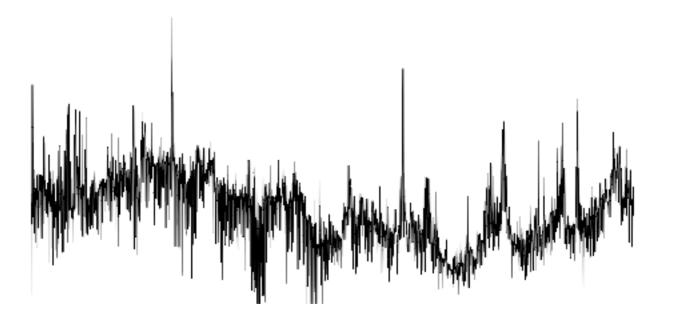
## ELECTRICITY PRICE FORECASTING



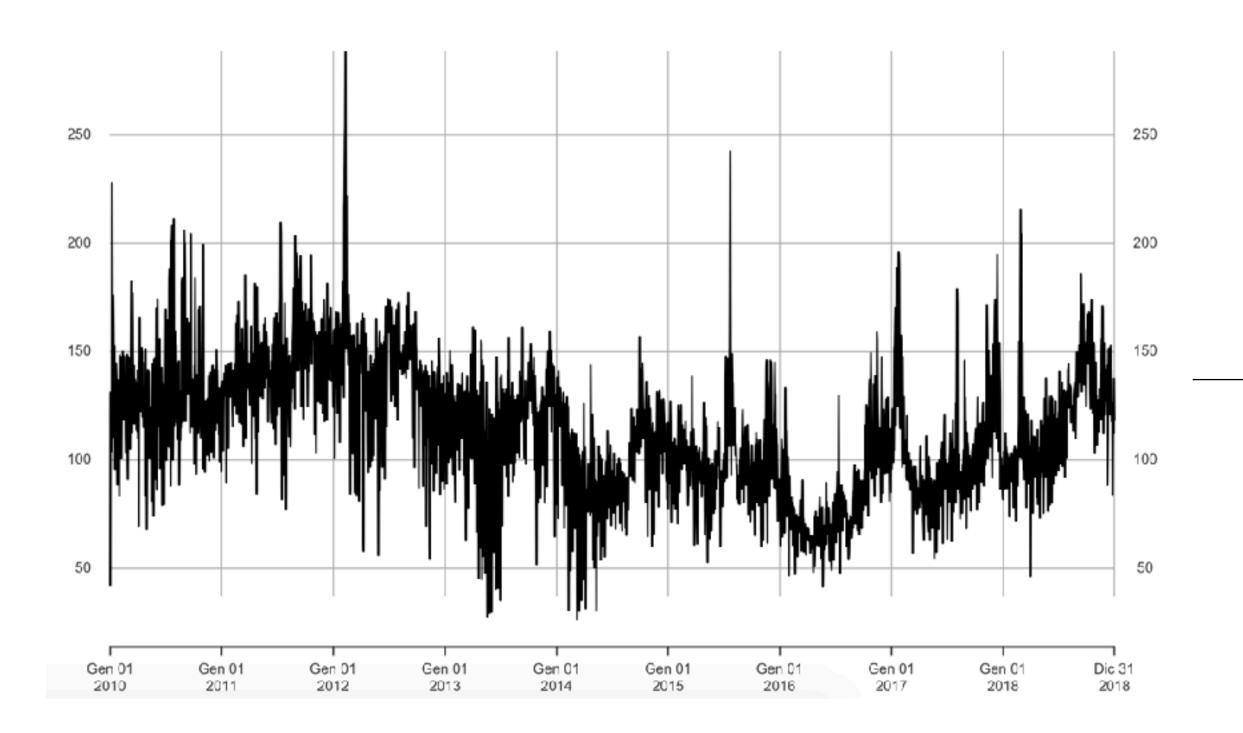
Streaming Data Management and Time Series Analysis

Academic Year 2019/2020

# PROJECT WORKFLOW

#### THE TASK

The goal is the daily prediction over a 11 months horizon using 9-years price data with ARIMA, UCM and Machine Leaning models



## MODELS

**ARIMA** 

UCM

KNN

LSTM RNN

#### PREPROCESSING

- Logarithmic Transformation
- Train-Val Split (90% 10%)

