Calibrating gyrochronology using Galactic kinematics

Ruth Angus,^{1,2,3} Yuxi (Lucy) Lu,^{3,1} Dan Foreman-Mackey,² Adrian M. Price-Whelan,² Jason Curtis,¹ and Emily Cunningham²

Department of Astrophysics, American Museum of Natural History, 200 Central Park West, Manhattan, NY, USA
 Center for Computational Astrophysics, Flatiron Institute, 162 5th Avenue, Manhattan, NY, USA
 Department of Astronomy, Columbia University, Manhattan, NY, USA

ABSTRACT

Gyrochronology, the method of inferring the age of a star from its rotation period, could provide ages for billions of stars over the coming decade of time-domain astronomy. However, the gyrochronology relations remain poorly calibrated due to a lack of precise ages for old, cool main-sequence stars. Now however, with proper motion measurements from Gaia, Galactic kinematics can be used as an age proxy, and the magnetic and rotational evolution of stars can be examined in detail. We demonstrate that kinematic ages, inferred from the velocity dispersions of groups of stars, beautifully illustrate the time and mass-dependence of the gyrochronology relations. We use the kinematic ages of field stars, plus benchmark clusters and asteroseismic stars, to calibrate a new empirical Gaussian process gyrochronology relation, that fully captures the complex rotational evolution of cool dwarfs over a range of masses and ages. We use cross validation to demonstrate that this relation accurately predicts ages for GKM dwarfs.

Keywords: Stellar Rotation — Stellar Evolution — Stellar Activity — Stellar Magnetic Fields — Low Mass Stars — Solar Analogs — Milky Way Dynamics

1. INTRODUCTION

Low mass dwarfs are the most common stars in the Milky Way, and their ages could reveal the evolution of Galactic stellar populations and planetary systems. However, the ages of GKM stars are difficult to measure because their luminosities and temperatures evolve slowly on the main sequence. Fortunately, rotation-dating, or 'gyrochronology' provides a promising means to measure precise ages for these cool dwarfs. (e.g. Schatzman 1962; Weber & Davis 1967; Kraft 1967; Skumanich 1972; Kawaler 1988; Pinsonneault et al. 1989; Barnes 2003, 2007; Mamajek & Hillenbrand 2008; Barnes 2010; Meibom et al. 2011, 2015; van Saders et al. 2016). The rotation periods of GKM stars evolve relatively rapidly, and a fully calibrated gyrochronology model that captures the time and mass-dependence of stellar spin down could provide ages that are precise to within 20% for millions of Milky Way stars in the time-domain era (Epstein & Pinsonneault 2014; Najita et al. 2016; Angus et al. 2019). However, gyrochronology models are not yet reliably calibrated, especially for low-mass and old stars.

A lack of low-mass and old calibration stars has previously limited the mass and age coverage of gyrochronology relations, which require precise age and rotation period measurements. Historically the calibration sample has been limited to open clusters and asteroseismic stars, which can be precisely dated with isochrone fitting and main sequence turn off, or precise oscillation frequency analysis. The rotation periods of both cluster and asteroseismic stars can be measured with precise time-series photometry. Magnetically active regions create inhomogeneous surface features and produce periodic variability in their integrated, broad-band emission. The photometric rotation periods of thousands of stars have been measured with the Kepler/K2 and TESS space missions (Borucki et al. 2010; Howell et al. 2014; Ricker et al. 2015).

For the purposes of calibrating gyrochronology, open clusters provide good mass coverage for young stars: rotation periods have been measured for F to mid M dwarfs up to ages of around 700 Myr. In contrast, asteroseismic stars provide reasonable age coverage for hot stars: ages and photometric surface rotation periods have been measured for F, G and early K dwarfs up to ages of 10 Gyr. However, neither asteroseismology nor cluster analysis can provide rotation periods and ages for old, late K and M dwarfs. In addition, cluster and asteroseismic stars generally provide sparse coverage of the rotation period-effective temperature plane, and cannot reveal the detailed evolution of stellar

rotation rates. As a result, most empirical gyrochronology relations are only reliable for G dwarfs up to Solar age, K dwarfs up to 2-3 Gyr, and early M dwarfs up to < 1 Gyr.

The rotational evolution of cool dwarfs is not well understood because few old M dwarfs with rotation periods have age measurements. However, as we showed in Angus et~al.~(2020), the kinematic ages of field stars observed by Kepler, can provide a calibration sample with broad mass and age coverage. Although the Kepler sample does not include late M dwarfs, it can still be used to extend gyrochronology relations to much older ages for late K and early M dwarfs. By adding the ages and rotation periods of thousands of field stars to the open cluster and asteroseismic calibration sample, we can calibrate a gyrochronology relation that is applicable to FGK and early M dwarfs between the ages of $\sim 500~\rm Myr$ and 8 Gyr.

