

WING PARAMETERS INITIALIZATION

Hidden Area --> Import of Excel INPUT Wing Data

Hidden Area --> Preliminary Mapping of imported Data and Cranked Wing CHECK

Hidden Area --> Import and preliminary mapping of OTHER Excel Data

Hidden Area --> Calculation of a few Horizontal Tail parameters, needed to compute wing downwash gradient

INPUT WING PARAMETERS LIST

Wing global parameters

$$b_W = 27.249 \text{ m}$$

$$i_W = 2 \text{ deg}$$

$$c_{W_r} = 5.243 \text{ m}$$

$$c_{W_{kink}} = 0 \text{ m}$$

$$c_{W_t} = 1.189 \text{ m}$$

$$t_{over_c_{W_r}} = 0.11$$

$$t_{over_c_{W_{kink}}} = 0$$

$$t_{over_c_{W_t}} = 0.11$$

$$\alpha_{0l_W_r} = -0.047$$

$$\alpha_{0l_W_{kink}} = 0$$

$$\alpha_{0l_W_t} = -0.047$$

$$C_{l\alpha_W_r} = 6.016$$

$$C_{l\alpha_W_{kink}} = 0$$

$$C_{l\alpha_W_t} = 6.016$$

$$C_{m_ac_W_r} = -0.07$$

$$C_{m_ac_W_{kink}} = 0$$

$$C_{m_ac_W_t} = -0.07$$

$$\xi_{ac_W_r} = 0.256$$

$$\xi_{ac_W_{kink}} = 0$$

$$\xi_{ac_W_t} = 0.251$$

$$M_{cr_W_2D_r} = 0.65$$

$$M_{cr_W_2D_{kink}} = 0$$

$$M_{cr_W_2D_t} = 0.68$$

$$\varepsilon_{W_{kink}} = 0$$

$$\varepsilon_{W_t} = -0.035$$

$$\eta_{a_in} = 0.664$$

$$\eta_{a_out} = 0.908$$

$$c_a = 0.792 \text{ m}$$

$$\eta_{flap_in} = 0.179$$

$$\eta_{flap_out} = 0.604$$

$$c_{flap} = 0.792 \text{ m}$$

$$\Delta\alpha_{0l_W_flaps} = 0.035$$

Wing, inner panel parameters

$b_{W_1} = 27.249 \text{ m}$	$c_{W_r_1} = 5.243 \text{ m}$	$c_{W_t_1} = 1.189 \text{ m}$
$t_{over_c_{W_r_1}} = 0.11$	$t_{over_c_{W_t_1}} = 0.11$	
$A_{W_{LE_1}} = 28 \text{ deg}$	$\Gamma_{W_1} = 2.2 \text{ deg}$	$\varepsilon_{W_t_1} = -2 \text{ deg}$
$\alpha_{0L_{W_r_1}} = -2.7 \text{ deg}$	$\alpha_{0L_{W_t_1}} = -2.7 \text{ deg}$	
$C_{l_{\alpha_{W_r_1}}} = 0.105 \text{ deg}^{-1}$	$C_{l_{\alpha_{W_t_1}}} = 0.105 \text{ deg}^{-1}$	
$C_{m_{ac_{W_r_1}}} = -0.07$	$C_{m_{ac_{W_t_1}}} = -0.07$	
$\xi_{ac_{W_r_1}} = 0.256$	$\xi_{ac_{W_t_1}} = 0.251$	$\xi_{imax_{W_1}} = 0.4$
$M_{cr_{W_2D_r_1}} = 0.65$	$M_{cr_{W_2D_t_1}} = 0.68$	

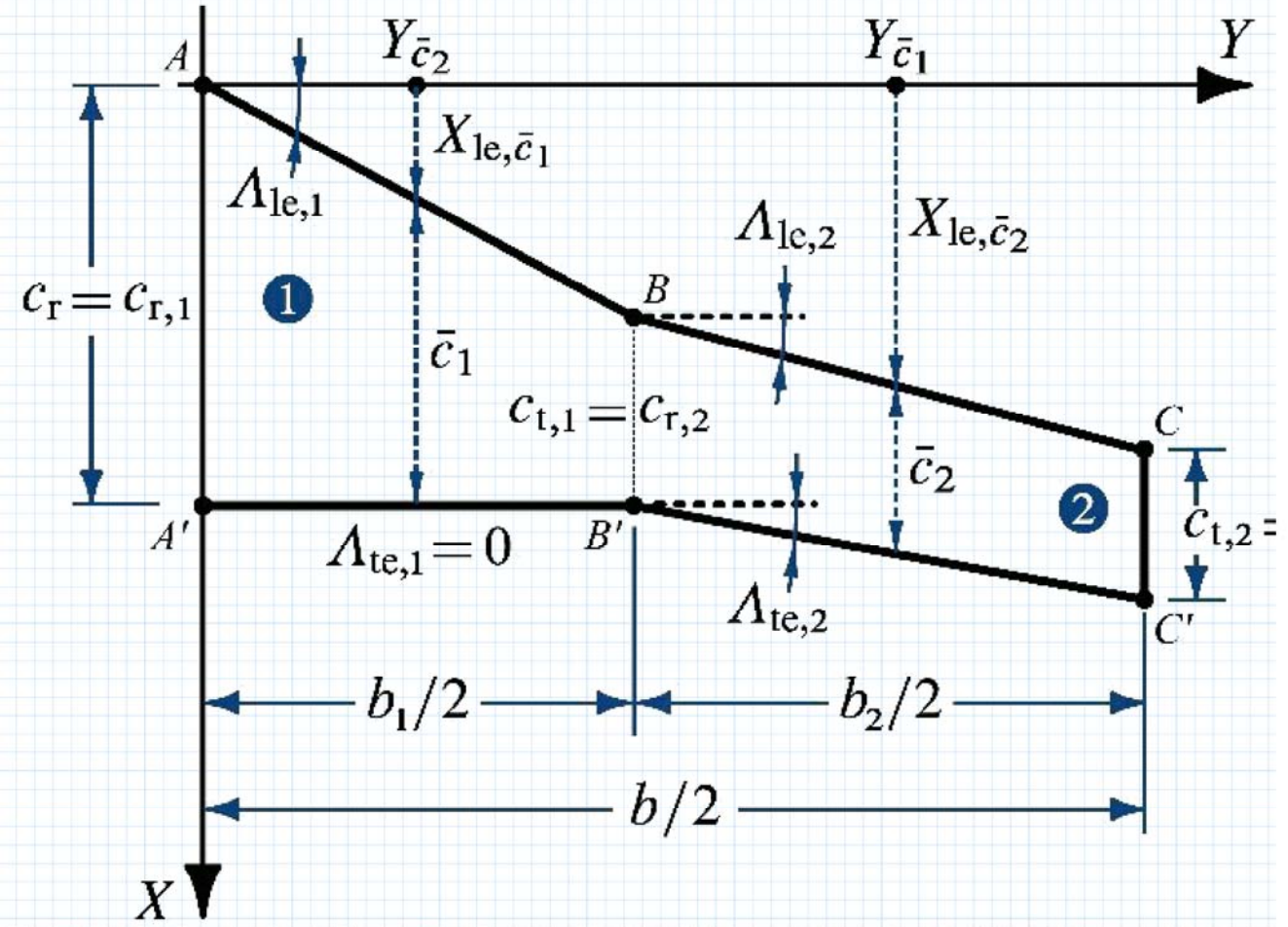
Wing, outer panel parameters

$b_{W_2} = 0 \text{ m}$	$c_{W_r_2} = 1.189 \text{ m}$	$c_{W_t_2} = 1.189 \text{ m}$
$t_{over_c_{W_r_2}} = 0.11$	$t_{over_c_{W_t_2}} = 0.11$	
$A_{W_{LE_2}} = 0 \text{ deg}$	$\Gamma_{W_2} = 0 \text{ deg}$	$\varepsilon_{W_t_2} = -2 \text{ deg}$
$\alpha_{0L_{W_r_2}} = -2.7 \text{ deg}$	$\alpha_{0L_{W_t_2}} = -2.7 \text{ deg}$	
$C_{l_{\alpha_{W_r_2}}} = 0.105 \text{ deg}^{-1}$	$C_{l_{\alpha_{W_t_2}}} = 0.105 \text{ deg}^{-1}$	
$C_{m_{ac_{W_r_2}}} = -0.07$	$C_{m_{ac_{W_t_2}}} = -0.07$	
$\xi_{ac_{W_r_2}} = 0.251$	$\xi_{ac_{W_t_2}} = 0.251$	$\xi_{imax_{W_2}} = 0$
$M_{cr_{W_2D_r_2}} = 0.68$	$M_{cr_{W_2D_t_2}} = 0.68$	

Imported parameters

$M_1 = 0.696$	$b_H = 11.217 \text{ m}$	$\Delta X_{W_{LE_Nose}} = 11.125 \text{ m}$
	$A_{H_{LE}} = 35 \text{ deg}$	$\Delta X_{HT_{LE_Nose}} = 27.859 \text{ m}$
	$\Gamma_H = 0 \text{ deg}$	$\Delta Z_{W_{LE_Nose}} = -0.945 \text{ m}$
	$c_{H_r} = 3.322 \text{ m}$	$\Delta Z_{HT_{LE_Nose}} = 6.096 \text{ m}$
	$c_{H_t} = 1.219 \text{ m}$	

