## Review: A Semi-Bregman Proximal Alternating Method for a Class of Nonconvex Problems: Local and Global Convergence Analysis

Ryota Iwamoto

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## 1 Introduction

We consider the following non-convex and non-smooth block optimization model:

$$\min_{x \in \mathbb{R}^n} \quad \Psi(x, y) \coloneqq F(x) + \Phi(y) + Q(x, y)$$
s.t.  $x \in \mathbb{R}^n, \quad y \in \mathbb{R}^m$  (1)

In the above model, F and  $\Phi$  are non-smooth functions, and Q is a smooth function. This model has been studied in various fields in recent years, mostly non-convex optimization. In this paper, we focus our attention on the following class of smooth coupling functions:

$$Q(x,y) = \frac{\rho}{2} \|q(x) - y\|$$
 (2)

where  $\rho > 0$  and  $q \colon \mathbb{R}^n \to \mathbb{R}^m$  is a continuously differentiable mapping.

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