#### METRICS

MAE

COMPARISON AND CONCLUSIONS

**ARIMA** 

UCM

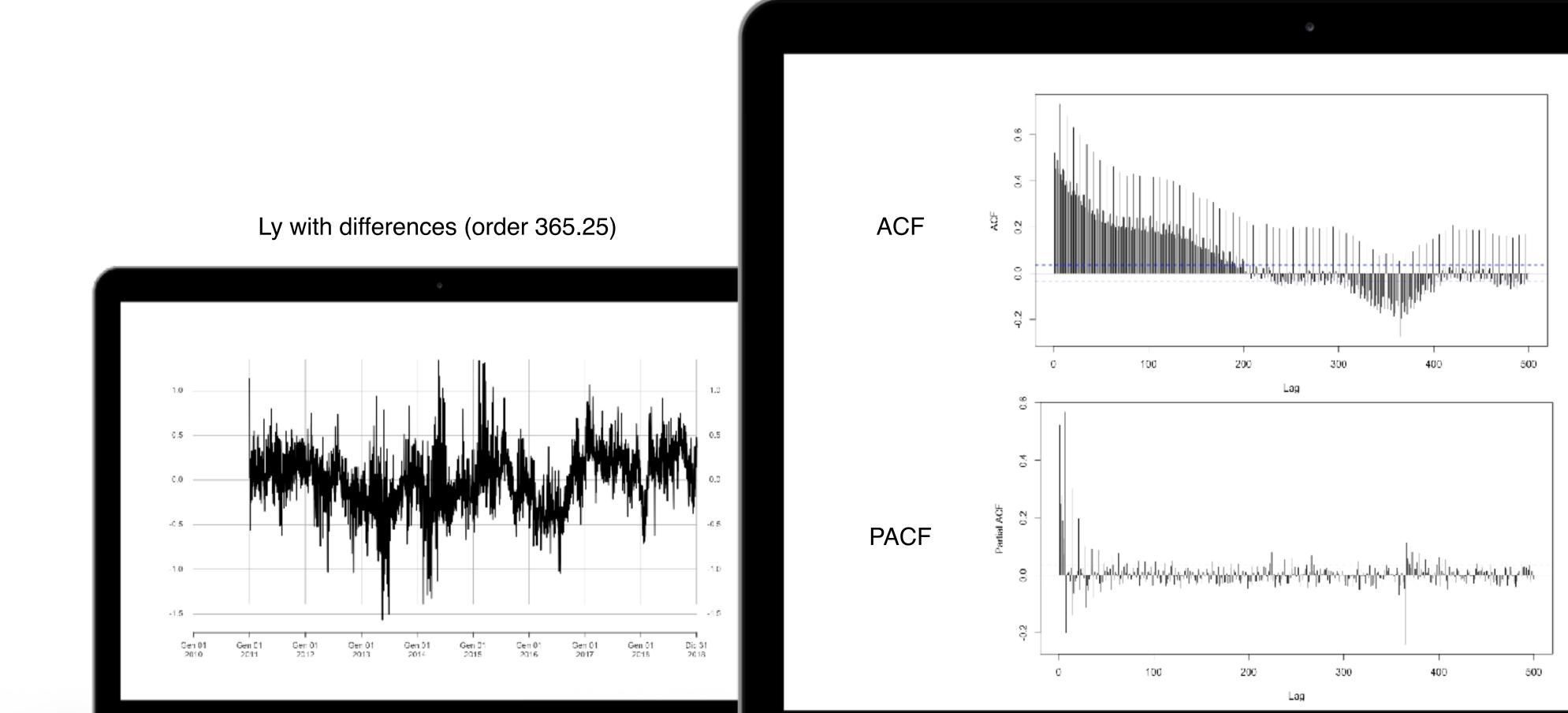
KNN

LSTM RNN

COMPARISON AND CONCLUSIONS

## ARIMA

Identification



**ARIMA** 

UCM

KNN

LSTM RNN

COMPARISON AND CONCLUSIONS

### ARIMA

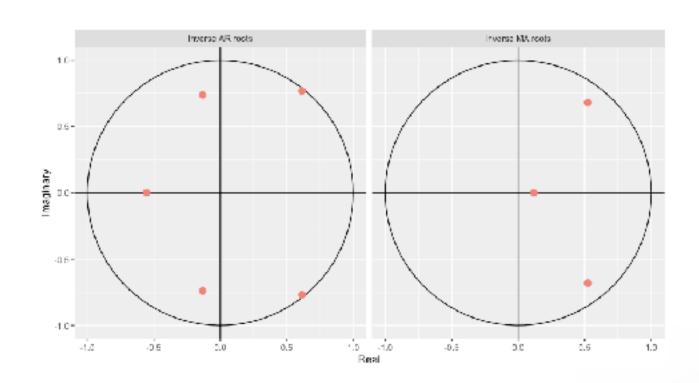
#### Estimation

#### ISSUES

 R can't handle differences of order greater than 350. SARIMA is not applicable for daily data

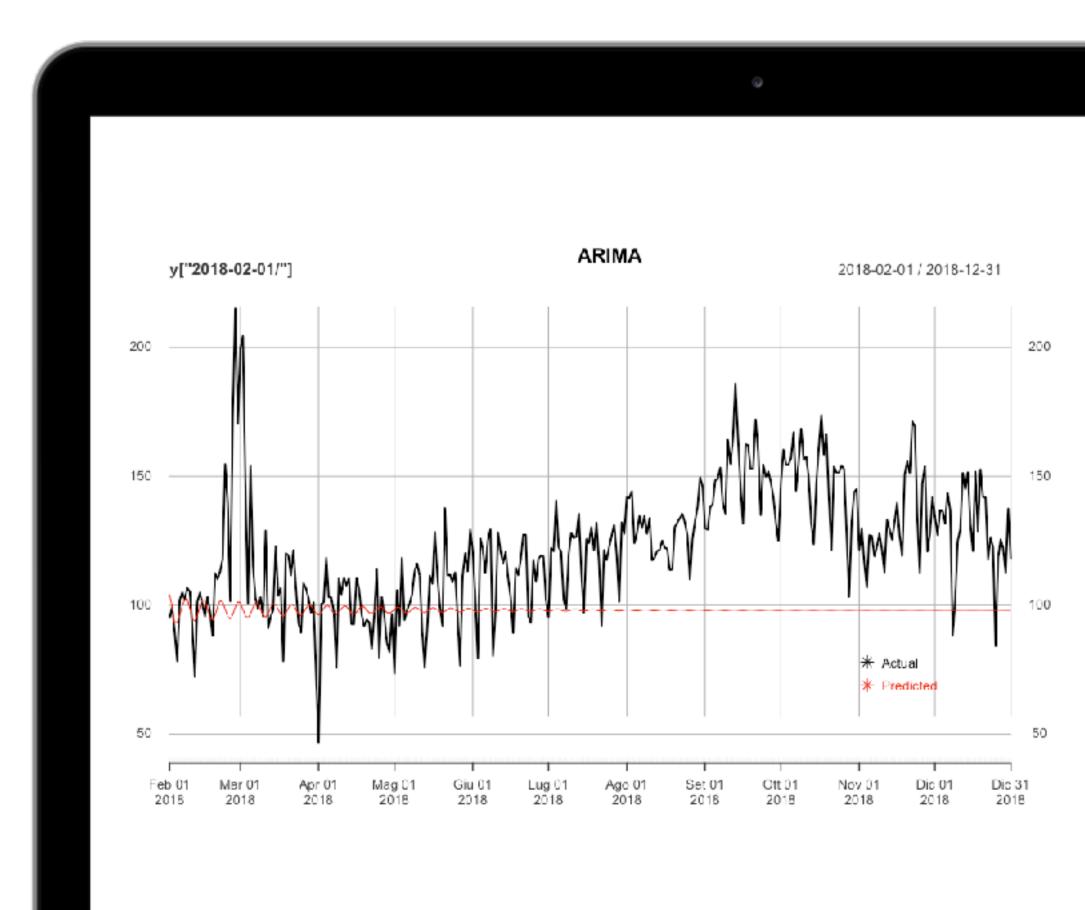
#### MODEL

- AutoARIMA is deployed for the identification
- ARIMA(5,1,3) is used for forecasting



#### EVALUATION

• MAE = 0.236165



Overview

U C M

**ARIMA** 

UCM

KNN

LSTM RNN

COMPARISON AND CONCLUSIONS

| MODEL | COMPONENTS  |
|-------|---|
| 1     | LLT + DUMMY SEASONALITY (7)   |
| 2     | IRW + CYCLE + DUMMY SEASONALITY (7)   |
| 3     | IRW + CYCLE + TRIG DETERMINISTIC SEASONALITY (365)                            |
| 4     | LLT + DUMMY SEASONALITY (7) + TRIG SEASONALITY (365)                          |
| 5     | IRW + DUMMY SEASONALITY (7) + TRIG SEASONALITY (365)                          |
| 6     | IRW + CYCLE + DUMMY SEASONALITY (7) + TRIG DETERMINISTIC<br>SEASONALITY (365) |
| 7     | IRW + CYCLE + DUMMY SEASONALITY (7) + TRIG SEASONALITY (365)                  |
| 8     | LLT + CYCLE + DUMMY SEASONALITY (7) + TRIG SEASONALITY (365)                  |

