



ROYAL HOLLOWAY UNIVERSITY OF LONDON

PH4100: MAJOR PROJECT

# Meshing of Primitive Solids in Pyg4ometry & BDSIM

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## Abstract

The testing and analysis of radiation travelling through geometries of devices, such as a medical magnets, spacecraft or new particle accelerators, is often a very expensive and time consuming process. The open-source software packages Pyg4ometry & BDSIM are designed to enable scientists and people within in the industry to virtually simulate these tests, with accurate physics concepts. This project looks at improving the 3D simulation of the events and devices, by the remeshing of the basic primitive solids.

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# 1 Introduction

## 1.1 Report Structure

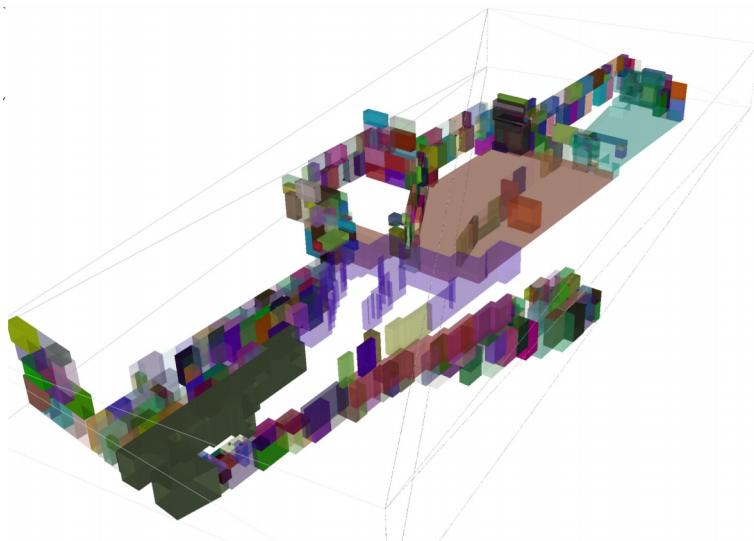
The subsequent Subsections of the introduction will go on to discuss the background (Section 1.2), motivations (Section 1.3) and aims (Section 1.4) of the project. Then following Sections are structured in the following way. First the software packages that are used and referenced throughout this report are discussed in Section 3, the concepts and details of the primitive meshing used in Pyg4ometry (Section 4). The interactions of meshed solids and objects in BDSIM (Section 5) and a conclusion and summary of the results of the report (Section 6). Followed by an Appendix A.1, which lists a variety of content produced in the project, but is not included in the report its self, in the interest of being incise.

## 1.2 Project Background - Applications of Particle Tracking

Radiation is the transport of energy through matter or a vacuum in the form of electromagnetic waves and/or particles. On Earth we experience harmless radiation everyday, such as small doses of UV (or Ultraviolet) radiation from the Sun. However in many cases radiation is unwanted and or needs to be controlled, which is where radiation tracking comes into play. The various types of radiation are discussed in Section 2. There is a large number of sectors that the simulation of particle radiation tracking is an invaluable tool.

### 1.2.1 High Energy Physics

The most obvious field which radiation tracking is important is all things nuclear and particle physics, i.e nuclear reactors, weapons and accelerators (accelerators being the main focus in this project), which all typically involve high energy physics. There are many types of radiation that need to be carefully taken into account in order to minimise damage to instruments and the people operating them. Particle accelerators work by accelerating charged particles up to high energies using electric fields and uses magnetic fields to steer a particles trajectory. The cost of construction and upgrades for accelerators and nuclear power plants are extremely high, therefore CAD (or Computer Aided Design) and simulations can be very helpful with the planning of new sites and concepts. Figure 1 shows a CAD model of the shielding used in a section of CERN (or The European Organization for Nuclear Research translated from French) home to the LHC (or Large Hadron Collider).



**Figure 1:** Converted CAD file (STEP to GDML) of the shielding at CERN East Area T8 and T11 test beam lines. Figure 4 from Source [4].

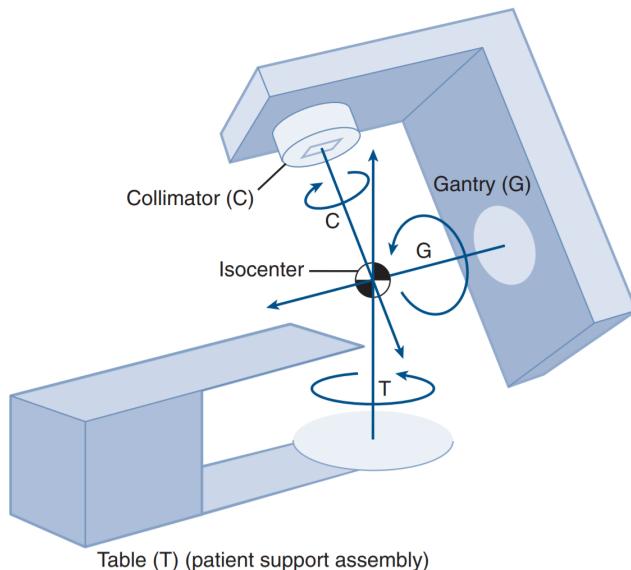
### 1.2.2 Space Exploration

Space exploration is also a large field in which radiation tracking and shielding is a key concept to consider. Beyond the Earth's atmosphere the Universe is full of GCR (or Galactic Cosmic Rays) radiation making the shielding of spacecraft and astronauts a major priority. Traditionally protection against unwanted radiation has involved placing an absorber in between the target and the source. However for the case of astronauts the size of the required absorber is extremely large and unpractical and will likely cause showers of more harmful secondary radiation. Therefore the use of magnetic fields is being investigated as a way to divert the charged electromagnetic radiation away from a target apposed to stopping it [2].

### 1.2.3 Medical

Another less obvious but essential field which radiation tracking is required in is medical treatment. X-ray radiation from vacuum tubes is not only used to check for fractures or breaks in bones it also used in radiotherapy. The X-rays are used to target unwanted growths in the body through small doses of harmful radiation, with the aim of removing cancerous tissue with minimum damage to the neighbouring organs. This can be especially difficult when the tumor is in the vicinity of organs that move within the body, such as the lungs. As the patient needs to breath in order to live, therefore the movement of the organs needs to be accounted for when aiming the particles.

A patients organs also move with the body's orientation with respect to gravity therefore the patient must positioned laying down on a table that rotates perpendicular to the direction of gravity. The accelerator unit must then rotate around the patient to imitate the most stationary conditions. An example machine can be seen in Figure 2, where patients would be placed on the table to undergo treatment by radiotherapy, the isocenter being the optimal target position of the cancerous cells to be within the patients body. A more recent type of radiotherapy that is proton therapy, which involves the use of small particle accelerators.



**Figure 2:** A diagram of a gantry-based radiation therapy machine. Figure 27.44 from Source [15].

## 1.3 Project Motivations

Historically it has been very hard to simulate particle radiation through matter correctly, being both expensive and time consuming. As computer technology has developed through recent years particle physicists have began building models to simulate these radiation events, employing techniques such as the Monte Carlo method. Currently many independent industries all require the ability to conduct

radiation tracking simulations, but work in different file formats, which is where one of the biggest problems lie. Many software tools for radiation tracking are format specific and require complex file conversions. Pyg4ometry is used a easy tool to convert between these representations ad allow a wider audience to utilise these radiation tracking softwares.

- allowing all industry formats to be used
- nuclear codes , fluka?
- other packages such as GUImesh do same thing

## 1.4 Project Aims

The aims of this project are to contribute towards the optimization of the Pyg4ometry package (Section 3.1) and subsequently BDSIM (Section 3.3), by improving parts of the code and conducting performance test to produce results that can be analysed. The main areas for improvement and where most of the computational energy in wasted, is in the meshing of the primitive Geant4 (Section 3.2) compatible solids. The inefficient computation is primarily due to the unnecessary use of boolean operations (Section 4.3.2).

The first part of the part of the project and report focuses on the meshing of the primitive solids. Discussing the comparison of methods and techniques used to make not only primitive solids, but also complex compound ones. The second part of the project focuses on the performance of the meshes within BDSIM. Investigating the effects of material and particle energy, on the duration of interactions within a solid.

