GetKroneckerOfPauliString

```
SetDirectory @ NotebookDirectory[];
Import["../Link/QuESTlink.m"];
```

Doc

? GetKroneckerOfPauliString

Symbol

GetKroneckerOfPauliString[product, n] expands the given

Pauli product into an explicit n-Pauli Kronecker form. The zero target in the

given product corresponds to the rightmost Pauli in the Kronecker form.

GetKroneckerOfPauliString[string, n] returns a list of

{kronecker, coefficient} pairs; one for each term in the given Pauli string.

GetKroneckerOfPauliString[string] infers the number of Paulis from the given string or product.

This function is useful for converting QuESTlink's Pauli strings

(i.e. subscript index notation) into fixed-size structures for easy comparison.

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Correctness

Product

GetKroneckerOfPauliString[X_{θ}] GetKroneckerOfPauliString[Z_{θ}]

 $\bigotimes X$

 $\bigotimes Z$

GetKroneckerOfPauliString[X₀ Y₁ Z₂ Id₃]

 $\text{Id} \otimes Z \otimes Y \otimes X$

 ${\tt GetKroneckerOfPauliString[Z_9]}$

GetKroneckerOfPauliString[X₀ Y₁ Z₂ Id₃, 10]

 $\texttt{Id} \otimes \texttt{Id} \otimes \texttt{Id} \otimes \texttt{Id} \otimes \texttt{Id} \otimes \texttt{Id} \otimes \texttt{Id} \otimes \texttt{Z} \otimes \texttt{Y} \otimes \texttt{X}$

```
str = X_0 Y_1 Z_2 X_3 Y_4;
matr = KroneckerProduct @@ (PauliMatrix[# /. {Id \rightarrow 0, X \rightarrow 1, Y \rightarrow 2, Z \rightarrow 3}] & /@
       GetKroneckerOfPauliString[str]);
matr === Normal @ CalcPauliExpressionMatrix[str]
True
```

String

```
GetKroneckerOfPauliString[X<sub>0</sub> Y<sub>1</sub> Z<sub>2</sub> Id<sub>3</sub>]
GetKroneckerOfPauliString[a X<sub>0</sub> Y<sub>1</sub> Z<sub>2</sub> Id<sub>3</sub>]
\text{Id} \otimes Z \otimes Y \otimes X
\{\{Id \otimes Z \otimes Y \otimes X, a\}\}
GetKroneckerOfPauliString[a X_0 Y_1 Z_2 Id_3 + b c X_4 + d e f Y_0 + Z_0 + X_1 Z_4]
\{\{X \otimes Id \otimes Id \otimes Id \otimes Id, bc\}, \{Id \otimes Id \otimes Id \otimes Id \otimes Y, def\},\}
  \{Id \otimes Id \otimes Id \otimes Id \otimes Z, 1\}, \{Id \otimes Id \otimes Z \otimes Y \otimes X, a\}, \{Z \otimes Id \otimes Id \otimes X \otimes Id, 1\}\}
```

Errors

\$Failed

```
GetKroneckerOfPauliString[X_1 + a]
··· GetKroneckerOfPauliString: Invalid arguments. See ?GetKroneckerOfPauliString
$Failed
GetKroneckerOfPauliString[X_1, 1]
GetKroneckerOfPauliString: The given Pauli string targeted a larger index qubit than the number of qubits
        specified.
$Failed
GetKroneckerOfPauliString[X₀ + Y₁, 1]
... GetKroneckerOfPauliString: The given Pauli string targeted a larger index qubit than the number of qubits
        specified.
GetKroneckerOfPauliString[X<sub>0</sub> + Y<sub>1</sub>, 0]
••• GetKroneckerOfPauliString: Invalid arguments. See ?GetKroneckerOfPauliString
$Failed
GetKroneckerOfPauliString[Y1 X1]
••• GetKroneckerOfPauliString: Invalid arguments. See ?GetKroneckerOfPauliString
```

${\tt GetKronecker0fPauliString[X_1\,X_1]}$

••• GetKroneckerOfPauliString: Invalid arguments. See ?GetKroneckerOfPauliString

\$Failed

GetKroneckerOfPauliString[]

 $\underbrace{\cdots} \textbf{GetKroneckerOfPauliString:} \textbf{Invalid arguments. See ?GetKroneckerOfPauliString}$

\$Failed