ML-101: An Introduction to Machine Learning

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"Machine learning is glorified statistics"

"Machine learning is statistics scaled up to big data"

"Machine learning is for Computer Science majors who couldn't pass a Statistics course." – A disgruntled statistician

ML is an HYBRID field

- (Convex) Optimization
- Bayesian Statistics
- Lots and lots of linear algebra
- Sampling Theory
- Inspiration from biology, psychology

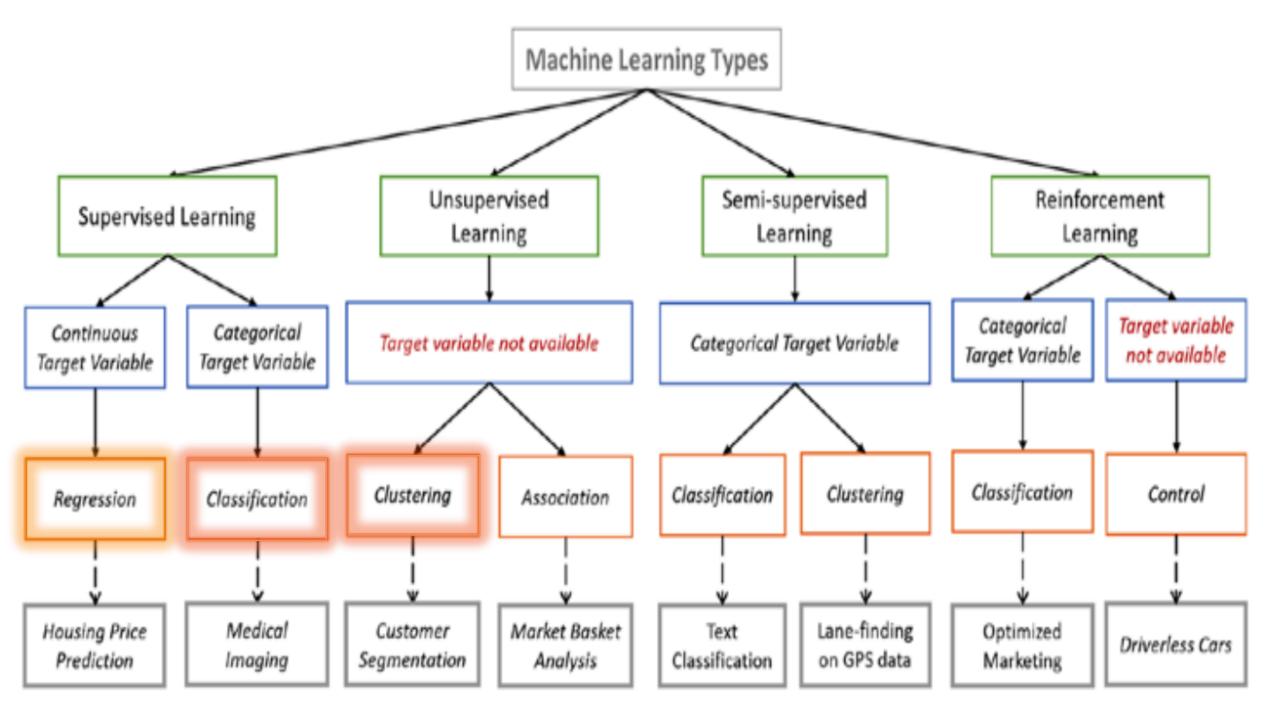
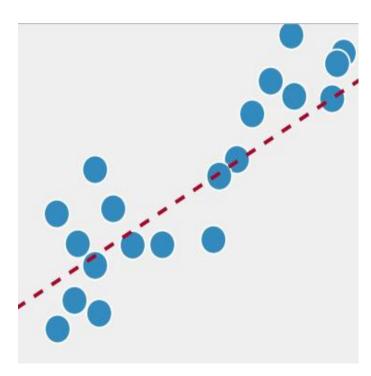
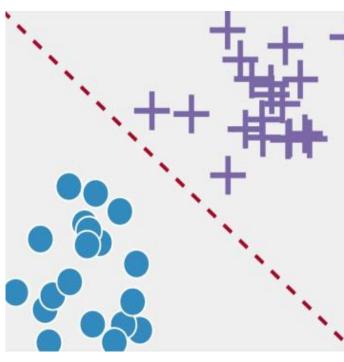


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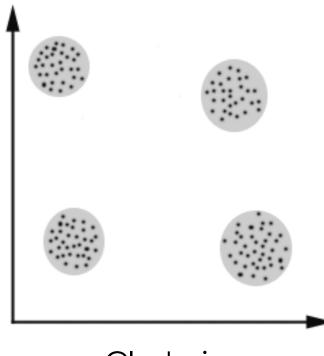
https://medium.com/@heyozramos/regression-vsclassification-86d73c281c5e home.deib.polimi.it



Regression



Classification

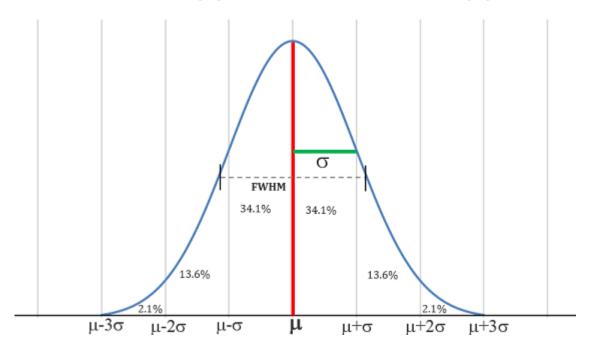


Clustering

Some Basic Statistics

Probability Distributions

The probability of a real-valued variable x falling in the interval $(x, x + \delta x)$ is given by $p(x)\delta x$ for $\delta x \to 0$, then p(x) is called the probability density over x



The Gaussian Distribution

$$p(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(x-\mu)^2/2\sigma^2}$$

Some Basic Statistics contd.