## 2 Types of Radiation Emission

There are two main categories of radiation emission; ionising and non-ionising. Non-ionising (or NIR) can be harmful if exposed to for long periods of time or in high intensities, such as UV light can cause skin cancer or shining a strong laser into an eye can cause blindness. In order for a type of radiation to be ionising it must be an electromagnetic wave or particle with enough energy to "ionise" a neighbouring atom, typically travelling at a velocity greater than 1% the speed of light. "Ionisation" is the process of detaching an electron from an atom or molecule. This report only focuses on forms of ionising radiation as they are the ones more commonly associated with particle interactions.

Bremsstrahlung is the electromagnetic radiation, which is typically in the form of a photon, created as the result of a charged particle decelerating after it has been deflected from another charged particle. The larger the loss in kinetic energy, i.e the greater the deceleration of the initial particle, the larger the frequency of the emitted photon. Medical X-ray tubes rely on Bremsstrahlung to create a continuously emitted spectrum. The X-ray tubes work by using an electric field to accelerate electrons within a vacuum, which is then aimed towards a target, such as a broken arm against a photographic absorber.

Cherenkov radiation is important within nuclear reactors and is the reason why submerged reactors often appear to glow blue. The blue colour this is due to the radiating particles traveling faster than the speed of light in the same medium, acting in the same fashion as a sonic boom. Thus causing a continuous moving source of radiation in the visible spectrum. The blue colour is very faint and can only really appear at high energies, such as the ones found in nuclear reactors.

Nuclear fission relies on the ionising radiation of free neutrons, which can then go on to trigger a further neutron to be emitted from a new isotope. Only appears in matter

### 3 Software Packages

This section goes through each package of software related to and used throughout the duration of the project. It outlines the key details of each package, describing its function and link to the project. At the time of the project a lot of the prerequisite packages were only compatible with Linux systems. Due to owning a machine that operated on windows, a lot of time was initially spent setting up virtual machines running Centos 7 (standard free Linux used by CERN [1]). However despite getting it setup, the packages were not performing nearly as well as they were on the fellow Apple MacBooks. Therefore for the main duration of project, a Linux laptop was loaned out from the particle physics department of Royal Holloway (a 2011 Apple MacBook Pro running OS El Capitan). This legacy operating system came pre-installed with the some of the required packages, and allowed for easy installation of outstanding backdated versions.

#### 3.1 Pyg4ometry

Pyg4ometry is an open-source Python package written by the John Adams Institute (JAI) [3], its purpose is to convert 3D CAD (Computer Aided Design) models between different representations to allow compatibility with BDSIM for the testing of new concepts [4]. The “4” in “Pyg4ometry” comes from the consistency the package has with Geant4 (Section 3.2). The package is a key tool for allowing multiple file formats, such as STEP/STL files to be converted into GDML files, which are then compatible with BDSIM. GDML (Geometry Description Markup Language) is a format based on XML files. This increases the number of people who can utilise the package, as many people within in the industry use different file formats to store 3D CAD models..

Most of the development in this project is conducted in Pyg4ometry and managed using an online bitbucket code repository [5] in combination with Sourcetree [8] (An open-source git management GUI). The package is currently written in and only supports Python 2.7, however as of January 2020 support for Python 2 has been discontinued as the newer version Python 3 is taking over. The transition to Python 3 means adjusting the syntax of several functions and files in Pyg4ometry, this has began, but a full transition will take sometime as it is not an immediate priority.

#### 3.2 Geant4

Geant4 (or GEometry ANd Tracking) is a software developed in C++ for the simulation and tracking of particles traveling through matter. The package is used by many particle physicists and is one of the more popular packages for handling the geometry within interactions. Geant4 has its own preset solids that are used for simulating particle interactions. For ease of conversion between file formats Pyg4ometry uses the same conventions when meshing its primitive solids. Geant4 has a large inbuilt database which contains the properties of most materials and particles.

The materials used in Pyg4ometry and throughout this project are also from the Geant4 database [10]. In this report the three main materials used are *G4\_Fe*, *G4\_Ti* and *G4\_Galactic* (Iron,Titanium and Vacuum). The use of *G4\_Galactic* is arguably the most important as it is used to set the material of the world environment in with other objects are placed into. By default the world material in BDSIM is set to be air, which means the particles would interact before passing into the object being tested, this was avoided by using the option *worldMaterial = “G4\_Galactic”* within the GMAD files. Other properties for each Geant4 material are also used in this project, such as the stopping power (Section 5.3.1).

#### 3.3 BDSIM

BDSIM (or Beam Delivery SIMulation) is an open-source software package also written by JAI, for the use of modelling particle beam interactions. BDSIM has many applications, such as modelling complex particle accelerators like the LHC (Large Hadron Collider) or concepts magnets for medical scanners

used to treat tumours. The package allows a user to specify the physics being used for a particular particle interaction, such as the particle energy and the number of secondaries produced. The scattering of the particle trajectories and decays are computed using Monte Carlo simulations, to make the results as consistent with experimental results as possible. The software outputs a full analysis of each run, and can even allow multiple runs to execute at once (batch mode).

### 3.3.1 Pybdsim

BDSIM has a Python library called Pybdsim which allows interactions to be run and analysed using Python scripts. This is how all the plots in Section 4 are generated. Pybdsim also allows for the navigation of ROOT analysis files to extract data to plot, mentioned more in Section 3.4.

## 3.4 ROOT

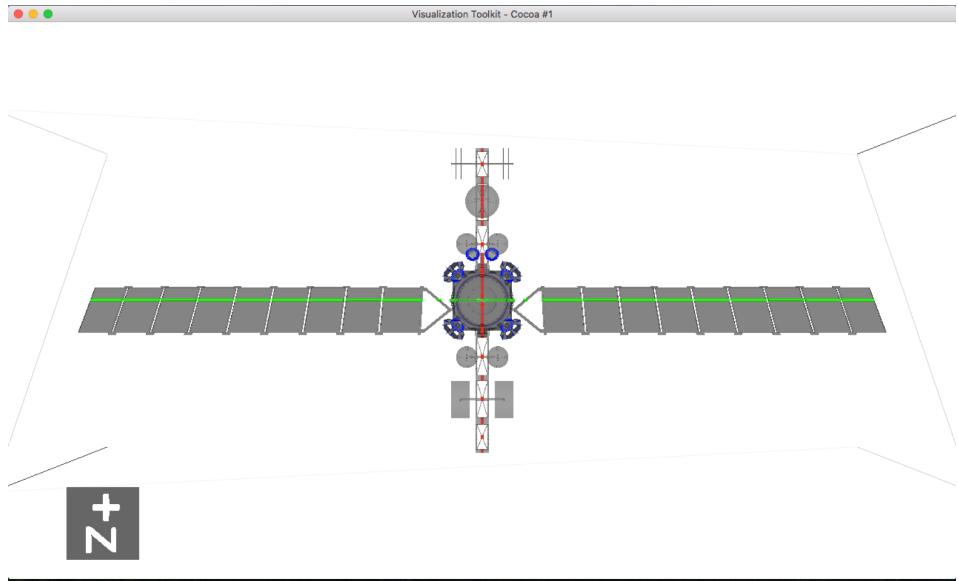
Surprisingly ROOT is not an acronym and is named after the idea that it is a system for other system to grow off of, much like the roots of a tree that has many branches. ROOT is adopted by many physics communities such as CERN [1], where it was first written. Naturally making it a popular format for particle physicists in particular and is the why it is the default output for analysis by BDSIM. ROOT has its own GUI for file browsing due to the nature of its formatting. Despite ROOT generating its own plots, no ROOT files or plots are shown in the report, as the data has been extracted from the root files and been replotted using Python and Matplotlib (library for creating publication grade figures).

