657269 + /-0.000815 Ha

Be2 dimer total energy:

DFT-SCAN -29.3124577 Ha

DMC-SCAN = -29.32036 + /-0.00043 Ha

Be2 atomization energy:

DFT-SCAN = -13.83 mHa

DMC-SCAN = -5.82 + / -0.9 mHa

Single Atom reference:

DFT-SCAN = -0.994018 Ha

DMC-SCAN =-1.00412 +/-0.00042 Ha

Be2 dimer total energy:

DFT-SCAN -1.999310 Ha

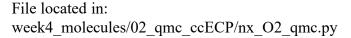
DMC-SCAN = -2.01167 + -0.00044 Ha

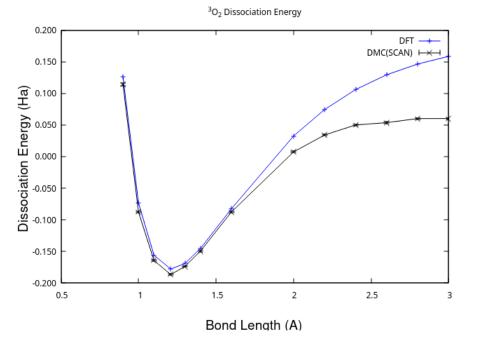
Be2 atomization energy:

DFT-SCAN = -11.27 mHa

DMC-SCAN = -3.43 + / -0.65 Ha

### <sup>3</sup>O<sub>2</sub> Dissociation curve





Trial WF:DFT-SCAN / ccECP cc-pvtz Spin State: Triplet

$$E_d^{exp} = 0.18816 \text{ Ha}$$

$$E_d^{DFT} = 0.1805 \text{ Ha}$$

$$E_d^{DMC}=0.1864 (5) \text{ Ha}$$

- DMC dissociation energy of O2 in very good agreement with experimental value
- Using ECPs (less electrons) and Nexus, it is possible to drive a full dissociation curve automatically (but verification is always necessary!)

Questions?

# Examples of applications

### Systematic reduction of the fixed node error

The fixed node error can be systematically reduced for both solids and molecules by increasing the complexity of the trial wavefunction.

$$\Psi_{T}(R) = J(R)\Psi_{AS}(R) = e^{J_{1}+J_{2}+...}\sum_{k} c_{k} \sum_{q} D_{k,q}^{\uparrow}(R^{\uparrow})D_{k,q}^{\downarrow}(R^{\downarrow})$$
Multideterminant expansion

#### Correlation (Jastrow)

$$\boldsymbol{J}_1 = \sum_{i}^{N} \sum_{l}^{N_{ions}} \boldsymbol{u}_1 \big( \big| \boldsymbol{r}_i - \boldsymbol{r}_l \big| \big)$$

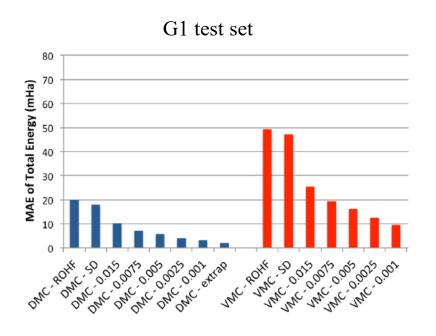
$$J_2 = \sum_{i \neq j}^{N} u_2 \Big( |r_i - r_j| \Big)$$

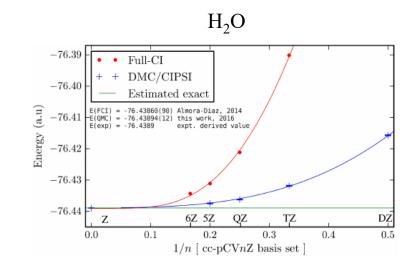
- Using advanced trial wavefunctions like CASSCF, or selected Configuration Interaction (sCI)
- Orbital optimization
- Using backflow
- Combination of all the above
- (..)

