Instant Insanity Project
Math 482 – TTH 12:30PM-1:45PM
Professor John Dye
Contributors:

Programming Instant Insanity

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Preface:

Instant Insanity is a "fun" puzzle about blocks and colors. It's asymptotic time complexity grows exponentially. To solve the puzzle, the blocks must be arranged on top of eachother in one stack/column with each side showing each color exactly once. In other words, from each direction you face the stack, you should see a column in which no color repeats and every color is represented. With puzzles that have no solution, a minimal obstacle can be determined. This is a representative smallest set of cubes which which are not compatible with the original set. This minimal obstacle set is found by iterating down through each set size until a size is determined to not have any possible collisions- regardless of which cubes are chosen. Then, the minimal obstacle is considered to be any of the smallest sets found which indeed did result in an unstackable set (ie had any collisions and is one larger than the set size in which no collisions could be found). When searching for sets that are not compatible, there is no concern in terms of finding a subsolution- the only concerns are collisions. In other words, we aren't concerned with whether or not each color appears *exactly* once in each column; we are just concerned with whether or not the colors appear *more* than once in each column.

Puzzle Iteration and Finding the Solution

Python is currently one of the most widely used languages in the industry, therefore we decided it is best to use in this project as we are most comfortable with it. Here follows an explanation of the components of the program.

cubes generator(colors)

This function constructs the puzzle by building cubes out of the color set that is given and stacks the cubes on top of one another.

find min obs(cubes)

This function uses brute force to find the minimal obstacle. It sets up all the combinations of all the subsets of the puzzle. It begins by checking the puzzle that's a size of 30 cubes. If it has no solution then it goes down and checks every 30 choose k combination until a

every subset of a combination all have solutions. It will have then found the minimal obstacle. This function relies on the solve stack function to operate.

solve_stack(cubes, visited, solution_num)

Once called, this function will follow a Depth-First-Search for a set of cubes, along with having a known count of visited cubes (to avoid incorrect overlap). The first iteration "i" loops through all of the cubes and checks each of the three possible pairs of the current cube. If it finds a half solution, it will begin to check the puzzle for second compatible half solution to solve the stack of cubes. It is written arbitrarily enough to work for any size stack of cubes although the computational requirements will increase exponentially. If it does not find a half solution after the 2 pairs of colors for the first cube, it will break out of the iteration loop of the Depth-First-Search and finalize with no solution found.

Program Structure:

- Pseudocode: (Not finished. Based on Cormen's pseudo -Pablo)
 - (to make an arrow its "<-- ")

```
find min obs(cubes)
1. i \leftarrow 0
2. Multiplicity ← [array of size 30]
3. Half solution flag \leftarrow False
4. Half solution counter \leftarrow 0
5. iterate through all the cubes
6. Do if -1 < i < length of cubes
                backwards iteration flag ← True
7.
                Next half solution flag \leftarrow False
8.
9. iterate through the Cube's pair of opposite sides
10. for each pair of the current cube:
11.
12. #this stops the dfs at the third thread (no solution)
13.
      if we are on the first cube, half solution, and third color pair:
14.
          Half solution flag ← False
15.
          Backward iteration flag ← False
          Exit the current iterator
16.
17.
18. if a half solution hasn't been found, the iterator is at the end of iteration, and the current pair
    is taken by the current thread, then
         if we are not at the third pair of the current cube:
19.
20.
             visited[i][i] = 0
21.
             multiplicity[cubes[i][j][0]-1] -= 1
22.
             multiplicity[cubes[i][j][1]-1] -= 1
23.
             i += 1
```

```
24.
          else:
25.
            visited[i][i] = 0
            multiplicity[cubes[i][j][0]-1] -= 1
            multiplicity[cubes[i][j][1]-1] -= 1
            next half solution = True
       #half solution found
       if next half solution:
          break
       #(If this pair hasnt been visited, and the count of the colors of the pair are under 2,
       #then pick this pair and add one to the color count)
       if visited[i][i] == 0 and multiplicity[cubes[i][i][0] - 1] + 1 < 3 and
multiplicity[cubes[i][j][1] - 1] + 1 < 3:
          visited[i][j] = solution num
          multiplicity[cubes[i][i][0] - 1] += 1
          multiplicity[cubes[i][j][1] - 1] += 1
          moving backwards = False
          i += 1
          break
     #(moves back the thread to the previous cube to select the available pair. If on the last pair,
move back until possible)
     if moving backwards:
       i = i - 1
       done backtracking = False
       while not done backtracking and i \ge 0:
          for k in range(3):
            if visited[i][k] == solution num:
               visited[i][k] = 0
               multiplicity[cubes[i][k][0] - 1] = 1
               multiplicity[cubes[i][k][1] - 1] -= 1
               k = k + 1
               while k < 3:
                  if visited[i][k] == 0 and (multiplicity[cubes[i][k][0] - 1] + 1) < 3 and
(multiplicity[cubes[i][k][1] - 1] + 1) < 3:
                    visited[i][k] = solution num
                    multiplicity[cubes[i][k][0] - 1] += 1
                    multiplicity[cubes[i][k][1] - 1] += 1
                    done backtracking = True
                    i += 1
                    break
                  k = k + 1
               break
          if not done backtracking:
            i = i - 1
```

```
#found the end of the stack, Therefore solution.
     if i == len(cubes):
       half sol flag = True
     #found the end of the stack on the first solution
     if i == len(cubes) and solution num != 2:
       half sol counter += 1
       #print("First Half Solution")
       #for t in range(len(visited)):
          #print(visited[t])
       #Find second half solution
       half sol flag = solve stack(cubes, visited, 2)
       if not half sol flag:
          i = 1
  if i == -1:
     half sol flag = False
     #print("Number of half solutions: ", half sol counter)
     #print("No Solution")
  #if half sol flag and solution num == 1:
     #print("Number of half solutions: ", half sol counter)
     #print("Complete Solution")
     #for t in range(len(visited)):
       print(visited[t])
  #if half sol flag == False and solution num == 1 and i == -1:
     #print("No Solution")
  #if half sol flag == True and solution num == 2:
     #print("Solution Found")
  return half sol flag
Code:
import math as math
from itertools import combinations
def cubes_generator(colors):
  cubes = ∏
  cube = []
  pair = []
  for i in range(180):
    pair.append(colors[i])
```

```
if (i + 1) \% 2 == 0:
      cube.append(pair)
      pair = \Pi
    if (i + 1) \% 6 == 0:
      cubes.append(cube)
      cube = []
  return cubes
def solve_stack(cubes, visited, solution_num):
  multiplicity = [0 \text{ for i in range}(30)]
  half sol flag = False
  half sol counter = 0
  while -1 < i < len(cubes):
    moving_forward = True
    next_half_solution = False
    for j in range(3):
      # Stops the dfs at the third thread
      if i == 0 and solution_num == 1 and j == 2:
        half_sol_flag = False
        moving_forward = False
        break
      if half_sol_flag == False and i == (len(cubes) - 1) and visited[i][j] == solution_num:
        if i < 2:
           visited[i][j] = 0
           multiplicity[cubes[i][j][0]-1] -= 1
           multiplicity[cubes[i][j][1]-1] -= 1
          i += 1
        else:
           visited[i][j] = 0
           multiplicity[cubes[i][j][0]-1] -= 1
           multiplicity[cubes[i][j][1]-1] -= 1
           next half solution = True
      if next half solution:
        break
      if visited[i][j] == 0 and multiplicity[cubes[i][j][0] - 1] + 1 < 3 and
multiplicity[cubes[i][j][1] - 1] + 1 < 3:
        visited[i][j] = solution_num
        multiplicity[cubes[i][j][0] - 1] += 1
        multiplicity[cubes[i][j][1] - 1] += 1
        moving_forward = False
        i += 1
```

```
break
```

```
if moving_forward:
      i = i - 1
      done_backtracking = False
      while not done_backtracking and i >= 0:
        for k in range(3):
          if visited[i][k] == solution_num:
             visited[i][k] = 0
             multiplicity[cubes[i][k][0] - 1] -= 1
             multiplicity[cubes[i][k][1] - 1] -= 1
             k = k + 1
             while k < 3:
               if visited[i][k] == 0 and (multiplicity[cubes[i][k][0] - 1] + 1) < 3 and
(multiplicity[cubes[i][k][1] - 1] + 1) < 3:
                 visited[i][k] = solution_num
                 multiplicity[cubes[i][k][0] - 1] += 1
                 multiplicity[cubes[i][k][1] - 1] += 1
                 done_backtracking = True
                 i += 1
                 break
               k = k + 1
             break
        if not done_backtracking:
          i = i - 1
    if i == len(cubes):
      half_sol_flag = True
    if i == len(cubes) and solution_num!= 2:
      half_sol_counter += 1
      print("First Half Solution")
      for t in range(len(visited)):
        print(visited[t])
      half_sol_flag = solve_stack(cubes, visited, 2)
      if not half_sol_flag:
        i -= 1
  if i == -1:
    half_sol_flag = False
    print("Number of half solutions: ", half_sol_counter)
    print("No Solution")
  if half sol flag and solution num == 1:
    print("NUmber of half solutions: ", half_sol_counter)
    print("Complete Solution")
```

```
for t in range(len(visited)):
     print(visited[t])
  if half sol flag == False and solution num == 1 and i == -1:
    print("No Solution")
  if half sol flag == True and solution num == 2:
    print("Solution Found")
  return half_sol_flag
def find_min_obs(cubes):
  min_obs = len(cubes) + 1
  i = len(cubes)
  while i > 0:
    solution = False
    subsets = combinations(cubes, i)
    for subset in subsets:
      visited = [[0, 0, 0]] for i in range(len(subset))]
      solution = solve stack(subset, visited, 1)
      if not solution:
        print("A 'No Solution' was found in a stack of ", i," cubes!")
        print("Minimum obstacle is now: ", min obs -1)
        min obs -= 1
        for element in subset:
          print(element)
        break
      else:
        print("A Solution Was Found")
    if solution:
      print("Every subset of ", i , " cubes had a solution")
      print("Minimum Obstacle: ", min obs)
      if min obs > len(cubes):
        print("No Minimal Obstacle")
      break
    i = 1
# Puzzle 1
color1 = [1 + math.floor(n * math.pi) % 30 for n in range(1, 181)]
# Puzzle 2
color2 = [(1 + math.floor(i * math.e % 30)) for i in range(1,181)]
# Puzzle 3
color3 = [(1 + math.floor(i*math.sqrt(3)) \% 30) for i in range(1,181)]
# Puzzle 4
color4 = [(1 + math.floor(i * math.sqrt(5)) % 30) for i in range(1,181)]
```

```
cubes = cubes_generator(color1)
```