1.1. Core-envelope decoupling

In Angus et al. (2020) we demonstrated that Galactic kinematics can be used to explore the evolution of stellar rotation. We showed that velocity dispersion, an established age proxy in the Galactic thin disk, increases smoothly as a function of rotation period, indicating that rotation period increases with age as expected. Using velocity dispersion as an age proxy, we also showed that old K dwarfs spin down more slowly than G dwarfs: their rotational evolution appears to 'stall' after around 1 Gyr, in a manner that reflects the behavior of K dwarfs observed in open clusters (Curtis et al. 2019). At young ages ($\sim 0.5 - 1$ Gyr), K dwarfs spin more slowly than G dwarfs of the same age, because their deeper convection zones generate stronger magnetic fields, which leads to more efficient magnetic braking. However, at old ages ($\gtrsim 1$ Gyr) K dwarfs rotate at the same rate or more rapidly than contemporary G dwarfs. The leading explanation for this phenomenon is that angular momentum is transferred from the core to the surface over longer timescales for lower-mass stars (Spada & Lanzafame 2019), i.e. they experience a more extended phase of 'core-envelope decoupling'.

A period of core-envelope decoupling is necessary to explain the observed rotation periods of stars in extremely young open clusters (1-10 Gyr) (e.g. Irwin et al. 2007; Bouvier 2008; Denissenkov et al. 2010; Spada et al. 2011; Reiners & Mohanty 2012; Gallet & Bouvier 2013). During this phase there is little transfer of angular momentum between radiative core and convective envelope and, as wind-braking removes angular momentum from the envelope, it decelerates while the core continues to spin rapidly. Over time however, angular momentum is transported across the interface between the two zones, and momentum from the rapidly spinning interior surfaces, inhibiting the deceleration of the outer envelope. Currently, the rotation periods of field and cluster stars can only be reproduced by semi-empirical models with a mass-dependent timescale for core-envelope coupling (Spada & Lanzafame 2019; Curtis et al. 2019, Angus et al., 2020).

1.2. Using kinematics as an age proxy

The star forming molecular gas clouds observed in the Milky Way have a low out-of-plane, or vertical, velocity (e.g. Stark & Brand 1989; Stark & Lee 2005; Aumer & Binney 2009; Martig et al. 2014; Aumer et al. 2016). In contrast, the vertical velocities of older stars are observed to be larger in magnitude on average (Strömberg 1946; Wielen 1977; Nordström et al. 2004; Holmberg et al. 2007, 2009; Aumer & Binney 2009; Casagrande et al. 2011; Ting & Rix 2019; Yu & Liu 2018). There are two possible explanations for this observed increase in velocity dispersion with age: either stars are born kinematically 'cool' and their orbits are heated over time via interactions with giant molecular clouds (see Sellwood 2014, for a review of secular evolution in the MW), or stars formed kinematically 'hotter' in the past (e.g. Bird et al. 2013). Either way, the vertical velocity dispersions of thin disk stars are observed to increase with stellar age. This behavior is codified by Age-Velocity dispersion Relations (AVRs), which typically express the relationship between age and velocity dispersion as a power law: $\sigma_v \propto t^{\beta}$, with free parameter, β (e.g. Holmberg et al. 2009; Yu & Liu 2018). These expressions can be used to infer the ages of groups of stars from their velocity dispersions, as we do in this paper (see section ??).

Kinematic ages have been used to explore the evolution of cool dwarfs for over a decade. West et al. (2004, 2006) found that the fraction of magnetically active M dwarfs decreases over time, by using the vertical distances of stars from the Galactic mid-plane as an age proxy, and West et al. (2008) used kinematic ages to calculate the expected activity lifetime for M dwarfs of different spectral types. Faherty et al. (2009) used tangential velocities to infer the ages of M, L and T dwarfs, and showed that dwarfs with lower surface gravities tended to be kinematically younger, and Kiman et al. (2019) used velocity dispersion as an age proxy to explore the evolution of $H\alpha$ equivalent width (a magnetic activity indicator), in M dwarfs.

AVRs are usually calibrated in Galactocentric velocity coordinates $(v_{\mathbf{x}}, v_{\mathbf{y}}, v_{\mathbf{z}} \text{ or } UVW)$, and these velocities can only be calculated with full 6D positional and velocity information, however most Kepler rotators do not have RV measurements¹. In Angus et~al.~(2020) we used velocity in the direction of Galactic latitude $(v_{\mathbf{b}})$ as a stand-in for $v_{\mathbf{z}}$ because, in the Galactic coordinate system, velocities can be calculated from 3D positions and 2D proper motions. The Kepler field lies at low Galactic latitude, so $v_{\mathbf{b}}$ is a close approximation to $v_{\mathbf{z}}$. Though $v_{\mathbf{b}}$ velocity dispersion does not equal $v_{\mathbf{z}}$ velocity dispersion, it still increases monotonically over time and provides accurate age rankings for Kepler stars. Unfortunately however, given that AVRs are calibrated in Galactocentric coordinates $(v_{\mathbf{x}}, v_{\mathbf{y}}, v_{\mathbf{z}})$, we could not directly translate $v_{\mathbf{b}}$ velocity dispersions to ages.