**ARIMA** 

UCM

KNN

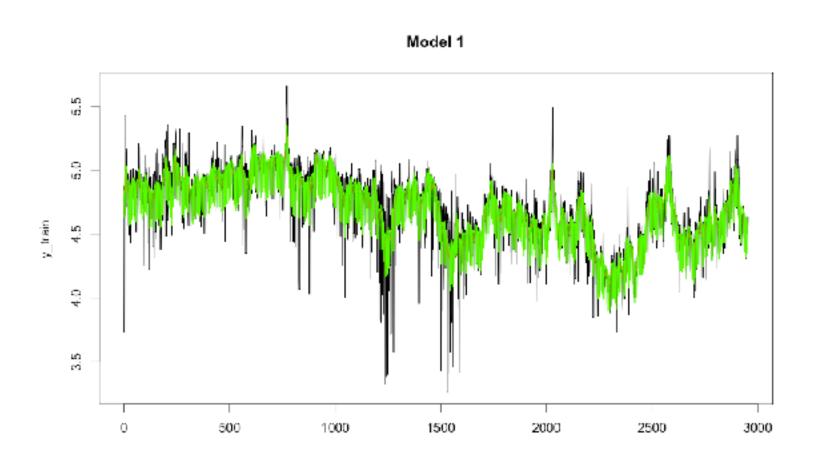
LSTM RNN

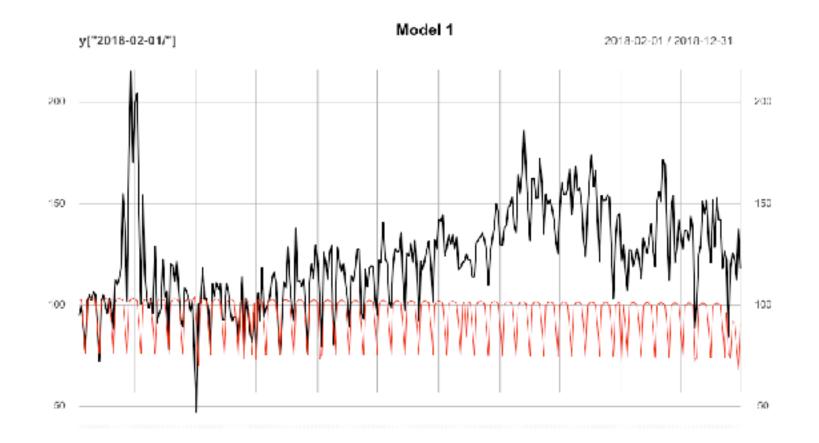
COMPARISON AND CONCLUSIONS

## U C M

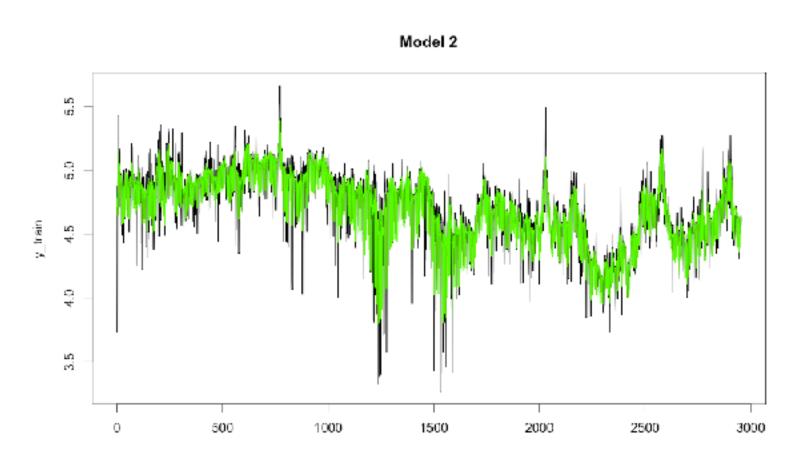
#### MODELS 1-2

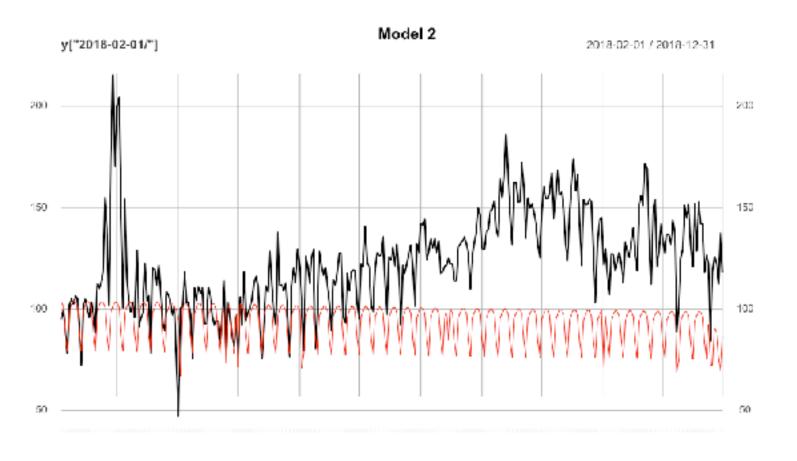
### LLT + DUMMY SEASONALITY (7)





