LATERAL-DIRECTIONAL PARAMETERS INITIALIZATION

Hidden Area --> Import of Excel INPUT Data

Hidden Area --> Preliminary Mapping of imported Data

Hidden Area --> Import and preliminary mapping of OTHER Excel Data

Other input parameters to be defined here

 $C_{Roll}\!\coloneqq\!0$

 $C_N \coloneqq 0$

 $C_{Roll0}\!\coloneqq\!0$

 $C_{N0} \coloneqq 0$

 $\beta = 2 \, \, deg = 0.035$

$$p \coloneqq -0.274 \ \frac{\textit{deg}}{\textit{s}} = -0.005 \ \frac{\textit{rad}}{\textit{s}}$$

$$r = 0.261 \frac{deg}{s} = 0.005 \frac{1}{s}$$

$$p_{bar} \coloneqq \frac{p \cdot b_W}{2 \cdot V_1} = -0.000313$$

$$r_{bar} \coloneqq \frac{r \cdot b_W}{2 \cdot V_1} = 0.000298$$

$$p_{bar} = -0.017912 \ deg$$

$$r_{bar} = 0.017062 \; deg$$

LATERAL-DIRECTIONAL PARAMETERS

Input parameters

$$mass = (4.5 \cdot 10^4) \ kg$$

$$C_{D0} = 0.027$$

$$\Delta Z_W_{LE}_Nose = -0.945 \ m$$

$$\Delta X_W_{LE}_Nose = 11.125 \ m$$

$$\Delta X_{LE}Nose = 27.859 \ m$$

$$\Delta X_VT_{LE}_Nose = 22.296$$
 m

$$\Delta Z_HT_{LE}_Nose = 6.096 \ m$$

$$\Delta Z_VT_{LE}_Nose = 1.951~m$$

Imported parameters

$$M_1 = 0.696$$

$$V_1 = 208.41 \frac{m}{s}$$

$$p_{dyn} = (8.961 \cdot 10^3) \, Pa$$

$$Re_{per.unit.len} = (5.902 \cdot 10^6) \frac{1}{m}$$

$$d_B = 2.79 \ m$$

$$Z_1 = 3.69 \ m$$

$$Z_2 = 3.38 \ m$$

$$r_1 = 1.52 \ m$$

$$l_B = 28.16 \ m$$

$$S_{B_side} = 86.48~\textbf{m}^2$$

$$Z_{MAX} = 3.26 \ m$$

$$\omega_{MAX} = 3.26 \ m$$

$$b_V = 4.831 \ m$$

$$C_{L\alpha \ V}$$
 = 5.615

$$\eta_{V_}times_1_plus_d\sigma_over_d\beta = 1.007$$

$$S_V = 20.54 \ m^2$$

$$X_{MAC_LE_V} = 2.383 \ m$$

$$Y_{MAC_V} = 2.222 \ m$$

$$MAC_V = 4.334$$
 m

$$\tau_{rd}\!=\!0.68$$

$$\eta_{rd_in} = 0$$

$$\eta_{rd\ out} = 0.656$$

$$\lambda_V\!=\!0.613$$

$$\eta_V = 0.97$$

$$MAC_{H} = 2.433 \ m$$

$$\alpha_{0L_H} = 0$$
 deg

$$S_H = 25.47 \; m^2$$

$$\eta_H = 0.95$$

$$AR_{H} = 4.94$$

$$b_H = 11.217 \ m$$

$$\Lambda_{H\ c2} = 27.147\ {\it deg}$$

$$\lambda_H = 0.367$$

$$\Lambda_{H_c4} = 31.238 \; deg$$

$$\Gamma_H = 0 \, deg$$

$$\alpha_{0l_H_r} = 0$$
 deg

$$\alpha_{0l\ H\ t} = 0$$
 deg

$$C_L = 0.562$$

$$\alpha_{WB} = 3.186 \ deg$$

$$C_{L\!H}\!=\!-0.114$$

$$N_{eng_1}\!=\!2$$

$$N_{eng_2}\!=\!0$$

$$N_{enq} = 2$$

$$S_{enq} = 1.14 \; \boldsymbol{m}^2$$

$$C_{N\alpha_eng}\!=\!0.334$$

$$x_{CG} = 1.002 \ m$$

$$\Delta X_CG_eng_1 = -5.35$$
 m

$$\Delta X_{CG}eng_2 = 0$$
 m

$$\Delta X_CG_Nose = 14.99 \ m$$

$$\Delta Z_{-}W_{c4} _{r-}B_{CL} = -0.894 \ m$$

$$\Delta Z_HT_{c4_r}_B_{CL} = -7.724 \ m$$

$$MAC_W = 3.642 \ m$$

$$X_{MAC_LE_W} = 2.861 \ m$$

$$b_W = 27.249 \ m$$

$$C_{L\alpha_W} = 0.109 \; deg^{-1}$$

$$i_W = 2 \, \, deg$$

