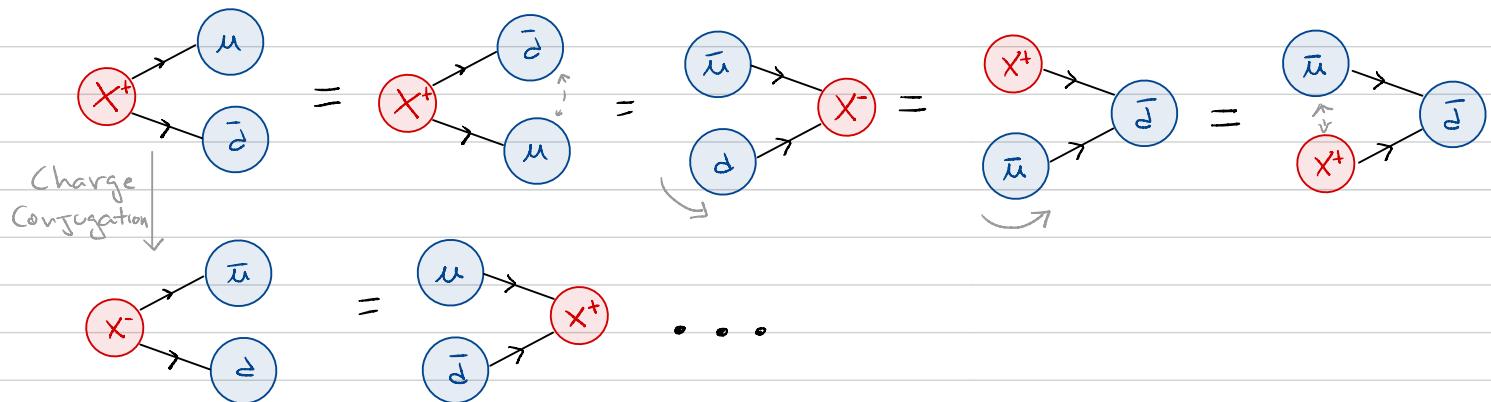
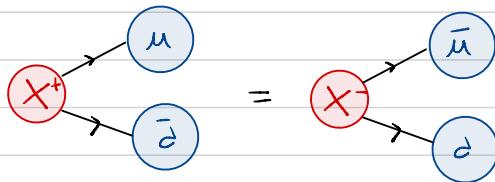


— Vertex: Canonical Representation

- We need to be able to match vertices irrespective of their ordering:

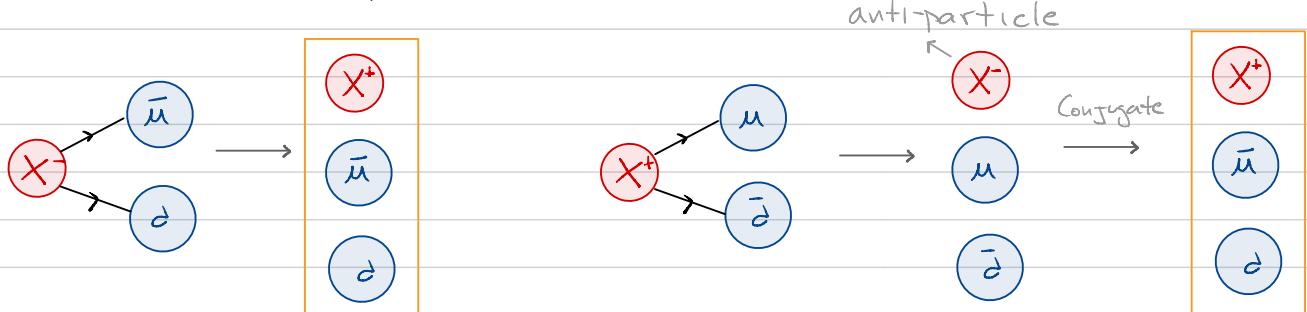


- In addition vertices differing only by charge conjugation should also be considered as equivalent (assumes C-conservation):

