## Towards critical and supercritical electromagnetic fields

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S. Bulanov, A. Ilderton, arXiv:2209.11720v1 (2022)

Notebook: Óscar Amaro, January 2023 @ GoLP-EPP

## Introduction

In this notebook we reproduce some results from the paper.

## Figure 2

```
Clear[\chi, a0, f, \lambda, P, \alpha\chi23, \chia03, f\chi3, \gamma0, \varepsilon0]

Clear[A, R, Dnm]

LogLogPlot[\left\{A\left(Abs\left[\frac{r+ct}{R}\right]^{\Lambda}1.5+1\right)^{\Lambda}(-1)\left(Abs\left[\frac{ct}{Dnm}\right]+1\right)^{\Lambda}(-1)\right\}

\left\{A \to 130, R \to 0.2, Dnm \to 0.3, ct \to 0, r \to coor 10^{\Lambda}3\right\},

A\left(Abs\left[\frac{r}{Dnm}\right]+1\right)^{\Lambda}(-1) /. \left\{A \to 130, R \to 0.2, Dnm \to 0.3, r \to coor 10^{\Lambda}3\right\},

\left\{coor, 10^{\Lambda}-5, 10^{\Lambda}1\right\}, PlotRange \to \{10^{\Lambda}-6, 10^{\Lambda}2.1\},

PlotLegends \to \{"t=0", "|x|+ct=0"\}]

0.001

-t=0

|x|+ct=0
```

0.100

0.001

0.010

## Appendix A

```
ln[54] = Clear[\chi, a0, f, \lambda, P, \alpha\chi 23, \chi a03, f\chi 3, \chi 0, \epsilon 0]
      \chi = 3.7 \in 0 P^0.5 / \lambda; (*[]*)
      a0 = 780 P^{0.5};
      f = 3.6 \times 10^{-6} P / \lambda^{2};
      \alpha \chi 23 = 0.017 \in 0^{(2/3)} P^{(1/3)} / \lambda^{(2/3)};
      \chi a03 = 7.8 \times 10^{4} - 9 \in 0 / P / \lambda;
      f\chi 3 = 7 \times 10^{4} - 8 \lambda / \epsilon 0^{4} 3 / P^{0.5};
      \gamma 0 = 2 \times 10^{4};
      \epsilon 0 = \gamma 0.511 \times 10^{-3}; (* [GeV] *)
      imgsz = 250;
      GraphicsRow[{
          LogLogPlot[\{\chi /. \{\lambda \to 0.8\}, \chi /. \{\lambda \to 0.8/3\}, \chi /. \{\lambda \to 0.8/10\}\},
            {P, 0.01, 100}, AspectRatio → 2, ImageSize → imgsz, Frame → True,
           PlotLabel \rightarrow "\chi", FrameLabel \rightarrow {"input power [PW]", ""},
           PlotRange → {2, 9000}, PlotStyle → {Red, Orange, Blue}],
          LogLogPlot[\{a0 /. \{\lambda \to 0.8\}, a0 /. \{\lambda \to 0.8 / 3\}, a0 /. \{\lambda \to 0.8 / 10\}\},
           {P, 0.01, 100}, AspectRatio → 2, ImageSize → imgsz, Frame → True,
           PlotLabel → "a0", FrameLabel → {"input power [PW]", ""},
           PlotRange → {60, 10<sup>4</sup>}, PlotStyle → {Red, Orange, Blue}],
          \label{logLogPlot} \texttt{LogLogPlot[}\{\alpha\chi23 \; /. \; \{\lambda \rightarrow 0.8\} \; , \; \alpha\chi23 \; /. \; \{\lambda \rightarrow 0.8 \; / \; 3\} \; , \; \alpha\chi23 \; /. \; \{\lambda \rightarrow 0.8 \; / \; 10\} \} \; ,
           {P, 0.01, 100}, AspectRatio → 2, ImageSize → imgsz, Frame → True,
           PlotLabel \rightarrow "\alpha \chi^2/3", FrameLabel \rightarrow {"input power [PW]", ""},
           PlotRange → {0.01, 2}, PlotStyle → {Red, Orange, Blue}],
          LogLogPlot[\{\chi = 0.8\}, \chi = 0.8\}, \chi = 0.8/3\}, \chi = 0.8/3\}, \chi = 0.8/10\}},
           {P, 0.01, 100}, AspectRatio → 2, ImageSize → imgsz, Frame → True,
           PlotLabel \rightarrow "\chi/a0^3", FrameLabel \rightarrow \{"input power [PW]", ""\},
           PlotRange \rightarrow {7 × 10 ^ - 8, 2 × 10 ^ - 4}, PlotStyle \rightarrow {Red, Orange, Blue}],
          LogLogPlot[\{f\chi 3 /. \{\lambda \to 0.8\}, f\chi 3 /. \{\lambda \to 0.8 / 3\}, f\chi 3 /. \{\lambda \to 0.8 / 10\}\},
           {P, 0.01, 100}, AspectRatio → 2, ImageSize → imgsz, Frame → True,
           PlotLabel \rightarrow "f/\chi^3", FrameLabel \rightarrow {"input power [PW]", ""},
           PlotRange \rightarrow {8 × 10 ^ -13, 5 × 10 ^ -10}, PlotStyle \rightarrow {Red, Orange, Blue}]
        }, Spacings → 0, ImageSize → 800]
```

