$$= \frac{2\pi R}{2 + \sqrt{\frac{R^2 \beta^2}{k^2} \left(1 + \frac{\tan^2 \Lambda_{c/2}}{\beta^2}\right) + 4}}$$