find_min_obs(cubes)

Output:

Solution for **Puzzle 1**: $1 + ((floor n\pi) \mod 30), 1 \le n \le 180$

```
A 'No Solution' was found in a stack of 30 cubes!
Minimum obstacle is now: 30
[[4, 7], [10, 13], [16, 19]]
[[22, 26], [29, 2], [5, 8]]
[[11, 14], [18, 21], [24, 27]]
[[30, 3], [6, 10], [13, 16]]
[[19, 22], [25, 28], [2, 5]]
[[8, 11], [14, 17], [20, 24]]
[[27, 30], [3, 6], [9, 12]]
[[16, 19], [22, 25], [28, 1]]
[[4, 8], [11, 14], [17, 20]]
[[23, 26], [30, 3], [6, 9]]
[[12, 15], [18, 22], [25, 28]]
[[1, 4], [7, 10], [14, 17]]
[[20, 23], [26, 29], [2, 6]]
[[9, 12], [15, 18], [21, 24]]
[[28, 1], [4, 7], [10, 13]]
[[16, 20], [23, 26], [29, 2]]
[[5, 8], [12, 15], [18, 21]]
[[24, 27], [30, 4], [7, 10]]
[[13, 16], [19, 22], [25, 29]]
[[2, 5], [8, 11], [14, 17]]
[[21, 24], [27, 30], [3, 6]]
[[9, 13], [16, 19], [22, 25]]
[[28, 1], [5, 8], [11, 14]]
[[17, 20], [23, 27], [30, 3]]
[[6, 9], [12, 15], [19, 22]]
[[25, 28], [1, 4], [7, 11]]
[[14, 17], [20, 23], [26, 29]]
[[3, 6], [9, 12], [15, 18]]
[[21, 25], [28, 1], [4, 7]]
[[10, 13], [17, 20], [23, 26]]
Every subset of 29 cubes had a solution
```

.....