$$\Lambda_{W_c4_eqv} = 28.018 \; deg$$

$$\xi_{ac\ W} = 16.788\ deg$$

$$S_W = 87.62 \ m^2$$

$$AR_W\!=\!8.474$$

$$e_W = 0.918$$

$$\Lambda_{W_c2_eqv} = 20.97$$
 deg

$$\lambda_W = 0.227$$

$$\lambda_{W_eqv} \!=\! 0.227$$

$$\Gamma_{W_eqv} = 2.177 \ deg$$

$$\alpha_{0l_W_r}\!=\!-0.047$$

$$\alpha_{0l_W_t} = -0.047$$

$$X_{ac\ W} = 3.928\ m$$

$$c_{W_r} = 5.243 \; m$$

$$\eta_{aileron_in} = 0.664$$

$$\eta_{aileron_out}\!=\!0.908$$

$$c_{aileron} = 0.792$$
 m

$$Z_{MAC_W} = 0.207 \ \boldsymbol{m}$$

$$c_{W_mean_@a}\!=\!2.056~\textbf{\textit{m}}$$

$$C_{Y\!\beta}\!\coloneqq\! C_{N\alpha_eng}$$

$$C_{Y\beta} = 0.006 \; deg^{-1}$$

$$C_{N\beta_eng_1} \coloneqq -C_{Y\beta} \cdot \frac{S_{eng}}{S_W} \cdot \frac{\Delta X_CG_eng_1}{MAC_W} \cdot \frac{N_{eng_1}}{N_{eng}} = 0.006$$

$$C_{N\beta_{eng_1}}\!=\!\left(1.114 \cdot 10^{^{-4}}\right) \, \mathbf{deg}^{^{-1}}$$

$$C_{N\beta_eng_2}\!\coloneqq\!-C_{Y\beta}\!\cdot\!\frac{S_{eng}}{S_W}\!\cdot\!\frac{\Delta X_CG_eng_2}{MAC_W}\!\cdot\!\frac{N_{eng_2}}{N_{eng}}\!=\!0$$

$$C_{N\beta eng} = 0 \ deg^{-1}$$

• REMARK: This is the Yawing Moment Coefficient due to sideslip angle

ATERAL-DIRECTIONAL CALCULATIONS

$$S_{fAVG} := \pi \cdot d_B \cdot \left(\frac{Z_1 + Z_2}{2} \right) = 30.984 \ m^2$$

$$S_{fAVG} = 30.984 \ m^2$$

$$\Delta C_{Roll\beta}_over_\Gamma_W \coloneqq -\frac{(0.0005)}{\deg^2} \cdot AR_W \cdot \left(\left(\frac{\sqrt{\frac{4 \cdot S_{fAVG}}{\pi}}}{b_W} \right)^2 \right) = -0.739$$

$$\Delta C_{Roll\beta}$$
over Γ_W = $-2.251 \cdot 10^{-4} \frac{1}{\text{deg}^2}$

$$\Delta C_{Roll\beta_}over_\Gamma_{H} \coloneqq -\frac{(0.0005)}{\deg^{2}} \cdot AR_{H} \cdot \left| \left(\frac{\sqrt{\frac{4 \cdot S_{fAVG}}{\pi}}}{b_{H}} \right)^{2} \right| = -2.542$$

$$\Delta C_{Roll\beta_}over_\Gamma_{H} = -7.745 \cdot 10^{-4} \frac{1}{deg^{2}}$$

$$\Delta C_{Roll\beta_ZW} \coloneqq \frac{1.2 \cdot \sqrt{AR_W}}{57.3} \cdot \frac{\Delta Z_W_{c4_r_}B_{CL}}{b_W} \cdot 2 \cdot \frac{\sqrt{\frac{4 \cdot S_{fAVG}}{\pi}}}{b_W} \cdot \frac{1}{\deg} = -0.053 \qquad \qquad \Delta C_{Roll\beta_ZW} = -9.221 \cdot 10^{-4} \cdot \frac{1}{\deg}$$

$$\Delta C_{Roll\beta_ZW} = -9.221 \cdot 10^{-4} \frac{1}{deq}$$

$$\Delta C_{Roll\beta_ZH} \coloneqq \frac{1.2 \cdot \sqrt{AR_H}}{57.3} \cdot \frac{\Delta Z_HT_{c4_r}_B_{CL}}{b_H} \cdot 2 \cdot \frac{\sqrt{\frac{4 \cdot S_{fAVG}}{\pi}}}{b_H} \cdot \frac{1}{\textbf{deg}} = -2.057 \qquad \Delta C_{Roll\beta_ZH} = -6.265 \cdot 10^{-4} \frac{1}{\textbf{deg}^2}$$

$$\Delta C_{Roll\beta_ZH} = -6.265 \cdot 10^{-4} \frac{1}{\text{deg}^2}$$

@Aerodynamic Database ---> (C | beta w b) k M Gamma vs Mach times cos(L c2) (AR over cos(L c2))