### IRW + CYCLE + DUMMY SEASONALITY (7)





**ARIMA** 

UCM

KNN

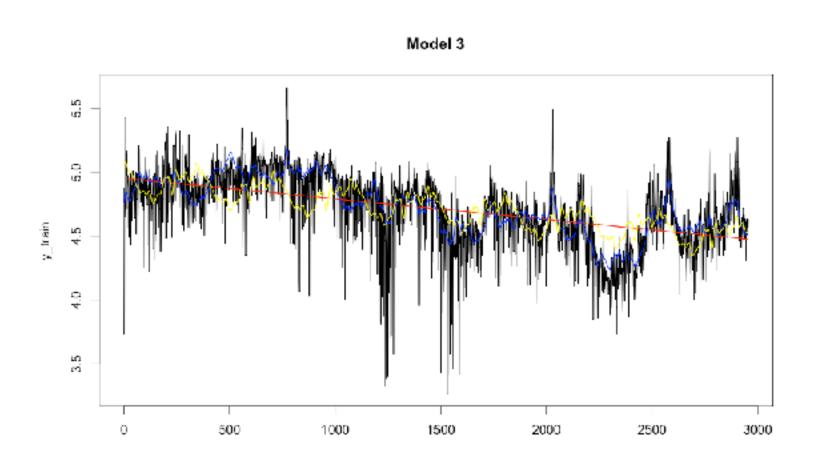
LSTM RNN

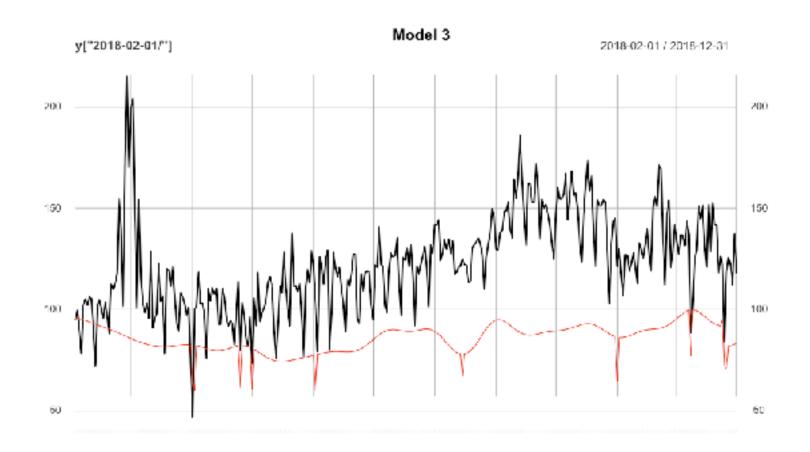
COMPARISON AND CONCLUSIONS

## U C M

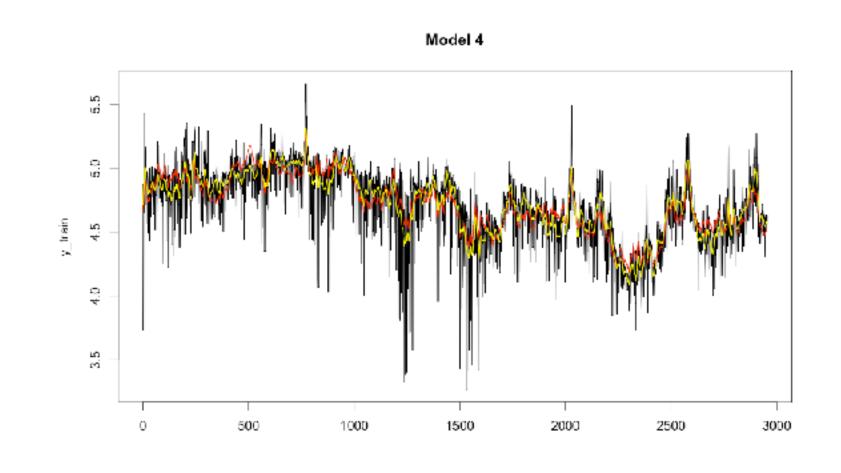
#### MODELS 3-4

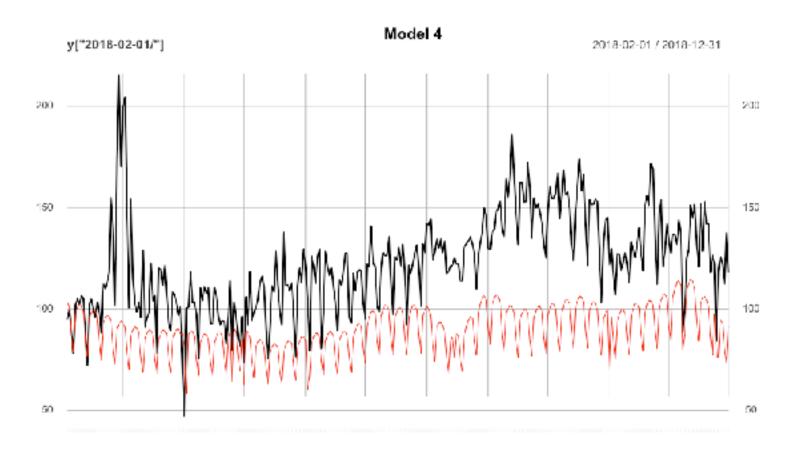
### IRW + CYCLE + TRIG DETERMINISTIC SEASONALITY (365)