❖ Mean

$$\mathbb{E}[f] = \sum_{x} p(x)f(x)$$

$$\mathbb{E}[f] = \int p(x)f(x) \, \mathrm{d}x.$$

Variance

$$\operatorname{var}[f] = \mathbb{E}\left[\left(f(x) - \mathbb{E}[f(x)]\right)^{2}\right]$$

$$var[f] = \mathbb{E}[f(x)^2] - \mathbb{E}[f(x)]^2.$$

Covariance

$$cov[x, y] = \mathbb{E}_{x,y} [\{x - \mathbb{E}[x]\} \{y - \mathbb{E}[y]\}]$$
$$= \mathbb{E}_{x,y} [xy] - \mathbb{E}[x] \mathbb{E}[y]$$

Standard Deviation

Pre-processing of Data

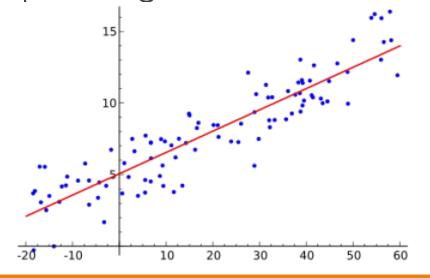
- ❖Remove noise
- Filtering and Sampling
- Feature Scaling and Zero-Mean [Normalization]
- Building dictionaries
- Encoding
- Handling missing data
- ◆PCA*
- Whitening

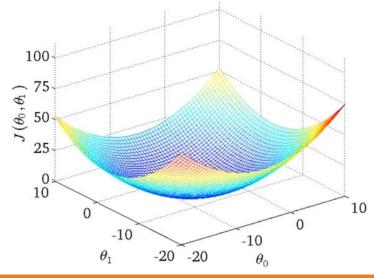
Linear Regression

- \Leftrightarrow Hypothesis Function: $h_{\theta}(\mathbf{x}) = \theta_0 + \theta_1.x_1 + ... + \theta_n.x_n$
- ❖Cost Function, J(**\theta**) Mean Squared Error

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} \left(h_{\theta}(x^{(i)}) - y^{(i)} \right)^{2}$$

Optimizing the cost Function via Gradient Descent





Gradient Descent

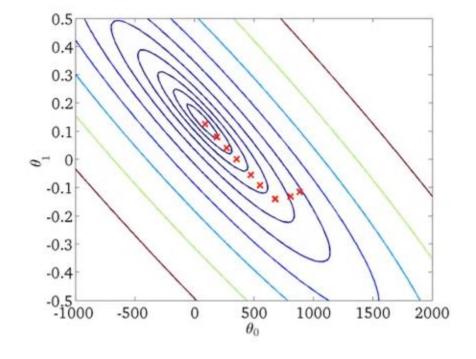
Cost Function

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} \left(h_{\theta}(x^{(i)}) - y^{(i)} \right)^{2}$$

Gradient Descent

Repeat till convergence{

$$\theta_j := \theta_j - \alpha \frac{1}{m} \sum_{i=1}^m \left(h_{\theta}(x^{(i)}) - y^{(i)} \right) x_j^{(i)}$$



}

Gradient Descent contd.

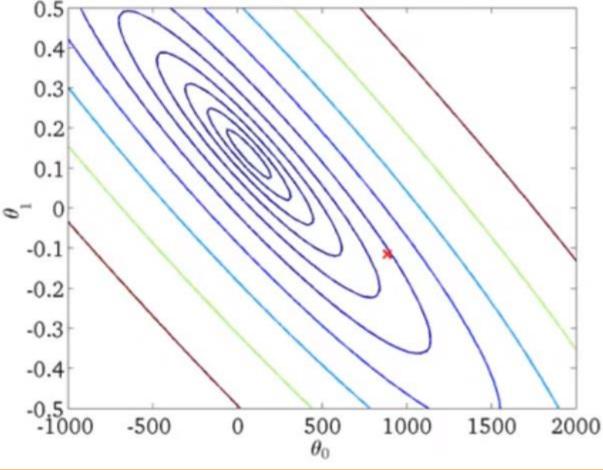
- To improve convergence
 - Feature Scaling and Mean Normali

$$x'=rac{x-ar{x}}{\sigma}$$

Choosing the learning rate, α



- Stochastic Gradient Descent
- Mini-Batch Gradient Descent



Modifications to SGD

- ♦SGD + Momentum
- Nesterov
- AdaGrad
- ❖ RMSProp
- Adam

• • •

dx = compute_gradient(x)
 x += learning_rate *dx

```
dx = compute_gradient(x)
    vx = rho*vx + dx
x += learning_rate * vx
```

Cross Validation

- While training model, test data should NOT be touched
- Limited Data
- Split Data into train, validation, (test)

Holdout Method, K-fold CV, Leave-One-Out CV