@Aerodynamic Database ---> (C_l_beta_w_b)_C_l_beta_over_Gamma_w_vs_AR_(L_c2)_(lambda)

$$C_{Roll\beta}_over_\Gamma_W\!=\!-0.59$$

$$C_{Roll\beta}$$
over_ Γ_W = $-1.799 \cdot 10^{-4} \ deg^{-2}$

$$C_{Roll\beta}$$
_ $over$ _ Γ_H = -0.51

$$C_{Roll\beta}$$
over_ $\Gamma_H = -1.554 \cdot 10^{-4} \, deg^{-2}$

@Aerodynamic Database ---> (C_I_beta_w_b)_dC_I_beta_over_eps_w_times_tan_(L_c4)_vs_AR_(lambda)

$$\Delta C_{Roll\beta_}over_\varepsilon_{W_}times_tan \Lambda c4_{W} = -0.117$$

$$\Delta C_{Roll\beta}_over_\varepsilon_{W}_times_tan \\ \Lambda c4_{W} = -3.572 \cdot 10^{-5} \; \textit{deg}^{-2}$$

$$\Delta C_{Roll\beta_}over_\varepsilon_{H_}times_tan \Lambda c4_{H} = -0.106$$

$$\Delta C_{Roll\beta}_over_\varepsilon_{H}_times_tan \\ \Lambda c4_{H} = -3.217 \cdot 10^{-5}~\textit{deg}^{-2}$$

@Aerodynamic Database ---> (C_l_beta_w_b)_C_l_beta_over_C_Lift1_(L_c2)_vs_L_c2_(AR)_(lambda)

$$C_{Roll\beta W_}over_C_L@\varLambda_{c2}\!=\!-0.106$$

$$C_{Roll\beta W}$$
over $C_L@A_{c2} = -1.848 \cdot 10^{-3} \ deg^{-1}$

$$C_{Roll\beta H}$$
over $C_L@A_{c2}$ = -0.132

$$C_{Roll\beta H}$$
over $C_L@A_{c2} = -2.307 \cdot 10^{-3} \ deg^{-1}$

@Aerodynamic Database ---> (C | beta w b) C | beta over C Lift1 (L c2) vs L c2 (AR) (lambda)

$$C_{Roll\beta W}_over_C_L@AR_W = 0.015$$

$$C_{RollBW}$$
over $C_L@AR_W = (2.553 \cdot 10^{-4}) deg^{-1}$

$$C_{Roll\beta H}_over_C_L@AR_H\!=\!-0.047$$

$$C_{Roll\beta H}$$
over C_L @ AR_H = $-8.135 \cdot 10^{-4} \ deg^{-1}$

@Aerodynamic Database ---> (C_I_beta_w_b)_k_M_L_vs_Mach_times_cos(L_c2)_(AR_over_cos(L_c2))

$$K_{M AW} = 1.263$$

$$K_{M AH} = 1.115$$

@Aerodynamic Database ---> (C | beta w b) k M L vs Mach times cos(L c2) (AR over cos(L c2))

$$A_{W} \coloneqq \Delta X _W_{LE} _Nose + \frac{b_{W}}{2} \cdot \tan \left(\varLambda_{W_c2_eqv} \right) = 16.347 \ \textit{m}$$

$$A_W = 16.347 \ m$$

$$A_{H} \coloneqq \Delta X_HT_{LE}_Nose + \frac{b_{H}}{2} \cdot \tan \left< \Lambda_{H_c2} \right> = 30.735 \ \textit{m}$$

$$A_H = 30.735 \ m$$

 $K_{fW} = 0.884$

 $K_{fH} = 0.909$

Wing - Body - Horizontal Tail - Vertical Tail Dihedral Effect Calculations

 $C_{Roll\beta_WB_A_c2_AR} \coloneqq C_L \cdot \left\langle C_{Roll\beta W_over_C_L}@A_{c2} \cdot K_{M_AW} \cdot K_{fW} + C_{Roll\beta W_over_C_L}@AR_W \right\rangle = -0.058$