### LLT + DUMMY SEASONALITY (7) + TRIG SEASONALITY (365)





**ARIMA** 

UCM

KNN

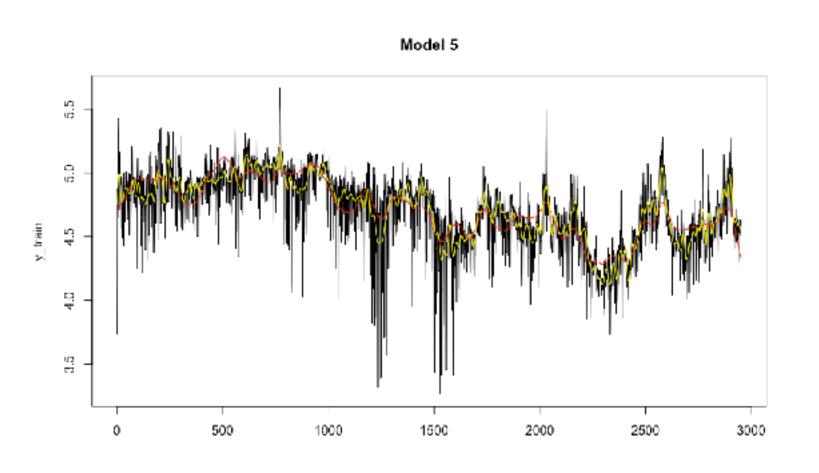
LSTM RNN

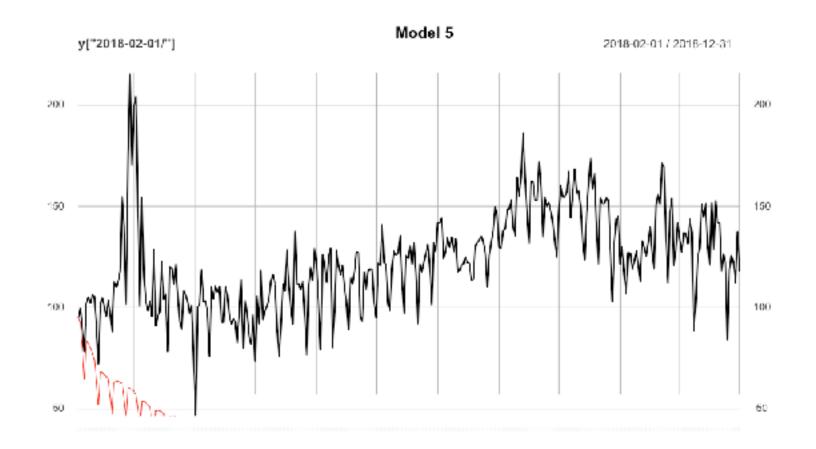
COMPARISON AND CONCLUSIONS

### U C M

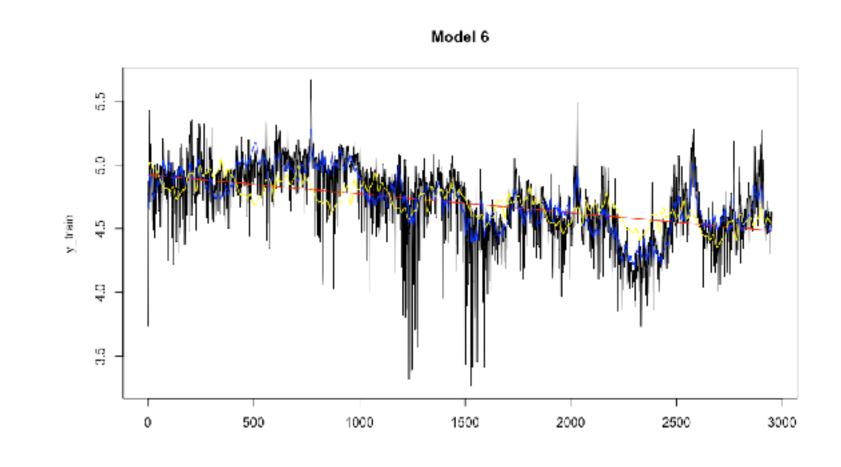
#### MODELS 5-6

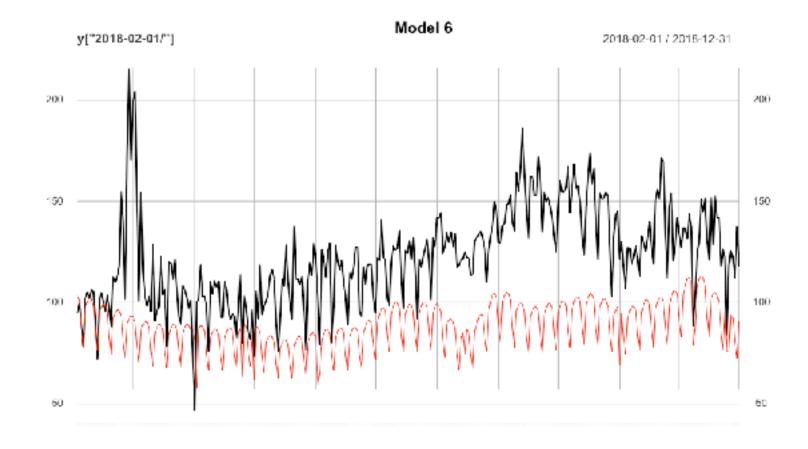
### IRW + DUMMY SEASONALITY (7) + TRIG SEASONALITY (365)