## 3.5 Freecad (Libraries)

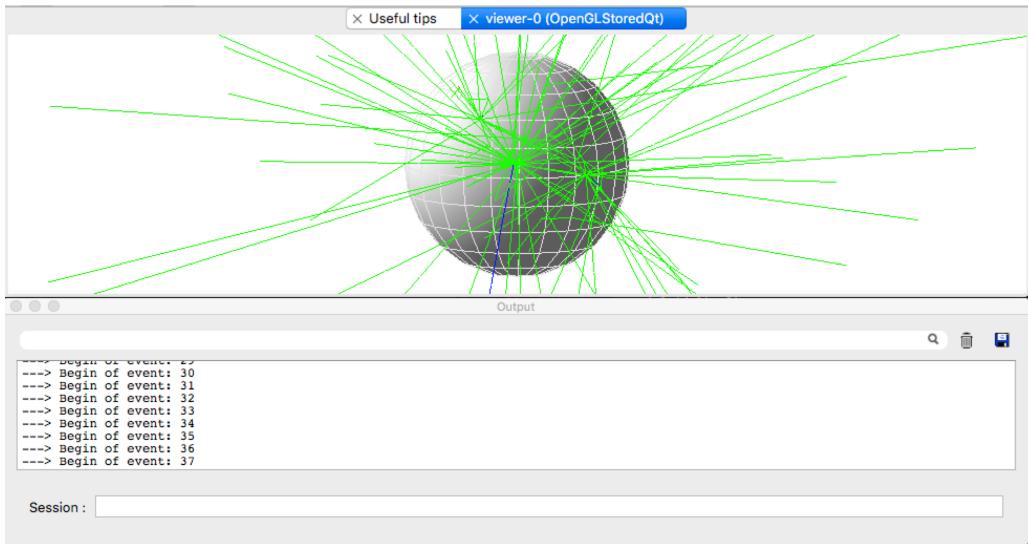
In this report the libraries from Freecad 0.18 ?? are used directly within Pyg4ometry (Section 3.1), without the use of the Freecad GUI. The libraries are used to import STEP (Standard for The Exchange of Product data) files and to convert them into a tessellated meshed solids, that can then be written out as a GDML file. As an exercise at the beginning of the project a few example CAD STEP files were downloaded from the internet and converted into meshed GDML files. One of the CAD models converted was a space satellite, which can be seen in Figure 3. Freecad itself can also be used to create CAD models that can then be tested in BDSIM, example magnet shown in Appendix D.

## 3.6 Visualisation

Most of the packages mentioned above have their own GUI's to visualise the meshed objects. However the only two used in this project are the ones connected with Pyg4ometry and BDSIM. Pyg4ometry uses VTK (or Visualization ToolKit), shown in Figure 3, to create its GUI's and BDSIM uses Geant4's GUI (as seen in Figure 4), which is another reason Pyg4ometry aims to be consistent with Geant4. Both the VTK and Geant4 GUI's allow meshed solids to be viewed as solids or as meshed structures. The Geant4 GUI has its own console in which commands can be carried out, allowing interactions to be altered from within the GUI as well as by Pybdsim.



**Figure 3:** STEP file of a space satellite imported into Pyg4ometry using the Freecad libraries and viewed in VTK.



**Figure 4:** BDSIM GUI screenshot of particle interaction and output window, using a Geant4 sphere with 10,000 1.3 GeV neutrons.

## 4 Primitive Meshing

This section will describe the work done to optimize the Python scripts that generate the three dimensional meshings for the primitive solids within the Pyg4ometry package (Section 3.1). All the primitive solids used are constructed such that they are compatible with Geant4’s solids. It was previously thought that it would be best to use purely triangular based meshes in combination with boolean operations (Section 4.3.2) to construct the 3D solids. As a triangle is the shape which has the minimum amount of points needed to define a face with containing an area, as well as always being on a single plane. However it had been realised that the computation of triangles and boolean operations in most cases is much more intensive and inefficient, compared with polygons and adapted trigonometry. In particular with the curved solids, i.e circular and elliptical based solids, due to the boolean operations generating more complicated meshes. Thus the first part of the major project was to rewrite the meshing scripts for all the curved primitive solids.

One of the major improvements to the Pyg4ometry meshing scripts was in the computation of cut

up primitive solids. The meshing of hollow or sliced solids were previously constructed by boolean subtractions and intersections, which involves using two or more separate solids and operating on them to create a final single solid. Discussed more in Section 4.3.2. Which resulted in a very computationally heavy and less aesthetic outcome, where the mesh lines (“slice and stack”), were not meshed in radial directions.

## 4.1 Co-ordinate Systems

The various primitive solids are all constructed by using the predefined parameters used by Geant4, to be consistent with Geant4’s own convention for solids. The parameters defining a 3D solid are properties relating to the co-ordinate system that the solid is constructed within, such as height or radius. The parameters are then used to generate points on the object via basic trigonometry, which can then be used as vertexes to define faces on the given solid. The number of faces and subsequently the number of points defines the mesh density. The order in which the points are appended is also very important and is detailed in Section 4.2.

```

1 def pycsgmesh( nslice , nstack , *args , **kwargs ):

3     # ...
5
6     polygons = []
7
8     for j0  in  range( nslice ):
9         j1 = j0
10        j2 = j0 + 1
11
12        vertices = []
13
14        for i0  in  range( nstack ):
15            i1 = i0
16            i2 = i0 + 1
17
18        #.....
19
20        return mesh

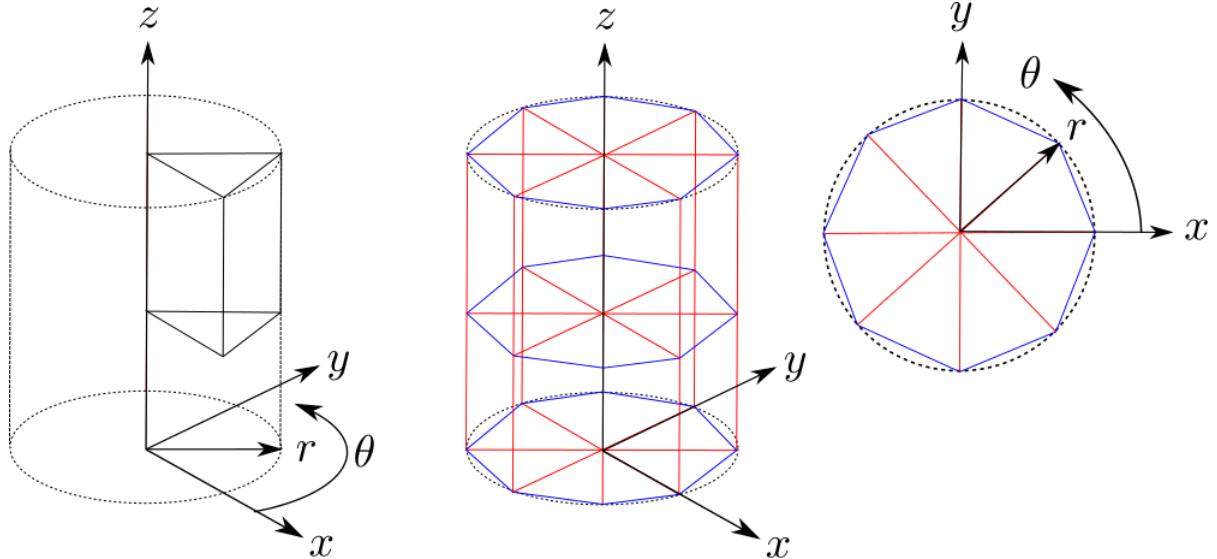
```

**Listing 1:** Basic Python script structure for new meshing of primitive solid in Pyg4ometry.

The Python meshing scripts for all co-ordinate systems follow a similar structure, using a `pycsgmesh()` function, the beginning of which can be seen in Listing 1. The “CSG” in “pycsg” stands for Constructive Solid Geometry, which is a modeling technique that uses Boolean operations to construct 3D solids. The script works by first defining an empty list of faces (polygons) and then running the associated trigonometric equations through a number of loops to generate and append polygons to that list. The number of loops is associated with the number of sections a surface of a solid is being split up into in a given co-ordinate system (“nslice” & “nstack” in Listing 1). The density of the meshing is defined by a user inputted number of slices and stacks, of which the orientations vary with co-ordinate system. The slice and stack used by the new meshing scripts for the solids in the cylindrical polar co-ordinate system is demonstrated in Figures 5, 8 & 9.

#### 4.1.1 Cylindrical Polar Co-ordinate System

In the cylindrical polar co-ordinate system the loops create 3 or 4 points at a time using an adaptation to the trigonometry in Equations 1, which can then be defined as a triangular or quadrilateral face. The only cases where the new meshing produces triangles is at the top and bottom faces of the cylinder. These cases are only true provided the solid does not have a minimum radius equal to zero (creating a tube or cone). The same logic for the triangular faces is identical to that of the quadrilateral, just using 3 vertex points to make a face.