In this paper, our aim was to use kinematic ages to calibrate a new gyrochronology relation, for which four main steps were required. Firstly, we inferred vertical velocity, v_z , for each star without an RV measurement by marginalizing over missing RVs using a hierarchical Bayesian model (see section ??). Secondly, we calculated velocity dispersion for every star using a moving, or rolling dispersion method (see section ??). Thirdly, these velocity dispersions were converted into ages using an AVR (Yu & Liu 2018, section ??). Finally, we used a Gaussian process model to capture the complexities of stellar rotational evolution and calibrated a new gyrochronology relation using our kinematic ages, plus benchmark cluster and asteroseismic stars in section ??.

¹ Although RVs for most will be released in Gaia DR3

2. THE DATA

This study focuses on stellar rotation in the original Kepler field, partly because Kepler provides the largest samples of homogeneously measured rotation periods, and partly because its low Galactic latitude allows us to marginalize over missing RV measurements and precisely infer vertical velocity, v_z . We combined two large rotation period catalogs constructed from original Kepler data: McQuillan et al. (2014) and Santos et al. (2019). These two studies used different techniques to measure rotation periods from Kepler light curves: autocorrelation functions and wavelets respectively. The Santos et al. (2019) study was specifically focused on cooler stars: K and M dwarfs, and includes a larger number of rotation periods for these stars. The combined catalogs provide a total of over 38,000 rotation periods.

We used the publicly available Kepler-Gaia DR2 crossmatched catalog² to combine the McQuillan et al. (2014) and Santos et al. (2019) rotation catalogs with the Gaia DR2 catalog of parallaxes, proper motions and apparent magnitudes. Reddening and extinction from dust was calculated for each star using the Bayestar dust map implemented in the dustmaps Python package (M. Green 2018), and astropy (Astropy Collaboration et al. 2013; Price-Whelan et al. 2018). We used Gaia DR2 photometric color, $G_{\rm BP}-G_{\rm RP}$, to estimate effective temperatures for the stars in our sample, using the calibrated relation in ?.

Unlike isolated main-sequence stars, the rotation periods of binary stars and subgiants cannot always be determined by their mass and age (or at least they do not always follow the *same* gyrochronology relationship as isolated dwarfs). Visual binaries and subgiants were therefore removed from the sample by applying cuts to the color-magnitude diagram (CMD), shown in figure ??. A 6th-order polynomial was fit to the main sequence and raised by 0.27 dex to approximate the division between single stars and photometric binaries (shown as the curved dashed line in figure ??). All stars above this line were removed from the sample. Potential subgiants were also removed by eliminating stars brighter than 4th absolute magnitude in *Gaia* G-band. This cut also removed a number of main sequence F stars from our sample, however these hot stars are not the focus of our gyrochronology study since their small convective zones inhibit the generation of a strong magnetic field. The removal of photometric binaries and evolved/hot stars reduced the total sample of around 38,000 stars by around 4,000.

3587 stars in our sample had RV measurements in Gaia DR2, with a median uncertainty of 1.88 kms⁻¹. Gaia DR2 included RVs for stars with Gaia apparent magnitudes between around 4th and 13th, and 3550 K $\lesssim T_{\rm eff} \gtrsim 6900$ K (Gaia Collaboration et al. 2018). We also crossmatched the McQuillan et al. (2014) sample with the 5th LAMOST data release (Cui et al. 2012; Xiang et al. 2019), adding a further 7466 RV measurements to the sample, and expanding the total number of stars with measured RVs to 11,053. The median uncertainty of the LAMOST RV measurements was 4.71 kms⁻¹ and, given that the Gaia RVs were more precise, on average, than the LAMOST RVs, we adopted the Gaia value in cases where both were available. Gaia DR3 will contain a large number of new RV measurements for stars in our sample.

