See chapter 3 in Regression and Other Stories.

Widen the notebook

```
html"""

<style>
    main {
        margin: 0 auto;
        max-width: 2000px;
        padding-left: max(160px, 10%);
        padding-right: max(160px, 10%);
}

</style>
"""
```

```
_{\circ} using Pkg \checkmark , DrWatson \checkmark
```

```
begin

# Specific to this notebook

using GLM 

# Graphics related

using GLMakie 

# Specific to ROSStanPluto

using StanSample 

# Common data files and functions

using RegressionAndOtherStories 
end
```

3.1 - Weighted averages

pop =

"United States"	310000000	36.8
"Mexico"	112000000	26.7
"Canada"	34000000	40.7
Canada	D-1000000	70.7
	33.73.33	"Canada" 34000000 httaFrame(stratum=1:3, country=

```
pop = DataFrame(stratum=1:3, country=
["United States", "Mexico", "Canada"],
population=Int[310e6, 112e6, 34e6],
average_age=[36.8, 26.7, 40.7])
```

34.61008771929824

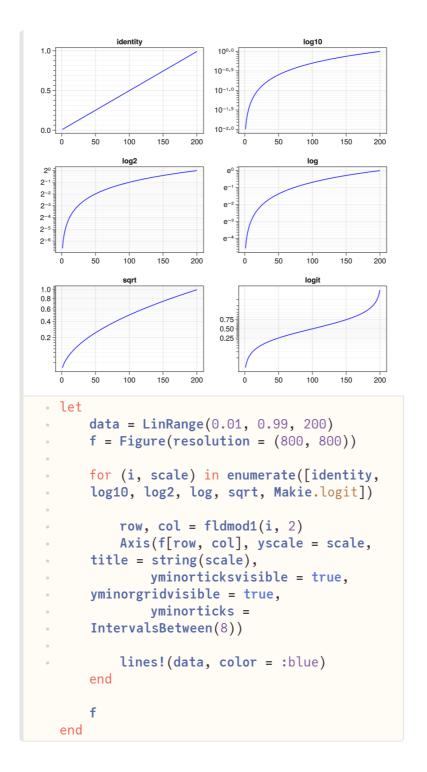
```
mean(pop.average_age,
weights(pop.population))
```

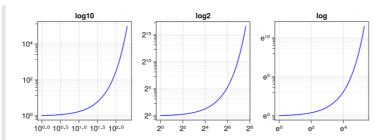
```
▶ [0.679825, 0.245614, 0.0745614]
```

```
weights(pop.population)/sum(pop.population)
```

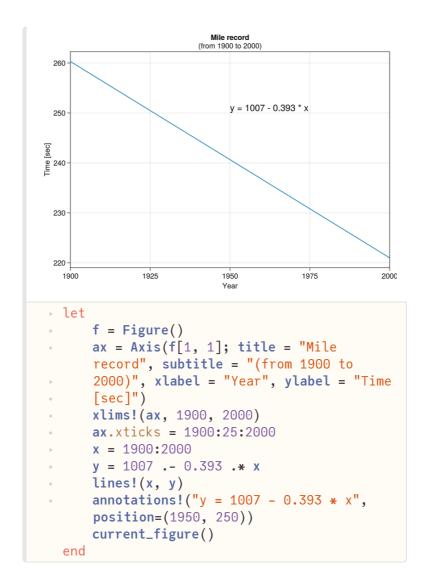
	variable	mean	min	median	
1	:stratum	2.0	1	2.0	- 3
2	:country	nothing	"Canada"	nothing	1
3	:population	1.52e8	34000000	1.12e8	3
4	:average_age	34.7333	26.7	36.8	4

3.3 - Graphing a line





```
• let
      data = 10 .^ LinRange(0.01, 5.0, 200)
      f = Figure(resolution = (800, 300))
      for (i, scale) in enumerate([log10,
      log2, log])
          row, col = fldmod1(i, 2)
          Axis(f[1, i], yscale = scale, xscale
      = scale, title = string(scale),
              yminorticksvisible = true,
      yminorgridvisible = true,
              yminorticks =
      IntervalsBetween(8))
          lines!(data, color = :blue)
     end
      f
  end
```



3.4 - Log and exponential scales

Simulated data for metabolic.