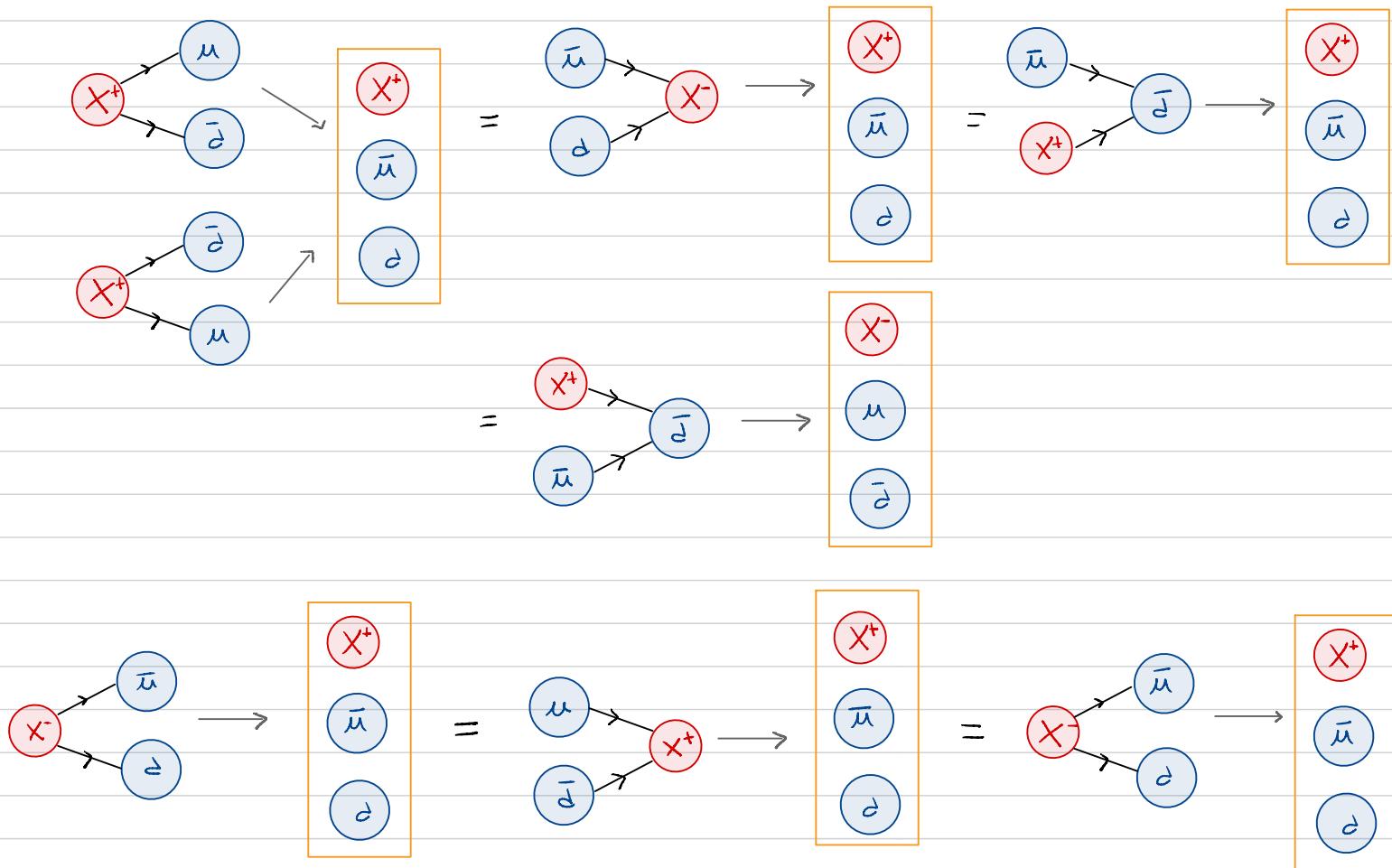


With this definition it is not necessary to keep track of all the vertices and their charge conjugation.