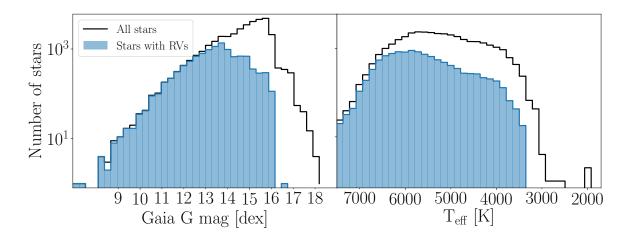
² Available at gaia-kepler.fun

3. STELLAR VELOCITIES

It has been demonstrated that the dispersion in vertical velocity, $v_{\mathbf{z}}$ for a group of stars increases with the age of that group (citations). However, velocities in Galactocentric coordinates, $v_{\mathbf{x}}$, $v_{\mathbf{y}}$ and $v_{\mathbf{z}}$, can only be calculated with full 6-D position and velocity information, *i.e.* proper motions, position and radial velocity. In Angus *et al.* (2020) we used velocity dispersions to explore rotational evolution and showed, in the appendix of that paper, that velocity in the direction of Galactic latitude, $v_{\mathbf{b}}$, which can be calculated without an RV measurement, is a close approximation to $v_{\mathbf{z}}$ for *Kepler* stars. This is because the *Kepler* field of view lies at relatively low Galactic latitudes, ($\sim 5-20^{\circ}$), so the **z**-direction is similar to the **b**-direction for *Kepler* stars. However, $v_{\mathbf{b}}$ is only a close approximation to $v_{\mathbf{z}}$ at extremely *low* latitudes, and even in the *Kepler* field which lies at $\mathbf{b} \approx 5\text{-}20^{\circ}$, kinematic ages calculated with $v_{\mathbf{b}}$ instead of $v_{\mathbf{z}}$ are systematically larger because of mixing between $v_{\mathbf{z}}$, $v_{\mathbf{x}}$ and $v_{\mathbf{y}}$. A direct measurement or precise estimate of $v_{\mathbf{z}}$ is necessary to calculate accurate kinematic ages. Less than 1 in 3 stars in our sample of *Kepler* rotators had a directly measured RV, but for these $\sim 11,000$ stars we calculated vertical velocities, $v_{\mathbf{z}}$, using the coordinates library of astropy (Astropy Collaboration et al. 2013; Price-Whelan et al. 2018).

Although RVs are available for almost one in three *Kepler* rotators, few late K and early M dwarfs have RV measurements due to the selection functions of the *Gaia* and *LAMOST* surveys. In our sample, one in 2.5 stars hotter than 5000 K had RV measurements, whereas only one in six stars cooler than 5000 K had RVs. *Gaia* DR2 only includes RVs for stars brighter than around 13th magnitude, and *LAMOST* only provides RVs for *Kepler* stars brighter than around 17th magnitude in *Gaia* G-band. Figure 1 shows the apparent magnitude and temperature distributions of the stars in our sample, with and without RVs. This figure reveals the combined selection functions of the *Gaia* DR2 and *LAMOST* RV surveys and shows that faint and cool stars have fewer RV measurements than hot, bright ones. Given

Figure 1. The apparent magnitude (left) and temperature (right) distributions of stars in our sample, with and without RV measurements from *Gaia* and *LAMOST*.



that rotational evolution is particularly poorly understood for M dwarfs, the cool stars with missing RVs are arguably the most interesting. To fill-in the low-temperature regime, we marginalized over missing RV measurements to infer velocities for stars without RVs.

3.1. Inferring 3D velocities (marginalizing over missing RV measurements)

For each star in our sample, we inferred $v_{\mathbf{x}}$, $v_{\mathbf{y}}$, and $v_{\mathbf{z}}$ from the 3D positions (right ascension, α , declination, δ , and parallax, π) and 2D proper motions (μ_{α} and μ_{δ}) provided in the *Gaia* DR2 catalog (Brown et al. 2011). We also simultaneously inferred distance, (instead of using inverse-parallax), to model velocities (see *e.g.* Bailer-Jones 2015; Bailer-Jones et al. 2018).

Using Bayes rule, the posterior probability of the parameters given the data can be written:

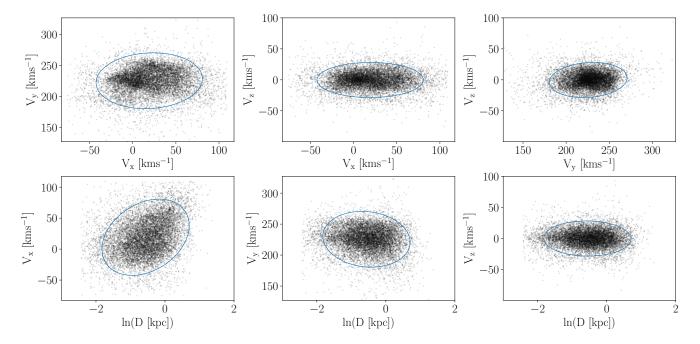
$$p(v_{\mathbf{x}\mathbf{y}\mathbf{z}}, D|\mu_{\alpha}, \mu_{\delta}, \alpha, \delta, \pi) = p(\mu_{\alpha}, \mu_{\delta}, \alpha, \delta, \pi|v_{\mathbf{x}\mathbf{y}\mathbf{z}}, D)p(v_{\mathbf{x}\mathbf{y}\mathbf{z}})p(D), \tag{1}$$

