SampleExpecPauliString

```
SetDirectory @ NotebookDirectory[];
Import["../Link/QuESTlink.m"] // Quiet;
CreateLocalQuESTEnv["../quest_link"];
```

Doc

? SampleExpecPauliString

Symbol

SampleExpecPauliString[initQureg, channel, pauliString, numSamples] estimates the expected value of pauliString under the given channel (a circuit including decoherence) upon the state-vector initQureg, through Monte Carlo sampling. This avoids the quadratically greater memory costs of density-matrix simulation, but may need many samples to be accurate.

SampleExpecPauliString[initQureg, channel, pauliString,

All] deterministically samples each channel decomposition once.

SampleExpecPauliString[initQureg, channel, pauliString, numSamples, {workQureg1, workQureg2}] uses the given persistent working registers to avoid their internal creation and destruction.

To get a sense of the circuits being sampled, see GetCircuitsFromChannel[].

Use option ShowProgress to monitor the progress of sampling.

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? ShowProgress

Symbol

Optional argument to ApplyCircuit and SampleExpecPauliString, indicating whether to show a progress bar during circuit evaluation (default False). This slows evaluation slightly.

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Correctness

```
getExactExpec[circ_, h_, \psii_] := (
    InitPureState[\rho, \psii];
    ApplyCircuit[ρ, circ];
    CalcExpecPauliString[\rho, h, \omega]
setRandomState[\psii_] :=
    SetQuregMatrix[\psii, RandomComplex[{0,1+i}, 2^n]];
```

Deterministic

```
testDeterm[circ_] := Module[
    {h, eTrue, eDeterm, err},
    h = GetRandomPauliString[n];
    setRandomState [\psi i];
    eTrue = getExactExpec[circ, h, ψi];
    eDeterm = SampleExpecPauliString[\psii, circ, h, All];
    err = (eTrue - eDeterm) /eTrue // Abs // Chop;
    Echo[eDeterm, "expec value: "];
    Echo[err, "error: "];
    If[err =!= 0, Style["ERRONEOUS EVALUATION", Red]]
]
```

Unitary mixtures

```
testDeterm @ Deph_0[.1]
» expec value: -5.71611
» error: 0
   testDeterm @ Deph<sub>0,1</sub>[.5]
» expec value: -13.9255
» error: 0
   testDeterm @ Depol<sub>0</sub>[.5]
» expec value: -1.38894
» error: 0
  testDeterm @ Depol<sub>0,2</sub>[.9]
» expec value: -5.28162
» error: 0
```

Non-unitary mixtures

```
testDeterm @ Damp<sub>0</sub>[.9]
» expec value: -2.27194
» error: 0
    k = Table[RandomVariate @ CircularUnitaryMatrixDistribution[2], 3];
    testDeterm @ KrausNonTP_{\theta}[k]
» expec value: 8.22717
» error: 0
    k = Table[RandomComplex[\{-1-i, 1+i\}, \{2^2, 2^2\}], 15];
    testDeterm @ KrausNonTP_{0,1}[k]
» expec value: -81.9149
» error: 0
Circuits
    u = Circuit[
         H_0 \; \mathsf{Damp}_{\theta} \texttt{[.1]} \; \mathsf{Deph}_1 \texttt{[.5]} \; \mathsf{Depol}_2 \texttt{[.5]} \; \mathsf{C}_{\theta} \texttt{[X}_1 \texttt{]} \; \mathsf{Deph}_{1,2} \texttt{[.5]} \; \mathsf{C}_2 \texttt{[S}_1 \texttt{]} \; \mathsf{Depol}_{\theta,1} \texttt{[.7]} \; \mathsf{SWAP}_{1,2} \texttt{]} \texttt{;}
    DrawCircuit[u]
```

testDeterm@u

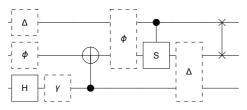
- » expec value: -5.43185
- » error: 0

Monte Carlo

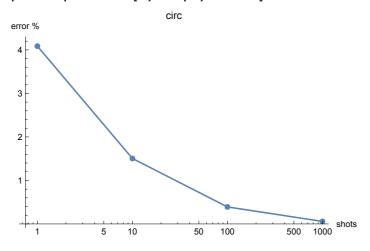
```
plotSampleErrors[circ_, shots_List, label_:None] := Module[
    {h, eTrue, eSamps, errs, data},
    h = GetRandomPauliString[n];
    setRandomState[\psi i];
    eTrue = getExactExpec[circ, h, ψi];
    eSamps = Table
        SampleExpecPauliString[\psii, circ, h, s],
        {s,shots}];
    errs = (eSamps - eTrue)/eTrue // Abs;
    data = Transpose @ {shots, errs};
    ListLogLinearPlot[
        data,
        AxesLabel → {"shots", "error %"},
        PlotMarkers → Automatic, Joined→True,
        PlotLabel → If[label===None, circ, label]
    ]
]
```

u = Circuit[

 $H_0 Damp_0[.1] Deph_1[.5] Depol_2[.5] C_0[X_1] Deph_{1,2}[.5] C_2[S_1] Depol_{0,1}[.7] SWAP_{1,2}];$ DrawCircuit[u]