**Figure 5:** A diagram showing the meshing method for a cylindrical polar co-ordinate system, where the red lines indicate the slices (8) and the blue indicate the stacks (2). The diagram was drawn using the CAD software Inkscape.

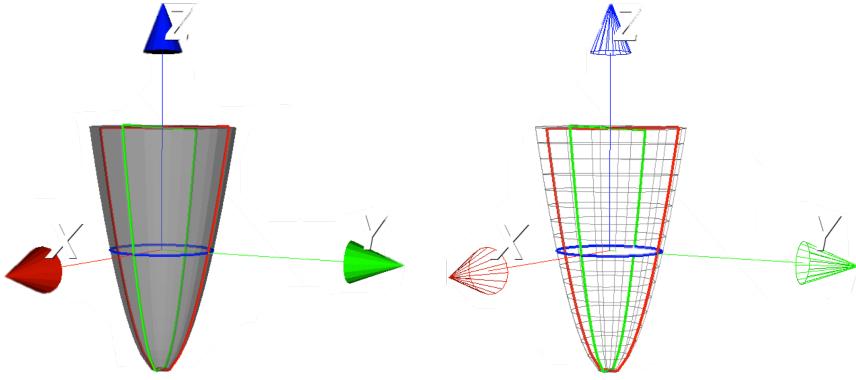
The trigonometry that converts the points from cylindrical polar co-ordinates to Cartesian, are:

$$\begin{aligned} x &= r \cos \theta \\ y &= r \sin \theta \\ z &= z \end{aligned} \tag{1}$$

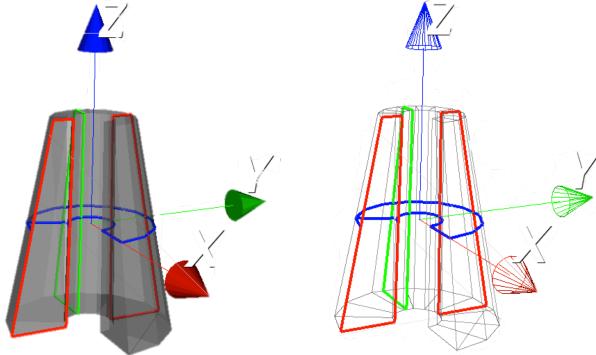
The only time a stack is needed in the cylindrical co-ordinate system is when the solid has a non-linear function in the r-z plane. For example a paraboloid (Figure 6) would need a stack, but a linear cone (Figure 7) would not. This is due to the fact how that a plane can not represent a curved surface with a singular face.

#### 4.1.2 Spherical Co-ordinate System

The meshing for the primitive solids in spherical co-ordinate systems are constructed by similar means the that of the cylindrical. Just with different trigonometric equations (Equations 2) as a result of



**Figure 6:** A VTK screenshot of a paraboloid constructed with the meshing method in cylindrical polar co-ordinate system, where the red lines indicate the points residing on the  $x=0$  plane, the blue lines indicate points on the  $z=0$  plane and green lines indicate points on the  $y=0$  plane.



**Figure 7:** A VTK screenshot of Cons constructed with the meshing method in cylindrical polar co-ordinate system, where the red lines indicate the points residing on the  $x=0$  plane, the blue lines indicate points on the  $z=0$  plane and green lines indicate points on the  $y=0$  plane.

two angle parameters  $\phi$  and  $\theta$ . The stack (blue) and slice (red) for solids in the spherical co-ordinate system works in the same way as the longitudinal and latitudinal mapping on a globe, shown in Figure 8.

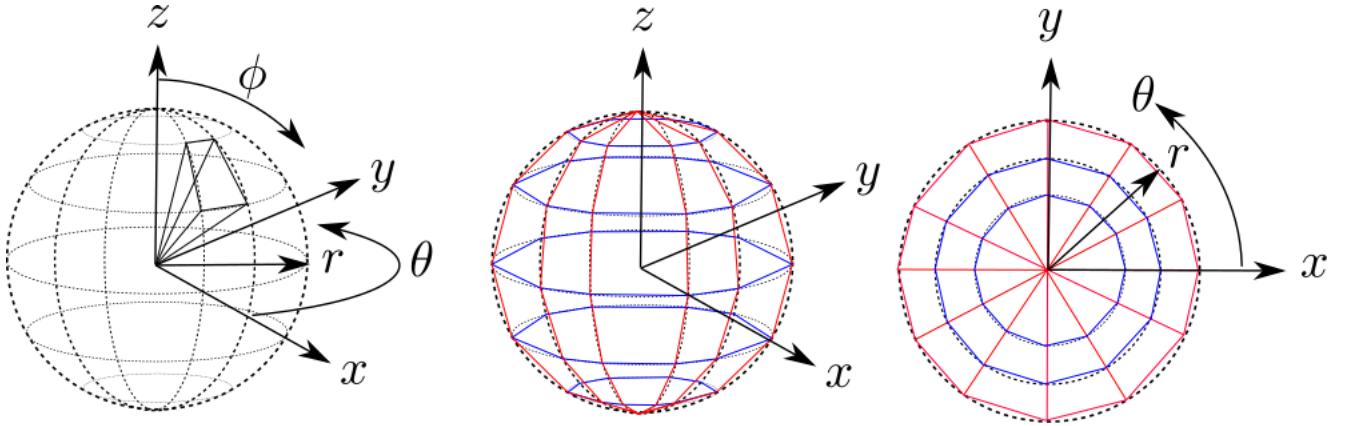
The trigonometry that converts the points from spherical co-ordinates to Cartesian, are:

$$\begin{aligned} x &= r \cos \theta \sin \phi \\ y &= r \sin \theta \sin \phi \\ z &= z \end{aligned} \tag{2}$$

The structure of the code for a spherical system is the same as used in Listing 1. The only time triangles are constructed in the spherical co-ordinate system is if a complete pole exists at the top or bottom of the solid. The solids constructed in the spherical always have both a stack and a slice.

#### 4.1.3 Toroidal Co-ordinate System

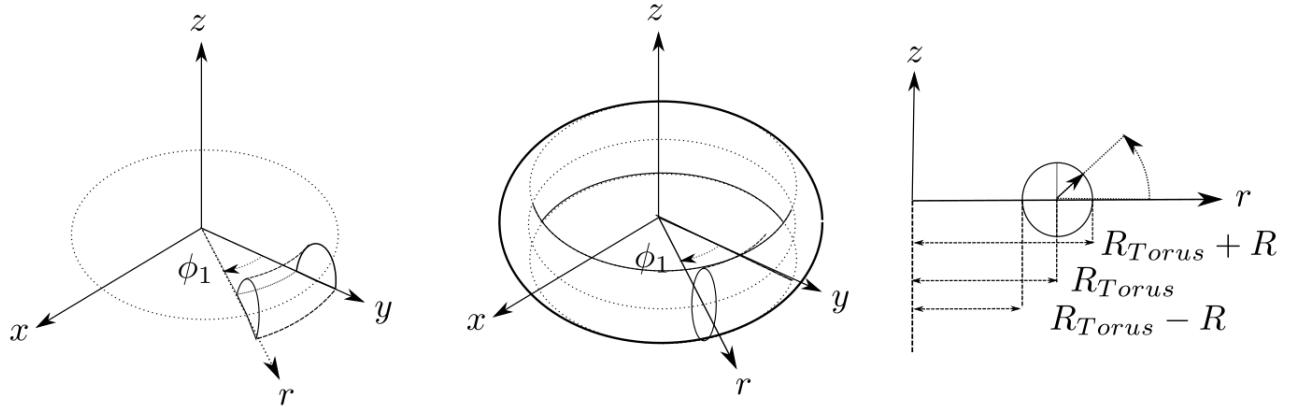
The toroidal co-ordinate system is a special case and is only needed, for toroidal based solids. The stack and slice for a toroidal shape is much harder to visualise, due to the fact it is a rotating co-ordinate system. A toroidal slice is an  $R_{Torus}$  radial cut taken out of the angle  $\phi$  and a toroidal stack is a  $R$  radial cut out of the angle  $\theta$ , where the angles and radii are displayed in Figure 9.