- Hence to simplify the matching all vertices are represented with all particles as outgoing. In addition if the particle with largest PDG and which is not its own anti-particle is an anti-particle (PDG < 0), all the particles are charge conjugated:



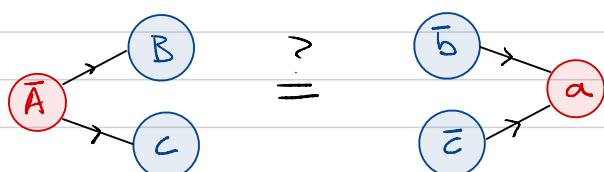
- Applying this definition of a "canonical" representation of a vertex we have:

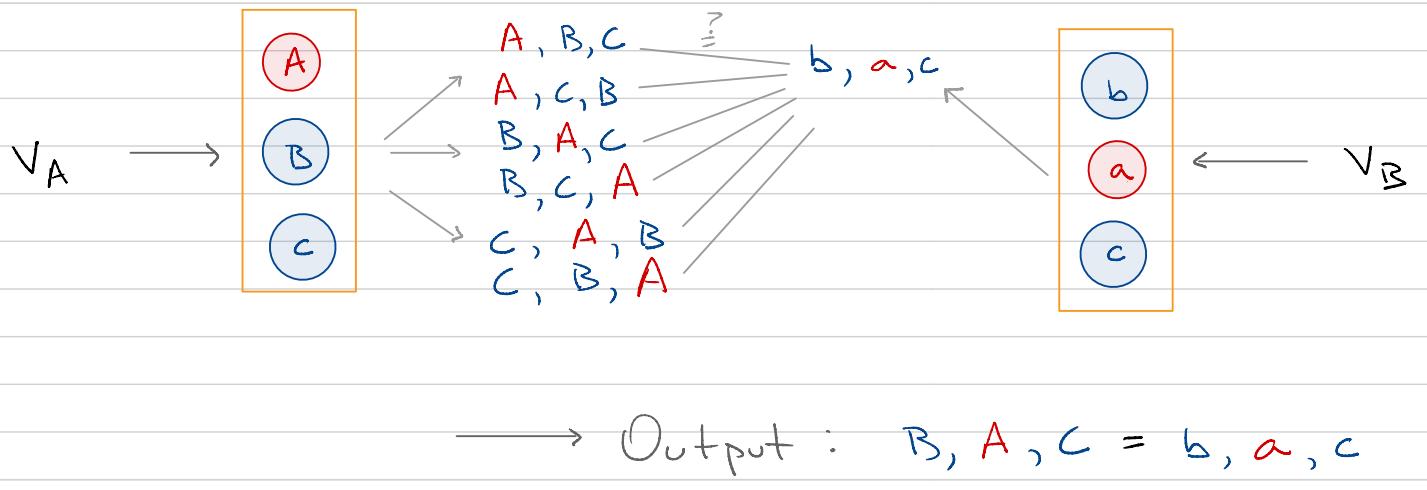


— Vertex: Matching

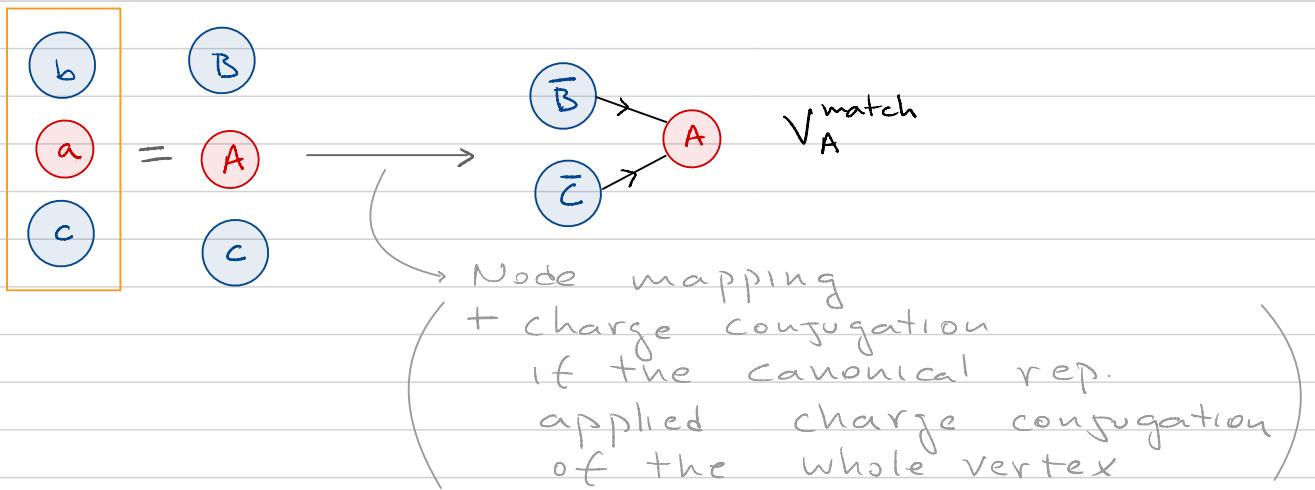
- Using this "canonical representation" of a vertex, it is only need to compare two lists of particles irrespective of their ordering.

$$V_A \stackrel{?}{=} V_B$$