WING PARAMETERS CALCULATIONS



Wing, inner panel basic parameters

$$\lambda_{W_1} := \frac{c_{W_{t,1}}}{c_{W_{r,1}}} = 0.227$$

$$\lambda_{W_1} = 0.227$$

$$S_{W_1} := \frac{b_{W_1}}{2} \cdot c_{W_{r,1}} \cdot (1 + \lambda_{W_1}) = 87.623 \text{ m}^2$$

$$S_{W_1} = 87.623 \text{ m}^2$$

$$AR_{W_1} := \frac{b_{W_1}^2}{S_{W_1}} = 8.474$$

$$AR_{W_1} = 8.474$$

$$MAC_{W_1} := \frac{2}{3} \cdot c_{W_{r,1}} \cdot \left(\frac{1 + \lambda_{W_1}^2 + \lambda_{W_1}}{1 + \lambda_{W_1}} \right) = 3.642 \text{ m}$$

$$MAC_{W_1} = 3.642 \text{ m}$$

$$X_{MAC_{LE_{W_1}}} := \frac{b_{W_1}}{6} \cdot \frac{(1 + 2 \cdot \lambda_{W_1})}{(1 + \lambda_{W_1})} \cdot \tan(\Lambda_{W_{LE_1}}) = 2.861 \text{ m}$$

$$X_{MAC_{LE_{W_1}}} = 2.861 \text{ m}$$

$$Y_{MAC_{W_1}} := \frac{b_{W_1}}{6} \cdot \frac{1 + 2 \cdot \lambda_{W_1}}{1 + \lambda_{W_1}} = 5.381 \text{ m}$$

$$Y_{MAC_{W_1}} = 5.381 \text{ m}$$

$$Z_{MAC_{W_1}} := Y_{MAC_{W_1}} \cdot \tan(\Gamma_{W_1}) = 0.207 \text{ m}$$

$$Z_{MAC_{W_1}} = 0.207 \text{ m}$$

Wing, outer panel basic parameters

$$\lambda_{W_2} := \frac{c_{W_t_2}}{c_{W_r_2}} = 1$$

$$\lambda_{W_2} = 1$$

$$S_{W_2} := \frac{b_{W_2}}{2} \cdot c_{W_r_2} \cdot (1 + \lambda_{W_2}) = 0 \text{ m}^2$$

$$S_{W_2} = 0 \text{ m}^2$$

$$AR_{W_2} := \frac{2 \cdot b_{W_2}}{c_{W_r_2} \cdot (1 + \lambda_{W_2})} = 0$$

$$AR_{W_2} = 0$$

$$MAC_{W_2} := \frac{2}{3} \cdot c_{W_r_2} \cdot \left(\frac{1 + \lambda_{W_2}^2 + \lambda_{W_2}}{1 + \lambda_{W_2}} \right) = 1.189 \text{ m}$$

$$MAC_{W_2} = 1.189 \text{ m}$$

$$X_{MAC_LE_W_2} := \frac{b_{W_2}}{6} \cdot \frac{(1 + 2 \cdot \lambda_{W_2})}{(1 + \lambda_{W_2})} \cdot \tan(\Lambda_{W_LE_2}) = 0 \text{ m}$$

$$X_{MAC_LE_W_2} = 0 \text{ m}$$

$$Y_{MAC_W_2} := \left(\frac{b_{W_2}}{6} \cdot \frac{1 + 2 \cdot \lambda_{W_2}}{1 + \lambda_{W_2}} \right) = 0 \text{ m}$$

$$Y_{MAC_W_2} = 0 \text{ m}$$

$$Z_{MAC_W_2} := Y_{MAC_W_2} \cdot \tan(\Gamma_{W_2}) = 0 \text{ m}$$

$$Z_{MAC_W_2} = 0 \text{ m}$$

Wing, global basic parameters

$$\lambda_W := \frac{c_{W_t}}{c_{W_r}} = 0.227$$

$$\lambda_W = 0.227$$

$$S_W := S_{W_1} + S_{W_2} = 87.623 \text{ m}^2$$

$$S_W = 87.623 \text{ m}^2$$

$$AR_W := \frac{(b_{W_1} + b_{W_2})^2}{S_W} = 8.474$$

$$AR_W = 8.474$$

$$MAC_W := \frac{S_{W_1} \cdot MAC_{W_1} + S_{W_2} \cdot MAC_{W_2}}{S_{W_1} + S_{W_2}} = 3.642 \text{ m}$$

$$MAC_W = 3.642 \text{ m}$$

$$\xi_{tmax_W} := \frac{\xi_{tmax_W_1} \cdot S_{W_1} + \xi_{tmax_W_2} \cdot S_{W_2}}{S_{W_1} + S_{W_2}} = 0.4$$

$$\xi_{tmax_W} = 0.4$$

Hidden Area --> Wing, linear laws defined over inner/outer panel semi-span

$$f_{c_W}(y) := \begin{cases} \text{if } y \leq \frac{b_{W_1}}{2} \\ \quad \text{return } f_{c_{W_1}}(y) \\ \text{else} \\ \quad \text{return } f_{c_{W_2}}(y) \end{cases}$$

$$f_{\alpha_{0L_2D_W}}(y) := \begin{cases} \text{if } y \leq \frac{b_{W_1}}{2} \\ \quad \text{return } f_{\alpha_{0L_W_2D_1}}(y) \\ \text{else} \\ \quad \text{return } f_{\alpha_{0L_W_2D_2}}(y) \end{cases}$$

$$f_{t_{over_cW}}(y) := \begin{cases} \text{if } y \leq \frac{b_{W_1}}{2} \\ \quad \text{return } f_{t_{over_cW_1}}(y) \\ \text{else} \\ \quad \text{return } f_{t_{over_cW_2}}(y) \end{cases}$$

$$f_{\epsilon_{g_W}}(y) := \begin{cases} \text{if } y \leq \frac{b_{W_1}}{2} \\ \quad \text{return } f_{\epsilon_{g_{W_1}}}(y) \\ \text{else} \\ \quad \text{return } f_{\epsilon_{g_{W_2}}}(y) \end{cases}$$

$$f_{C_{l\alpha_W}}(y) := \begin{cases} \text{if } y \leq \frac{b_{W_1}}{2} \\ \quad \text{return } f_{C_{l\alpha_{W_1}}}(y) \\ \text{else} \\ \quad \text{return } f_{C_{l\alpha_{W_2}}}(y) \end{cases}$$

$$f_{C_{m_{ac_2D_W}}}(y) := \begin{cases} \text{if } y \leq \frac{b_{W_1}}{2} \\ \quad \text{return } f_{C_{m_{ac_2D_{W_1}}}}(y) \\ \text{else} \\ \quad \text{return } f_{C_{m_{ac_2D_{W_2}}}}(y) \end{cases}$$

$$f_{\xi_{ac_2D_W}}(y) := \begin{cases} \text{if } y \leq \frac{b_{W_1}}{2} \\ \quad \text{return } f_{\xi_{ac_2D_{W_1}}}(y) \\ \text{else} \\ \quad \text{return } f_{\xi_{ac_2D_{W_2}}}(y) \end{cases}$$

$$f_{M_{cr_2D_W}}(y) := \begin{cases} \text{if } y \leq \frac{b_{W_1}}{2} \\ \quad \text{return } f_{M_{cr_{W_2D_1}}}(y) \\ \text{else} \\ \quad \text{return } f_{M_{cr_{W_2D_2}}}(y) \end{cases}$$

Wing, inner panel 2D mean quantities

$$t_{over_cW_mean_1} := \frac{2}{S_{W_1}} \cdot \int_0^{\frac{b_{W_1}}{2}} f_{cW}(y) \cdot f_{t_over_cW}(y) dy = 0.11$$

$$t_{over_cW_mean_1} = 0.11$$

$$C_{l\alpha_W_mean_1} := \frac{2}{S_{W_1}} \cdot \int_0^{\frac{b_{W_1}}{2}} f_{cW}(y) \cdot f_{C_{l\alpha_W}}(y) dy = 6.016$$

$$C_{l\alpha_W_mean_1} = 0.105 \text{ deg}^{-1}$$

$$\alpha_{0l_W_mean_1} := \frac{2}{S_{W_1}} \cdot \int_0^{\frac{b_{W_1}}{2}} f_{cW}(y) \cdot f_{\alpha_{0l_2D_W}}(y) dy = -0.047 \text{ rad}$$

$$\alpha_{0l_W_mean_1} = -2.7 \text{ deg}$$

$$C_{m_ac_W_mean_1} := \frac{2}{S_{W_1} \cdot MAC_{W_1}} \cdot \int_0^{\frac{b_{W_1}}{2}} f_{cW}(y)^2 \cdot f_{C_{m_ac_2D_W}}(y) dy = -0.07$$

$$C_{m_ac_W_mean_1} = -0.07$$

Wing, outer panel 2D mean quantities

$$t_{over_cW_mean_2} := \text{if} \left(bCrk = 0, t_{over_cW_t}, \frac{2}{S_{W_2}} \cdot \int_0^{\frac{b_W}{2}} f_{cW}(y) \cdot f_{t_over_cW}(y) dy \right) = 0.11$$

$$t_{over_cW_mean_2} = 0.11$$

$$C_{l\alpha_W_mean_2} := \text{if} \left(bCrk = 0, C_{l\alpha_W_t}, \frac{2}{S_{W_2}} \cdot \int_0^{\frac{b_W}{2}} f_{cW}(y) \cdot f_{C_{l\alpha_W}}(y) dy \right) = 6.016 \text{ rad}^{-1}$$

$$C_{l\alpha_W_mean_2} = 0.105 \text{ deg}^{-1}$$

$$\alpha_{0l_W_mean_2} := \text{if} \left(bCrk = 0, \alpha_{0l_W_t}, \frac{2}{S_{W_2}} \cdot \int_0^{\frac{b_W}{2}} f_{cW}(y) \cdot f_{\alpha_{0l_2D_W}}(y) dy \right) = -0.047 \text{ rad}$$

$$\alpha_{0l_W_mean_2} = -2.7 \text{ deg}$$

$$C_{m_ac_W_mean_2} := \text{if} \left(bCrk = 0, C_{m_ac_W_t}, \frac{2}{S_{W_2} \cdot MAC_{W_2}} \cdot \int_0^{\frac{b_W}{2}} f_{cW}(y)^2 \cdot f_{C_{m_ac_2D_W}}(y) dy \right) = -0.07$$

$$C_{m_ac_W_mean_2} = -0.07$$

Wing, global 2D mean quantities

$$t_{over_cW_mean} := \frac{2}{S_W} \cdot \int_0^{\frac{b_W}{2}} f_{cW}(y) \cdot f_{t_over_cW}(y) dy = 0.11$$

$$t_{over_cW_mean} = 0.11$$

$$C_{l\alpha_W_mean} := \frac{2}{S_W} \cdot \int_0^{\frac{b_W}{2}} f_{cW}(y) \cdot f_{C_{l\alpha_W}}(y) dy = 6.016$$

$$C_{l\alpha_W_mean} = 0.105 \text{ deg}^{-1}$$

$$\alpha_{0l_W_mean} := \frac{2}{S_W} \cdot \int_0^{\frac{b_W}{2}} f_{cW}(y) \cdot f_{\alpha_{0l_2D_W}}(y) dy = -0.047 \text{ rad}$$

$$\alpha_{0l_W_mean} = -2.7 \text{ deg}$$

$$C_{m_ac_W_mean} := \frac{2}{S_W \cdot MAC_W} \cdot \int_0^{\frac{b_W}{2}} f_{cW}(y)^2 \cdot f_{C_{m_ac_2D_W}}(y) dy = -0.07$$

