

(Easy) Let $A \in \mathbb{R}^{n \times n}$ be a real symmetric matrix, λ_i is the i -th largest eigenvalue of A . Let X be any invertible matrix in $\mathbb{R}^{n \times n}$, prove that the i -th largest eigenvalue of $B = X^T(A - \lambda_i I)X$ is zero.