Minimum Obstacle: 30

```
A 'No Solution' was found in a stack of 30 cubes!
Minimum obstacle is now: 30
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
[[27, 30], [2, 5], [8, 10]]
[[13, 16], [19, 21], [24, 27]]
[[29, 2], [5, 8], [10, 13]]
[[16, 18], [21, 24], [27, 29]]
[[2, 5], [7, 10], [13, 16]]
[[18, 21], [24, 26], [29, 2]]
[[5, 7], [10, 13], [16, 18]]
[[21, 24], [26, 29], [2, 5]]
[[7, 10], [13, 15], [18, 21]]
[[24, 26], [29, 2], [4, 7]]
[[10, 13], [15, 18], [21, 23]]
[[26, 29], [2, 4], [7, 10]]
A 'No Solution' was found in a stack of 29 cubes!
Minimum obstacle is now: 29
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
```

```
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
[[27, 30], [2, 5], [8, 10]]
[[13, 16], [19, 21], [24, 27]]
[[29, 2], [5, 8], [10, 13]]
[[16, 18], [21, 24], [27, 29]]
[[2, 5], [7, 10], [13, 16]]
[[18, 21], [24, 26], [29, 2]]
[[5, 7], [10, 13], [16, 18]]
[[21, 24], [26, 29], [2, 5]]
[[7, 10], [13, 15], [18, 21]]
[[24, 26], [29, 2], [4, 7]]
[[10, 13], [15, 18], [21, 23]]
A 'No Solution' was found in a stack of 28 cubes!
Minimum obstacle is now: 28
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
[[27, 30], [2, 5], [8, 10]]
[[13, 16], [19, 21], [24, 27]]
[[29, 2], [5, 8], [10, 13]]
[[16, 18], [21, 24], [27, 29]]
[[2, 5], [7, 10], [13, 16]]
[[18, 21], [24, 26], [29, 2]]
```

[[5, 7], [10, 13], [16, 18]]

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[[21, 24], [26, 29], [2, 5]]
[[7, 10], [13, 15], [18, 21]]
[[24, 26], [29, 2], [4, 7]]
A 'No Solution' was found in a stack of 27 cubes!
Minimum obstacle is now: 27
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
[[27, 30], [2, 5], [8, 10]]
[[13, 16], [19, 21], [24, 27]]
[[29, 2], [5, 8], [10, 13]]
[[16, 18], [21, 24], [27, 29]]
[[2, 5], [7, 10], [13, 16]]
[[18, 21], [24, 26], [29, 2]]
[[5, 7], [10, 13], [16, 18]]
[[21, 24], [26, 29], [2, 5]]
[[7, 10], [13, 15], [18, 21]]
A 'No Solution' was found in a stack of 26 cubes!
Minimum obstacle is now: 26
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
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```
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
[[27, 30], [2, 5], [8, 10]]
[[13, 16], [19, 21], [24, 27]]
[[29, 2], [5, 8], [10, 13]]
[[16, 18], [21, 24], [27, 29]]
[[2, 5], [7, 10], [13, 16]]
[[18, 21], [24, 26], [29, 2]]
[[5, 7], [10, 13], [16, 18]]
[[21, 24], [26, 29], [2, 5]]
A 'No Solution' was found in a stack of 25 cubes!
Minimum obstacle is now: 25
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
[[27, 30], [2, 5], [8, 10]]
[[13, 16], [19, 21], [24, 27]]
[[29, 2], [5, 8], [10, 13]]
[[16, 18], [21, 24], [27, 29]]
[[2, 5], [7, 10], [13, 16]]
[[18, 21], [24, 26], [29, 2]]
[[5, 7], [10, 13], [16, 18]]
A 'No Solution' was found in a stack of 24 cubes!
Minimum obstacle is now: 24
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
```