	body_mass	rate
1	3.37299	3.81612
2	4.22996	4.44614
3	4.2483	4.53196
4	5.18917	5.25043
5	5.2266	5.24007
6	5.58684	5.47417
7	5.6116	5.47214
8	5.68689	5.46699
9	5.70901	5.56547
10	5.82045	5.68044
: mc	ore	
200	9.20264	8.27002

```
begin

x = sort(rand(Uniform(0.01, 10000),
200))

y = 4.1 * x.^0.74 .+ [rand.(Normal.(0,
sqrt(x[i])), 1)[1] for i in 1:length(x)]
metabolic = DataFrame(:body_mass => log.
(x), :rate => log.(y))
end
```

```
• stan3_1 = "
data {
      int N;
      vector[N] m;
      vector[N] r;
parameters {
      real a;
      real b;
      real sigma;
• }
- model {
      vector[N] mu;
      a ~ normal(0, 0.3);
      b \sim normal(0, 0.3);
      sigma ~ exponential(1);
      mu = a + b * m;
      r ~ normal(mu, sigma);
· }";
```

```
parameters
                              mcse
                                            std
                  mean
                1.31402
                           0.000626168
                                         0.01915
1
   "b"
                0.750804
                           7.73031e-5
                                         0.00237
2
   "sigma"
                0.0367817
                           4.54935e-5
                                         0.00192
3
```

```
data = (N =
    length(metabolic.body_mass), m =
    metabolic.body_mass, r = metabolic.rate)
global m3_1s = SampleModel("m3.1s",
    stan3_1)
global rc3_1s = stan_sample(m3_1s; data)
success(rc3_1s) && describe(m3_1s)
end
```

	parameters	median	mad_sd	mean	st
1	"a"	1.314	0.019	1.314	0.01
2	"b"	0.751	0.002	0.751	0.00
3	"sigma"	0.037	0.002	0.037	0.00

```
Metabolic rate (linear scale
                                    Metabolic rate (log-log scale)
 4000
                              e2.0
 3000
                            \widehat{\mathbb{Z}}
Metobolic rate [W]
                            log(metobolic rate
 2000
 1000
              5000
                        10000
                                           e1.75
           Body mass [kg]
                                       log(body mass [kg])
• let
       x = LinRange(1, 10000, 1000)
       y = 4.1 * x.^{0.74}
       f = Figure()
       ax = Axis(f[1, 1]; title="Metabolic")
       rate (linear scale)", xlabel="Body mass
        [kg]", ylabel="Metobolic rate [W]")
       scatter!(exp.(metabolic.body_mass), exp.
        (metabolic.rate))
       lines!(x, y; color=:darkred)
       ax = Axis(f[1 , 2]; title="Metabolic")
       rate (log-log scale)", xscale=log,
       yscale=log,
            xlabel="log(body mass [kg])",
            ylabel="log(metobolic rate [W])")
        LinRange(minimum(metabolic.body_mass),
       maximum(metabolic.body_mass), 100)
       scatter!(metabolic.body_mass,
        metabolic.rate)
       lines!(x, ms3_1s[:a, :mean] .+
       ms3_1s[:b, :mean] * x; color=:darkred)
       current_figure()
   end
```

57.69669926958961

```
exp(exp(1.4))
```

3.5 - Probability distributions

```
height
                     sex
                  "female"
         63.5676
  1
         63.0259
                  "female"
  2
         68.9252
                  "female"
  3
         62.6759
                  "female"
                  "female"
         64.4957
  5
                  "female"
  6
         62.8069
         65.2323
                  "female"
  7
  8
         66.0099
                  "female"
  9
         66.5646
                  "female"
                  "female"
         62.3047
  10
: more
         68.4439
                  "male"
200000
```

```
begin

N = 1000000
heights = DataFrame()
height = vcat(rand(Normal(63.7, 2.7),
N),
rand(Normal(69.1, 2.9), N))
sex = repeat(["female", "male"],
inner=N)
heights.height = height
heights.sex = sex
heights
```

```
begin
    menHeights = heights[heights.sex .==
    "male", :height]
    womenHeights = heights[heights.sex .==
    "female", :height]
    (mean=mean(womenHeights),
    var=var(womenHeights),
    std=std(womenHeights),
    median=median(womenHeights),
    mad_sd=mad(womenHeights))
end
```

```
Density heights
0.15
                                              Women
0.05
0.00
   50
                60
 • let
           f = Figure()
           ax = Axis(f[1, 1]; title="Density")
           heights")
           density!(womenHeights; color=color
            = (:lightgreen, 0.4), label="Women")
           density!(menHeights; color=color =
            (:lightblue, 0.4), label="Men")
           axislegend()
       end
```