**Figure 8:** A diagram showing the meshing method for a spherical co-ordinate system, where the red lines indicate the slices (12) and the blue indicate the stacks (6). The diagram was drawn using the CAD software Inkscape.

The trigonometry that converts the points from toroidal co-ordinates to Cartesian, are:

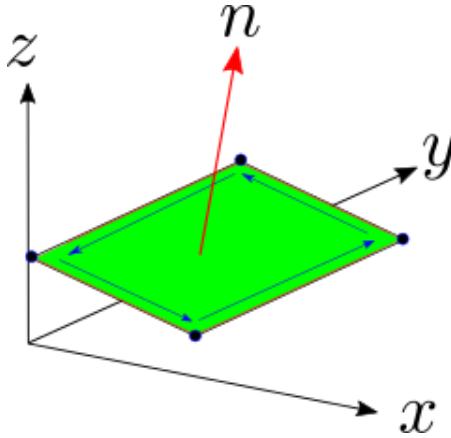
$$\begin{aligned} x &= R_{Torus} + R \cos \theta \cos \phi \\ y &= R_{Torus} + R \cos \theta \sin \phi \\ z &= R \sin \theta \end{aligned} \quad (3)$$



**Figure 9:** Diagram showing the meshing method for a toroidal co-ordinate system. Diagram drawn using the CAD software Inkscape.

## 4.2 Plane Direction

One key thing to be taken into account is the convention being used throughout the meshing scripts is the order in which points are appended to define a plane, i.e to define a face on a solid. This is important as the direction the normal of the plane points in, dictates whether a face is considered an inside or outside face on the given solid. Getting this order incorrect, will lead to missing faces, when the meshing is made.



**Figure 10:** A diagram showing the order convention of appending points to define the normal to a plane. The diagram was drawn using the CAD software Inkscape.

The convention is that the normal to a plane points away from the solids surface, making it an exterior face. The normal is in the  $z$  direction to a plane residing on  $z=0$ , if the points are appended anticlockwise in the  $x$ - $y$  plane. For points appending in the other direction (clockwise in the  $x$ - $y$  plane), the normal would be in the  $-z$  direction, making an interior face. The concept is shown in Figure 10.

The simplest way to test this is by performing boolean operations with a solid box, as the boolean operation will only work correctly if all the planes are correct on both shapes. This test only works for the visualiser in BDSIM as it uses Geant4, which displays face directions. VTK inside Pyg4ometry is a much more lenient visualiser and will display solids even if their normals are incorrect, giving you a false perspective of what is being displayed.

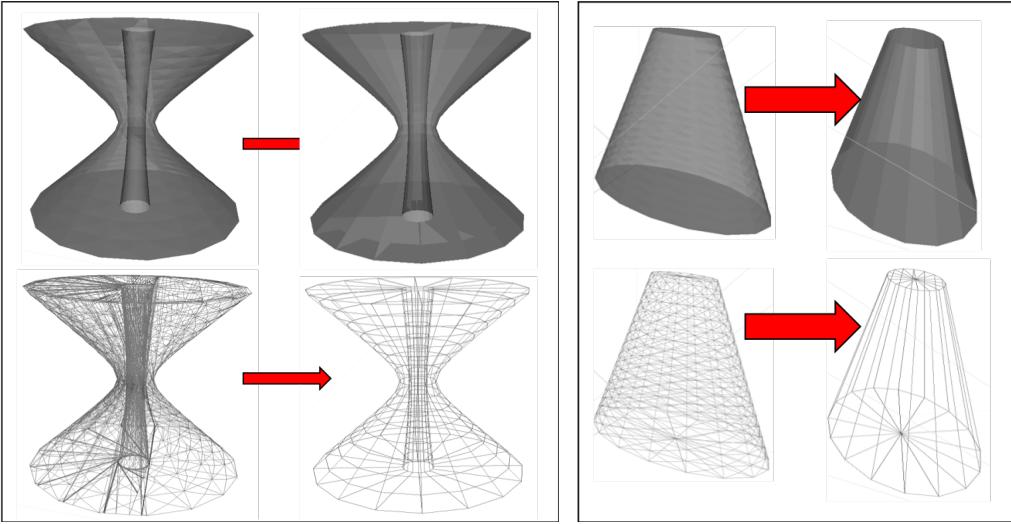
### 4.3 New Meshing of Curved Primitive Solids

In total there are 12 curved primitive solids, of which many of the examples and concepts are very similar. Therefore only a few select solids will be discussed in this section, but the remaining solids and their development can all be viewed in Appendix B. The naming convention of the solids being used in this project and within this report are the ones used by Geant4.

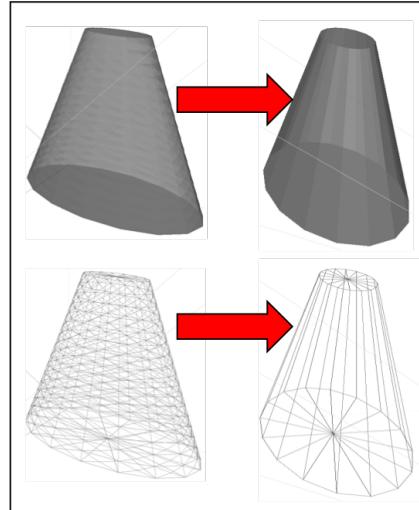
One of the curved solids for which the meshing was rewritten is the hyperboloid, the old and new meshing structures of the hyperboloid is shown in Figure 11. It can be seen that in this example the meshing at the top and bottom faces becomes more radially uniform. This is due to the replacement of boolean subtractions with simple trigonometry within the new meshing algorithm for the polycone.

Another curved solid that was remeshed is the ellipticalcone, as seen in Figure 12. Despite having no boolean operations to generate this solid, the meshing is still improved by replacing all the unnecessary triangular faces with quadrilateral ones. For the ellipticalcone it was also possible for the stack to be removed, as for a cone the faces in the  $r$ - $z$  plane (in cylindrical co-ordinates) are a linear function.

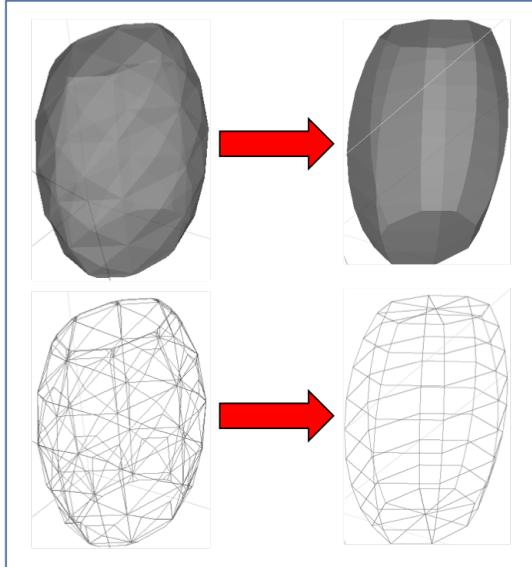
A feature that is also removed by the transition to the new meshing algorithms is the "grenade like" texture seen on the surfaces of the curved solids. The clearest example being the ellipsoid, shown in Figure 13, where it can be seen that the surface of the solid has not only become triangulated but also has a contour. This is due to the old mesh would tend to use quadrilateral faces but replace them with quadrilateral based pyramids to better estimate a true curve solid. This was done by rotating every other stack to be out of phase when appending vertexes. Despite this improving the mesh accuracy, it was removed as when you increase the orders of stack and slice to high enough orders the difference is negligible and is not worth the extra computation.