where D is distance. To calculate velocities, the \mathbf{x} , \mathbf{y} , \mathbf{z} position of each star was calculated from observations, α and δ , and parameter, distance $(1/\pi)$. These Galactocentric positions were calculated from equatorial coordinates by applying a matrix rotation, and a translation to account for the Solar position (-8.22, 0, 0 kpc in \mathbf{x} , \mathbf{y} and \mathbf{z}). Then, $v_{\mathbf{x}}$, $v_{\mathbf{y}}$, and $v_{\mathbf{z}}$ were inferred from a star's \mathbf{x} , \mathbf{y} , \mathbf{z} position and its $Gaia \ \mu_{\alpha}$ and μ_{δ} measurements.

3.2. The prior

The prior distribution over distance and velocities was constructed from the data. We calculated the means and covariances of the v_x , v_y , v_z and $\ln(D)$ distributions of stars with measured RVs and then used these means and covariances to construct a multivariate Gaussian prior over the parameters. Velocity outliers greater than 3- σ were removed before calculating the means and covariances of the distributions. The 2-dimensional log-distance and velocity distributions are displayed in figure 2, with 2- σ contours shown in blue.

Figure 2. The 2D velocity and distance distributions for stars with RV measurements, used to construct a multivariate Gaussian prior over velocity and distance parameters for stars without RVs. $2-\sigma$ contours are shown in blue.



Our goal was to infer the velocities of stars without RV measurements using a prior calculated from stars with RV measurements. However, stars with and without RVs are likely to be slightly different populations, the parameters of which depend on the Gaia and LAMOST selection function.

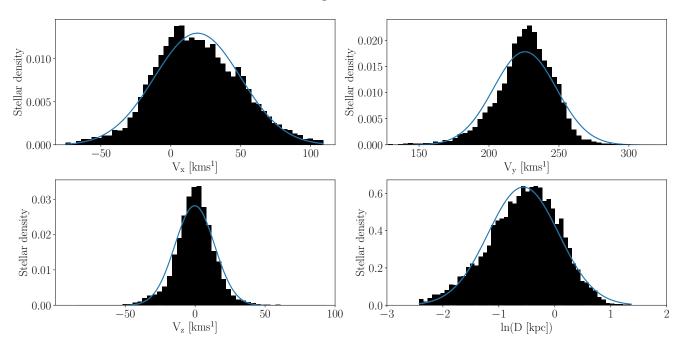
In particular, stars without RV measurements are more likely to be faint, and therefore, less massive. Lower-mass stars are, on average, older, and have larger velocity dispersions. So a prior based on the velocity distributions of stars with RVs will not necessarily reflect the velocities of those without.

For this reason, we tested how the choice of prior affected the velocities we inferred. We tested two priors: one calculated from the velocity distributions of the brightest half of the RV sample ($Gaia\ G$ -band apparent magnitude < 13.9), and one from the faintest half (G > 13.9). We selected the 500 faintest stars from the Gaia-LAMOST RV sample to test these two priors on. We chose the faintest stars as these are the most likely to be similar to the non-RV sample, and to enlarge the difference between the bright prior and the test sample. The results of this test are shown in figure ??

3.3. Inferred velocities

For each star in the *Kepler* field, we explored the posteriors of these four parameters using the PyMC3 No U-Turn Sampler (NUTS) algorithm, and the exoplanet Python library (citations). We tuned the PyMC3 sampler for 1500

Figure 3.



steps, with a target acceptance fraction of 0.9, then ran four chains of 1000 steps for a total of 4000 steps. Using PyMC3 made the inference procedure exceptionally fast – taking just a few seconds per star on a laptop.

To validate this method, we inferred velocities for stars in our sample with measured RVs and compared those inferred values with velocities calculated directly from 6D position, proper motion, and RV measurements. Figure ?? shows the v_x , v_y and v_z velocities we inferred, for 3000 stars chosen at random, compared with those calculated from measured RVs.

The three velocity components, $v_{\mathbf{x}}$, $v_{\mathbf{y}}$ and $v_{\mathbf{z}}$ were recovered with differing levels of precision: $v_{\mathbf{x}}$ and $v_{\mathbf{z}}$ are inferred more precisely than $v_{\mathbf{y}}$. This is because of the orientation of the *Kepler* field, shown in figure ??. The direction of the *Kepler* field is almost aligned with the \mathbf{y} -axis of the Galactocentric coordinate system and is almost perpendicular to the \mathbf{x} and \mathbf{z} -axes. For this reason, the \mathbf{y} -direction is similar to the radial direction, for observers near the Sun, so $v_{\mathbf{y}}$ is poorly constrained without an RV measurement. On the other hand, $v_{\mathbf{x}}$ and $v_{\mathbf{z}}$ are almost perpendicular to the radial direction and can be precisely inferred with proper motions alone.