$$C_{m_ac_W_mean} = -0.07$$

Wing, 3D alpha-zero-lift for inner panel, outer panel and whole wing

$$\alpha_{0L_W_1} := \frac{2}{S_{W_1}} \cdot \int_0^{\frac{b_{W_1}}{2}} f_{c_W}(y) \cdot (f_{\alpha_{0L_2D_W}}(y) - f_{\epsilon_{g_W}}(y)) \, dy = -0.033 \text{ rad} \quad \alpha_{0L_W_1} = -1.91 \text{ deg}$$

$$\alpha_{0L_W_2} := \text{if} \left(\left(Crk = 0, \alpha_{0L_W_1}, \frac{2}{S_{W_2}} \cdot \int_{\frac{b_{W_1}}{2}}^{\frac{b_W}{2}} f_{c_W}(y) \cdot (f_{\alpha_{0L_2D_W}}(y) - f_{\epsilon_{g_W}}(y)) \, dy \right) \right) = -0.047 \text{ rad} \quad \alpha_{0L_W_2} = -2.7 \text{ deg}$$

$$\alpha_{0L_W} := \frac{2}{S_W} \cdot \int_0^{\frac{b_W}{2}} f_{c_W}(y) \cdot (f_{\alpha_{0L_2D_W}}(y) - f_{\epsilon_{g_W}}(y)) \, dy = -0.033 \text{ rad} \quad \alpha_{0L_W} = -1.91 \text{ deg}$$

Wing, sweep angles for inner/outer panel

$$f_{\Lambda}(x, \Lambda_{le}, AR, \lambda) := \text{if} \left(AR = 0, \Lambda_{le}, \text{atan} \left(\tan(\Lambda_{le}) - \frac{4 \cdot x \cdot (1 - \lambda)}{AR \cdot (1 + \lambda)} \right) \right)$$

• Sweep angle function

$$\Lambda_{W_LE_1} := f_{\Lambda}(0, \Lambda_{W_LE_1}, AR_{W_1}, \lambda_{W_1}) = 0.489 \quad \Lambda_{W_LE_1} = 28 \text{ deg}$$

$$\Lambda_{W_TE_1} := f_{\Lambda}(1, \Lambda_{W_LE_1}, AR_{W_1}, \lambda_{W_1}) = 0.23 \quad \Lambda_{W_TE_1} = 13.179 \text{ deg}$$

$$\Lambda_{W_c4_1} := f_{\Lambda}(0.25, \Lambda_{W_LE_1}, AR_{W_1}, \lambda_{W_1}) = 0.429 \quad \Lambda_{W_c4_1} = 24.576 \text{ deg}$$

$$\Lambda_{W_c2_1} := f_{\Lambda}(0.5, \Lambda_{W_LE_1}, AR_{W_1}, \lambda_{W_1}) = 0.366 \quad \Lambda_{W_c2_1} = 20.954 \text{ deg}$$

$$\Lambda_{W_tmax_1} := f_{\Lambda}(\xi_{tmax_W_1}, \Lambda_{W_LE_1}, AR_{W_1}, \lambda_{W_1}) = 0.391 \quad \Lambda_{W_tmax_1} = 22.426 \text{ deg}$$

$$\Lambda_{W_LE_2} := f_{\Lambda}(0, \Lambda_{W_LE_2}, AR_{W_2}, \lambda_{W_2}) = 0 \quad \Lambda_{W_LE_2} = 0 \text{ deg}$$

$$\Lambda_{W_TE_2} := f_{\Lambda}(1, \Lambda_{W_LE_2}, AR_{W_2}, \lambda_{W_2}) = 0 \quad \Lambda_{W_TE_2} = 0 \text{ deg}$$

$$\Lambda_{W_c4_2} := f_{\Lambda}(0.25, \Lambda_{W_LE_2}, AR_{W_2}, \lambda_{W_2}) = 0 \quad \Lambda_{W_c4_2} = 0 \text{ deg}$$

$$\Lambda_{W_c2_2} := f_{\Lambda}(0.5, \Lambda_{W_LE_2}, AR_{W_2}, \lambda_{W_2}) = 0 \quad \Lambda_{W_c2_2} = 0 \text{ deg}$$

$$\Lambda_{W_tmax_2} := f_{\Lambda}(\xi_{tmax_W_2}, \Lambda_{W_LE_2}, AR_{W_2}, \lambda_{W_2}) = 0 \quad \Lambda_{W_tmax_2} = 0 \text{ deg}$$

Wing, Mean Aerodynamic Chord position with respect to Wing Apex

$$\begin{aligned} fY_{MAC_W}(MAC) &:= \text{if } MAC \geq c_{W_t1} \\ &\quad || \text{return } \frac{b_{W1} \cdot (MAC - c_{W_r1})}{2 \cdot (c_{W_t1} - c_{W_r1})} \\ &\quad || \\ \text{else} \\ &\quad || \text{return } \frac{b_{W1}}{2} + \frac{b_{W2} \cdot (MAC - c_{W_r2})}{2 \cdot (c_{W_t2} - c_{W_r2})} \\ &\quad || \end{aligned}$$

- Function for Mean Aerodynamic Chord distance from wing apex, along Y axis

$$\begin{aligned} fX_{MAC_LE_W}(MAC) &:= \text{if } MAC > c_{W_t1} \\ &\quad || \text{return } fY_{MAC_W}(MAC) \cdot \tan(\Lambda_{W_LE1}) \\ &\quad || \\ \text{else} \\ &\quad || \text{return } \frac{b_{W1}}{2} \cdot \tan(\Lambda_{W_LE1}) + \frac{b_{W2} \cdot (MAC - c_{W_r2})}{2 \cdot (c_{W_t2} - c_{W_r2})} \cdot \tan(\Lambda_{W_LE2}) \\ &\quad || \end{aligned}$$

- Function for Mean Aerodynamic Chord Leading Edge distance from wing apex, along X axis

$$\begin{aligned} fZ_{MAC_W}(MAC) &:= \text{if } fY_{MAC_W}(MAC) < \frac{b_{W1}}{2} \\ &\quad || \text{return } fY_{MAC_W}(MAC) \cdot \tan(\Gamma_{W1}) \\ &\quad || \\ \text{else} \\ &\quad || \text{return } \frac{b_{W1}}{2} \cdot \tan(\Gamma_{W1}) + \left(fY_{MAC_W}(MAC) - \frac{b_{W1}}{2} \right) \cdot \tan(\Gamma_{W2}) \\ &\quad || \end{aligned}$$

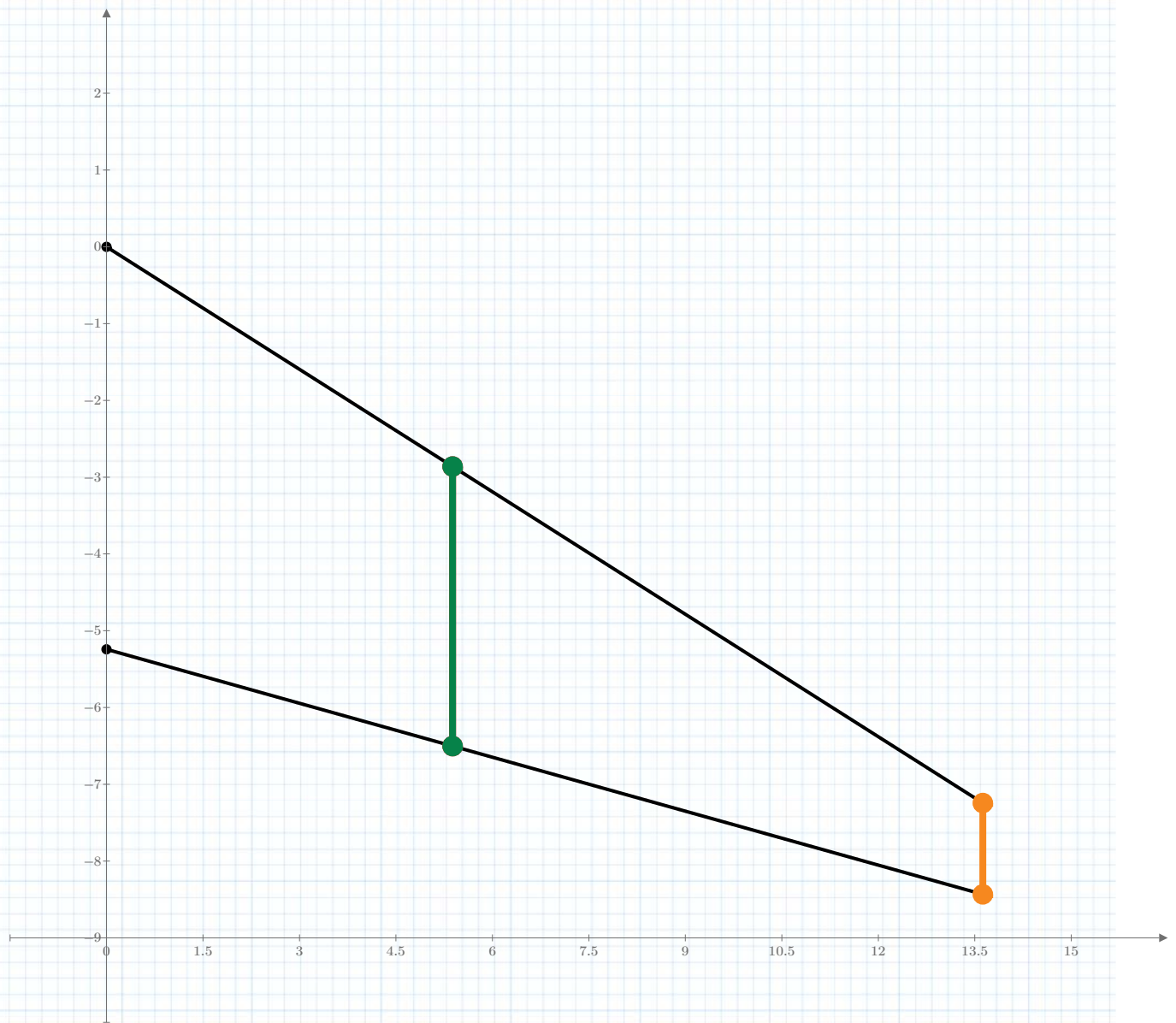
- Function for Mean Aerodynamic Chord distance from wing apex, along Z axis