```
[[22, 25], [28, 30], [3, 6]]
```

[[8, 11], [14, 17], [19, 22]]

[[25, 27], [30, 3], [6, 8]]

[[11, 14], [17, 19], [22, 25]]

[[27, 30], [3, 6], [8, 11]]

[[14, 16], [19, 22], [25, 27]]

[[30, 3], [5, 8], [11, 14]]

[[16, 19], [22, 24], [27, 30]]

[[3, 5], [8, 11], [13, 16]]

[[19, 22], [24, 27], [30, 3]]

[[5, 8], [11, 13], [16, 19]]

[[22, 24], [27, 30], [2, 5]]

[[8, 11], [13, 16], [19, 21]]

[[24, 27], [30, 2], [5, 8]]

[[10, 13], [16, 19], [21, 24]]

[[27, 30], [2, 5], [8, 10]]

[[13, 16], [19, 21], [24, 27]]

[[29, 2], [5, 8], [10, 13]]

[[16, 18], [21, 24], [27, 29]]

[[2, 5], [7, 10], [13, 16]]

[[18, 21], [24, 26], [29, 2]]

A 'No Solution' was found in a stack of 23 cubes!

Minimum obstacle is now: 23

[[3, 6], [9, 11], [14, 17]]

[[20, 22], [25, 28], [30, 3]]

[[6, 9], [11, 14], [17, 19]]

[[22, 25], [28, 30], [3, 6]]

[[8, 11], [14, 17], [19, 22]]

[[25, 27], [30, 3], [6, 8]]

[[11, 14], [17, 19], [22, 25]]

[[27, 30], [3, 6], [8, 11]]

[[14, 16], [19, 22], [25, 27]]

[[30, 3], [5, 8], [11, 14]]

[[16, 19], [22, 24], [27, 30]]

[[3, 5], [8, 11], [13, 16]]

[[19, 22], [24, 27], [30, 3]]

[[5, 8], [11, 13], [16, 19]]

[[22, 24], [27, 30], [2, 5]]

[[8, 11], [13, 16], [19, 21]]

[[24, 27], [30, 2], [5, 8]]

[[10, 13], [16, 19], [21, 24]]

[[27, 30], [2, 5], [8, 10]]

[[13, 16], [19, 21], [24, 27]]

[[29, 2], [5, 8], [10, 13]]

[[16, 18], [21, 24], [27, 29]]

[[2, 5], [7, 10], [13, 16]]

```
A 'No Solution' was found in a stack of 22 cubes!
```

Minimum obstacle is now: 22

[[3, 6], [9, 11], [14, 17]]

[[20, 22], [25, 28], [30, 3]]

[[6, 9], [11, 14], [17, 19]]

[[22, 25], [28, 30], [3, 6]]

[[8, 11], [14, 17], [19, 22]]

[[25, 27], [30, 3], [6, 8]]

[[11, 14], [17, 19], [22, 25]]

[[27, 30], [3, 6], [8, 11]]

[[14, 16], [19, 22], [25, 27]]

[[30, 3], [5, 8], [11, 14]]

[[16, 19], [22, 24], [27, 30]]

[[3, 5], [8, 11], [13, 16]]

[[19, 22], [24, 27], [30, 3]]

[[5, 8], [11, 13], [16, 19]]

[[22, 24], [27, 30], [2, 5]]

[[8, 11], [13, 16], [19, 21]]

[[24, 27], [30, 2], [5, 8]]

[[10, 13], [16, 19], [21, 24]]

[[27, 30], [2, 5], [8, 10]]

[[13, 16], [19, 21], [24, 27]]

[[29, 2], [5, 8], [10, 13]]

[[16, 18], [21, 24], [27, 29]]

A 'No Solution' was found in a stack of 21 cubes!

Minimum obstacle is now: 21

[[3, 6], [9, 11], [14, 17]]

[[20, 22], [25, 28], [30, 3]]

[[6, 9], [11, 14], [17, 19]]

[[22, 25], [28, 30], [3, 6]]

[[8, 11], [14, 17], [19, 22]]

[[25, 27], [30, 3], [6, 8]]

[[11, 14], [17, 19], [22, 25]]

[[27, 30], [3, 6], [8, 11]]

[[14, 16], [19, 22], [25, 27]]

[[30, 3], [5, 8], [11, 14]]

[[16, 19], [22, 24], [27, 30]]

[[3, 5], [8, 11], [13, 16]]

[[19, 22], [24, 27], [30, 3]]

[[5, 8], [11, 13], [16, 19]]

[[22, 24], [27, 30], [2, 5]]

[[8, 11], [13, 16], [19, 21]]

[[24, 27], [30, 2], [5, 8]]

[[10, 13], [16, 19], [21, 24]]

[[27, 30], [2, 5], [8, 10]]

[[13, 16], [19, 21], [24, 27]]

```
[[29, 2], [5, 8], [10, 13]]
A 'No Solution' was found in a stack of 20 cubes!
Minimum obstacle is now: 20
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
[[27, 30], [2, 5], [8, 10]]
[[13, 16], [19, 21], [24, 27]]
A 'No Solution' was found in a stack of 19 cubes!
Minimum obstacle is now: 19
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
[[27, 30], [2, 5], [8, 10]]
A 'No Solution' was found in a stack of 18 cubes!
```

Minimum obstacle is now: 18