- Once the vertices match, V_A can be brought to V_B format:



— Vertex: String Representation

- The vertex \leftrightarrow string mapping is given by:

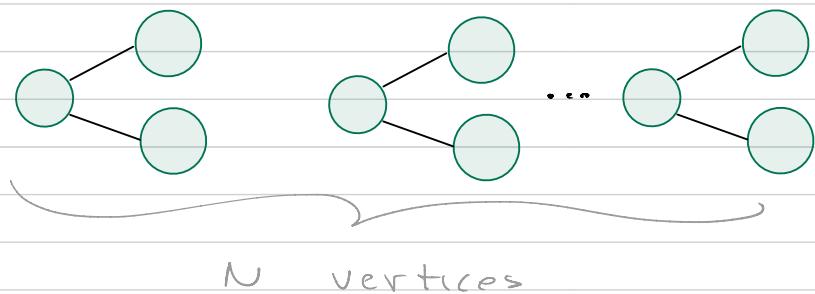
$$A, B, C \rightarrow \underbrace{a, b, \dots}_{\text{Incoming Particles}}$$

$\underbrace{\dots}_{\text{Outgoing Particles}}$

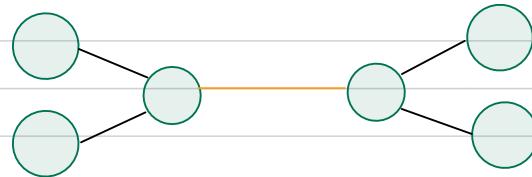
— Building $2 \rightarrow N$ Topologies

- Assuming we only have 3-point vertices, the $2 \rightarrow N$ topologies can be built (for a given N) with the following steps:

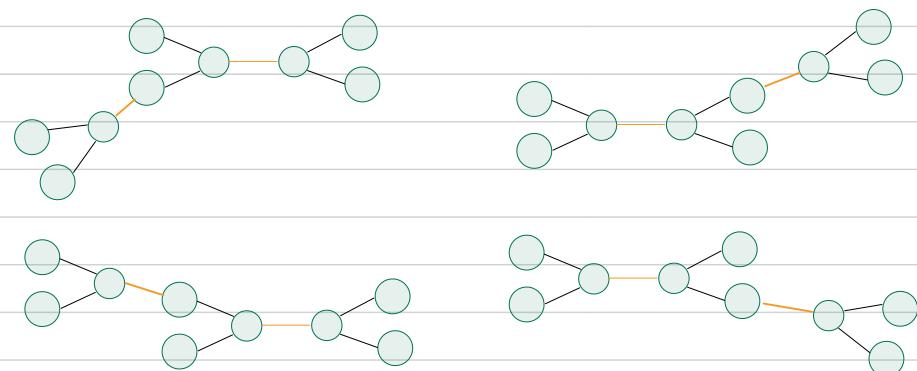
- 1) Create N vertices with empty or generic particles