$$X_{MAC_LE_W} := fX_{MAC_LE_W}(MAC_W) = 2.861 \text{ m}$$

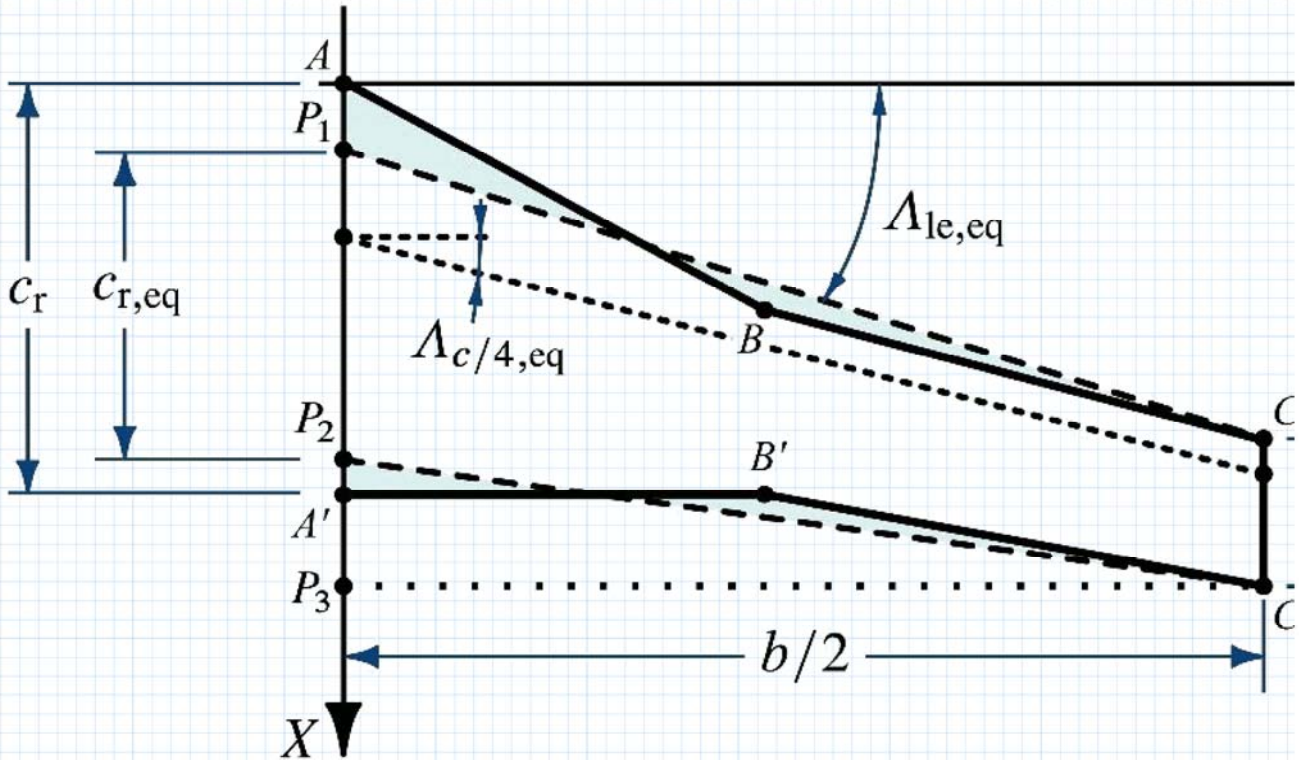
$$Y_{MAC_W} := fY_{MAC_W}(MAC_W) = 5.381 \text{ m}$$

$$Z_{MAC_W} := fZ_{MAC_W}(MAC_W) = 0.207 \text{ m}$$

Wing planform with Mean Aerodynamic Chord



EQUIVALENT WING PARAMETERS CALCULATIONS



Equivalent Wing, geometric parameters

$$X_B := \frac{b_{W_1}}{2} \cdot \tan(\Lambda_{W_{LE_1}}) = 7.244 \text{ m}$$

$$Y_B := \frac{b_{W_1}}{2} = 13.625 \text{ m}$$

$$X_C := X_B + \frac{b_{W_2}}{2} \cdot \tan(\Lambda_{W_{LE_2}}) = 7.244 \text{ m}$$

$$Y_C := \frac{b_W}{2} = 13.625 \text{ m}$$

$$X_{C'} := X_C + c_{W_{t_2}} = 8.433 \text{ m}$$

$$Y_{C'} := Y_C$$

$$X_{B'} := X_B + c_{W_{t_1}} = 8.433 \text{ m}$$

$$Y_{B'} := Y_B = 13.625 \text{ m}$$

$$X_{A'} := c_{W_{r_1}} = 5.243 \text{ m}$$

$$Y_{A'} := 0 \text{ m}$$

Hidden Area --> Equivalent Wing, equivalence of areas on leading edge

Hidden Area --> Equivalent Wing, equivalence of areas on trailing edge

Equivalent Wing, planform results

$$X_{P1} = 0 \text{ m}$$

$$X_{P2} = 5.243 \text{ m}$$

$$X_{W_{r_{LE_{eqv}}}} := X_{P1} = 0 \text{ m}$$

$$X_{W_{r_{TE_{eqv}}}} := X_{P2} = 5.243 \text{ m}$$

$$c_{W_{r_{eqv}}} := |X_{P2} - X_{P1}| = 5.243 \text{ m}$$

$$\lambda_{W_{eqv}} := \frac{c_{W_{t_1}}}{c_{W_{r_{eqv}}}} = 0.227$$

$$AR_{W_{eqv}} := \frac{b_W^2}{S_W} = 8.474$$

$$\Lambda_{W_LE_eqv} := \text{atan} \left(\frac{2 \cdot \langle X_C - X_{P1} \rangle}{b_{W_1} + b_{W_2}} \right) = 0.489 \text{ } \textcolor{blue}{rad}$$

$$\Lambda_{W_LE_eqv} = 28 \text{ } \textcolor{blue}{deg}$$

$$\Lambda_{W_TE_eqv} := \text{f}\Lambda \left(1.0, \Lambda_{W_LE_eqv}, AR_{W_eqv}, \lambda_{W_eqv} \right) = 0.23 \text{ } \textcolor{blue}{rad}$$

$$\Lambda_{W_TE_eqv} = 13.179 \text{ } \textcolor{blue}{deg}$$

$$\Lambda_{W_c4_eqv} := \text{f}\Lambda \left(0.25, \Lambda_{W_LE_eqv}, AR_{W_eqv}, \lambda_{W_eqv} \right) = 0.429 \text{ } \textcolor{blue}{rad}$$

$$\Lambda_{W_c4_eqv} = 24.576 \text{ } \textcolor{blue}{deg}$$

$$\Lambda_{W_c2_eqv} := \text{f}\Lambda \left(0.5, \Lambda_{W_LE_eqv}, AR_{W_eqv}, \lambda_{W_eqv} \right) = 0.366 \text{ } \textcolor{blue}{rad}$$

$$\Lambda_{W_c2_eqv} = 20.954 \text{ } \textcolor{blue}{deg}$$

$$\Lambda_{W_tmax_eqv} := \text{f}\Lambda \left(\xi_{tmax_W}, \Lambda_{W_LE_eqv}, AR_W, \lambda_{W_eqv} \right) = 0.391 \text{ } \textcolor{blue}{rad}$$

$$\Lambda_{W_tmax_eqv} = 22.426 \text{ } \textcolor{blue}{deg}$$

$$\Gamma_{W_eqv} := \frac{\Gamma_{W_1} \cdot S_{W_1} + \Gamma_{W_2} \cdot S_{W_2}}{S_{W_1} + S_{W_2}} = 0.038$$

$$\Gamma_{W_eqv} = 2.2 \text{ } \textcolor{blue}{deg}$$

$$MAC_{W_eqv} := \frac{2}{3} \cdot c_{W_r_eqv} \cdot \left(\frac{1 + \lambda_{W_eqv}^2 + \lambda_{W_eqv}}{1 + \lambda_{W_eqv}} \right) = 3.642 \text{ } \textcolor{blue}{m}$$

$$MAC_{W_eqv} = 3.642 \text{ } \textcolor{blue}{m}$$

$$X_{MAC_LE_W_eqv} := \frac{b_W}{6} \cdot \frac{\langle 1 + 2 \cdot \lambda_{W_eqv} \rangle}{\langle 1 + \lambda_{W_eqv} \rangle} \cdot \tan \langle \Lambda_{W_LE_eqv} \rangle = 2.861 \text{ } \textcolor{blue}{m}$$

$$X_{MAC_LE_W_eqv} = 2.861 \text{ } \textcolor{blue}{m}$$

$$Y_{MAC_W_eqv} := \left(\frac{b_W}{6} \cdot \frac{1 + 2 \cdot \lambda_{W_eqv}}{1 + \lambda_{W_eqv}} \right) = 5.381 \text{ } \textcolor{blue}{m}$$

$$Y_{MAC_W_eqv} = 5.381 \text{ } \textcolor{blue}{m}$$

$$Z_{MAC_W_eqv} := Y_{MAC_W_eqv} \cdot \tan \langle \Gamma_{W_eqv} \rangle = 0.207 \text{ } \textcolor{blue}{m}$$

$$Z_{MAC_W_eqv} = 0.207 \text{ } \textcolor{blue}{m}$$

CONSTRUCTED OUTBOARD PANEL PARAMETERS CALCULATIONS (DATCOM METHOD)