### IRW + CYCLE + DUMMY SEASONALITY (7) + TRIG DETERMINISTIC SEASONALITY (365)





**ARIMA** 

UCM

KNN

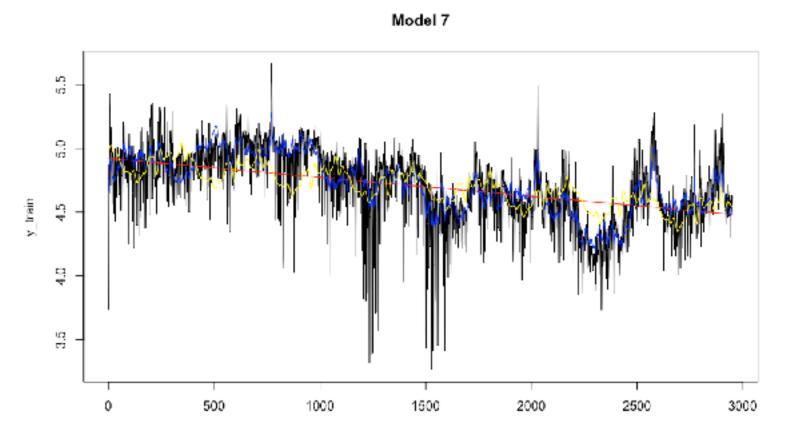
LSTM RNN

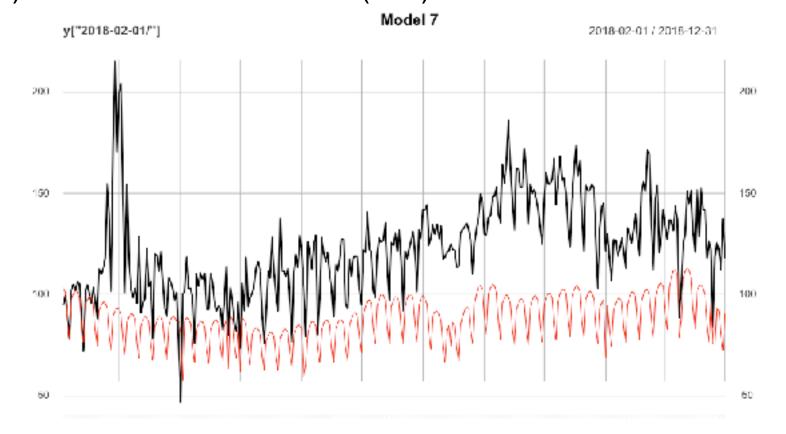
COMPARISON AND CONCLUSIONS

## UCM

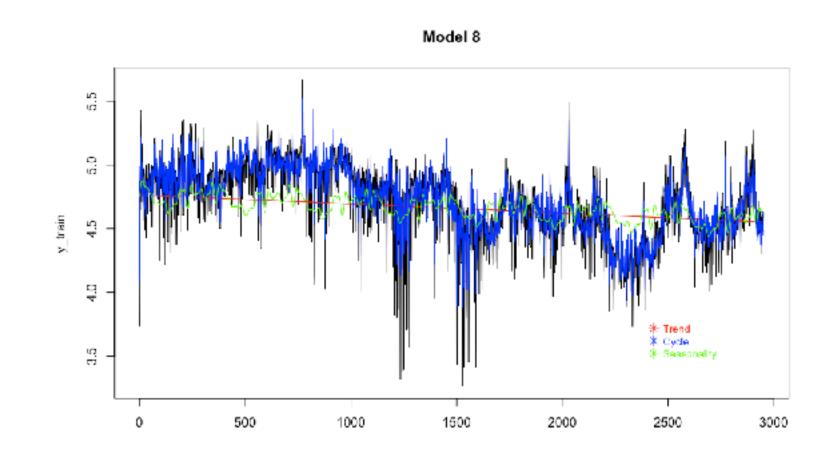
#### MODELS 7-8

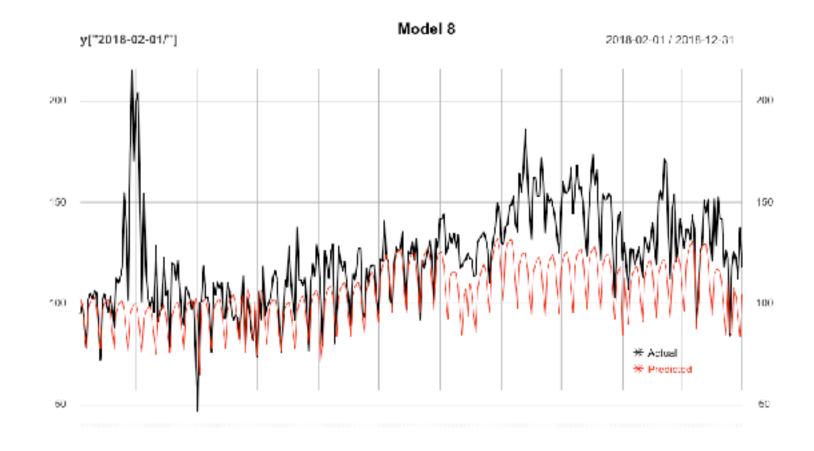
### IRW + CYCLE + DUMMY SEASONALITY (7) + TRIG SEASONALITY (365)





### LLT + CYCLE + DUMMY SEASONALITY (7) + TRIG SEASONALITY (365)





**ARIMA** 

**UCM** 

KNN

UPDATE FUNCTION

MODEL 8

LSTM RNN

COMPARISON AND CONCLUSIONS

### UCM

```
1149 # Update function
1150 v updt8 <- function(pars, model) {
        model $Q[1, 1, 1] <- exp(pars[1])
                                                                    #Level
        model Q[2, 2, 1] \leftarrow exp(pars[2])
                                                                     #slope
       model Q[3, 3, 1] \leftarrow exp(pars[4])
                                                                    #seas dummy
                                                                    #seas trig
        diag(model$Q[4:35, 4:35, 1]) <- exp(pars[5])
        model$Q[36, 36, 1] <- model$Q[37, 37, 1] <- exp(pars[3]) #cycle
        rho <- ext_sigmoid(pars[/]) * 0.99
        per <- ext_sigmoid(pars[8], 1825, 2555)
        lam <- Z*pi/per
        vpsi \leftarrow model (36, 36, 1) / (1 - rho^2)
        rho co <- rho*cos(lam)
        rho_si <- rho*sin(lam)
1161
1162
        s <- 365
1163
        modelT[23:24, 23:24, 1] \leftarrow c(cos((2*pi) / s), -sin((2*pi) / s),
1164
                                       sin((2*pi) / s), cos((2*pi) / s))
        model\T[25:26, 25:26, 1] <- c(cos((2*p1) / s * 2), -sin((2*p1) / s * 2),
1165
1166
                                       sin((2*pi) / s * 2), cos((2*pi) / s * 2))
        model\T[27:28, 27:28, 1] <- c(cos((2*pi) / s * 3), -sin((2*pi) / s * 3),
1167
1168
                                       sin((2*pi) / s * 3), cos((2*pi) / s * 3))
1169
        model\T[29:30, 29:30, 1] <- c(cos((2*pi) / s * 4), -sin((2*pi) / s * 4),
1170
                                       sin((7*pi) / s * 4), cos((7*pi) / s * 4))
        model\T[31:32, 31:32, 1] \leftarrow c(cos((2*pi) / s * 5), -sin((2*pi) / s * 5),
1171
1172
                                       sin((2*pi) / s * 5), cos((2*pi) / s * 5))
1173
        model\T[33:34, 33:34, 1] <- c(cos((2*pi) / s * 6), -sin((2*pi) / s * 6),
1174
                                       sin((2*pi) / s * 6), cos((2*pi) / s * 6))
11/5
        model I[35:36, 35:36, 1] \leftarrow c(cos((2*pi) / s * /), -sin((2*pi) / s * /),
1176
                                       sin((2*pi) / s * 7), cos((2*pi) / s * 7))
1177
        model\T[37:38, 37:38, 1] <- c(cos((2*pi) / s * 8), -sin((2*pi) / s * 8),
1178
                                       sin((2*pi) / s * 8), cos((2*pi) / s * 8))
        modelT[39:40, 39:40, 1] <- c(cos((2*pi) / s * 9), -sin((2*pi) / s * 9),
1179
1180
                                       sin((?*pi) / s * 9), cos((?*pi) / s * 9))
1181
        model\T[41:42, 41:42, 1] <- c(cos((2*pi) / s * 10), -sin((2*pi) / s * 10),
1182
                                       sin((2*pi) / s * 10), cos((2*pi) / s * 10))
        model T[43:44, 43:44, 1] \leftarrow c(cos((2*pi) / s * 11), -sin((2*pi) / s * 11),
1183
1184
                                       sin((2*pi) / s * 11), cos((2*pi) / s * 11))
        model I[45:46, 45:46, 1] <- c(cos((2*pi) / s * 12), -sin((2*pi) / s * 12),
1185
1186
                                       sin((2*pi) / s * 12), cos((2*pi) / s * 12))
1187
        model\T[47:48, 47:48, 1] <- c(cos((2*pi) / s * 13), -sin((2*pi) / s * 13),
                                       sin((2*pi) / s * 13), cos((2*pi) / s * 13))
1188
1189
        model T[49:50, 49:50, 1] <- c(cos((2*pi) / s * 14), -sin((2*pi) / s * 14),
1190
                                       sin((2*pi) / s * 14), cos((2*pi) / s * 14))
1191
        model T[51:52, 51:52, 1] \leftarrow c(cos((2*pi) / s * 15), -sin((2*pi) / s * 15),
                                       sin((2*pi) / s * 15), cos((2*pi) / s * 15))
1193
        model T[53:54, 53:54, 1] < c(cos((2*pi) / s * 16), -sin((2*pi) / s * 16))
                                       sin((2*p1) / s * 15), cos((2*p1) / s * 16))
1194
        model$T[55:56, 55:56, 1] <- c(rho_co, -rho_si,
1196
                                       rho_si, rho_co)
        model$P1inf[55, 55] <- model$P1inf[56, 56] <- 0
1197
        model$P1[55, 55] <- model$P1[56, 56] <- vpsi
        model$H[1, 1, 1] <- exp(pars[6])
1199
1701
```