 $C_{Roll\beta_WB_\Gamma_W_eqv} \coloneqq C_L \cdot \Gamma_{W_eqv} \cdot \left(C_{Roll\beta_over_\Gamma_W} \cdot K_{M\Gamma_W} + \Delta C_{Roll\beta_over_\Gamma_W} \right) = -0.03$

 $C_{Roll\beta_WB_\varepsilon_W} \coloneqq C_L \cdot \left(\Delta C_{Roll\beta_ZW} + \left(\alpha_{0l_W_t} - \alpha_{0l_W_r} \right) \cdot \tan \left(A_{W_c4_eqv} \right) \cdot \Delta C_{Roll\beta_over_\varepsilon_{W_}times_tanAc4_W} \right) = -0.03$

 $C_{Roll\beta_WB} \coloneqq C_{Roll\beta_WB_A_c2_AR} + C_{Roll\beta_WB_\Gamma_W_eqv} + C_{Roll\beta_WB_\varepsilon_W} = -0.118$

 $C_{Roll\beta_WB} = -0.118$

 $C_{Roll\beta WB} = -0.00206 \ deg^{-1}$

 $C_{Roll\beta_H_A_c2_AR} \coloneqq \eta_H \cdot \frac{S_H}{S_W} \cdot \frac{b_H}{b_W} \cdot C_{LH} \cdot \left\langle C_{Roll\beta H_over_C_L}@A_{c2} \cdot K_{M_AH} \cdot K_{fH} + C_{Roll\beta H_over_C_L}@AR_H \right\rangle = 0.002$

 $C_{Roll\beta_H_\Gamma_H} \coloneqq \eta_H \cdot \frac{S_H}{S_W} \cdot \frac{b_H}{b_W} \cdot C_{LH} \cdot \Gamma_H \cdot \left(C_{Roll\beta_over_\Gamma_H} \cdot K_{M\Gamma_H} + \Delta C_{Roll\beta_over_\Gamma_H} \right) = 0$

 $C_{Roll\beta_H_\varepsilon_H} \coloneqq \eta_H \cdot \frac{S_H}{S_W} \cdot \frac{b_H}{b_W} \cdot C_{LH} \cdot \left\langle \Delta C_{Roll\beta_ZH} + \left\langle \alpha_{0l_H_t} - \alpha_{0l_H_r} \right\rangle \cdot \tan \left\langle \Lambda_{H_c4} \right\rangle \cdot \Delta C_{Roll\beta_over_\varepsilon_H_times_tanAc4_H} \right\rangle = 0.027$

 $C_{Roll\beta_H} \coloneqq C_{Roll\beta_H_A_c2_AR} + C_{Roll\beta_H_\Gamma_H} + C_{Roll\beta_H_\varepsilon_H} = 0.029$

 $C_{Roll\beta H} = 0.029$

 $C_{Roll3\ H} = (5.065 \cdot 10^{-4}) \ deg^{-1}$

 $\Delta X_VT_{ac}_CG \coloneqq \Delta X_VT_{LE}_Nose + X_{MAC_LE_V} + \frac{MAC_V}{4} - \Delta X_CG_Nose = 10.773 \ \textit{m}$

 $X_{V} \coloneqq \Delta X_VT_{ac}_CG = 10.773$ **m**

 $\Delta Z_VT_{ac}_W_{ac} \coloneqq Y_{MAC_V} + \Delta Z_VT_{LE}_Nose - \Delta Z_W_{LE}_Nose - Z_{MAC_W} = 4.911 \ \textit{m}$

 $\Delta Z_{-}VT_{ac}_{-}W_{ac} = 4.911$ m

 $\Delta Z_VT_{ac}_CG \coloneqq \Delta Z_VT_{ac}_W_{ac} + \Delta Z_W_{LE}_Nose \cdot \frac{X_{ac}_W}{c_{W_r} \cdot \cos{(i_W)}} = 4.202 \ \textit{m}$

 $Z_V \coloneqq \Delta Z_VT_{ac}_CG = 4.202 \ \emph{m}$

@Aerodynamic Database ---> (C_y_beta_v)_K_Y_V_vs_b_v_over_2_times_r1

$$C_{Roll\beta_V} \coloneqq -K_{Y_V} \cdot C_{L\alpha_V} \cdot \eta_{V_} times_1_plus_d\sigma_over_d\beta \cdot \frac{S_V}{S_W} \cdot \frac{Z_V \cdot \cos{\langle \alpha_{WB} \rangle} - X_V \cdot \sin{\langle \alpha_{WB} \rangle}}{b_W} = -0.133$$

$$C_{Roll\beta} \coloneqq C_{Roll\beta\ WB} + C_{Roll\beta\ H} + C_{Roll\beta\ V} = -0.222$$