Constructed Outboard Panel parameters calculation

$$\Delta y := \text{if} \left(b_{Crk} = 0, 0 \cdot \text{m}, \frac{1}{2} \cdot \left(\frac{b_{W-1}}{2} \right) \right) = 0 \text{ m}$$

$$\Delta y = 0 \text{ m}$$

$$b'_{W-2} := b_{W-2} + 2 \Delta y = 0 \text{ m}$$

$$b'_{W-2} = 0 \text{ m}$$

$$b_{W-2} = 0 \text{ m}$$

$$\frac{b'_{W-2}}{2} = 0 \text{ m}$$

$$\frac{b_{W-2}}{2} = 0 \text{ m}$$

$$c'_{W-r-2} := c_{W-2} \left(\frac{b_{W-1}}{2} - \Delta y \right) = 1.189 \text{ m}$$

$$c'_{W-r-2} = 1.189 \text{ m}$$

$$c_{W-r-2} = 1.189 \text{ m}$$

$$\lambda'_{W-2} := \frac{c_{W-t-2}}{c'_{W-r-2}} = 1$$

$$\lambda'_{W-2} = 1$$

$$\lambda_{W-2} = 1$$

$$S'_{W-2} := \frac{b'_{W-2}}{2} \cdot c'_{W-r-2} \cdot (1 + \lambda'_{W-2}) = 0 \text{ m}^2$$

$$S'_{W-2} = 0 \text{ m}^2$$

$$S_{W-2} = 0 \text{ m}^2$$

$$AR'_{W-2} := \frac{2 \cdot b'_{W-2}}{c'_{W-r-2} \cdot (1 + \lambda'_{W-2})} = 0$$

$$AR'_{W-2} = 0$$

$$AR_{W-2} = 0$$

$$MAC'_{W-2} := \frac{2}{3} \cdot c'_{W-r-2} \cdot \left(\frac{1 + \lambda'^2_{W-2} + \lambda'_{W-2}}{1 + \lambda'_{W-2}} \right) = 1.189 \text{ m}$$

$$MAC'_{W-2} = 1.189 \text{ m}$$

$$MAC_{W-2} = 1.189 \text{ m}$$

$$Y'_{MAC-W-2} := \frac{b'_{W-2}}{6} \cdot \frac{1 + 2 \cdot \lambda'_{W-2}}{1 + \lambda'_{W-2}} = 0 \text{ m}$$

$$Y'_{MAC-W-2} = 0 \text{ m}$$

$$Y_{MAC-W-2} = 0 \text{ m}$$

$$X'_{MAC-LE-W-2} := Y'_{MAC-W-2} \cdot \tan(\Lambda_{W-LE-2}) = 0 \text{ m}$$

$$X'_{MAC-LE-W-2} = 0 \text{ m}$$

$$X_{MAC-LE-W-2} = 0 \text{ m}$$

$$X'_{LE-r-W-2} := \frac{b_{W-1}}{2} \cdot \tan(\Lambda_{W-LE-1}) - \Delta y \cdot \tan(\Lambda_{W-LE-2}) = 7.244 \text{ m}$$

$$Y'_{LE-r-W-2} := \frac{b_{W-1}}{2} - \Delta y = 13.625 \text{ m}$$

$$X'_{LE-t-W-2} := \frac{b_{W-1}}{2} \cdot \tan(\Lambda_{W-LE-1}) + \frac{b_{W-2}}{2} \cdot \tan(\Lambda_{W-LE-2}) = 7.244 \text{ m}$$

$$Y'_{LE-t-W-2} := \frac{b_{W-1} + b_{W-2}}{2} = 13.625 \text{ m}$$

$$X'_{TE-t-W-2} := X'_{LE-t-W-2} + c_{W-t-2} = 8.433 \text{ m}$$

$$Y'_{TE-t-W-2} := Y'_{LE-t-W-2} = 13.625 \text{ m}$$

$$X'_{TE-r-W-2} := X'_{LE-r-W-2} + c'_{W-r-2} = 8.433 \text{ m}$$

$$Y'_{TE-r-W-2} := Y'_{LE-r-W-2} = 13.625 \text{ m}$$

Comparison among Cranked, Equivalent, and Constructed Outboard Panel Wing planforms



MISCELLANEOUS DATA CALCULATIONS

Induced drag factors, only due to geometric effects

$$e_{W_alt_1} := \frac{2}{2 - AR_{W_1} + \sqrt{4 + AR_{W_1}^2 (1 + \tan(\Lambda_{W_tmax_1})^2)}} = 0.688$$

$$e_{W_alt_1} = 0.688$$

$$e_{W_alt_2} := \frac{2}{2 - AR_{W_2} + \sqrt{4 + AR_{W_2}^2 (1 + \tan(\Lambda_{W_tmax_2})^2)}} = 0.5$$

$$e_{W_alt_2} = 0.5$$

$$e_{W_alt} := \frac{2}{2 - AR_W + \sqrt{4 + AR_W^2 (1 + \tan(\Lambda_{W_tmax_eqv})^2)}} = 0.688$$

$$e_{W_alt} = 0.688$$

$$e_{W_1_alt_A0} := 1.78 \cdot (1 - 0.045 \cdot AR_{W_1}^{0.68}) - 0.64 = 0.797$$

$$e_{W_2_alt_A0} := 1.78 \cdot (1 - 0.045 \cdot AR_{W_2}^{0.68}) - 0.64 = 1.14$$

$$e_{W_alt_A0} := 1.78 \cdot (1 - 0.045 \cdot AR_W^{0.68}) - 0.64 = 0.797$$

• **Alternative formula: valid for unswept wings**

$$e_{W_1_alt_A} := 4.61 \cdot (1 - 0.045 \cdot AR_{W_1}^{0.68}) \cdot \cos(\Lambda_{W_LE_1})^{0.15} - 3.1 = 0.554$$

$$e_{W_2_alt_A} := 4.61 \cdot (1 - 0.045 \cdot AR_{W_2}^{0.68}) \cdot \cos(\Lambda_{W_LE_2})^{0.15} - 3.1 = 1.51$$

$$e_{W_alt_A} := 4.61 \cdot (1 - 0.045 \cdot AR_W^{0.68}) \cdot \cos(\Lambda_{W_LE_eqv})^{0.15} - 3.1 = 0.554$$

• **Alternative formula: valid for swept wings**

3d critical Mach number at mean aerodynamic chord

$$M_{cr_W_1_3D_@MAC_1} := \frac{fM_{cr_2D_W}(Y_{MAC_W_1})}{\cos(\Lambda_{W_LE_1})} = 0.784$$

$$M_{cr_W_1_3D_@MAC_1} = 0.784$$

$$M_{cr_W_2_3D_@MAC_2} := \frac{fM_{cr_2D_W}(Y_{MAC_W_2})}{\cos(\Lambda_{W_LE_2})} = 0.68$$

$$M_{cr_W_2_3D_@MAC_2} = 0.68$$

$$M_{cr_W_3D_@MAC} := \frac{fM_{cr_2D_W}(Y_{MAC_W})}{\cos(\Lambda_{W_LE_eqv})} = 0.784$$

$$M_{cr_W_3D_@MAC} = 0.784$$

Ailerons inner and outer stations and area

$$y_{a_in} := \eta_{a_in} \cdot \frac{b_W}{2} = 9.047 \text{ m}$$

$$y_{a_in} = 9.047 \text{ m}$$

$$y_{a_out} := \eta_{a_out} \cdot \frac{b_W}{2} = 12.371 \text{ m}$$

$$y_{a_out} = 12.371 \text{ m}$$

$$c_{W_mean_@a} := fC_W \left(\frac{y_{a_in} + y_{a_out}}{2} \right) = 2.056$$

$$c_{W_mean_@a} = 2.056$$

$$S_a := 2 \cdot c_a \cdot (y_{a_out} - y_{a_in}) = 5.269 \text{ m}^2$$

$$S_a = 5.269 \text{ m}^2$$

Flaps inner and outer stations and area

$$y_{flap_in} := \eta_{flap_in} \cdot \frac{b_W}{2} = 2.439 \text{ m}$$

$$y_{flap_in} = 2.439 \text{ m}$$

$$y_{flap_out} := \eta_{flap_out} \cdot \frac{b_W}{2} = 8.229 \text{ m}$$

$$y_{flap_out} = 8.229 \text{ m}$$

$$S_{flap} := 2 \cdot c_{flap} \cdot (y_{flap_out} - y_{flap_in}) = 9.178 \text{ m}^2$$

$$S_{flap} = 9.178 \text{ m}^2$$

$$\alpha_{0L_W_flaps_open} := \alpha_{0L_W} + \frac{S_{flap}}{S_W} \cdot \Delta\alpha_{0L_W_flaps} = -0.03$$

$$\alpha_{0L_W_flaps_open} = -1.701 \text{ deg}$$

WING LIFT CURVE SLOPE

Wing Lift Curve Slope, function definitions

• Polhamus Formula Coefficient

$$f_{k_{Polhamus}}(M, M_{cr_3D}, \Lambda_{LE}, \lambda, AR) := \begin{cases} \text{if } (M < M_{cr_3D}) \wedge (\Lambda_{LE} < 32 \text{ deg}) \wedge (\lambda > 0.4) \wedge (\lambda < 1) \wedge (AR > 3) \wedge (AR < 8) \\ \quad \text{if } AR < 4 \\ \quad \quad \text{return } 1 + \frac{AR \cdot (1.87 - 0.000233 \cdot \Lambda_{LE})}{100} \\ \quad \text{else} \\ \quad \quad \text{return } 1 + \frac{((8.2 - 2.3 \cdot \Lambda_{LE}) - AR \cdot (0.22 - 0.153 \cdot \Lambda_{LE}))}{100} \\ \text{else} \\ \quad \text{(---> Polhamus Formula is not valid)} \\ \text{return } 100 \end{cases}$$

• General Formula for Lift Curve Slope

$$f_{C_{L\alpha_W}}(M, k_P, AR, \Lambda_{c2}, C_{l\alpha@MAC}, \Lambda_{LE}) := \begin{cases} \text{if } AR = 0 \\ \quad \text{return } C_{l\alpha@MAC} \\ \text{if } k_P \neq 100 \quad \text{(---> use Polhamus Formula)} \\ \quad \text{return } \frac{2 \cdot \pi \cdot AR}{2 + \sqrt{\left(\left(\frac{AR^2 \cdot (1 - M^2)}{k_P^2} \left(1 + \frac{\tan^2(\Lambda_{c2})}{(1 - M^2)} \right) \right) + 4 \right)}} \\ \text{else} \quad \text{(---> use alternative formula)} \\ \quad a_0 \leftarrow \frac{C_{l\alpha@MAC}}{\sqrt{1 - M^2 \cdot \cos^2(\Lambda_{LE})}} \\ \quad \text{return } \frac{a_0 \cdot \cos(\Lambda_{LE})}{\sqrt{1 - (M \cdot \cos(\Lambda_{LE}))^2 + \left(\frac{a_0 \cdot \cos(\Lambda_{LE})}{\pi \cdot AR} \right)^2}} + \frac{a_0 \cdot \cos(\Lambda_{LE})}{\pi \cdot AR} \end{cases}$$