U C M
COMPARISON

**ARIMA** 

UCM

KNN

LSTM RNN

COMPARISON AND CONCLUSIONS

| MODEL | COMPONENTS  | TRAIN MAE | VAL MAE |
|-------|---|-----------|---------|
| 1     | LLT + DUMMY SEASONALITY (7)   | 0.073     | 0.255   |
| 2     | IRW + CYCLE + DUMMY SEASONALITY (7)   | 0.062     | 0.273   |
| 3     | IRW + CYCLE + TRIG DETERMINISTIC<br>SEASONALITY (365)                         | 0.106     | 0.349   |
| 4     | LLT + DUMMY SEASONALITY (7) + TRIG<br>SEASONALITY (365)                       | 0.064     | 0.309   |
| 5     | IRW + DUMMY SEASONALITY (7) + TRIG<br>SEASONALITY (365)                       | 0.080     | 1.906   |
| 6     | IRW + CYCLE + DUMMY SEASONALITY (7) + TRIG<br>DETERMINISTIC SEASONALITY (365) | 0.063     | 0.322   |
| 7     | IRW + CYCLE + DUMMY SEASONALITY (7) + TRIG<br>SEASONALITY (365)               | 0.063     | 0.323   |
| 8     | LLT + CYCLE + DUMMY SEASONALITY (7) + TRIG<br>SEASONALITY (365)               | 1.9e-15   | 0.158   |