**Figure 11:** VTK screenshots of hyperboloid meshing Development (Solid & Mesh View)



**Figure 12:** VTK screenshots of ellipticalcone meshing Development (Solid & Mesh View)



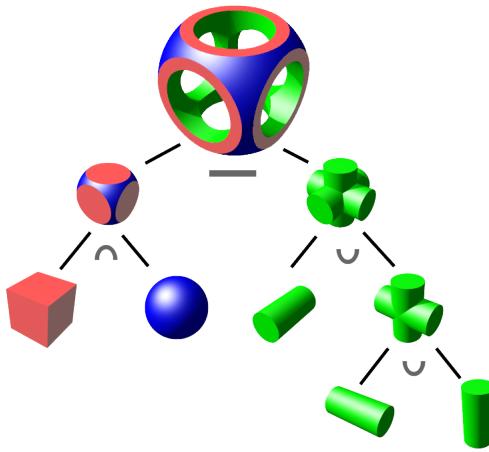
**Figure 13:** VTK screenshots of ellipsoid meshing Development (Solid & Mesh View)

#### 4.3.1 Degenerate Points

Degenerate points are another common mistake which can cause missing faces to occur, due to creating a face with null area. Multiple meshing points occupying the same point in space can spring a few errors, sometimes without entirely crashing the meshing script, making it a potentially hard error to identify. It is typically given away when a *DivisionByZero* error occurs, within the pycsg meshing of a solid. You can identify whether this is the error by debugging each polygon and triangle in a mesh, looking out for a face that has two or more vertices with the same  $(x, y, z)$  coordinates. This typically happens when you intend to mesh a triangle, but are still using the format for meshing a quadrilateral face. Or it can be due to the incorrect choice of an incorrect stack and slice iteration when constructing a face, as mentioned before in Section 4.1.

#### 4.3.2 Boolean Operations

One of the largest improvements to the performance of the new meshing methods compared with the previous methods, is the discarding of boolean operations in order to create hollow or cut-up primitive solids. The idea can be clearly seen in Figure 14, where you conduct basic operations on simple solids,

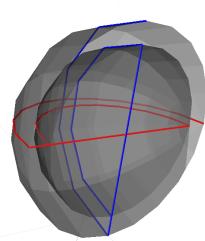


**Figure 14:** An example CSG showing the basic method of constructing a more complicated 3D solid out of boolean operations with simpler primitive solids.

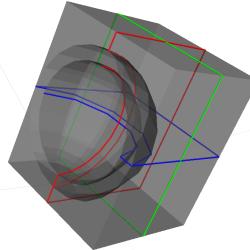
Where - = Boolean Subtraction, n = Boolean Intersection, u = Boolean Unions.

resulting in a more complex solid being made.

Figures 15 & 16 are of the meshed boolean union and subtraction of a solid box with a hollow sphere (in solid view). The coloured lines are representing the perpendicular planes to the axes in which the final object is placed in. These were made in the process of checking the normals before passing them into BDSIM to undergo particle interactions.



**Figure 15:** Example screenshot of a Boolean Union produced in Pyg4ometry & viewed in VTK.

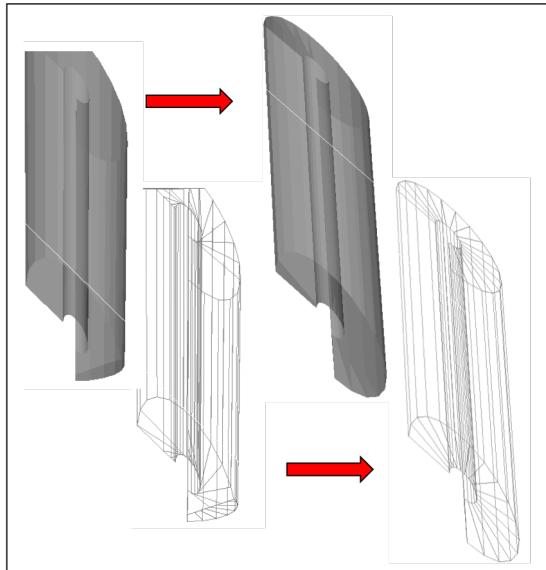


**Figure 16:** Example screenshot of a Boolean Subtraction produced in Pyg4ometry & viewed in VTK.

The old meshing algorithms heavily relied on these operations, using intersections to slice solids and subtractions to make solids hollow or cut-up. For example CutTubs, as seen in Figure 17, is made from two cylinders and a rotated Box, first the two cylinders were subtracted from one another, creating regular Tubs (as seen in Appendix Figure 42). The hollowed out cylinder was then intersected with the tilted box to create angled tips. This has now all been replaced with clean trigonometry.

The appearance of the mesh structure itself is also affected by the use of boolean operations, the boolean operations worked by trying to identify common mesh points then remesh. This created a lot of non-radially uniform mesh sections as seen in solids such as the hyperboloid, mentioned before in Figure 11, in which the new meshing algorithm outputs clean radial faces at for the top and bottom sides of the solid.

In summary As proven by the above examples the boolean operations worked, however are very computationally heavy compared with that of the adapted trigonometry that is implemented in the new method. This is the case especially when one or more of the orginal solids is curved in structure.



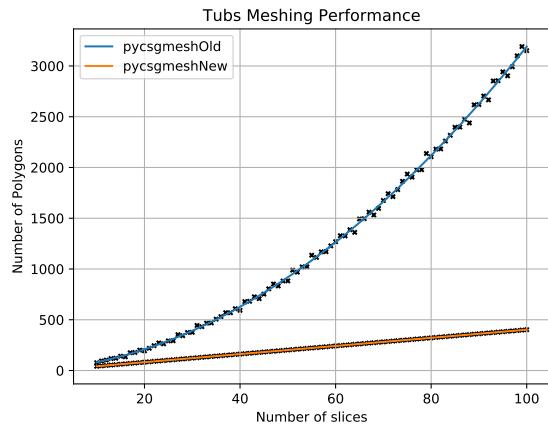
**Figure 17:** VTK screenshots of CutTubs meshing Development (Solid & Mesh View)

## 4.4 Meshing Performance Testing

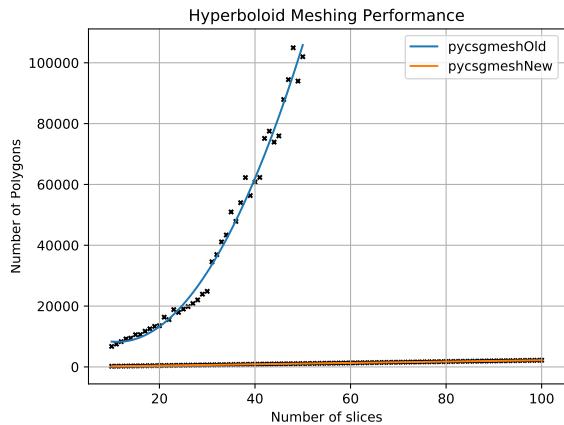
### 4.4.1 Polygon Count

One way in which the meshing performance of the Pyg4ometry primitive solids was tested, was by counting the number of polygons produced by both the old and new meshing algorithms. I.e counting the number of triangular and quadrangular faces on a solid, in order to make a comparison. A plot for each primitive solid counting its number of generated polygons was produced.

They were generated by varying the user input for the number of slices across a range. Most were put through the range of (10-100) slices, whilst keeping the number of stacks at a constant 10. However a few of old meshing scripts took too long to execute at higher mesh densities. Leading to a few solids only being measured across a shorter range of slices e.g the old Hyperboloid pycsgmesh() function was left to run for a duration of over 2 hours and only collected data up to a slice of 50, shown in Figure 19.



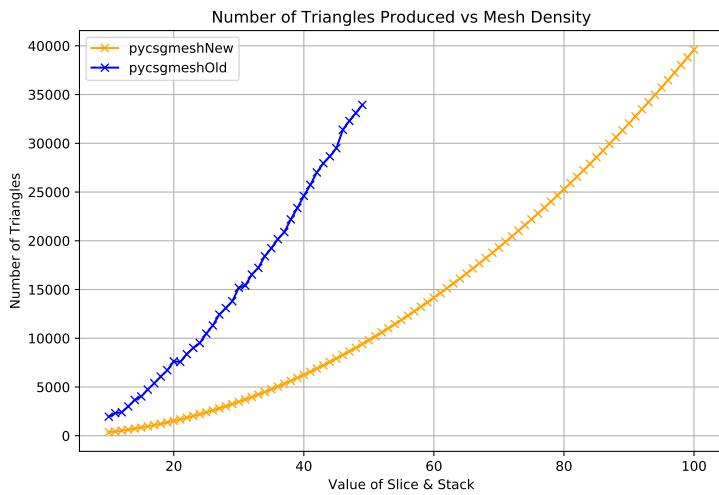
**Figure 18:** A plot showing the comparison of the number of polygons (and triangles) generated by the new and old meshing methods, across a range of slices 10-100.



**Figure 19:** A plot showing the comparison of the number of polygons (and triangles) generated by the new and old meshing methods, across a range of slices 10-100.

