Let  $a_1, a_2, \ldots, a_n$  be a set of real numbers.  $C = (c_{ij}) \in \mathbb{R}^{n \times n}$  is a matrix and the entries of C is defined as  $c_{ij} = |a_i| + |a_j| - |a_i - a_j|$ . Prove that C is positive semidefinite. Hint: you can permute the rows and columns of C so that it could have blocked structure.