Wing Lift Curve Slope, classic formula for inner/outer panel and whole wing

$$C_{L\alpha W_1_classic} := \frac{C_{l\alpha W_mean_1}}{\sqrt{1-M_1^2} + \frac{C_{l\alpha W_mean_1}}{\pi \cdot AR_{W_1} \cdot e_{W_alt_1}}} = 5.748$$

$$C_{L\alpha W_1_classic} = 0.1 \text{ deg}^{-1}$$

$$C_{L\alpha W_2_classic} := \text{if} \left(bCrk = 0, \frac{C_{l\alpha W_mean_2}}{\sqrt{1-M_1^2}}, \frac{C_{l\alpha W_mean_2}}{\sqrt{1-M_1^2} + \frac{C_{l\alpha W_mean_2}}{\pi \cdot AR_{W_2} \cdot e_{W_alt_2}}} \right) = 8.378 \text{ rad}^{-1}$$

$$C_{L\alpha W_2_classic} = 0.146 \text{ deg}^{-1}$$

$$C_{L\alpha W_classic} := \frac{C_{l\alpha W_mean}}{\sqrt{1-M_1^2} + \frac{C_{l\alpha W_mean}}{\pi \cdot AR_W \cdot e_{W_alt}}} = 5.748 \text{ rad}^{-1}$$

$$C_{L\alpha W_classic} = 0.1 \text{ deg}^{-1}$$

Wing Lift Curve Slope, general formula for inner/outer panel and whole wing

$$k_{Polhamus_1} := f_{k_{Polhamus}}(M_1, M_{cr_W_1_3D_@MAC_1}, A_{W_LE_1}, \lambda_{W_1}, AR_{W_1}) = 100$$

$$k_{Polhamus_1} = 100$$

$$C_{l\alpha W_1_@MAC_1} := f_{C_{l\alpha W}}(Y_{MAC_W_1}) = 6.016 \text{ rad}^{-1}$$

$$C_{l\alpha W_1_@MAC_1} = 0.105 \text{ deg}^{-1}$$

$$C_{L\alpha W_1_@M0} := f_{C_{L\alpha W}}(0, k_{Polhamus_1}, AR_{W_1}, A_{W_c2_1}, C_{l\alpha W_1_@MAC_1}, A_{W_LE_1})$$

$$C_{L\alpha W_1_@M0} = 4.357 \text{ rad}^{-1}$$

$$C_{L\alpha W_1_@M0} = 0.076 \text{ deg}^{-1}$$

$$C_{L\alpha W_1} := f_{C_{L\alpha W}}(M_1, k_{Polhamus_1}, AR_{W_1}, A_{W_c2_1}, C_{l\alpha W_1_@MAC_1}, A_{W_LE_1})$$

$$C_{L\alpha W_1} = 6.227 \text{ rad}^{-1}$$

$$C_{L\alpha W_1} = 0.109 \text{ deg}^{-1}$$

$$k_{Polhamus_2} := f_{k_{Polhamus}}(M_1, M_{cr_W_2_3D_@MAC_2}, A_{W_LE_2}, \lambda_{W_2}, AR_{W_2}) = 100$$

$$k_{Polhamus_2} = 100$$

$$C_{l\alpha W_2_@MAC_2} := f_{C_{l\alpha W}}(Y_{MAC_W_2}) = 6.016 \text{ rad}^{-1}$$

$$C_{l\alpha W_2_@MAC_2} = 0.105 \text{ deg}^{-1}$$

$$C_{L\alpha W_2_@M0} := f_{C_{L\alpha W}}(0, k_{Polhamus_2}, AR_{W_2}, A_{W_c2_2}, C_{l\alpha W_2_@MAC_2}, A_{W_LE_2})$$

$$C_{L\alpha W_2_@M0} = 6.016 \text{ rad}^{-1}$$

$$C_{L\alpha W_2_@M0} = 0.105 \text{ deg}^{-1}$$

$$C_{L\alpha W_2} := f_{C_{L\alpha W}}(M_1, k_{Polhamus_2}, AR_{W_2}, A_{W_c2_2}, C_{l\alpha W_2_@MAC_2}, A_{W_LE_2})$$

$$C_{L\alpha W_2} = 6.016 \text{ rad}^{-1}$$

$$C_{L\alpha W_2} = 0.105 \text{ deg}^{-1}$$

$$k_{Polhamus_W} := f_{k_{Polhamus}}(M_1, M_{cr_W_3D_@MAC}, A_{W_LE_eqv}, \lambda_{W_eqv}, AR_{W_eqv}) = 100$$

$$k_{Polhamus_W} = 100$$

$$C_{l\alpha W_@MAC} := f_{C_{l\alpha W}}(Y_{MAC_W}) = 6.016 \text{ rad}^{-1}$$

$$C_{l\alpha W_@MAC} = 0.105 \text{ deg}^{-1}$$

$$C_{L\alpha W_@M0} := f_{C_{L\alpha W}}(0, k_{Polhamus_W}, AR_{W_eqv}, A_{W_c2_eqv}, C_{l\alpha W_@MAC}, A_{W_LE_eqv})$$

$$C_{L\alpha W_@M0} = 4.357 \text{ rad}^{-1}$$

$$C_{L\alpha W_@M0} = 0.076 \text{ deg}^{-1}$$

$$C_{L\alpha W} := f_{C_{L\alpha W}}(M_1, k_{Polhamus_W}, AR_{W_eqv}, A_{W_c2_eqv}, C_{l\alpha W_@MAC}, A_{W_LE_eqv})$$

$$C_{L\alpha W} = 6.227 \text{ rad}^{-1}$$

$$C_{L\alpha W} = 0.109 \text{ deg}^{-1}$$

Wing lift coefficient at initial conditions

$$C_{L0_W_1} := C_{L\alpha_W_1} \cdot (i_W - \alpha_{0L_W_1}) = 0.425$$

$$C_{L0_W_1} = 0.425$$

$$C_{L0_W_2} := C_{L\alpha_W_2} \cdot (i_W - \alpha_{0L_W_2}) = 0.494$$

$$C_{L0_W_2} = 0.494$$

$$C_{L0_W} := C_{L\alpha_W} \cdot (i_W - \alpha_{0L_W}) = 0.425$$

$$C_{L0_W} = 0.425$$

Induced drag factor, due to both geometric and aerodynamic effects

$$\text{fe}(C_{L\alpha}, AR, \lambda, \Lambda_{LE}) := \begin{cases} \lambda_e \leftarrow \frac{AR \cdot \lambda}{\cos(\Lambda_{LE})} \\ R \leftarrow 0.0004 \cdot \lambda_e^3 - 0.008 \cdot \lambda_e^2 + 0.0501 \cdot \lambda_e + 0.8642 \\ \text{return if} \left(AR = 0, 0, \frac{1.1 \cdot C_{L\alpha}}{R \cdot C_{L\alpha} + (1 - R) \pi \cdot AR} \right) \end{cases}$$

- Function for calculating wing induced drag factor, including aerodynamic and geometric effects

$$e_{W_1} := \text{fe}(C_{L\alpha_W_1}, AR_{W_1}, \lambda_{W_1}, \Lambda_{W_LE_1}) = 0.918$$

$$e_{W_1} = 0.918$$

$$e_{W_2} := \text{fe}(C_{L\alpha_W_2}, AR_{W_2}, \lambda_{W_2}, \Lambda_{W_LE_2}) = 0$$

$$e_{W_2} = 0$$

$$e_W := \text{fe}(C_{L\alpha_W}, AR_W, \lambda_W, \Lambda_{W_LE_eqv}) = 0.918$$

$$e_W = 0.918$$

WING AERODYNAMIC CENTER - GRAPHICAL METHOD (DATCOM/NAPOLITANO)

@Aerodynamic Database ---> (x_bar_ac_w)_k1_vs_lambda

$$K1_{ac_W_1_Datcom} = 1.432$$

$$K1_{ac_W_2_Datcom} = 1$$

$$K1_{ac_W_eqv_Datcom} = 1.432$$

@Aerodynamic Database ---> (x_bar_ac_w)_k2_vs_L_LE_(AR)_lambda

$$K2_{ac_W_1_Datcom} = 0.553$$

$$K2_{ac_W_2_Datcom} = 0$$

$$K2_{ac_W_eqv_Datcom} = 0.553$$

@Aerodynamic Database ---> (x_bar_ac_w)_x'_ac_over_root_chord_vs_tan(L_LE)_over_beta_(AR_times_tan(L_LE))_lambda

$$X_{ac_over_c_r_W_1_Datcom} = 0.757$$

$$X_{ac_over_c_r_W_2_Datcom} = 0.256$$

$$X_{ac_over_c_r_W_eqv_Datcom} = 0.757$$

$$X_{ac_over_c_{r_W_Datcom}} := \frac{X_{ac_over_c_{r_W_1_Datcom}} \cdot S_{W_1} \cdot C_{L\alpha_W_1} + X_{ac_over_c_{r_W_2_Datcom}} \cdot S_{W_2} \cdot C_{L\alpha_W_2}}{S_{W_1} \cdot C_{L\alpha_W_1} + S_{W_2} \cdot C_{L\alpha_W_2}} = 0.757$$

Adimensional aerodynamic center position with respect to MAC leading edge

$$\xi_{ac_W_1} := K1_{ac_W_1_Datcom} \cdot (X_{ac_over_c_{r_W_1_Datcom}} - K2_{ac_W_1_Datcom}) = 0.293$$

$$\xi_{ac_W_1} = 0.293$$

$$\xi_{ac_W_2} := K1_{ac_W_2_Datcom} \cdot (X_{ac_over_c_{r_W_2_Datcom}} - K2_{ac_W_2_Datcom}) = 0.256$$

$$\xi_{ac_W_2} = 0.256$$

$$\xi_{ac_W_eqv} := K1_{ac_W_eqv_Datcom} \cdot (X_{ac_over_c_{r_W_eqv_Datcom}} - K2_{ac_W_eqv_Datcom}) = 0.293$$

$$\xi_{ac_W_eqv} = 0.293$$

$$\xi_{ac_W} := \frac{\xi_{ac_W_1} \cdot S_{W_1} \cdot C_{L\alpha_W_1} + \xi_{ac_W_2} \cdot S_{W_2} \cdot C_{L\alpha_W_2}}{S_{W_1} \cdot C_{L\alpha_W_1} + S_{W_2} \cdot C_{L\alpha_W_2}} = 0.293$$

