

EXTENDS *Integers*, *GCD*

CONSTANTS *M*, *N*

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```
--fair algorithm Euclid{
  variables  $x \in 1 \dots N, y \in 1 \dots N, x0 = x, y0 = y$ ;
  variables  $x = M, y = N$ ;
  { judge: while (  $x \neq y$  ) { do : if (  $x < y$  ) {  $y := y - x$  }
                                else {  $x := x - y$  }
                                } ;

  print  $\langle x, y \rangle$ ;
  assert (  $x = y$  )  $\wedge$  (  $x = GCD(x0, y0)$  );
}
```

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BEGIN TRANSLATION ( $chksum(pcal) = \text{"65d8d3f8"} \wedge chksum(tla) = \text{"9d2756b"}$ )

VARIABLES  $x, y, pc$

$vars \triangleq \langle x, y, pc \rangle$

$Init \triangleq$  Global variables

$\wedge x = M$

$\wedge y = N$

$\wedge pc = \text{"judge"}$

$judge \triangleq \wedge pc = \text{"judge"}$   
 $\wedge \text{IF } x \neq y$   
     THEN  $\wedge pc' = \text{"do"}$   
     ELSE  $\wedge pc' = \text{"Done"}$   
 $\wedge \text{UNCHANGED } \langle x, y \rangle$

$do \triangleq \wedge pc = \text{"do"}$   
 $\wedge \text{IF } x < y$   
     THEN  $\wedge y' = y - x$   
          $\wedge x' = x$   
     ELSE  $\wedge x' = x - y$   
          $\wedge y' = y$   
 $\wedge pc' = \text{"judge"}$

Allow infinite stuttering to prevent deadlock on termination.

$Terminating \triangleq pc = \text{"Done"} \wedge \text{UNCHANGED } vars$

$Next \triangleq judge \vee do$   
 $\vee Terminating$

$Spec \triangleq \wedge Init \wedge \square [Next]_{vars}$   
 $\wedge \text{WF}_{vars}(Next)$

$Termination \triangleq \Diamond(pc = \text{"Done"})$

END TRANSLATION

$Safety \triangleq (pc = \text{"Done"}) \Rightarrow (x = y) \wedge (x = GCD(M, N))$

Safety and Liveness (Termination in this part) means Correctness

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\ \* Modification History  
\ \* Last modified Sun Sep 26 09:36:52 CST 2021 by wrz  
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