- 2) Connect two vertices with an edge ("propagator") to obtain a base topology



- 3) Connect the 3rd vertex adding an edge to each possible node, generating multiple topologies:

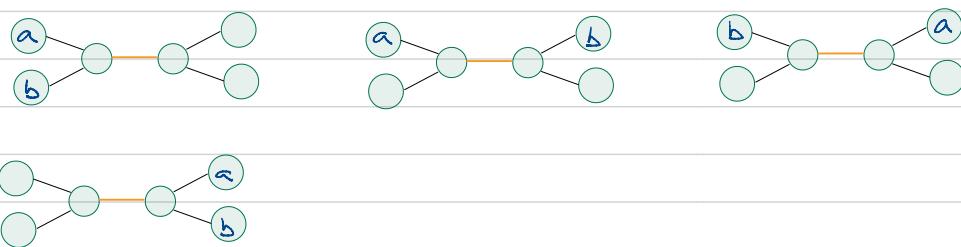
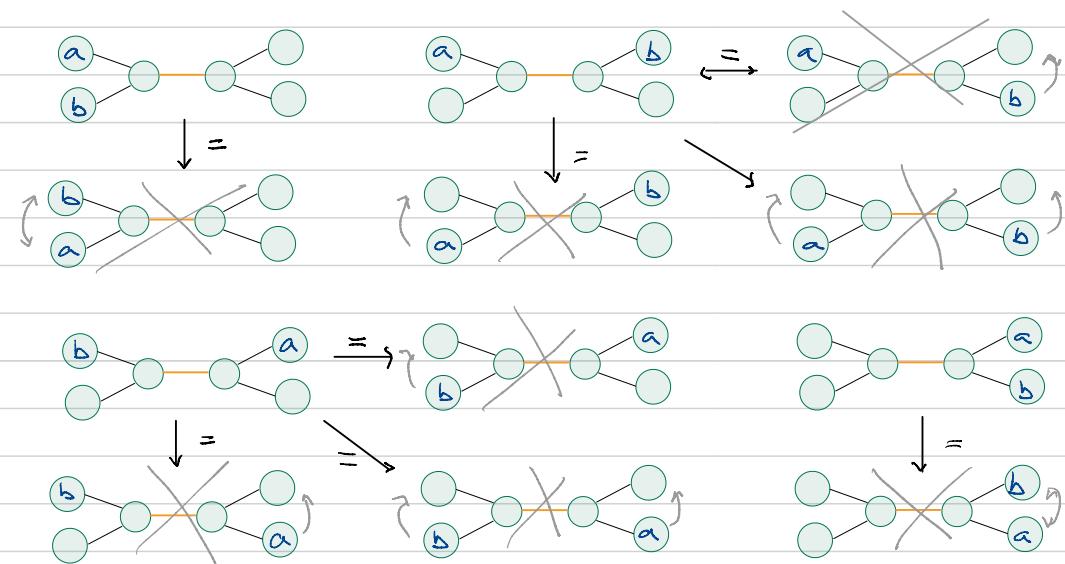


4) For each new topology repeat step 3 until all vertices have been attached

5) For each final topology choose all combinations of pairs of external nodes as the initial states. The remaining N nodes will be final states

- The procedure above is general, but it can lead to **duplicate diagrams**.