 $C_{Roll\beta} = -0.00388 \ deg^{-1}$

Wing - Body - Horizontal Tail - Vertical Tail Rolling Moment Coefficient due to Ailerons Deflection

$$k_M \coloneqq \frac{C_{L\alpha_W} \cdot \sqrt{1 - {M_1}^2}}{2 \cdot \pi} = 0.712$$

$$k_M \coloneqq \frac{C_{L\alpha_W} \cdot \sqrt{1 - {M_1}^2}}{2 \cdot \pi} = 0.712 \qquad \qquad \Lambda_M \coloneqq \operatorname{atan}\left(\frac{\operatorname{tan}\left(\Lambda_{W_c4_eqv}\right)}{\sqrt{1 - {M_1}^2}}\right) = 36.54 \; \operatorname{\textit{deg}}$$

$$\beta_times_AR_over_k \coloneqq \frac{\sqrt{1 - {M_1}^2} \cdot AR_W}{k_M} = 8.55$$

@Aerodynamic Database ---> (C | delta a) RME vs eta (Lambda beta) (beta times AR over k) (lambda)

 $RME_{in} = 0.461$

 $RME_{out} = 0.662$

$$\Delta RME \coloneqq RME_{out} - RME_{in} = 0.2$$

$$C_{Roll\delta}^{'}\!\coloneqq\!-\frac{\Delta RME \cdot k_{M}}{\sqrt{1-{M_{1}}^{2}}}\!=\!-0.1986$$

@Aerodynamic Database ---> (control_surface)_tau_e_vs_c_control_surface_over_c_horizontal_tail

 $\tau_a\!=\!0.597$

$$C_{Roll\delta a} \coloneqq C_{Roll\delta}' \bullet \tau_a = -0.119$$

$$C_{Roll\delta a} = -0.002 \frac{1}{\textit{deg}}$$

Wing - Body - Horizontal Tail - Vertical Tail Rolling Moment Coefficient due to Rudder Deflection

$$Z_r = 0.95 \cdot Z_V = 3.992 \ m$$

$$X_r := 1.05 \cdot X_V = 11.311 \ m$$

@Aerodynamic Database ---> (C n delta r) K R vs eta (lambda v)

 $K_r = 0.787$

$$C_{Roll\delta r} \coloneqq C_{L\alpha_V} \cdot \eta_V \cdot \frac{S_V}{S_W} \cdot K_r \cdot \tau_{rd} \cdot \left(\frac{Z_r \cdot \cos\left(\alpha_{WB}\right) - X_r \cdot \sin\left(\alpha_{WB}\right)}{b_W} \right) = 0.084$$

Wing - Body - Horizontal Tail - Vertical Tail Yawing Moment Coefficient due to Sideslip Angle

$$C_{N\beta_W}\!\coloneqq\!0$$

$$C_{N\beta}_{H} := 0$$

@Aerodynamic Database ---> (C_n_beta_b)_K_N_times_1e-3_vs_x_cg_over_l_b_(squared_l_b_over_S_b_s)_(square_root_(h1_over_h2))_(h_b_over_w_b)

 $K_N = 0.001$

@Aerodynamic Database ---> (C_n_beta_b)_K_Re_b_vs_Re_l_b_times_1e-6

$$Re_{l_B}\!\coloneqq\!Re_{per.unit.len}\!\boldsymbol{\cdot} l_B\!=\!1.662\boldsymbol{\cdot} 10^8$$

 $K_{Re} = 2.025$

$$C_{N\beta_B} \coloneqq -57.3 \cdot K_N \cdot K_{Re_B} \cdot \frac{S_{B_side}}{S_W} \cdot \frac{l_B}{b_W} = -0.155$$

$$C_{N\beta_B} = -0.003 \frac{1}{dea}$$

$$C_{N\beta_V} \coloneqq K_{Y_V} \cdot C_{L\alpha_V} \cdot \eta_{V_times_1_plus_d\sigma_over_d\beta} \cdot \frac{S_V}{S_W} \cdot \frac{Z_V \cdot \sin{(\alpha_{WB})} + X_V \cdot \cos{(\alpha_{WB})}}{b_W} = 0.406$$

$$C_{Neta_V}{=}\,0.007\,rac{1}{ extbf{\textit{deg}}}$$

$$C_{N\beta} \coloneqq C_{N\beta_W} + C_{N\beta_H} + C_{N\beta_B} + C_{N\beta_V} + C_{N\beta_eng_1} + C_{N\beta_eng_2} = 0.257$$

$$C_{N\beta} = 0.004 \frac{1}{deq}$$

Wing - Body - Horizontal Tail - Vertical Tail Yawing Moment Coefficient due to Ailerons Deflection