Aerodynamic center position with respect to wing apex

$$X_{ac_W_1} := \xi_{ac_W_1} \cdot MAC_{W_1} + X_{MAC_LE_W_1} = 3.928 \text{ m}$$

$$X_{ac_W_1} = 3.928 \text{ m}$$

$$X_{ac_W_2} := \xi_{ac_W_2} \cdot MAC_{W_2} + X_{MAC_LE_W_2} = 0.304 \text{ m}$$

$$X_{ac_W_2} = 0.304 \text{ m}$$

$$X_{ac_W_eqv} := \xi_{ac_W_eqv} \cdot MAC_{W_eqv} + X_{MAC_LE_W_eqv} = 3.928 \text{ m}$$

$$X_{ac_W_eqv} = 3.928 \text{ m}$$

$$X_{ac_W} := \xi_{ac_W} \cdot MAC_W + X_{MAC_LE_W} = 3.928 \text{ m}$$

$$X_{ac_W} = 3.928 \text{ m}$$

Aerodynamic center position with respect to MAC leading edge

$$x_{ac_W_1} := X_{ac_W_1} - X_{MAC_LE_W_1} = 1.067 \text{ m}$$

$$x_{ac_W_1} = 1.067 \text{ m}$$

$$x_{ac_W_2} := X_{ac_W_2} - X_{MAC_LE_W_2} = 0.304 \text{ m}$$

$$x_{ac_W_2} = 0.304 \text{ m}$$

$$x_{ac_W_eqv} := X_{ac_W_eqv} - X_{MAC_LE_W_eqv} = 1.067 \text{ m}$$

$$x_{ac_W_eqv} = 1.067 \text{ m}$$

$$x_{ac_W} := X_{ac_W} - X_{MAC_LE_W} = 1.067 \text{ m}$$

$$x_{ac_W} = 1.067 \text{ m}$$



SHRENK'S METHOD FOR BASIC AND ADDITIONAL WING LOADING

Loading function definitions and remarkable values

$$f c_{\text{eff}}(y) := \frac{f c_W(y) \cdot f C_{l_{\alpha_W}}(y)}{C_{l_{\alpha_W \text{ mean}}}}$$

$$c_{\text{ell}_0} := \frac{4 \cdot S_W}{\pi \cdot b_W} \quad f c_{\text{ell}}(y) := c_{\text{ell}_0} \cdot \sqrt{1 - \left(\frac{y}{\frac{b_W}{2}} \right)^2}$$

$$f \alpha_b(y) := \alpha_{0L_W} - (f \alpha_{0L_{2D_W}}(y) - f \varepsilon_{g_W}(y))$$

$$f C_{l_b}(y) := \frac{1}{2} \cdot f c_W(y) \cdot f C_{l_{\alpha_W}}(y) \cdot f \alpha_b(y)$$

$$f C_{l_a}(y) := \frac{1}{2} \cdot (f c_{\text{eff}}(y) + f c_{\text{ell}}(y))$$

$$f C_l(y) := f C_{l_b}(y) + f C_{l_a}(y)$$

$$C_{L_b} := \frac{2}{S_W} \cdot \int_0^{\frac{b_W}{2}} f C_{l_b}(y) dy = -2.697 \cdot 10^{-19}$$

$$C_{L_a} := \frac{2}{S_W} \cdot \int_0^{\frac{b_W}{2}} f C_{l_a}(y) dy = 1$$

- Effective chord distribution function

- Elliptic chord distribution function

- "Basic" angle of attack function

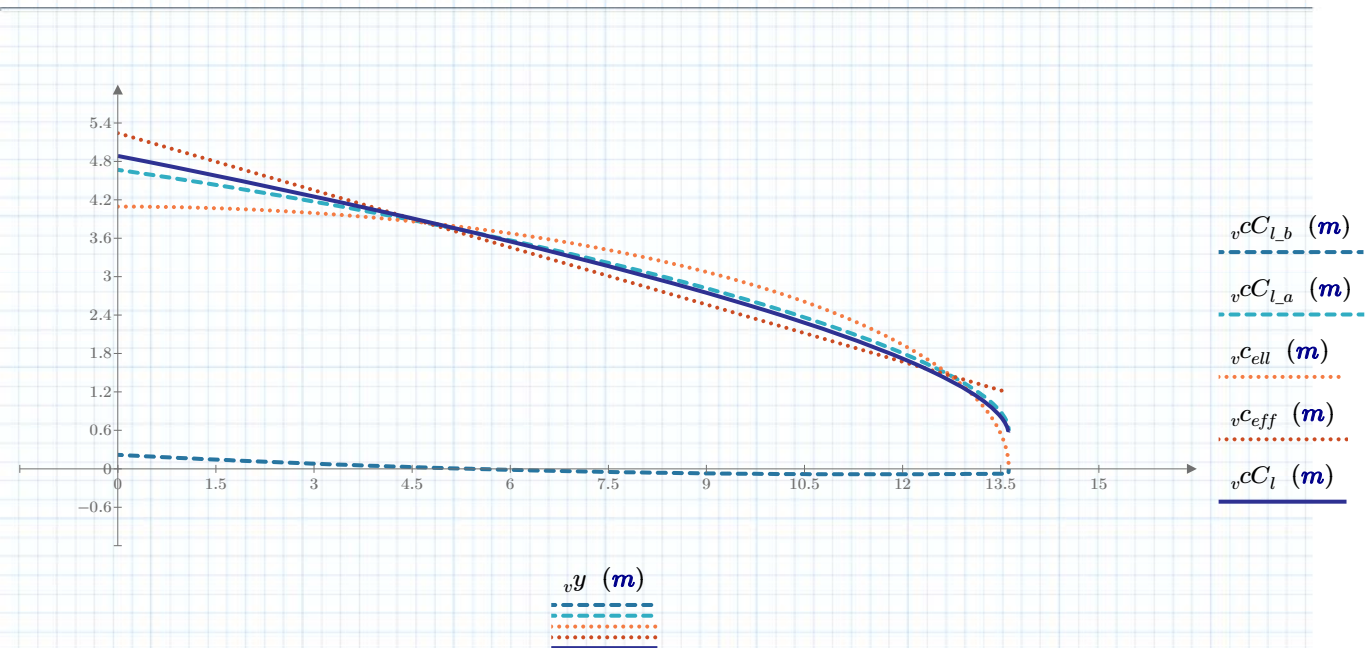
- Basic wing loading

- Additional wing loading function

- Wing loading function

- **REMARK:** the effects of wing sweep angle are neglected

Spanwise loading curve plots



3D PITCHING MOMENT COEFFICIENT ABOUT WING AERODYNAMIC CENTER

Exact formulation

$$\begin{aligned} r_{x_{b_W}}(y) &:= \text{if } y \leq \frac{b_{W_1}}{2} \\ &\quad \left\| \begin{aligned} &\text{return } X_{ac_W} - (y \cdot \tan(\Lambda_{W_LE_1}) + r_{c_W}(y) \cdot r_{\xi_{ac_2D_W}}(y)) \\ &\text{else} \\ &\left\| \begin{aligned} &\text{return } X_{ac_W} - \left(\frac{b_{W_1}}{2} \cdot \tan(\Lambda_{W_LE_1}) + \left(y - \frac{b_{W_1}}{2} \right) \cdot \tan(\Lambda_{W_LE_2}) + r_{c_W}(y) \cdot r_{\xi_{ac_2D_W}}(y) \right) \end{aligned} \right\| \end{aligned} \right. \end{aligned}$$

• Moment arm from section's aerodynamic center to wing 3D aerodynamic center

$$C_{M_ac_W_b} := \frac{2}{S_W \cdot MAC_W} \cdot \int_0^{\frac{b_W}{2}} r_{c_{l_b}}(y) \cdot r_{x_{b_W}}(y) \, dy = 0.013$$

$$C_{M_ac_W_b} = 0.013$$

$$C_{M_ac_W_a} := \frac{2}{S_W \cdot MAC_W} \cdot \int_0^{\frac{b_W}{2}} r_{c_{m_ac_2D_W}}(y) \cdot r_{c_W}(y)^2 \, dy = -0.07$$

$$C_{M_ac_W_a} = -0.07$$

$$C_{M_ac_W} := C_{M_ac_W_b} + C_{M_ac_W_a} = -0.057$$

$$C_{M_ac_W} = -0.05704$$

Approximated formulation (Roskam)

$$C_{M_ac_W_b_Roskam} := \frac{2 \cdot \pi}{S_W \cdot MAC_W} \cdot \int_0^{\frac{b_W}{2}} r_{\alpha_b}(y) \cdot r_{c_W}(y) \cdot r_{x_{b_W}}(y) \, dy = 0.014$$

$$C_{M_ac_W_b_Roskam} = 0.014$$

$$C_{M_ac_W_Roskam} := C_{M_ac_W_b_Roskam} + C_{M_ac_W_a} = -0.056$$

$$C_{M_ac_W_Roskam} = -0.056$$



DOWNWASH

Prandtl Lifting Line Theory (LLT)

$$f\varepsilon_{\alpha_{LLT}W}(C_{L\alpha}, AR, e, M) := \text{if} \left(AR = 0, 0, 2 \cdot \frac{C_{L\alpha}}{\pi \cdot AR \cdot e} \cdot \frac{1}{\sqrt{1-M^2}} \right)$$

• Downwash gradient according to linear theory

$$\varepsilon_{\alpha_{LLT}@M0_W} := f\varepsilon_{\alpha_{LLT}W}(C_{L\alpha_W}, AR_W, e_W, 0) = 0.51$$

$$\varepsilon_{\alpha_{LLT}@M0_W} = 0.51$$

$$\varepsilon_{\alpha_{LLT}W} := f\varepsilon_{\alpha_{LLT}W}(C_{L\alpha_W}, AR_W, e_W, M_1) = 0.71$$

$$\varepsilon_{\alpha_{LLT}W} = 0.71$$

$$\varepsilon_{0_{LLT}W} := \varepsilon_{\alpha_{LLT}W} \cdot (i_W - \alpha_{0L_W}) = 0.048$$

$$\varepsilon_{0_{LLT}W} = 2.775 \text{ deg}$$

DATCOM Method

$$\Delta X_{HT_{LE-W_{LE}}} := \Delta X_{HT_{LE-Nose}} - \Delta X_{W_{LE-Nose}} = 16.734 \text{ m}$$

$$\Delta X_{HT_{LE-W_{LE}}} = 16.7 \text{ m}$$

$$\Delta Z_{HT_{LE-W_{LE}}} := \Delta Z_{HT_{LE-Nose}} - \Delta Z_{W_{LE-Nose}} = 7.041 \text{ m}$$

$$\Delta Z_{HT_{LE-W_{LE}}} = 7.04 \text{ m}$$

$$\xi_{ac_H} := K1_{ac_H_{Datcom}} \cdot (X_{ac-over_c_{r_H_{Datcom}}} - K2_{ac_H_{Datcom}}) = 0.264$$

$$\xi_{ac_H} = 0.264$$

$$\Delta Z_{HT_{MAC4-W_{MAC4}}} := \Delta Z_{HT_{LE-W_{LE}}} + Y_{MAC_H} \cdot \tan(\Gamma_H) - Y_{MAC_W} \cdot \tan(\Gamma_{W_{eqv}}) = 6.834 \text{ m}$$