0.49714220980937984

```
begin
wdf = Normal(63.65, 2.68)
cdf(wdf, 63.65 + 0.67 * 2.68) -
cdf(wdf, 63.65 - 0.67 * 2.68)
end
```

0.6826894921370859

- cdf(wdf, 63.65 + 2.68) - cdf(wdf, 63.65 2.68)

0.9544997361036417

- cdf(wdf, 63.65+2*2.68) - cdf(wdf, 63.65-2*2.68)

```
0.15

0.05

68%

13.5%

13.5%

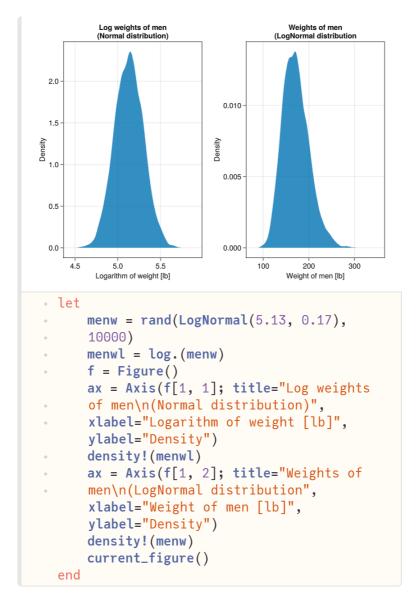
2.5%

55 60 65 70
```

```
let
      wdf = Normal(63.65, 2.68)
      x = range(55.0, 72.5; length=100)
      lines(x, pdf.(wdf, x); color=:darkblue)
      x1 = range(63.65 - 3 * 2.68, 63.65 - 2)
      * 2.68; length=20)
      band!(x1, fill(0, length(x1)), pdf.
      (wdf, x1);
          color = (:blue, 0.25), label =
          "Label")
      x1 = range(63.65 + 2 * 2.68, 63.65 + 3)
      * 2.68; length=20)
      band!(x1, fill(0, length(x1)), pdf.
      (wdf, x1);
          color = (:blue, 0.25), label =
          "Label")
      x1 = range(63.65 - 2 * 2.68, 63.65 - 1)
      * 2.68; length=20)
      band!(x1, fill(0, length(x1)), pdf.
      (wdf, x1);
          color = (:blue, 0.45), label =
          "Label")
      x1 = range(63.65 + 1 * 2.68, 63.65 + 2
      * 2.68; length=20)
      band!(x1, fill(0, length(x1)), pdf.
      (wdf, x1);
          color = (:blue, 0.45), label =
          "Label")
      x1 = range(63.65 - 1 * 2.68, 63.65;
      length=20)
```

```
band!(x1, fill(0, length(x1)), pdf.
    (wdf, x1);
        color = (:blue, 0.55), label =
        "Label")
   x1 = range(63.65, 63.65 + 2.68;
    length=20)
   band!(x1, fill(0, length(x1)), pdf.
    (wdf, x1);
        color = (:blue, 0.55), label =
        "Label")
    text!("68%", position = (63.65, 0.05),
    align = (:center, :center),
        textsize = 30)
    text!("13.5%", position = (67.5, 0.02),
    align = (:center, :center),
        textsize = 20)
    text!("13.5%", position = (59.6, 0.02),
    align = (:center, :center),
        textsize = 20)
   text!("2.5%", position = (69.75,
    0.0045), align = (:center, :center),
        textsize = 15)
    text!("2.5%", position = (57.7,
    0.0045), align = (:center, :center),
        textsize = 15)
   current_figure()
end
```

LogNormal



Binomial

```
median
                        mad sd
   parameters
                                    mean
                                               st
   "bv"
                6.0
                         1.483
                                   5.971
                                            2.11
1
• let
      df = DataFrame(bv = rand(Binomial(20,
      0.3), 1000))
      model_summary(df, [:bv])
  end
```

Poisson

```
▶[6, 4, 3, 3, 1, 4, 9, 7, 9, 5]

• rand(Poisson(4.52), 10)
```

3.6 - Probability modeling

```
20689.577579211084
- 1 / (pdf(Normal(0.49, 0.04), 0.5) / 200000)
```

```
20.689577579211083

- 1 / (1000pdf(Normal(0.49, 0.04), 0.5) /
200000)
```