Figure 4. Vertical velocities calculated with full 6D information vs vertical velocities inferred without RV, for all 3000 McQuillan et al. (2014) stars with Gaia RV measurements.

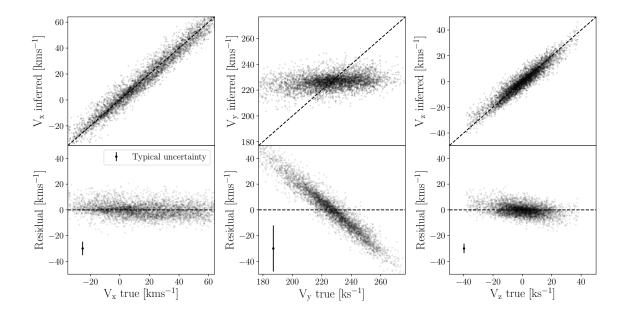
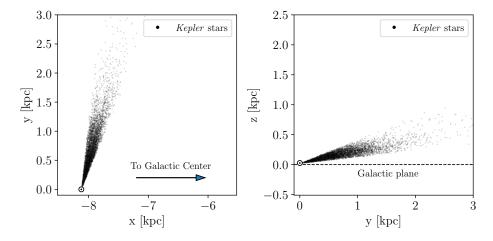


Figure 5. \mathbf{x} , \mathbf{y} and \mathbf{z} positions of stars observed by *Kepler*, showing the orientation of the *Kepler* field. The direction of the field is almost aligned with the \mathbf{y} -axis and almost perpendicular to the \mathbf{x} and \mathbf{z} -axes, which is why $v_{\mathbf{x}}$ and $v_{\mathbf{z}}$ can be tightly constrained for stars without RVs, but $v_{\mathbf{y}}$ cannot.



4. KINEMATIC AGES

4.1. Calculating velocity dispersions

A kinematic age can be calculated from the velocity dispersion, *i.e.* standard deviation, of a group of stars. These velocity dispersions can then be converted into an age using an AVR (*e.g.* Holmberg et al. 2009; Yu & Liu 2018). Kinematic ages represent the average age of a group of stars and are most informative when stars are grouped by age. If a group of stars have similar ages, their kinematic age will be close the age of each individual. On the other hand, the kinematic age of a group with large age variance will not provide much information about the ages of individual stars. Velocity distributions themselves do not reveal whether a group of stars have similar or different ages, since either case the velocities are Gaussian-distributed. Fortunately however, we can group Kepler stars by age using the implicit assumption that underpins gyrochronology: that stars with the same rotation period and color are the same age. We discuss the implications of this assumption and cases where it doesn't apply in the Discussion of this paper (section ??).

In this paper, we calculated the kinematic age of each individual star in our sample, by grouping it with its neighbors in $\log(P_{\rm rot})$ – $T_{\rm eff}$ space. This method is similar to calculating a rolling, or running standard deviation and allowed us to assign a unique age to each star. However, ages calculated this way are tightly correlated, and their correlation depends strongly on window-size.

We tested two methods of grouping stars: K-nearest neighbors, and bins in $\log(P_{\text{rot}})$ and T_{eff} . In the K-nearest neighbors method, each star was grouped with the K-nearest stars in $\log(P_{\text{rot}})$ - T_{eff} space. Groups created this way spanned a small $\log(P_{\text{rot}})$ - T_{eff} range where the stellar number density was large, and a large range where the number density was small. In other words, the number of stars was fixed but the window-size changed. In the fixed range method, stars were grouped within a fixed $\log(P_{\text{rot}})$ - T_{eff} window. This method created groups with large numbers of stars in densely populated regions of the $\log(P_{\text{rot}})$ - T_{eff} plane, and small numbers of stars in sparsely populated regions, i.e. the number of stars changed but the window-size was fixed. To choose the best method, and to optimize for the parameters of each (K and window-size), we conducted a set of tests.

4.2. Converting velocity dispersion to age with an AVR

We used the Yu & Liu (2018) AVR to convert velocity dispersion to age. This relation was calibrated using the ages and velocities of red clump stars. They divided their sample into metal rich and poor subsets, and calibrated separate AVRs for each, plus a global AVR. Their AVR is a power law:

$$\sigma_{vz} = \alpha t^{\beta},\tag{2}$$

where α and β take values (6.38, 0.578) for metal rich stars (3.89, 1.01) for metal poor stars, and (5.47, 0.765) for all stars.

We used $1.5 \times$ the Median Absolute Deviation (MAD) of velocities, which is a robust approximation to the standard deviation and is less sensitive to outliers. Velocity outliers could be binary stars or could be generated by underestimated parallax or proper motion uncertainties.