Figures 18 & 19 are two of many plots, which are all displayed in the Appendix B. As you can see in both Figures, the new meshing function is much more computationally reduced compared with the old meshing functions, generating far less faces per slice and stack. The number of polygons increases more uniformly and linearly for the new pycsgmesh() function. On the hand the old pycsgmesh() function exhibits a more scattered and quadratic relationship, due to the boolean operations. This is also confirmed by the values tabled in the Appendix 4, which contains the quadratic fitting parameters to all the polygon count plots. If you extrapolated both graphs it is clear than the new mesh is not only improving the structural appearance of the meshed solids, but also saving large amounts of computational power and time.

The next section goes on the test spheres of varying slice and stack within BDSIM. Figure 20 shows the total number of triangles on the interior and exterior surfaces for a given slice and stack equal to the same value on a G4\_W sphere. The old meshing would only meshed up to a maximum resolution of slice and stack equalling 48, before it would max out Pythons recursion limit. Where as the new meshing could go to 100 stack, 100 slice with out any issues at all.

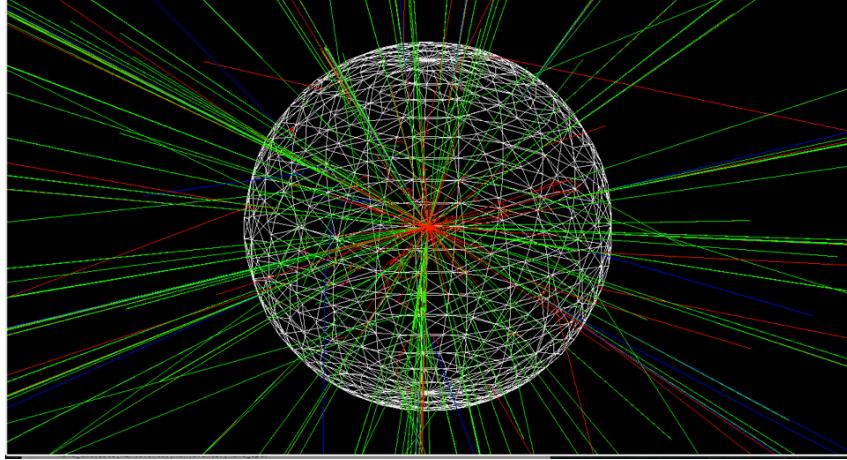


**Figure 20:** TODO

It can be seen that in Figure 20 the new pycsgmesh() function has a much smooth gradient and that the old function has small peaks occurring at certain intervals of stack and slice. This is most likely to do with the boolean subtractions of the spheres favouring the old mesh at particular densities.

## 5 BDSIM Interactions

The second aim of this project was to measure how the physics is altered, between the new and old meshings as the mesh density is varied. As mentioned before Geant4 already has its own set of primitive solids, which can be used as a guideline for comparison, due to no slice and stack dependence. The physics being measured will be features such as the trajectories and energy deposition, through solids. BDSIM uses the colour convention for representing a particles charge from Geant4, green is neutral, blue is positive and red is negative. Figure 21 shows a spherical distribution of 100 1.3 GeV electrons radiating outwards from the centre of a G4\_Ti sphere, where it can be seen that red electrons and many green neutron secondaries are produced. A secondary particle is anything that is produced as a result of the initial particles interacting with the solid, therefore a secondary itself can produce another particle which is considered to also be a secondary particle. The Monte Carlo simulation in BDSIM uses a numbering system for storing particles, assigning each particle a unique number for ease of identifying what happens in a set interaction. The numbering system adopted in BDSIM is the one created by PDG (or the Particle Data Group) [12], which is an international collaboration dedicated to analysing and publishing the properties of particles.



**Figure 21:** A BDSIM screenshot of a G4\_W Geant4 Sphere generated with new meshing interacting with 1.3 GeV electrons.

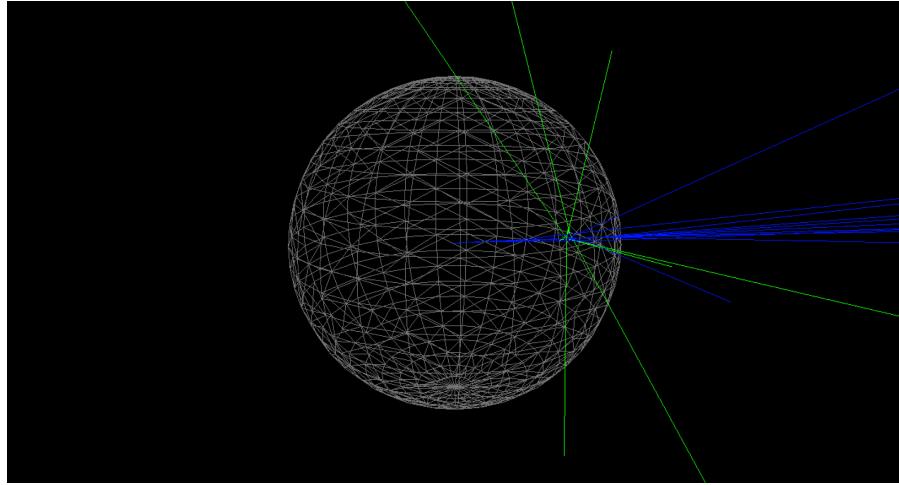
## 5.1 Monte Carlo Simulation

The probability of certain particle interactions occurring in a given BDSIM event, such as the decays or scattering of a particles trajectories is generated by a Monte Carlo simulation. The basic principle behind the Monte Carlo algorithms is the use of large random sampling to find numerical results. This is perfect for simulating the probabilities of particular particle interactions happening, as two initially identical interaction setups can have two non identical interactions, with a given probability. Each event in BDSIM is associated with a specific seed number produced via this Monte Carlo method. The uniqueness of each seed allows a particular event to be repeatedly simulated under the same physics conditions, which is key to this project when it comes to comparing the interactions of different objects fairly. The other properties of the particle and physics processes that may occur can also be user defined to tweak the experiment. Properties such as the particles initial energy, whether secondaries get produced and much more. The seeds used in this project could not be logically chosen due to the fact they are generated via the Monte Carlo simulation. Therefore they were selected by running a lot of test runs in BDSIM to see which seeds generate a decent amount of secondaries.

BDSIM works by running a GMAD file and then outputs a ROOT (Section 3.4) file with the option of using the GUI, allows the user to visualise the interactions in an interactive 3D environment. A GMAD file contains the basic information needed to produce an interaction in BDSIM, i.e a particle and path to file of the target object (Typically of the format GDML). The option “physicsList” defines the physics which is used for the interaction, for the project the option was set to “g4FTFP\_BERT”, which contains all the standard electromagnetism and particle physics required for this project. The ROOT file contains a detailed analysis of the interaction. One of the elements analysed within this project is the CPU duration time distribution of an interaction in BDSIM.

The shape chosen to be tested within BDSIM for this project was the sphere, which is made of a minimum and maximum radius, making it a hollow solid. The reason a sphere was chosen because it is the ideal shape testing radiation in all directions, as its thickness can be controlled radially. As seen in Figure 39 the sphere was originally chosen to be oriented such that the particle beam is fired from the centre of the sphere outwards. The conversion from a Pyg4ometry mesh into a Geant4 tessellated solid, results in only triangular faces. This is why all the quadrilateral faces are cut into two in Figure 39.

One way that was thought to analyse the energy deposition of the interactions, was to look at the CPU duration times as the mesh densities are increased. In this scenario the Geant4 solid was used as a guideline as it does not depend on a user defined stack & slice.