@Aerodynamic Database ---> (C_n_delta_a)_k_n_a_vs_eta_(AR)_(lambda)

 $\Delta K_{nA} = 0.024$

$$C_{N\delta a}\!\coloneqq\!-\Delta\!K_{n_A}\!\cdot\!C_L\!\cdot\!C_{Roll\delta a}\!=\!0.002$$

$$C_{N\delta a} = (2.809 \cdot 10^{-5}) \frac{1}{dea}$$

Wing - Body - Horizontal Tail - Vertical Tail Yawing Moment Coefficient due to Rudder Deflection

$$C_{N\delta r} \coloneqq -C_{L\alpha_V} \cdot \eta_V \cdot \frac{S_V}{S_W} \cdot K_r \cdot \tau_{rd} \cdot \left(\frac{Z_r \cdot \sin\left(\alpha_{WB}\right) + X_r \cdot \cos\left(\alpha_{WB}\right)}{b_W} \right) = -0.289$$

$$C_{N\delta r}$$
 = $-5.039 \cdot 10^{-3}$ $\frac{1}{deg}$

UNSTEADY LATERAL-DIRECTIONAL FLIGHT COEFFICIENTS

Wing - Body - Horizontal Tail - Vertical Tail Rolling Moment Coefficient due to Roll Rate

$$k_{Roll_Rate_W} \coloneqq \frac{C_{L\alpha_W} \boldsymbol{\cdot} \sqrt{1 - {M_1}^2}}{2 \boldsymbol{\cdot} \pi} = 0.712$$

$$k_{Roll_Rate_H} \coloneqq \frac{C_{L\alpha_H} \cdot \sqrt{1 - {M_1}^2}}{2 \cdot \pi} = 0.53$$

@Aerodynamic Database ---> (C_I_p_w)_RDP_vs_Lambda_beta_(beta_times_AR_over_k)_(lambda)

 $RDP_{W} = -0.404$

$$RDP_{H} = -0.375$$

$$C_{Rollp_W} \coloneqq RDP_W \bullet \frac{k_{Roll_Rate_W}}{\sqrt{1 - {M_1}^2}} = -0.401$$

$$C_{Rollp_H} \coloneqq \frac{1}{2} \cdot RDP_H \cdot \frac{k_{Roll_Rate_H}}{\sqrt{1 - {M_1}^2}} \cdot \frac{S_H}{S_W} \cdot \left(\frac{b_H}{b_W}\right)^2 = -0.007$$

$$C_{Rollp_V} \coloneqq -2 \cdot K_{Y_V} \cdot C_{L\alpha_V} \cdot \eta_{V_} times_1_plus_d\sigma_over_d\beta \cdot \frac{S_V}{S_W} \cdot \left(\frac{Z_V}{b_W}\right)^2 = -47.917 \cdot 10^{-3}$$

$$C_{Rollp} \coloneqq C_{Rollp_W} + C_{Rollp_H} + C_{Rollp_V} = -0.456$$

Wing - Body - Horizontal Tail - Vertical Tail Yawing Moment Coefficient due to Roll Rate

$$B \coloneqq -\frac{1}{6} \cdot \frac{AR_W + 6 \cdot (AR_W + \cos{(\Lambda_{W_c4_eqv})}) \cdot \left[\left(\xi_{CG} - \xi_{ac_W} \right) \cdot \frac{\tan{(\Lambda_{W_c4_eqv})}}{AR_W} + \frac{\tan{(\Lambda_{W_c4_eqv})}^2}{12} \right]}{AR_W + \cos{(\Lambda_{W_c4_eqv})}} = -0.173$$

$$C_{Np}_over_C_L@M_0_C_{L_ZL} \coloneqq \frac{B}{\sqrt{1 - {M_1}^2 \cdot \cos \left< \Lambda_{W_c4_eqv} \right>^2}} = -0.22$$

$$C\coloneqq\frac{AR_{W}+4\cdot\cos\left(\varLambda_{W_c4_eqv}\right)}{AR_{W}\cdot B+4\cdot\cos\left(\varLambda_{W_c4_eqv}\right)}\cdot\frac{AR_{W}\cdot B+0.5\cdot\left(AR_{W}\cdot B+4\cdot\cos\left(\varLambda_{W_c4_eqv}\right)\cdot\tan\left(\varLambda_{W_c4_eqv}\right)^{2}\right)}{AR_{W}+0.5\cdot\left(AR_{W}\cdot B+4\cdot\cos\left(\varLambda_{W_c4_eqv}\right)\cdot\tan\left(\varLambda_{W_c4_eqv}\right)^{2}\right)}=-1.204$$

$$C_{Np}_over_C_L@M_1_C_{L_ZL} \coloneqq C \cdot C_{Np}_over_C_L@M_0_C_{L_ZL} = 0.265$$