4.3. Comparing kinematic ages with asteroseismic and cluster ages

4.4. A Gaussian process gyrochronology relation

5. RESULTS

6. DISCUSSION

7. CONCLUSION

This work was partly developed at the 2019 KITP conference 'Better stars, better planets'. Parts of this project are based on ideas explored at the Gaia sprints at the Flatiron Institute in New York City, 2016 and MPIA, Heidelberg, 2017. This work made use of the gaia-kepler.fun crossmatch database created by Megan Bedell.

Some of the data presented in this paper were obtained from the Mikulski Archive for Space Telescopes (MAST). STScI is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS5-26555. Support for MAST for non-HST data is provided by the NASA Office of Space Science via grant NNX09AF08G and by other grants and contracts. This paper includes data collected by the Kepler mission. Funding for the *Kepler* mission is provided by the NASA Science Mission directorate.

This work has made use of data from the European Space Agency (ESA) mission *Gaia* (https://www.cosmos.esa.int/gaia), processed by the *Gaia* Data Processing and Analysis Consortium (DPAC, https://www.cosmos.esa.int/web/gaia/dpac/consortium). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the *Gaia* Multilateral Agreement.

REFERENCES

- Angus, R., Morton, T. D., & Foreman-Mackey *et al*, D. 2019, AJ, 158, 173, doi: 10.3847/1538-3881/ab3c53
- Astropy Collaboration, Robitaille, T. P., & Tollerud et al,
 E. J. 2013, A&A, 558, A33,
 doi: 10.1051/0004-6361/201322068
- Aumer, M., Binney, J., & Schönrich, R. 2016, MNRAS, 462, 1697, doi: 10.1093/mnras/stw1639
- Aumer, M., & Binney, J. J. 2009, MNRAS, 397, 1286, doi: 10.1111/j.1365-2966.2009.15053.x
- Bailer-Jones, C. A. L. 2015, PASP, 127, 994, doi: 10.1086/683116
- Bailer-Jones, C. A. L., Rybizki, J., & Fouesneau et al, M. 2018, AJ, 156, 58, doi: 10.3847/1538-3881/aacb21
- Barnes, S. A. 2003, ApJ, 586, 464, doi: 10.1086/367639
- —. 2007, ApJ, 669, 1167, doi: 10.1086/519295
- —. 2010, ApJ, 722, 222, doi: 10.1088/0004-637X/722/1/222
- Bird, J. C., Kazantzidis, S., & Weinberg et al, D. H. 2013, ApJ, 773, 43, doi: 10.1088/0004-637X/773/1/43
- Borucki, W. J., Koch, D., & Basri *et al*, G. 2010, Science, 327, 977, doi: 10.1126/science.1185402
- Bouvier, J. 2008, A&A, 489, L53, doi: 10.1051/0004-6361:200810574
- Brown, T. M., Latham, D. W., & Everett *et al*, M. E. 2011, AJ, 142, 112, doi: 10.1088/0004-6256/142/4/112
- Casagrande, L., Schönrich, R., & Asplund *et al*, M. 2011, A&A, 530, A138, doi: 10.1051/0004-6361/201016276
- Cui, X.-Q., Zhao, Y.-H., & Chu et al., Y.-Q. 2012, Research in Astronomy and Astrophysics, 12, 1197, doi: 10.1088/1674-4527/12/9/003
- Curtis, J. L., Agüeros, M. A., & Douglas et al, S. 2019, arXiv e-prints. https://arxiv.org/abs/1905.06869
- Denissenkov, P. A., Pinsonneault, M., & Terndrup et al,
 D. M. 2010, ApJ, 716, 1269,
 doi: 10.1088/0004-637X/716/2/1269
- Epstein, C. R., & Pinsonneault, M. H. 2014, ApJ, 780, 159, doi: 10.1088/0004-637X/780/2/159
- Faherty, J. K., Burgasser, A. J., & Cruz et al, K. L. 2009, AJ, 137, 1, doi: 10.1088/0004-6256/137/1/1
- Gaia Collaboration, Brown, A. G. A., & Vallenari et al., A. 2018, A&A, 616, A1, doi: 10.1051/0004-6361/201833051
- Gallet, F., & Bouvier, J. 2013, A&A, 556, A36, doi: 10.1051/0004-6361/201321302
- $\begin{array}{c} \text{Holmberg, J., Nordstr\"{o}m, B., \& Andersen, J. 2007, A\&A,} \\ 475, 519, \text{doi: } 10.1051/0004\text{-}6361\text{:}20077221} \end{array}$
- —. 2009, A&A, 501, 941, doi: 10.1051/0004-6361/200811191
- Howell, S. B., Sobeck, C., & Haas *et al*, M. 2014, PASP, 126, 398, doi: 10.1086/676406