- Normal to FRL
- Parallel to FRL

$$\Delta X_{HT_{MAC4-W_{MAC4}}} := \Delta X_{HT_{LE-W_{LE}}} + \left(X_{MAC_{LE_H}} + \frac{MAC_H}{4} \right) - \left(X_{MAC_{LE_W}} + \frac{MAC_W}{4} \right) = 15.231 \text{ m}$$

$$\Delta Z'_{HT_{MAC4-W_{MAC4}}} := \Delta X_{HT_{MAC4-W_{MAC4}}} \cdot \sin(i_W) + \Delta Z_{HT_{MAC4-W_{MAC4}}} \cdot \cos(i_W) = 7.362 \text{ m}$$

- Normal to root chord
- Parallel to root chord

$$\Delta X'_{HT_{MAC4-W_{MAC4}}} := \Delta X_{HT_{MAC4-W_{MAC4}}} \cdot \cos(i_W) - \Delta Z_{HT_{MAC4-W_{MAC4}}} \cdot \sin(i_W) = 14.983 \text{ m}$$

$$\Delta X_{HT_{ac-W_{ac}}} := \Delta X_{HT_{LE-W_{LE}}} + (X_{MAC_{LE_H}} + \xi_{ac_H} \cdot MAC_H) - X_{ac_W} = 15.107 \text{ m}$$

$$\Delta X_{HT_{ac-W_{ac}}} = 15.10 \text{ m}$$

$$\Delta Z_{HT_{ac-W_{ac}}} := \Delta Z_{HT_{MAC4-W_{MAC4}}} = 6.834 \text{ m}$$

$$\Delta Z_{HT_{ac-W_{ac}}} = 6.834 \text{ m}$$

$$fK_{AR}(AR) := \frac{1}{AR} - \frac{1}{1 + (AR)^{1.7}}$$

$$fK_{\lambda}(\lambda) := \frac{10 - 3 \cdot \lambda}{7}$$

- Empirical coefficients function definitions

$$K_M(M, C_{L\alpha @ M0}, C_{L\alpha}) := \begin{cases} \text{return } \sqrt{1 - M^2} & \text{if } M \leq 0.7 \\ \text{return } \frac{C_{L\alpha}}{C_{L\alpha @ M0}} & \text{else} \end{cases}$$

$$fK_{MAC4}(\Delta Z', \Delta X', b) := \frac{1 - \frac{\Delta Z'}{b}}{\sqrt[3]{2 \cdot \frac{\Delta X'}{b}}}$$

$$K_{AR_W} := fK_{AR}(AR_W) = 0.092$$

$$K_{AR_W} = 0.092$$

$$K_{\lambda_W} := fK_{\lambda}(\lambda_W) = 1.331$$

$$K_{\lambda_W} = 1.331$$

$$K_{MAC4_{WH}} := fK_{MAC4}(\Delta Z'_{HT_{MAC4-W_{MAC4}}}, \Delta X'_{HT_{MAC4-W_{MAC4}}}, b_W) = 0.707$$

$$K_{MAC4_{WH}} = 0.707$$

$$K_{M_W} := K_M(M_1, C_{L\alpha_{W @ M0}}, C_{L\alpha_W}) = 0.718$$

$$K_{M_W} = 0.718$$

$$\varepsilon_{\alpha @ M0_W} := 4.44 \cdot (K_{AR_W} \cdot K_{\lambda_W} \cdot K_{MAC4_{WH}} \cdot \sqrt{\cos(\Lambda_{W_{c4_{eqv}}})})^{1.19} = 0.229$$

$$\varepsilon_{\alpha @ M0_W} = 0.229$$

$$\varepsilon_{\alpha_W} := \varepsilon_{\alpha @ M0_W} \cdot \sqrt{1 - M_1^2}$$

$$\varepsilon_{\alpha_W} = 0.164$$

$$\varepsilon_{0_W} := \varepsilon_{\alpha_W} \cdot (i_W - \alpha_{0L_W}) = 0.011$$

$$\varepsilon_{0_W} = 0.643 \text{ deg}$$

MISCELLANEOUS PARAMETERS PLOT

$v c_W$ (m)

$v x_{b_W}$ (m)

$v \varepsilon_g$ (deg)

$v \alpha_{0l_{2D}}$ (deg)



$v y$ (m)

MAPPING AND OUTPUT CREATION

Includi << ../Default_Map_Wing.mcdx

Excel Writing

```
First_RowW_1 := 4
BlockW_1 := fmap_matrix_transform ( mWing_Data_Mapimported )
Excel_OutputW_1 := fwrite_full_output ( sOutput_Excel_File , BlockW_1 , nsheet , First_RowW_1 )
```

```
First_RowW_2 := First_RowW_1 + rows ( BlockW_1 ) + 2 = 25
BlockW_2 := fmap_matrix_transform ( mWing_Data_Mapinput )
Excel_OutputW_2 := fwrite_full_output ( sOutput_Excel_File , BlockW_2 , nsheet , First_RowW_2 )
```

```
First_RowW_3 := First_RowW_2 + rows ( BlockW_2 ) + 2 = 87
BlockW_3 := fmap_matrix_transform ( mWing_Data_Map )
Excel_OutputW_3 := fwrite_full_output ( sOutput_Excel_File , BlockW_3 , nsheet , First_RowW_3 )
```

```
First_RowW_4 := First_RowW_3 + rows ( BlockW_3 ) + 2 = 373
BlockW_4 := fmap_matrix_transform ( mWing_Data_MapCOP )
Excel_OutputW_4 := fwrite_full_output ( sOutput_Excel_File , BlockW_4 , nsheet , First_RowW_4 )
```

```
First_RowW_5 := First_RowW_4 + rows ( BlockW_4 ) + 2 = 407
BlockW_5 := fmap_matrix_transform ( mWing_Data_MapLLCcoeffs )
Excel_OutputW_5 := fwrite_full_output ( sOutput_Excel_File , BlockW_5 , nsheet , First_RowW_5 )
```

```
First_RowW_6 := First_RowW_5 + rows ( BlockW_5 ) + 2 = 475
BlockW_6 := fmap_matrix_transform ( mWing_Data_MapMisc )
Excel_OutputW_6 := fwrite_full_output ( sOutput_Excel_File , BlockW_6 , nsheet , First_RowW_6 )
```

CSV Tabs Writing

```
mCSVW_1 := augment ( vy , vcell , vceff , vcCl_a , vcCl_b ) •  $\frac{1}{m}$ 
CSV_OutputW_1 := WRITECSV ( “.\Output\WING_shrenk_loading(y,c_ell,c_eff,cCl_a,cCl_b).csv” , mCSVW_1 )
```

```
mCSVW_2 := augment (  $y \cdot \frac{1}{m}$  ,  $x_{b_W} \cdot \frac{1}{m}$  ,  $IC_{M_{ac_W_b}} \cdot \frac{1}{m^2}$  ,  $IC_{M_{ac_W_b_Roskam}} \cdot \frac{1}{m^2}$  )
CSV_OutputW_2 := WRITECSV ( “.\Output\WING_shrenk-roskam_loading(y,x_b,IC_M_b,IC_M_b_Roskam).csv” , mCSVW_2 )
```

```
mCSVW_3 := augment (  $y \cdot \frac{1}{m}$  ,  $c_W \cdot \frac{1}{m}$  ,  $\alpha_{0L_{2D}}$  ,  $\epsilon_g$  ,  $c_{l\alpha_W}$  ,  $c_{m_{ac_{2D_W}}}$  ,  $\xi_{ac_{2D_W}}$  )
CSV_OutputW_3 := WRITECSV ( “.\Output\WING_linear_laws(y,c,alphaz,epsilon,Clalpha,Cmac,Csiac).csv” , mCSVW_3 )
```

$${}_mCSV_{W_4} := \text{augment} \left({}_vX_W, {}_vY_W \right) \cdot \frac{1}{\textcolor{blue}{m}}$$

$$CSV_Output_{W_4} := \text{WRITECSV} \left(“.\backslash\text{Output}\backslash\text{WING_planform}(X_W,Y_W).csv” , {}_mCSV_{W_4} \right)$$

$${}_mCSV_{W_5} := \text{augment} \left({}_vX_{mac.1}, {}_vY_{mac.1}, {}_vX_{mac.2}, {}_vY_{mac.2}, {}_vX_{mac.W}, {}_vY_{mac.W}, {}_vX_{ac_W}, {}_vY_{ac_W} \right) \cdot \frac{1}{\textcolor{blue}{m}}$$

$$CSV_Output_{W_5} := \text{WRITECSV} \left(“.\backslash\text{Output}\backslash\text{WING_planform_MAC_and_AC}(Xmac1,Ymac1,Xmac2,Ymac2,XmacW,YmacW).csv” , {}_mCSV_{W_5} \right)$$

$${}_mCSV_{W_6} := \text{augment} \left({}_vX_{ac_2D}, {}_vY_{ac_2D} \right) \cdot \frac{1}{\textcolor{blue}{m}}$$

$$CSV_Output_{W_6} := \text{WRITECSV} \left(“.\backslash\text{Output}\backslash\text{WING_planform_ac2D}(Xac2D,Yac2D).csv” , {}_mCSV_{W_6} \right)$$

TeX Macro writing on .tex

$${}_vcomplete_macros_W := \text{stack} \left(Block_{W_1}^{(2)}, Block_{W_2}^{(2)}, Block_{W_3}^{(2)}, Block_{W_4}^{(2)}, Block_{W_5}^{(2)}, Block_{W_6}^{(2)} \right)$$

$${}_vtex_W := \text{fwrite_matrix} \left(“.\backslash\text{Output}\backslash\text{WING_TeX_Macros.tex” , } {}_vcomplete_macros_W, “ ” \right)$$