Ptolemy's table of chords

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Famous table of chord lengths according to Ptolemy's *Almagest* (e.g. 1515) converted into decimal values and calculated in comparison using the sine function, see Toomer (1984). Chord lengths l_0 are calculated according to *Ptolemy's theorem* (fig. 1) as the relation between four sides and two diagonals of a cyclic quadrilateral where

$$AC \cdot BD = AB \cdot CD + BC \cdot AD$$
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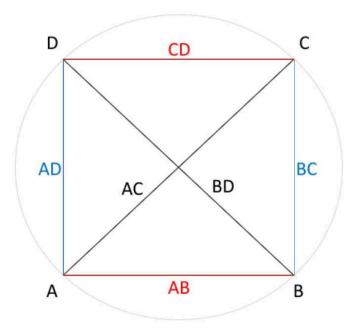


Figure 1: Cyclic quadrilateral.

Chord lengths l_0 (fig. 2) are expressed in fractional parts of sexagesimal numerals $x\ y\ z$. Decimal values l_1 are calculated as

$$l_1 = x + \frac{y}{60} + \frac{z}{60^2}.$$

Sixtieths is the average interpolation number to be added to lenght l_0 or l_1 each time angle increases by one minute of arc, that is n=30 times per half angle degree α .

Lengths l_2 to given arcus α and diameter d are calculated using the sine function where

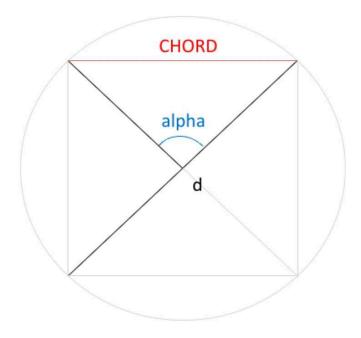


Figure 2: Chord length representation.

$$l_2 = d \cdot \sin \frac{\alpha \cdot \pi}{360}.$$

Differences diff show the difference between (1) sixtieth and arithmetical interpolation as well as the difference between (2) the calculation types of chord lengths l_1 and l_2 , see chords.md or chords.xlsx tables.

References

Ptolemaeus, C. (1515). Almagestum CL. Ptolemei Pheludiensis Alexandrini astronomorum principis opus ingens ac nobile omnes celoru motus continens. Felicibus astris eat in lucem ductu Petri Liechtenstein coloniensis germani ... Venetiis. https://doi.org/10.3931/e-rara-206

Toomer, G. J. (1984). *Ptolemy's Almagest*. Duckworth, London & Springer, New York. https://www.cambridge.org/core/journals/journal-of-hellenic-studies/article/abs/ptolemy-almagest-trans-and-ed-g-j-toomer