```
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[10, 13], [16, 19], [21, 24]]
A 'No Solution' was found in a stack of 17 cubes!
Minimum obstacle is now: 17
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
A 'No Solution' was found in a stack of 16 cubes!
Minimum obstacle is now: 16
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[6, 9], [11, 14], [17, 19]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
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[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[22, 24], [27, 30], [2, 5]]
[[8, 11], [13, 16], [19, 21]]
A 'No Solution' was found in a stack of 15 cubes!
Minimum obstacle is now: 15
[[3, 6], [9, 11], [14, 17]]
[[20, 22], [25, 28], [30, 3]]
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[11, 14], [17, 19], [22, 25]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[22, 24], [27, 30], [2, 5]]
[[24, 27], [30, 2], [5, 8]]
[[27, 30], [2, 5], [8, 10]]
A 'No Solution' was found in a stack of 14 cubes!
Minimum obstacle is now: 14
[[22, 25], [28, 30], [3, 6]]
[[8, 11], [14, 17], [19, 22]]
[[25, 27], [30, 3], [6, 8]]
[[27, 30], [3, 6], [8, 11]]
[[14, 16], [19, 22], [25, 27]]
[[30, 3], [5, 8], [11, 14]]
[[16, 19], [22, 24], [27, 30]]
[[3, 5], [8, 11], [13, 16]]
[[19, 22], [24, 27], [30, 3]]
[[5, 8], [11, 13], [16, 19]]
[[8, 11], [13, 16], [19, 21]]
[[24, 27], [30, 2], [5, 8]]
[[27, 30], [2, 5], [8, 10]]
[[13, 16], [19, 21], [24, 27]]
Every subset of 13 cubes had a solution
```

Minimum Obstacle: 14

Solution for **Puzzle 3**: $1 + ((floor n\sqrt{3}) \mod 30), 1 \le n \le 180$

```
A 'No Solution' was found in a stack of 30 cubes!
Minimum obstacle is now: 30
[[2, 4], [6, 7], [9, 11]]
[[13, 14], [16, 18], [20, 21]]
[[23, 25], [26, 28], [30, 2]]
[[3, 5], [7, 9], [10, 12]]
[[14, 16], [17, 19], [21, 22]]
[[24, 26], [28, 29], [1, 3]]
[[5, 6], [8, 10], [12, 13]]
[[15, 17], [18, 20], [22, 24]]
[[25, 27], [29, 1], [2, 4]]
[[6, 7], [9, 11], [13, 14]]
[[16, 18], [20, 21], [23, 25]]
[[27, 28], [30, 2], [3, 5]]
[[7, 9], [10, 12], [14, 16]]
[[17, 19], [21, 23], [24, 26]]
[[28, 29], [1, 3], [5, 6]]
[[8, 10], [12, 13], [15, 17]]
[[19, 20], [22, 24], [25, 27]]
[[29, 1], [2, 4], [6, 8]]
[[9, 11], [13, 14], [16, 18]]
[[20, 21], [23, 25], [27, 28]]
[[30, 2], [4, 5], [7, 9]]
[[10, 12], [14, 16], [17, 19]]
[[21, 23], [24, 26], [28, 30]]
[[1, 3], [5, 6], [8, 10]]
[[12, 13], [15, 17], [19, 20]]
[[22, 24], [26, 27], [29, 1]]
[[2, 4], [6, 8], [9, 11]]
[[13, 15], [16, 18], [20, 21]]
[[23, 25], [27, 28], [30, 2]]
[[4, 5], [7, 9], [11, 12]]
A 'No Solution' was found in a stack of 29 cubes!
Minimum obstacle is now: 29
[[2, 4], [6, 7], [9, 11]]
[[13, 14], [16, 18], [20, 21]]
[[23, 25], [26, 28], [30, 2]]
[[3, 5], [7, 9], [10, 12]]
[[14, 16], [17, 19], [21, 22]]
[[24, 26], [28, 29], [1, 3]]
[[5, 6], [8, 10], [12, 13]]
[[15, 17], [18, 20], [22, 24]]
[[25, 27], [29, 1], [2, 4]]
[[6, 7], [9, 11], [13, 14]]
```