### Using multideterminants

- sCI evolves in Hilbert space
- DMC evolves in real space

Strategy: Increase the complexity of the trial wavefunction using a multideterminant expansion



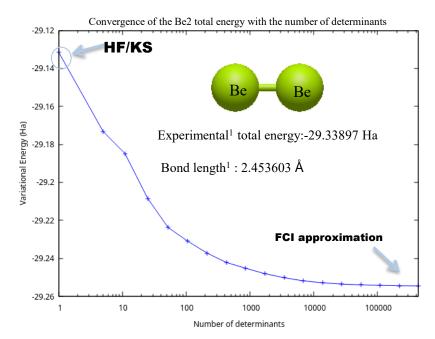


Basis set	FCI size	# dets used in DMC	$E_0^{var}$	$FCI,\ Almora-Dìaz[27]$	Deviation
cc-pCVDZ	$\sim 10^{10}$	172 256	-76.282136	-76.282865	0.0007
cc-pCVTZ	$\sim 2.10^{14}$	640 426	-76.388287	-76.390158	0.0018
cc-pCVQZ	$\sim 2.10^{17}$	666 927	-76.419324	-76.421148	0.0018
cc-pCV5Z	$\sim 7.10^{19}$	$1\ 423\ 377$	-76.428550	-76.431105	0.0025

Caffarel et. al , J. Chem. Phys. 144, 151103 (2016); http://dx.doi.org/10.1063/1.4947093

Morales et al. J. Chem. Theory Comput. 8, 2181–2188, (2012)

### Using sCI (CIPSI flavor)



- Convergence at 0.1 mHa with 0.45M determinants
- Selected CI (CIPSI) systematically reduces the energy
- Selecting all determinants leads rigorously to the FCI energy
- Refer to QMCPACK manual For details about how to generate the trial wavefunction Quantum Package 2

1. Define a reference wave function:

$$|\Psi\rangle = \sum_{i \in D} c_i |i\rangle$$
  $E_{var} = \frac{\langle \Psi | \hat{H} | \Psi \rangle}{\langle \Psi | \Psi \rangle}$ 

2. Generate external Determinants

All single and double excitations

3. Second order perturbative contribution of each determinant  $|\alpha\rangle$ 

$$\Delta E = \frac{\langle \Psi | \hat{H} | \alpha \rangle \langle \alpha | \hat{H} | \Psi \rangle}{E_{var} - \langle \alpha | \hat{H} | \alpha \rangle}$$

- 4. Select  $|\alpha\rangle$ 's with largest  $\Delta E_{\alpha}$  and add them to Determinant space (D)
- 5. Diagonalize  $\hat{H}$  in D then update  $|\Psi\rangle$  and  $E_{var}$
- 6. Iterate until reaching convergence.

#### Running a DMC Calculation

File located in: week4 molecules/03 qmc MD/nx Be2 ae qmc workflow.py

#### Important:



- QP2 is not installed in the VM! It is recommended to follow the tutorial on QP2 from the 2019 QMCPACK workshop <a href="https://github.com/QMCPACK/qmcpack\_workshop\_2019">https://github.com/QMCPACK/qmcpack\_workshop\_2019</a>
- The multideterminant trial wavefunction generated with QP2 is provided in week4\_molecules/02\_qmc\_MD/Refs/Be2/QP/QP.h5
- Calculations are started from the existing H5 File
- We follow same steps for time step extrapolation as SD runs

```
# convert orbitals to QMCPACK format
c4q = generate_convert4qmc(
   identifier = 'c4q',
   path = 'Be2/QP',
   job = job(cores=1),
   add_cusp = True,
   multidet = 'QP.h5',
   orbitals = 'QP.h5',
}
```

#### sCI workflow

We generate initial orbitals from HF in a cc-pvtz basis-set

We generate a multideterminant wavefunction using CIPSI and converge the energy to the FCI limit (0.5M determinants)

We truncate the wavefunction to keep only coefficients larger than 10<sup>-5</sup> (395 determinants)