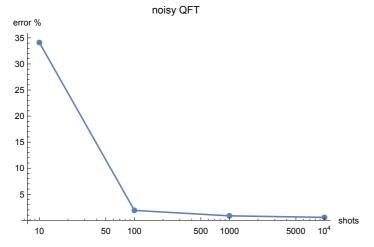


plotSampleErrors[u, samps, "circ"]



```
u = GetKnownCircuit["QFT", n];
u \; = \; u \; /. \; \left\{g \colon \__{q_-} \; \Rightarrow \; \left\{g, \; \mathsf{Damp}_q[.5] \right\}, \; g \colon \__{q1_-,q2_-}[\_] \; \Rightarrow \left\{g, \; \mathsf{Depol}_{q1,q2}[.9] \right\} \right\};
u = Flatten@u;
DrawCircuit[u]
```

plotSampleErrors[u, {10, 10^2, 10^3, 10^4}, "noisy QFT"]



Options

ShowProgress

```
u = Table[Depol_{0,1}[.5], 10^4];
h = GetRandomPauliString[n];
SampleExpecPauliString[\psii, u, h, 10^4, ShowProgress \rightarrow True]
-0.908556
```

Working registers

```
tmp = CreateQuregs[n, 2];
Timing @ SampleExpecPauliString [\psi_i, Deph_{0.1}[.2], h, All]
Timing @ SampleExpecPauliString[\psii, Deph<sub>0,1</sub>[.2], h, All, tmp]
{First@% < First@%%, Last@% === Last@%%}
{0.006356, 8.50575}
{0.004842, 8.50575}
{True, True}
```

Warnings

```
SampleExpecPauliString [\psi i, Deph_{0,1}[.2], h, 100]
```

... SampleExpecPauliString: As many or more samples were requested than there are unique decompositions of the circuit (of which there are 4). Proceeding instead with deterministic simulation of each decomposition in-turn. Hide this warning by setting the number of samples to All, or using Quiet[].

0.362668

Errors

```
SampleExpecPauliString [\psi_i, Deph_{0,1}[.2], h, 1, CreateQuregs[2, 2]]
... SampleExpecPauliString: The working quregs must have the same number of qubits as the initial qureg.
$Failed
SampleExpecPauliString[\psii, Deph<sub>0,1</sub>[.2], h, 1, CreateQuregs[n, 1]]
SampleExpecPauliString [\psi_i, Deph_{0,1}[.2], h, 1, CreateQuregs[n, 3]]
••• SampleExpecPauliString: Invalid arguments. See ?SampleExpecPauliString
$Failed
••• SampleExpecPauliString: Invalid arguments. See ?SampleExpecPauliString
$Failed
```

```
SampleExpecPauliString[\psii, Deph<sub>0,1</sub>[.2], h, 0]
SampleExpecPauliString[\psii, Deph<sub>0,1</sub>[.2], h, -10]
SampleExpecPauliString[\psii, Deph<sub>0,1</sub>[.2], h, 1.5]
••• SampleExpecPauliString: The number of samples must be a positive integer.
$Failed
••• SampleExpecPauliString: The number of samples must be a positive integer.
$Failed
••• SampleExpecPauliString: Invalid arguments. See ?SampleExpecPauliString
$Failed
SampleExpecPauliString[invalid\psi, Deph<sub>0.1</sub>[.2], h, 1]
SampleExpecPauliString[ψi, invalidCirc, h, 1]
SampleExpecPauliString [\psi i, Deph_{0,1}[.2], invalidPauli, 1]
SampleExpecPauliString[\psii, Deph<sub>0,1</sub>[.2], h, invalidShots]
••• SampleExpecPauliString: Invalid arguments. See ?SampleExpecPauliString
$Failed
••• SampleExpecPauliString: Invalid arguments. See ?SampleExpecPauliString
$Failed
••• SampleExpecPauliString: Invalid arguments. See ?SampleExpecPauliString
$Failed
```

••• SampleExpecPauliString: Invalid arguments. See ?SampleExpecPauliString

\$Failed