- Irwin, J., Hodgkin, S., & Aigrain *et al*, S. 2007, MNRAS, 377, 741, doi: 10.1111/j.1365-2966.2007.11640.x
- Kawaler, S. D. 1988, ApJ, 333, 236, doi: 10.1086/166740
- Kiman, R., Schmidt, S. J., & Angus et al, R. 2019, AJ, 157, 231, doi: 10.3847/1538-3881/ab1753
- Kraft, R. P. 1967, ApJ, 150, 551, doi: 10.1086/149359
- M. Green, G. 2018, The Journal of Open Source Software, 3, 695, doi: 10.21105/joss.00695
- Mamajek, E. E., & Hillenbrand, L. A. 2008, ApJ, 687, 1264, doi: 10.1086/591785
- Martig, M., Minchev, I., & Flynn, C. 2014, MNRAS, 443, 2452, doi: 10.1093/mnras/stu1322
- McQuillan, A., Mazeh, T., & Aigrain, S. 2014, ApJS, 211, 24, doi: 10.1088/0067-0049/211/2/24
- Meibom, S., Barnes, S. A., & Latham et al, D. W. 2011, ApJL, 733, L9, doi: 10.1088/2041-8205/733/1/L9
- Meibom, S., Barnes, S. A., & Platais *et al*, I. 2015, Nature, 517, 589, doi: 10.1038/nature14118
- Najita, J., Willman, B., & Finkbeiner et al, D. P. 2016, arXiv e-prints, arXiv:1610.01661. https://arxiv.org/abs/1610.01661
- Nordström, B., Mayor, M., & Andersen et al, J. 2004, A&A, 418, 989, doi: 10.1051/0004-6361:20035959
- Pinsonneault, M. H., Kawaler, S. D., & Sofia *et al*, S. 1989, ApJ, 338, 424, doi: 10.1086/167210
- Price-Whelan, A. M., Sipőcz, B. M., & Günther *et al*, H. M. 2018, AJ, 156, 123, doi: 10.3847/1538-3881/aabc4f
- Reiners, A., & Mohanty, S. 2012, ApJ, 746, 43, doi: 10.1088/0004-637X/746/1/43
- Ricker, G. R., Winn, J. N., & Vanderspek et al, R. 2015, Journal of Astronomical Telescopes, Instruments, and Systems, 1, 014003, doi: 10.1117/1.JATIS.1.1.014003
- Santos, A. R. G., García, R. A., & Mathur et~al, S. 2019, ApJS, 244, 21, doi: 10.3847/1538-4365/ab3b56
- Schatzman, E. 1962, Annales d'Astrophysique, 25, 18
- Sellwood, J. A. 2014, Reviews of Modern Physics, 86, 1, doi: 10.1103/RevModPhys.86.1
- Skumanich, A. 1972, ApJ, 171, 565, doi: 10.1086/151310 Spada, F., & Lanzafame, A. C. 2019, arXiv e-prints,
- arXiv:1908.00345. https://arxiv.org/abs/1908.00345
- Spada, F., Lanzafame, A. C., & Lanza et al, A. F. 2011, MNRAS, 416, 447, doi: 10.1111/j.1365-2966.2011.19052.x
- Stark, A. A., & Brand, J. 1989, ApJ, 339, 763, doi: 10.1086/167334
- Stark, A. A., & Lee, Y. 2005, ApJL, 619, L159, doi: 10.1086/427936
- Strömberg, G. 1946, ApJ, 104, 12, doi: 10.1086/144830
- Ting, Y.-S., & Rix, H.-W. 2019, ApJ, 878, 21, doi: 10.3847/1538-4357/ab1ea5

van Saders, J. L., Ceillier, T., & Metcalfe et~al, T. S. 2016, Nature, 529, 181, doi: 10.1038/nature16168

Weber, E. J., & Davis, Jr., L. 1967, ApJ, 148, 217, doi: 10.1086/149138

West, A. A., Bochanski, J. J., & Hawley *et al*, S. L. 2006, AJ, 132, 2507, doi: 10.1086/508652

West, A. A., Hawley, S. L., & Bochanski et al, J. J. 2008, AJ, 135, 785, doi: 10.1088/0004-6256/135/3/785

West, A. A., Hawley, S. L., & Walkowicz *et al*, L. M. 2004, AJ, 128, 426, doi: 10.1086/421364

Wielen, R. 1977, A&A, 60, 263

Xiang, M., Ting, Y.-S., & Rix *et al.*, H.-W. 2019, ApJS, 245, 34, doi: 10.3847/1538-4365/ab5364

Yu, J., & Liu, C. 2018, MNRAS, 475, 1093,

doi: 10.1093/mnras/stx3204