```
[[16, 18], [20, 21], [23, 25]]
[[27, 28], [30, 2], [3, 5]]
[[7, 9], [10, 12], [14, 16]]
[[17, 19], [21, 23], [24, 26]]
[[28, 29], [1, 3], [5, 6]]
[[8, 10], [12, 13], [15, 17]]
[[19, 20], [22, 24], [25, 27]]
[[29, 1], [2, 4], [6, 8]]
[[9, 11], [13, 14], [16, 18]]
[[20, 21], [23, 25], [27, 28]]
[[30, 2], [4, 5], [7, 9]]
[[10, 12], [14, 16], [17, 19]]
[[21, 23], [24, 26], [28, 30]]
[[1, 3], [5, 6], [8, 10]]
[[12, 13], [15, 17], [19, 20]]
[[22, 24], [26, 27], [29, 1]]
[[2, 4], [6, 8], [9, 11]]
[[13, 15], [16, 18], [20, 21]]
[[23, 25], [27, 28], [30, 2]]
A 'No Solution' was found in a stack of 28 cubes!
Minimum obstacle is now: 28
[[2, 4], [6, 7], [9, 11]]
[[13, 14], [16, 18], [20, 21]]
[[23, 25], [26, 28], [30, 2]]
[[3, 5], [7, 9], [10, 12]]
[[14, 16], [17, 19], [21, 22]]
[[24, 26], [28, 29], [1, 3]]
[[5, 6], [8, 10], [12, 13]]
[[15, 17], [18, 20], [22, 24]]
[[25, 27], [29, 1], [2, 4]]
[[6, 7], [9, 11], [13, 14]]
[[16, 18], [20, 21], [23, 25]]
[[27, 28], [30, 2], [3, 5]]
[[7, 9], [10, 12], [14, 16]]
[[17, 19], [21, 23], [24, 26]]
[[28, 29], [1, 3], [5, 6]]
[[8, 10], [12, 13], [15, 17]]
[[19, 20], [22, 24], [25, 27]]
[[29, 1], [2, 4], [6, 8]]
[[9, 11], [13, 14], [16, 18]]
[[20, 21], [23, 25], [27, 28]]
[[30, 2], [4, 5], [7, 9]]
[[10, 12], [14, 16], [17, 19]]
[[21, 23], [24, 26], [28, 30]]
[[1, 3], [5, 6], [8, 10]]
[[12, 13], [15, 17], [19, 20]]
```

```
[[22, 24], [26, 27], [29, 1]]
[[2, 4], [6, 8], [9, 11]]
[[13, 15], [16, 18], [20, 21]]
A 'No Solution' was found in a stack of 27 cubes!
Minimum obstacle is now: 27
[[2, 4], [6, 7], [9, 11]]
[[13, 14], [16, 18], [20, 21]]
[[23, 25], [26, 28], [30, 2]]
[[3, 5], [7, 9], [10, 12]]
[[14, 16], [17, 19], [21, 22]]
[[24, 26], [28, 29], [1, 3]]
[[5, 6], [8, 10], [12, 13]]
[[15, 17], [18, 20], [22, 24]]
[[25, 27], [29, 1], [2, 4]]
[[6, 7], [9, 11], [13, 14]]
[[16, 18], [20, 21], [23, 25]]
[[27, 28], [30, 2], [3, 5]]
[[7, 9], [10, 12], [14, 16]]
[[17, 19], [21, 23], [24, 26]]
[[28, 29], [1, 3], [5, 6]]
[[8, 10], [12, 13], [15, 17]]
[[19, 20], [22, 24], [25, 27]]
[[29, 1], [2, 4], [6, 8]]
[[9, 11], [13, 14], [16, 18]]
[[20, 21], [23, 25], [27, 28]]
[[30, 2], [4, 5], [7, 9]]
[[10, 12], [14, 16], [17, 19]]
[[21, 23], [24, 26], [28, 30]]
[[1, 3], [5, 6], [8, 10]]
[[2, 4], [6, 8], [9, 11]]
[[13, 15], [16, 18], [20, 21]]
[[23, 25], [27, 28], [30, 2]]
A 'No Solution' was found in a stack of 26 cubes!
Minimum obstacle is now: 26
[[2, 4], [6, 7], [9, 11]]
[[13, 14], [16, 18], [20, 21]]
[[23, 25], [26, 28], [30, 2]]
[[3, 5], [7, 9], [10, 12]]
[[14, 16], [17, 19], [21, 22]]
[[24, 26], [28, 29], [1, 3]]
[[5, 6], [8, 10], [12, 13]]
[[15, 17], [18, 20], [22, 24]]
[[25, 27], [29, 1], [2, 4]]
[[6, 7], [9, 11], [13, 14]]
[[16, 18], [20, 21], [23, 25]]
[[27, 28], [30, 2], [3, 5]]
```