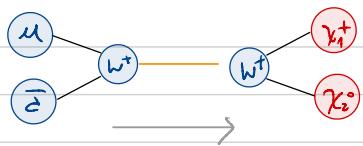
— Exemplo: $2 \rightarrow 2$



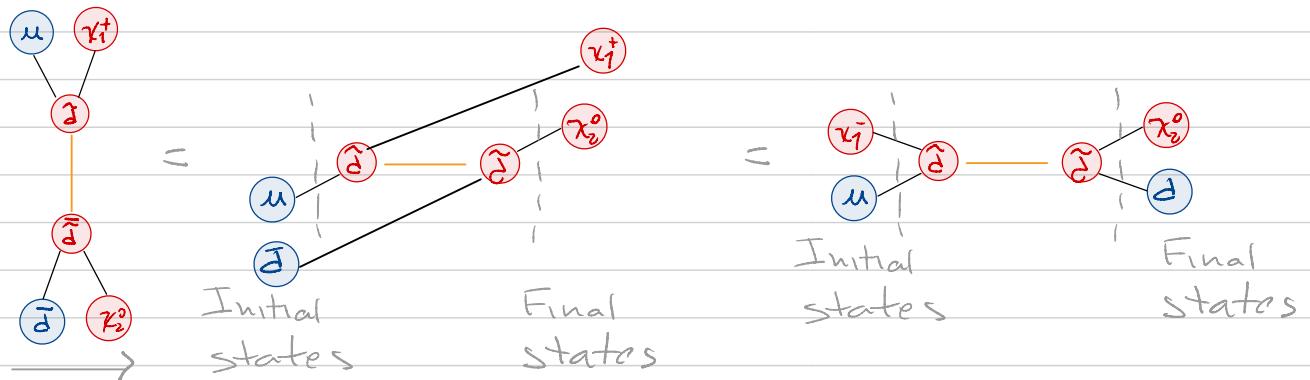
For $a, b \rightarrow x, y$ we should have:



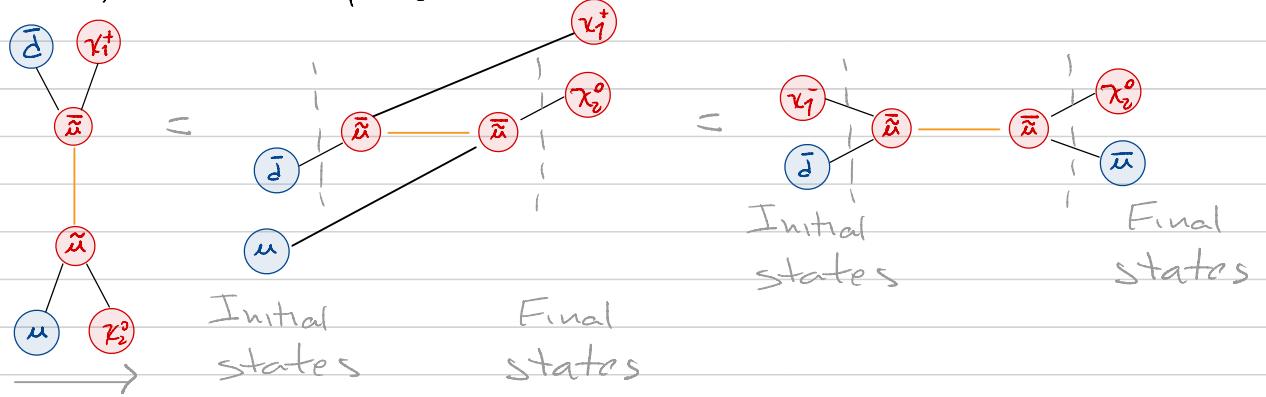
$$u, \bar{d} \rightarrow \tilde{\chi}_1^+, \tilde{\chi}_2^0$$



