Exam for the lecture

## "Econometrics II"

for students in the M.Sc. programmes summer term 2018

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#### **Seat location:**

Name: Surname	Vorname: Name
Studiengang Course of study:	Geburtsort: Place of birth
Matrikelnummer: Student ID	Bachelor University:

#### **Declaration:**

	PLEASE SIGN!!!	
I hereby declare that I am able to be examined.		
	Signature:	-

#### **Preliminary remarks:**

- Write down your name and enrolment/matriculation number on all paper sheets provided for answers by the examiner.
- To write down your answers, use only the paper provided by the examiner.

#### **Result:** (TO BE FILLED IN ONLY BY THE EXAMINER!)

Problem	1	2	3	4	5	Home Assignment	Σ
Points earned							
Grade							

Kiel,	
	Professor Dr. Jens Boysen-Hogrefe

# Examination in Econometrics II (Summer Term 2018)

October 8, 2018, 8.30 - 9.30

### Preliminary remarks:

- 1. Please read these instructions carefully!
- 2. At the beginning of the exam, fill in the cover sheet and hand in after the exam is finished!
- 3. You are permitted to use the following auxiliary tools:
  - (a) a non-programable pocket calculator,
  - (b) the formulary for Econometrics II without notes!
- 4. Conduct each test at the 5% level.
- 5. Write your name and enrolment (matriculation) number on every sheet of paper!
- 6. Don't use a pencil!
- 7. The exam problems are printed on 2 pages plus 2 double sheets for answers. Check your exam for completeness!
- 8. Round your solutions to 4 decimal places.
- 9. You have 60 minutes in total to answer the exam questions.

Good luck!

## Part 1 - Cross Section (21 credits)

1. Consider the exponential regression model where  $E(y_i|\mathbf{x}_i) = \mu(\mathbf{x}_i) = e^{\mathbf{x}_i\beta}$  and the distribution of  $y_i$  conditional on  $\mathbf{x}_i$  is the exponential distribution,

$$f(y_i|\mathbf{x}_i,\boldsymbol{\beta}) = \frac{1}{\mu(\mathbf{x}_i)} \exp\left(\frac{-y_i}{\mu(\mathbf{x}_i)}\right).$$
 (1)

Remember that this distribution has the property that  $Var(y_i|\mathbf{x}_i) = [E(y_i|\mathbf{x}_i)]^2$ .

- (a) (2P) Write down the conditional log likelihood function for observation i.
- (b) (4P) Derive the score with respect to  $\beta$  for observation i. Show directly that the score has conditional mean zero.
- (c) (2P) Derive the Hessian with respect to  $\beta$  for observation i.
- (d) (5P) Show that the conditional information matrix equality holds.
- 2. Consider the following model:

$$y_i = \beta_0 + (\beta_1 x_{1i}^{1/\beta_3} + \beta_2 x_{2i}^{1/\beta_3})^{\beta_3} + u_i, \tag{2}$$

where  $x_{1i}$ ,  $x_{2i}$  are input factors (in logs),  $y_i$  is output (in log) and  $u_i$  is white noise with mean zero and variance  $\sigma^2$ . Using a sample of size N you want to test the null hypothesis  $H_0$ :  $\beta_3 = 1$ .

- (a) (3P) Which test is the easiest to use in this particular situation? Why?
- (b) (3P) Explain the testing principle chosen in (a) graphically.
- (c) (2P) Suppose that the null hypothesis above is not rejected and  $\hat{\beta}_1 = 0.11$ . Interpret  $\hat{\beta}_1$ !

## Part 2 - Time Series (39 credits)

- 3. (13P) Consider the regression model  $y_t = \beta x_t + u_t$ , where  $u_t = \rho u_{t-1} + \varepsilon_t$  and  $\varepsilon_t$  is white noise with mean zero and variance  $\sigma_{\varepsilon}^2$ . The regressor  $x_t$  is generated by  $x_t = \alpha x_{t-1} + \gamma y_{t-1} + w_t$ , where  $w_t$  is white noise with mean zero and variance  $\sigma_w^2$ . The covariance between  $\varepsilon_t$  and  $w_t$  is denoted by  $E(w_t \varepsilon_t) = \sigma_{w\varepsilon}$ . Assume the parameter values are such that  $x_t$ ,  $y_t$ , and  $u_t$  are stationary. Additionally, you know that  $E(x_t u_t) = \frac{(1-\rho^2)\sigma_{w\varepsilon} + \gamma \rho \sigma_{\varepsilon}^2}{(1-\rho^2)[1-(\alpha+\gamma\beta)\rho]}$ .
  - (a) (5P) Show the convergence of the OLS estimate  $\hat{\beta}$  step by step!
  - (b) (8P) Under which conditions is the OLS estimator of  $\beta$  applied to  $y_t = \beta x_t + u_t$  consistent? Derive and shortly explain them!

4. You are given the following regression results (T=250):

$$\hat{y}_t = \underset{(0.0529)}{0.536} + \underset{(0.0145)}{0.245} t + \underset{(0.013)}{0.932} y_{t-1} + \underset{(0.134)}{0.9033} \Delta y_{t-1} + \underset{(0.102)}{0.361} \Delta y_{t-2} - \underset{(0.001)}{0.043} \Delta y_{t-3}.$$

- (a) (9P) Perform an ADF-test at the 5% level. Carefully state null and alternative hypotheses, characterize  $y_t$  under each hypothesis and derive a test decision.
- (b) (4P) For which shortcoming of the DF test does the ADF test correct? How does this work intuitively? Answer briefly!
- 5. Suppose that short term and long term interest rates are I(1). A graphical inspection suggests that they seem to be tied together in the long run even though there are large temporary deviations. A regression of the long term interest rate (LT) on the short term interest rate (ST) (both are given in percent),  $LT_t = \beta_0 + \beta_1 ST_t + \varepsilon_t$ , delivers the following results:

Model 1: OLS, using observations 1978:1–2004:4 ( $T=108$ ) Dependent variable: LT							
	Coefficient	Std. Erro	r <i>t</i> -ratio	p-value	2		
const ST	1.97181 0.863890	0.146506 0.0179190	13.4589 48.2109	0.0000 $0.0000$			
Mean depender	nt var 8.3	395402 S.	D. depende	nt var	3.017254		
Sum squared re	esid 42	.48695 S.	E. of regress	sion	0.633104		
$R^2$	0.0	956384 A	djusted $R^2$		0.955972		
F(1, 106)	23	24.288 P-	value(F)		6.30e-74		
Log-likelihood	-10	2.8669 Al	kaike criteri	on	209.7338		
Schwarz criteri	on 21	5.0981 Ha	nnan–Quin	in	211.9088		
$\hat{ ho}$	3.0	877578 D	ırbin–Watse	on	0.244529		

- (a) (5P) Explain in a few sentences the concept of cointegration between two I(1) processes.
- (b) (4P) Based on the regression output, what can be said about cointegration between ST and LT? Shortly explain your answer.
- (c) (4P) Suppose ST and LT are cointegrated. Interpret the estimated slope parameter. Are you able to check for statistical significance of this parameter in your regression output? Why or why not?