@Aerodynamic Database ---> (C_n_p_w)_dC_n_p_over_eps_w_vs_AR_(lambda)

$$\Delta C_{Np}$$
over ε_W = 5.315 • 10⁻⁴

$$C_{Np_W} \coloneqq -C_{Rollp_W} \cdot \tan\left(\alpha_{WB}\right) + C_{Rollp} \cdot \tan\left(\alpha_{WB}\right) + C_{Np_over_C_L} @M_{1_C_{L_ZL}} \cdot C_L + \Delta C_{Np_over_\varepsilon_W} \cdot \left(\alpha_{0l_W_t} - \alpha_{0l_W_r}\right) = 0.146$$

$$C_{Np_V} \coloneqq -2 \cdot K_{Y_V} \cdot C_{L\alpha_V} \cdot \eta_{V_times_1_plus_d\sigma_over_d\beta} \cdot \frac{S_V}{S_W} \cdot \left(\frac{Z_V \cdot \sin\left(\alpha_{WB}\right) + X_V \cdot \cos\left(\alpha_{WB}\right)}{b_W} \right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - X_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W} \right)$$

$$C_{Np\ V} = 18.045 \cdot 10^{-3}$$

$$C_{Np} := C_{Np \ W} + C_{Np \ V} = 0.164$$

Wing - Body - Horizontal Tail - Vertical Tail Rolling Moment Coefficient due to Yaw Rate

$$B \coloneqq \sqrt{1 - M_1^2 \cdot \cos\left(\Lambda_{W \ c4 \ egv}\right)^2} = 0.789$$

$$D \coloneqq \frac{1 + \frac{AR_W \cdot \left(1 - B^2\right)}{2 \cdot B \cdot \left(AR_W \cdot B + 2 \cdot \cos\left(\Lambda_{W_c4_eqv}\right)\right)} + \frac{AR_W \cdot B + 2 \cdot \cos\left(\Lambda_{W_c4_eqv}\right)}{AR_W \cdot B + 4 \cdot \cos\left(\Lambda_{W_c4_eqv}\right)} \cdot \frac{\tan\left(\Lambda_{W_c4_eqv}\right)^2}{8}}{1 + \frac{AR_W + 2 \cdot \cos\left(\Lambda_{W_c4_eqv}\right)}{AR_W + 4 \cdot \cos\left(\Lambda_{W_c4_eqv}\right)} \cdot \frac{\tan\left(\Lambda_{W_c4_eqv}\right)^2}{8}$$

@Aerodynamic Database ---> (C_l_r_w)_C_l_r_over_C_Lift1_vs_AR_(lambda)_(L_c2)

$C_{Rollr_over_C_L}@M_0_C_{L\ ZL}\!=\!0.299$

$$C_{Rollr}_over_C_L@M_{1}_C_{L_ZL} \coloneqq D \cdot C_{Rollr}_over_C_L@M_{0}_C_{L_ZL} = 0.369$$

$$\Delta C_{Rollr_over_\Gamma} \coloneqq \frac{1}{12} \cdot \frac{\pi \cdot AR_W \cdot \sin \left(\Lambda_{W_c4_eqv} \right)}{AR_W + 4 \cdot \cos \left(\Lambda_{W_c4_eqv} \right)} = 0.087$$

@Aerodynamic Database ---> (C_I_r_w)_dC_I_r_over_eps_w_vs_AR_(lambda)

ΔC_{Rollr} _over_ $\varepsilon = 0.014$

$$C_{Rollr_W} \coloneqq C_{Rollr_over_C_L} @ M_{1_C_{L_ZL}} \cdot C_L + \Delta C_{Rollr_over_\Gamma} \cdot \Gamma_{W_eqv} + \Delta C_{Rollr_over_\varepsilon} \cdot \left(\alpha_{0l_W_t} - \alpha_{0l_W_r}\right) = 0.211$$