$$\rightarrow u, \tilde{\chi}_1^- \rightarrow d, \tilde{\chi}_2^0$$

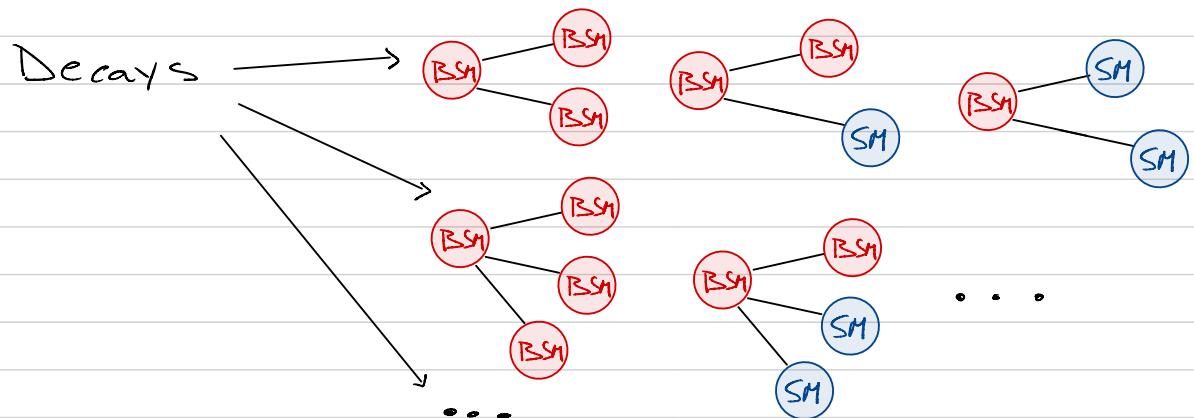
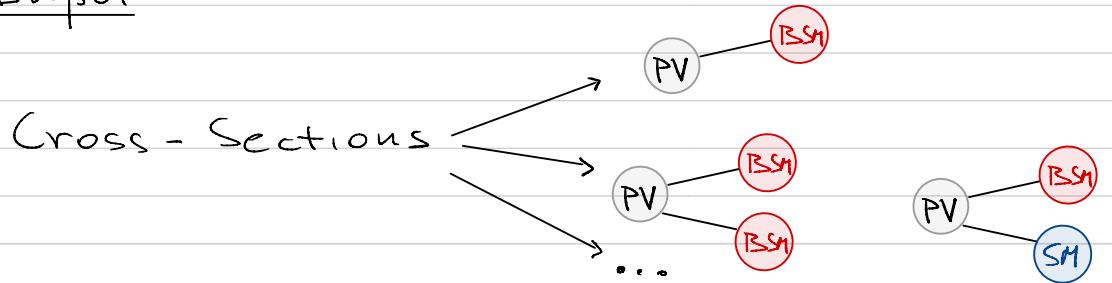


$$\rightarrow \bar{d}, \tilde{\chi}_1^- \rightarrow \bar{u}, \tilde{\chi}_2^0$$



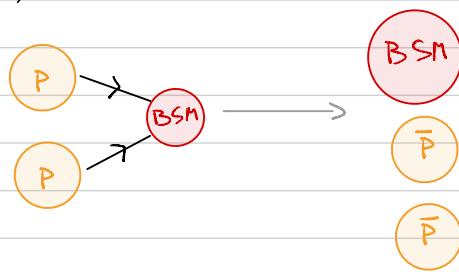
Creating Production Diagrams - S Models

- Input:



• Diagrams:

1) $Z \rightarrow 1$:

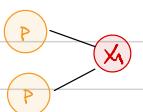


List of Vertices

Match

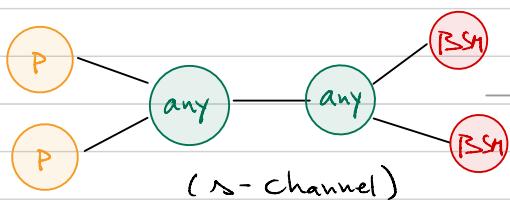
Matched Vertex
{
X-bar_1
P-bar}

Prod Graph



...

2) $Z \rightarrow 2$:



(\sim -channel)

List of Vertices

Match

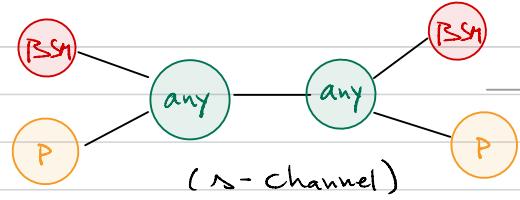
List of Vertices

...

ProdGraph



Matched Vertices



(\sim -channel)

List of Vertices

Match

List of Vertices

...

ProdGraph