#### Running a DMC Calculation

File located in: week4\_molecules/03\_qmc\_MD/nx\_Be2\_ae\_qmc\_workflow.py

CIPSI Variational Energy -29.2331 Ha

#### Single Determinant DMC

#### Multideterminant DMC

```
qmca -q ev runs/Be2/dmc_msd/*.scalar.dat

LocalEnergy Variance ratio

VMC series 0 -29.333057 +/- 0.000908 0.104126 +/- 0.001649 0.0035

DMC series 3 -29.337331 +/- 0.000403 0.107536 +/- 0.001219 0.0037
```

Experimental<sup>1</sup> total energy:-29.33897 Ha

- Small MSD expansion corrects the total energy to 1.5 +/- 0.5 mHa from experimental energy
- VMC energy with MSD wavefunction significantly more accurate than SD-DMC (Smaller variance)

#### Noncovalent Interactions



# Quantum Monte Carlo Methods Describe Noncovalent Interactions with Subchemical Accuracy

Matúš Dubecký,\*,† Petr Jurečka,† René Derian,‡ Pavel Hobza,<sup>§,†</sup> Michal Otyepka,† and Lubos Mitas<sup>||</sup>

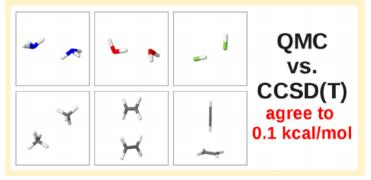
Journal of Chemical Theory and Computation

Letter

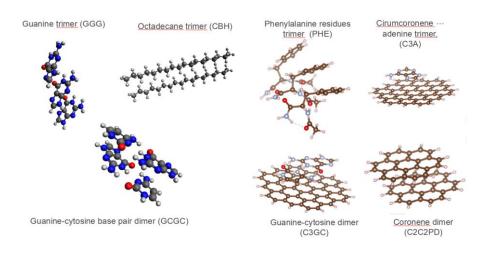
Table 1. Calculated FN-DMC Interaction Energies (kcal/mol), Based on B3LYP/aug-TZV Guiding Functions, Compared to the Previous FN-DMC and Reference CCSD(T)/CBS Data s,40 Together with the Corresponding Differences  $\Delta^a$ 

complex	reference	FN-DMC <sup>b</sup>	$\Delta^b$	FN-DMC <sup>c</sup>	$\Delta^c$
ammonia dimer	-3.15	$-3.19 \pm 0.09$	0.04	$-3.10 \pm 0.06$	-0.05
water dimer	-5.07	$-5.34 \pm 0.09$	0.27	$-5.15 \pm 0.08$	0.08
hydrogen fluoride dimer	-4.58			$-4.68 \pm 0.10$	0.10
methane dimer	-0.53	$-0.48 \pm 0.08$	-0.05	$-0.44 \pm 0.05$	-0.09
ethene dimer	-1.48	$-1.38 \pm 0.13$	-0.10	$-1.47 \pm 0.09$	-0.01
ethene/ethyne	-1.50	$-1.22 \pm 0.12$	-0.28	$-1.56 \pm 0.08$	0.06
benzene/water	-3.29	$-3.69 \pm 0.24$	0.40	$-3.53 \pm 0.13$	0.24
benzene/methane	-1.45	$-0.63 \pm 0.21$	-0.87	$-1.30 \pm 0.13$	-0.15
benzene dimer T	-2.71	$-3.77 \pm 0.39$	1.06	$-2.88 \pm 0.16$	0.17

 $<sup>^{</sup>a}$ The reference values for the test set (the top panel) are obtained by extrapolation of CCSD(T) (aug-TZV, aug-QZV) to the CBS limit, while for larger complexes (the bottom panel), the estimates combine contributions from MP2/CBS (aug-TZV, aug-QZV) and CCSD(T)/CBS (aug-DZV, aug-TZV).  $^{b}$ Körth et al.  $^{26}$   $^{c}$ This work.



### L7 Benchmark (van der Waals dominated molecules)



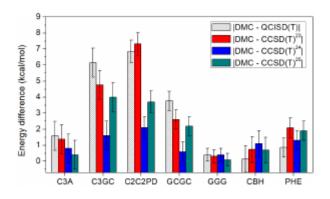


FIG. 1. Binding energy differences in kcal/mol relative to QCISD(T) and CCSD(T).