$$C_{Rollr_V} \coloneqq -2 \cdot K_{Y_V} \cdot C_{L\alpha_V} \cdot \eta_{V_} times_1_plus_d\sigma_over_d\beta \cdot \frac{S_V}{S_W} \cdot \left(\frac{Z_V \cdot \sin\left(\alpha_{WB}\right) + X_V \cdot \cos\left(\alpha_{WB}\right)}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - X_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - X_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - Z_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - Z_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - Z_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - Z_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - Z_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - Z_V \cdot \sin\left(\alpha_{WB}\right) - Z_V}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - Z_W}{b_W}\right) \cdot \left(\frac{Z_V \cdot \cos\left(\alpha_{WB}\right) - Z_W}{b_W}\right)$$

$$C_{Rollr\ V} = 18.045 \cdot 10^{-3}$$

$$C_{Rollr} \coloneqq C_{Rollr_W} + C_{Rollr_V} = 0.229$$

Wing - Body - Horizontal Tail - Vertical Tail Yawing Moment Coefficient due to Yaw Rate

@Aerodynamic Database ---> (C_n_r_w)_C_n_r_over_squared_(C_Lift1)_vs_AR_(lambda)_(L_c4)_(x_bar_ac_minus_x_bar_cg)

 $C_{Nr}_over_squared_C_L = 0.227$

@Aerodynamic Database ---> (C_n_r_w)_C_n_r_over_C_D0_bar_vs_AR_(L_c4)_(x_bar_ac_minus_x_bar_cg)

 $C_{Nr}_over_C_{D0} \!=\! -0.419$

 $C_{Nr\ W}\!:=\!C_{Nr_}over_squared_C_L\!\cdot\!C_L^{\ 2} + C_{Nr_}over_C_{D0}\!\cdot\!C_{D0}\!=\!0.06$

$$C_{Nr_V} \coloneqq -2 \cdot K_{Y_V} \cdot C_{L\alpha_V} \cdot \eta_{V_times_1_plus_d\sigma_over_d\beta} \cdot \frac{S_V}{S_W} \cdot \left(\frac{Z_V \cdot \sin{\langle \alpha_{WB} \rangle} + X_V \cdot \cos{\langle \alpha_{WB} \rangle}}{b_W} \right)^2 = -0.328$$

 $C_{Nr} \coloneqq C_{Nr_W} + C_{Nr_V} = -0.267$

Equilibrium system solution and results

 $\delta_a = -2.408 \; deg$

 $\delta_{rd} = 1.743 \; deg$

MAPPING AND OUTPUT CREATION

Includi << ..\Default_Map_Lateral_Directional.mcdx

Excel Writing

 $n_{sheet} \coloneqq 7$

 $First_Row_{LD} _{1} := 4$

 $Block_{LD_1} \coloneqq_{\mathsf{f}} \mathsf{map_matrix_transform} \left({}_{m} LatDir_Data_Map_{imported} \right)$

 $Excel_Output_{LD_1} \coloneqq {}_{\mathsf{f}} \mathsf{write_full_output} \left({}_{s}Output_Excel_File \,, Block_{LD_1} \,, n_{sheet}, First_Row_{LD_1} \right)$

 $First_Row_{LD_2} \coloneqq First_Row_{LD_1} + \text{rows} \left(Block_{LD_1}\right) + 2$

 $Block_{LD_2} := {}_{\mathbf{f}} \mathbf{map_matrix_transform} \left({}_{m} LatDir_Data_Map_{input} \right)$

 $Excel_Output_{LD_2} \coloneqq_{\mathbf{f}} \mathbf{write_full_output} \left({}_{s}Output_Excel_File \,, Block_{LD_2} \,, n_{sheet}, First_Row_{LD_2} \right)$

 $First_Row_{LD_3} \coloneqq First_Row_{LD_2} + rows \left(Block_{LD_2}\right) + 2$

 $Block_{LD_3} \coloneqq_{\mathbf{f}} \mathtt{map_matrix_transform} \left({_{m}LatDir_Data_Map} \right)$

 $Excel_Output_{LD_3} \coloneqq {}_{\mathbf{f}} \mathbf{write_full_output} \left({}_{s}Output_Excel_File \,, Block_{LD_3} \,, n_{sheet}, First_Row_{LD_3} \right)$

TeX Macro writing on .tex

$$\label{eq:complete_macros_loss} \begin{split} &_{v} complete_macros_{LD} \coloneqq \text{stack} \left(Block_{LD_1}^{(2)}, Block_{LD_2}^{(2)}, Block_{LD_3}^{(2)}\right) \\ &_{v} tex_{LD} \coloneqq \text{fwrite_matrix} \left(\text{``.} \text{`Output} \text{\botATERAL_DIRECTIONAL_TeX_Macros.tex''}, \\ &_{v} complete_macros_{LD}, \text{``'}\right) \end{split}$$