**ARIMA** 

UCM

KNN

LSTM RNN

COMPARISON AND CONCLUSIONS

### KNN

#### MULTIPLE INPUT MULTIPLE OUTPUT

#### HYPERPARAMETERS

- Lags = 1:1500
- K = 2

#### EVALUATION

• MAE = 0.243

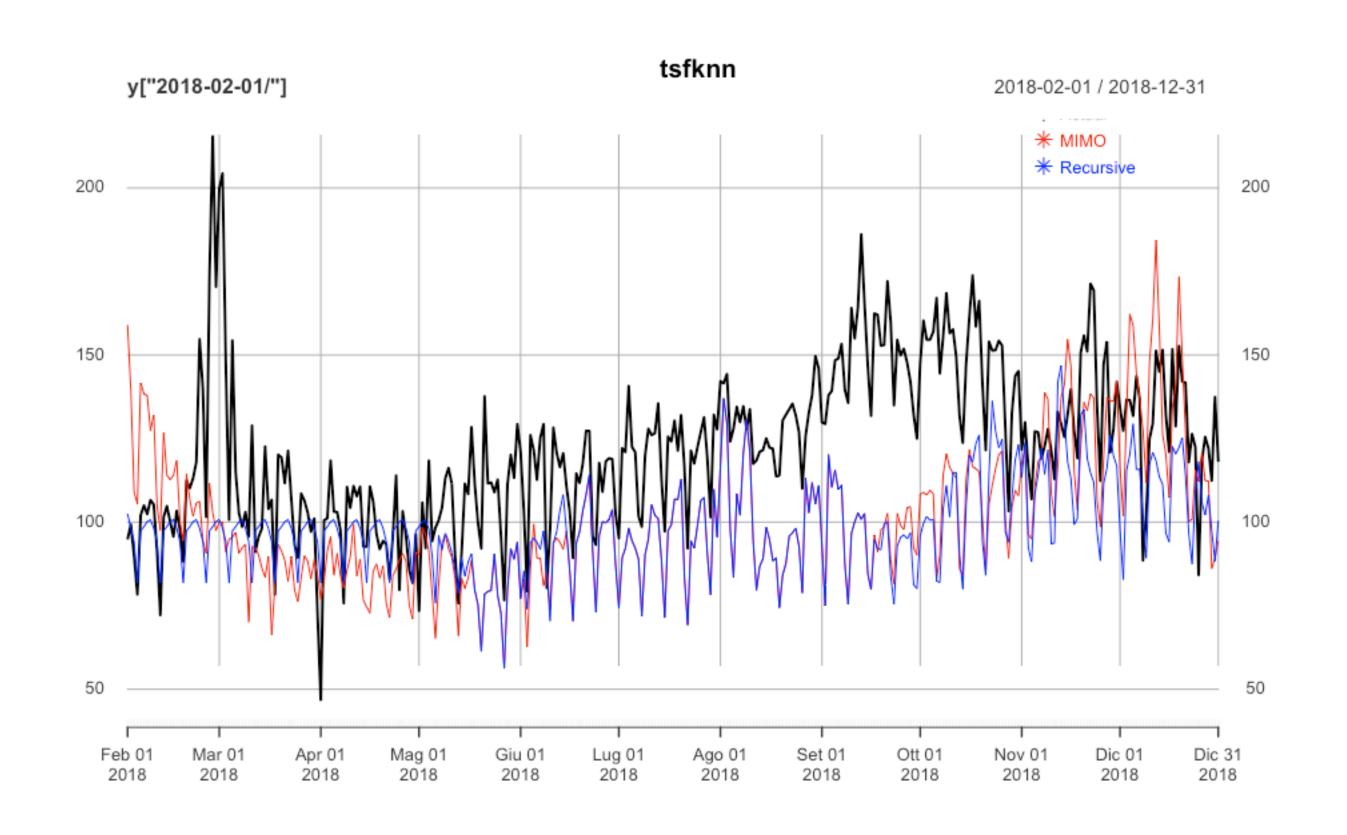
#### RECURSIVE

#### HYPERPARAMETERS

- Lags = 1:1500
- K = 2

#### EVALUATION

• MAE = 0.229



**ARIMA** 

UCM

KNN

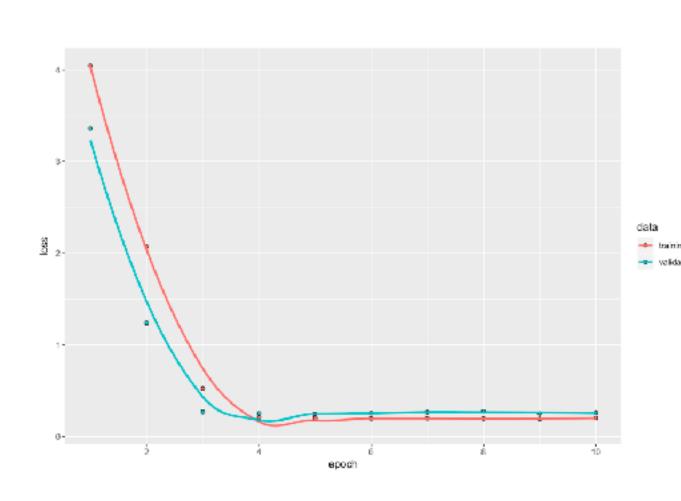
LSTM RNN

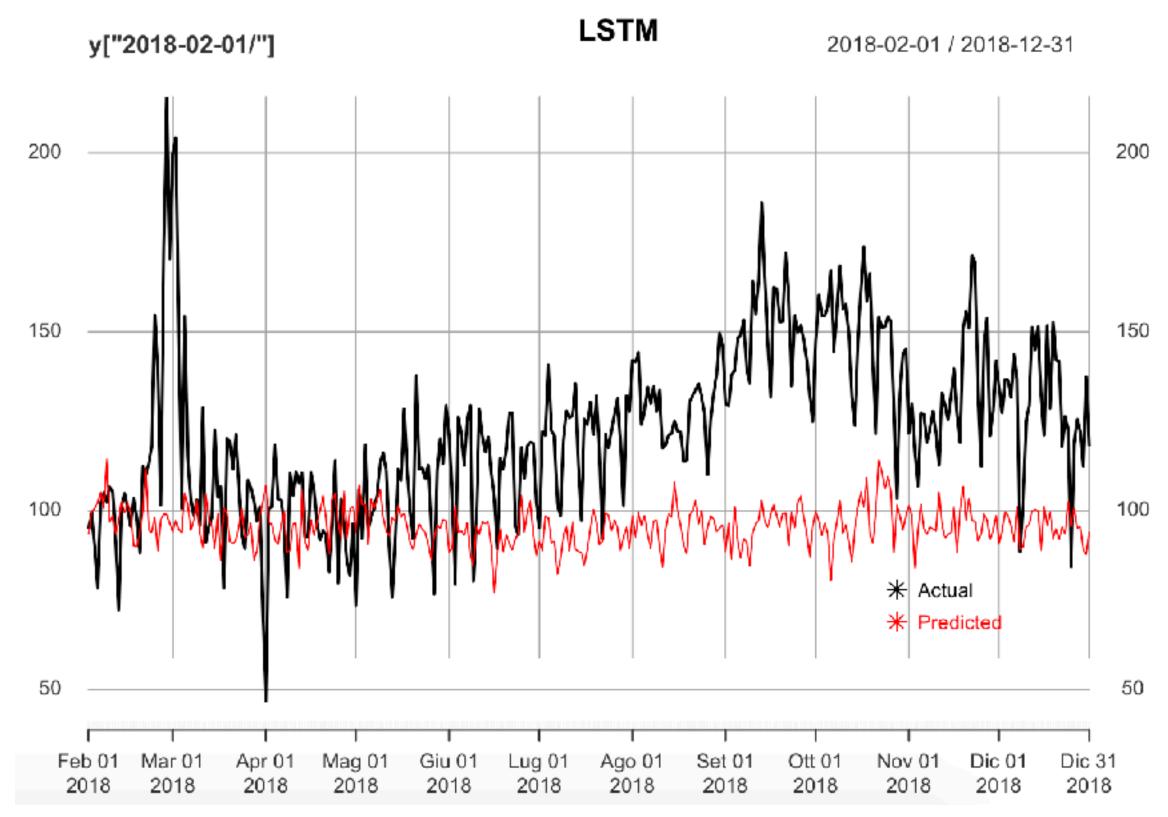
## COMPARISON AND CONCLUSIONS

### LSTM

#### HYPERPARAMETERS

- Lookback = 1500
- Batch size = 128
- LSTM Layer = 1
- LSTM neurons = 32
- Dropout = 0.3
- Recurrent Dropout = 0.3
- Activation function = "tanh"
- Dense Layer = 1 (334 neurons
- Optimizer = "rmsprop£
- Loss = "mae"
- Steps per epoch = 50
- Epochs = 10





#### EVALUATION

• MAE = 0.26

**ARIMA** 

UCM

KNN

LSTM RNN

COMPARISON AND CONCLUSIONS

## COMPARISON

| MODEL    | COMPONENTS  | TRAIN MAE | VAL MAE |
|----------|---|-----------|---------|
| ARIMA    |   | 0.110     | 0.236   |
| UCM 1    | LLT + DUMMY SEASONALITY (7)   | 0.073     | 0.255   |
| UCM 2    | IRW + CYCLE + DUMMY SEASONALITY (7)   | 0.062     | 0.273   |
| UCM 3    | IRW + CYCLE + TRIG DETERMINISTIC<br>SEASONALITY (365)                         | 0.106     | 0.349   |
| UCM 4    | LLT + DUMMY SEASONALITY (7) + TRIG<br>SEASONALITY (365)                       | 0.064     | 0.309   |
| UCM 5    | IRW + DUMMY SEASONALITY (7) + TRIG<br>SEASONALITY (365)                       | 0.080     | 1.906   |
| UCM 6    | IRW + CYCLE + DUMMY SEASONALITY (7) + TRIG<br>DETERMINISTIC SEASONALITY (365) | 0.063     | 0.322   |
| UCM 7    | IRW + CYCLE + DUMMY SEASONALITY (7) + TRIG<br>SEASONALITY (365)               | 0.063     | 0.323   |
| UCM 8    | LLT + CYCLE + DUMMY SEASONALITY (7) + TRIG<br>SEASONALITY (365)               | 1.9e-15   | 0.158   |
| KNN MIMO |   | NA        | 0.243   |
| KNN REC  |   | NA        | 0.229   |
| LSTM     |   | 0.2       | 0.26    |

**ARIMA** 

**UCM** 

KNN

**LSTM RNN** 

COMPARISON AND CONCLUSIONS

#### CONCLUSIONS

#### ADVANTAGES

- ARIMA captures the trend but less oscillations for many steps ahead
- UCM: the freedom of KFAS package allows to design specific models
- KNN: extremely fast to train
- RNN: design of ad-hoc models

#### ISSUES

- ARIMA: can't handle yearly seasonality for daily data
- UCM: identification of the best model
- KNN: distance metric
- RNN: training costs

#### NEXT STEPS

- ARIMA: handle yearly seasonality for daily data
- UCM: use of alternative models
- KNN: distance metric that weights more recent observations
- RNN: deeper network

## THANKS FOR YOUR ATTENTION



Raffaele Anselmo - 846842