```
[[7, 9], [10, 12], [14, 16]]
[[28, 29], [1, 3], [5, 6]]
[[8, 10], [12, 13], [15, 17]]
[[19, 20], [22, 24], [25, 27]]
[[29, 1], [2, 4], [6, 8]]
[[9, 11], [13, 14], [16, 18]]
[[20, 21], [23, 25], [27, 28]]
[[30, 2], [4, 5], [7, 9]]
[[10, 12], [14, 16], [17, 19]]
[[1, 3], [5, 6], [8, 10]]
[[12, 13], [15, 17], [19, 20]]
[[2, 4], [6, 8], [9, 11]]
[[13, 15], [16, 18], [20, 21]]
[[23, 25], [27, 28], [30, 2]]
A 'No Solution' was found in a stack of 25 cubes!
Minimum obstacle is now: 25
[[2, 4], [6, 7], [9, 11]]
[[13, 14], [16, 18], [20, 21]]
[[23, 25], [26, 28], [30, 2]]
[[3, 5], [7, 9], [10, 12]]
[[14, 16], [17, 19], [21, 22]]
[[24, 26], [28, 29], [1, 3]]
[[5, 6], [8, 10], [12, 13]]
[[25, 27], [29, 1], [2, 4]]
[[6, 7], [9, 11], [13, 14]]
[[16, 18], [20, 21], [23, 25]]
[[27, 28], [30, 2], [3, 5]]
[[7, 9], [10, 12], [14, 16]]
[[28, 29], [1, 3], [5, 6]]
[[8, 10], [12, 13], [15, 17]]
[[29, 1], [2, 4], [6, 8]]
[[9, 11], [13, 14], [16, 18]]
[[20, 21], [23, 25], [27, 28]]
[[30, 2], [4, 5], [7, 9]]
[[10, 12], [14, 16], [17, 19]]
[[21, 23], [24, 26], [28, 30]]
[[1, 3], [5, 6], [8, 10]]
[[2, 4], [6, 8], [9, 11]]
[[13, 15], [16, 18], [20, 21]]
[[23, 25], [27, 28], [30, 2]]
[[4, 5], [7, 9], [11, 12]]
Every subset of 24 cubes had a solution
Minimum Obstacle: 25
```

Solution for **Puzzle 4**: $1 + ((floor n\sqrt{5}) \mod 30), 1 \le n \le 180$

```
A 'No Solution' was found in a stack of 30 cubes!
Minimum obstacle is now: 30
[[3, 5], [7, 9], [12, 14]]
[[16, 18], [21, 23], [25, 27]]
[[30, 2], [4, 6], [9, 11]]
[[13, 15], [17, 20], [22, 24]]
[[26, 29], [1, 3], [5, 8]]
[[10, 12], [14, 17], [19, 21]]
[[23, 25], [28, 30], [2, 4]]
[[7, 9], [11, 13], [16, 18]]
[[20, 22], [25, 27], [29, 1]]
[[3, 6], [8, 10], [12, 15]]
[[17, 19], [21, 24], [26, 28]]
[[30, 3], [5, 7], [9, 11]]
[[14, 16], [18, 20], [23, 25]]
[[27, 29], [2, 4], [6, 8]]
[[11, 13], [15, 17], [20, 22]]
[[24, 26], [28, 1], [3, 5]]
[[7, 10], [12, 14], [16, 19]]
[[21, 23], [25, 28], [30, 2]]
[[4, 6], [9, 11], [13, 15]]
[[18, 20], [22, 24], [27, 29]]
[[1, 3], [6, 8], [10, 12]]
[[14, 17], [19, 21], [23, 26]]
[[28, 30], [2, 5], [7, 9]]
[[11, 14], [16, 18], [20, 22]]
[[25, 27], [29, 1], [4, 6]]
[[8, 10], [13, 15], [17, 19]]
[[22, 24], [26, 28], [1, 3]]
[[5, 7], [9, 12], [14, 16]]
[[18, 21], [23, 25], [27, 30]]
[[2, 4], [6, 9], [11, 13]]
Every subset of 29 cubes had a solution
Minimum Obstacle: 30
```

Extra Solution for **Puzzle 5**: $1 + ((floor n\sqrt{7}) \mod 30)$, $1 \le n \le 180$