- DMC in all electrons (up to 5000 MO) at CBS limit.
- CCSD(T) with ecp and approximated CBS.
- DMC in very good agreement with CCSD(T)
- DMC all electrons and ECP from different basissets, functionals and codes reach exact same binding energies

	CASINO1	QMCPACK <sup>2</sup>	Δ
GGG	-1.5+/- 0.3	-2.0 +/- 0.4	0.5 +/- 0.5
СВН	-11.4 +/- 0.4	-10.9 +/- 0.8	0.5 +/- 0.9
PHE	-26.5 +/- 0.7	-24.9 +/- 0.6	1.6 +/- 0.9
СЗА	-15.0 +/- 0.5	-16.6 +/- 0.9	1.6 +/- 1.0
GCGC	-12.3 +/- 0.3	-10.6 +/- 0.6	1.7 +/- 0.7
C3GC	-24.2 +/- 0.7	-25.1 +/- 0.9	0.9 +/- 1.1
C2C2PD	-18.1 +/- 0.4	-17.5 +/- 0.7	0.6 +/- 0.8

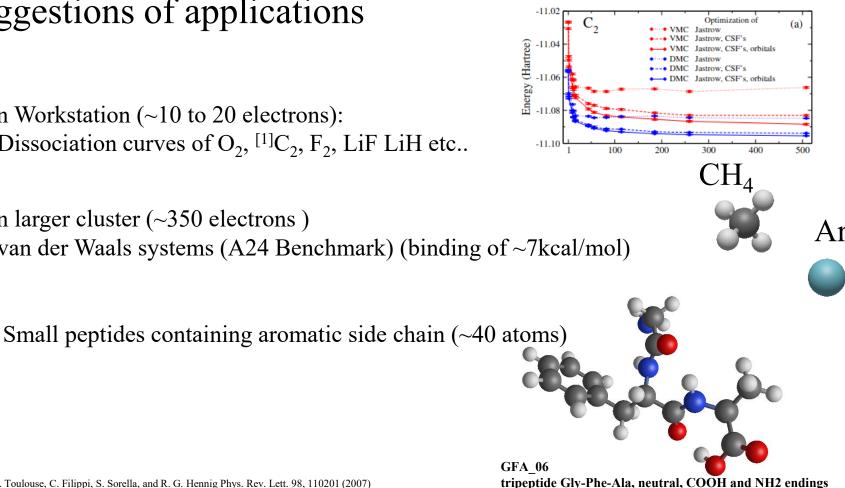
<sup>[1] &</sup>quot;Interactions between Large Molecules: Puzzle for Reference Quantum-Mechanical Methods" Y. S. Al-Hamdani, P. R. Nagy, D. Barton, M. Kallay, J.G. Brandenburg, A. Tkatchenko, arXiv:2009.08927 (2020)

<sup>[2] &</sup>quot;Quantum Monte Carlo benchmarking of large noncovalent complexes in the L7 benchmark set" A. Benali, H. Shin, O. Heinonen, J. Chem. Phys. **153**, 194113 (2020)

### Suggestions of applications

On Workstation (~10 to 20 electrons): Dissociation curves of O<sub>2</sub>, [1]C<sub>2</sub>, F<sub>2</sub>, LiF LiH etc..

On larger cluster (~350 electrons) van der Waals systems (A24 Benchmark) (binding of ~7kcal/mol)



## Summary

This tutorial covered how to run VMC and DMC with wavefunctions defined in gaussian basis sets

Basis set convergence, time-step, and other QMC parameters should be checked

DMC can be a very powerful tool to study consistently molecular systems

DMC dependence to the basis set is minimal when compared to quantum chemistry methods but requires carfeul checks and adequate extrapolations of local approximations.

It is possible to systematically improve the quality of the trial wavefunction and extrapolate out the fixed-node error with multideterminant wavefunctions, but at a higher computational cost.

Nexus can significantly reduce the complexity of a QMC calculation and can be used to manage large scale campaigns

Next week (#week 5) will be focused on QMC for solid state by Dr. Joshua Townsend (SNL)

Questions?