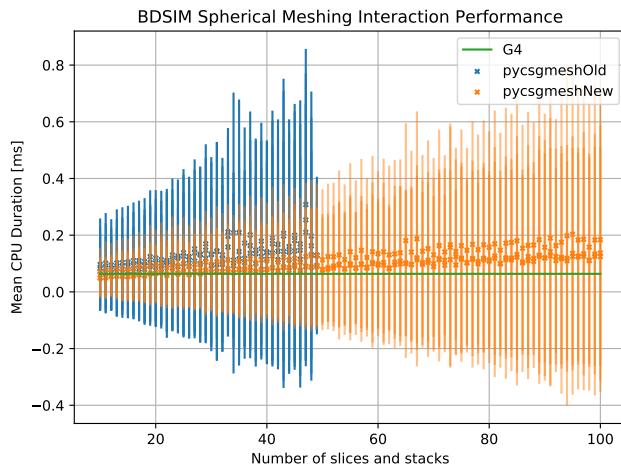


**Figure 22:** BDSIM screenshot of 10 1.3 GeV protons interacting with a Iron sphere, which has been constructed using the new meshing scripts. Mesh resolution is a stack & slice of 25 & 25. (Shown in mesh view)

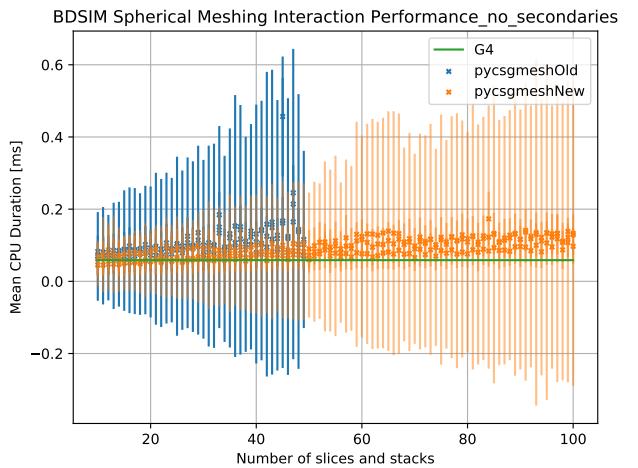
## 5.2 Iron Sphere Interactions

Property	value
$R_{Min}$	8.00 [mm]
$R_{Max}$	10.00 [mm]
Particle	$e^-$
Energy	1.3 GeV [MeV]
ngenerate	10,000

**Table 1:** TODO

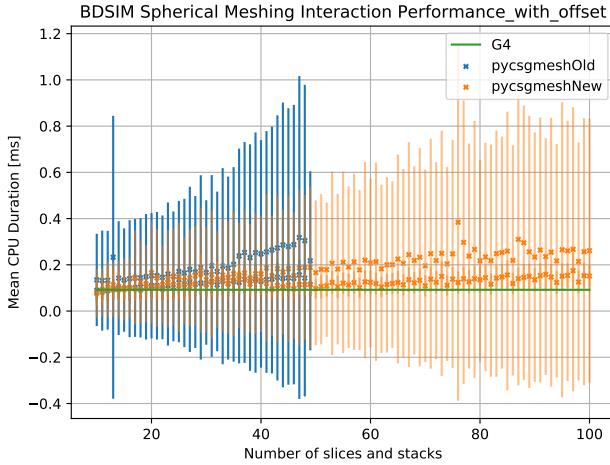


**Figure 23:** A plot showing mean CPU duration of 10,000 protons interacting with a Iron sphere of various meshed forms.

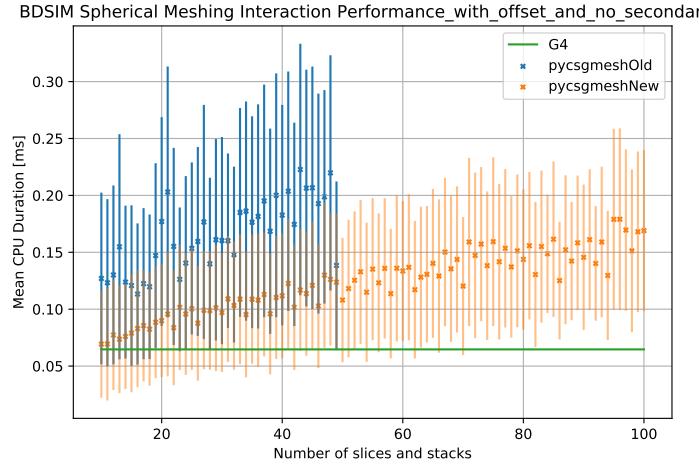


**Figure 24:** A plot showing mean CPU duration of 10,000 protons interacting with a Iron sphere of various meshed forms, with secondary particles disabled.

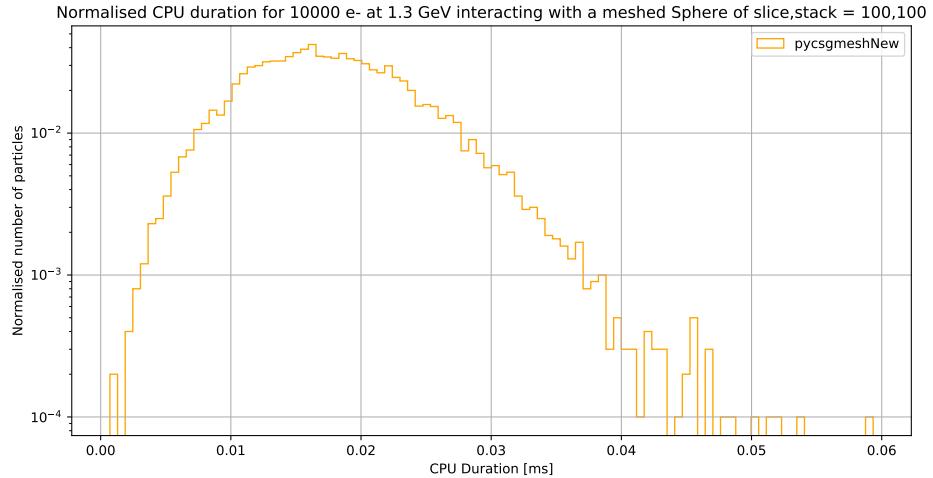
The reason for the standard deviations being so large is to do with a small number of particles in each event having a longer lifetime, thus skewing the standard deviation of the whole event. An example of this is shown in Figure 27, where the plot shows the CPU distribution for 10,000 10 MeV electrons



**Figure 25:** A plot showing mean CPU duration of 10,000 protons interacting with a Iron sphere of various meshed forms, with an 20 mm of set in the Z-axis.



**Figure 26:** A plot showing mean CPU duration of 10,000 protons interacting with a Iron sphere of various meshed forms, with secondary particles disabled, with an 20 mm of set in the Z-axis and secondaries disabled.



**Figure 27:** TODO

interacting with a G4\_Au sphere. The sphere in this example is contructed using the new pycsgmesh() function with a stack and slice both set at 100.

From Figures 43 and 43, you can see that as the number of stack and slice is increased the mean CPU duration for the protons increases at a slower rate for the new meshing.

It was orginally thought that the standard deviations of the CPU durations was related to the number of secondaries being produced. However this was disproved by Figure 43, where the same test was conducted with the BDSIM option that disables secondary particles from being produced implemented.

### 5.2.1 Error Reduction

To reduce the standard deviation of a data set the number of events needs to be increased, this proved by the relation ship shown in Equations 4. The relationship between the standard deviation and number of events is inversely square root proportional. Therefore the standard deviation should decrease with

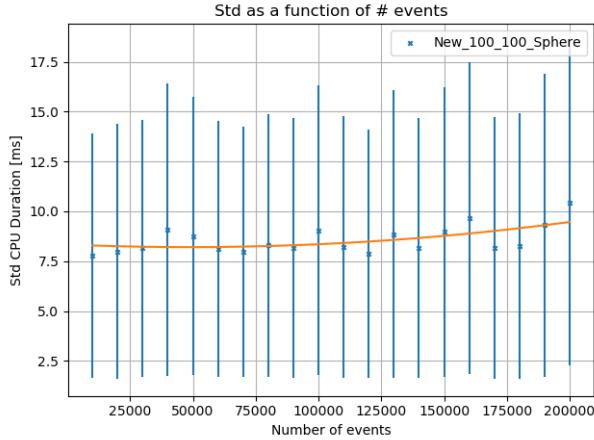
a increasing N.

$$\bar{x} = \frac{1}{N} \sum x_i$$

$$\sigma = \sqrt{\bar{x}^2} = \sqrt{\frac{1}{N} \sum (x_i - \bar{x})^2}$$

$$\sigma \propto \frac{1}{\sqrt{N}}$$
(4)

However Figure 43 shows...



**Figure 28:** TODO

The error bars are still very big so it was proposed to use the standard error of the main as an alternative. As well as as investigation for varying energy and the material of the target.

### 5.3 Choice of Materials

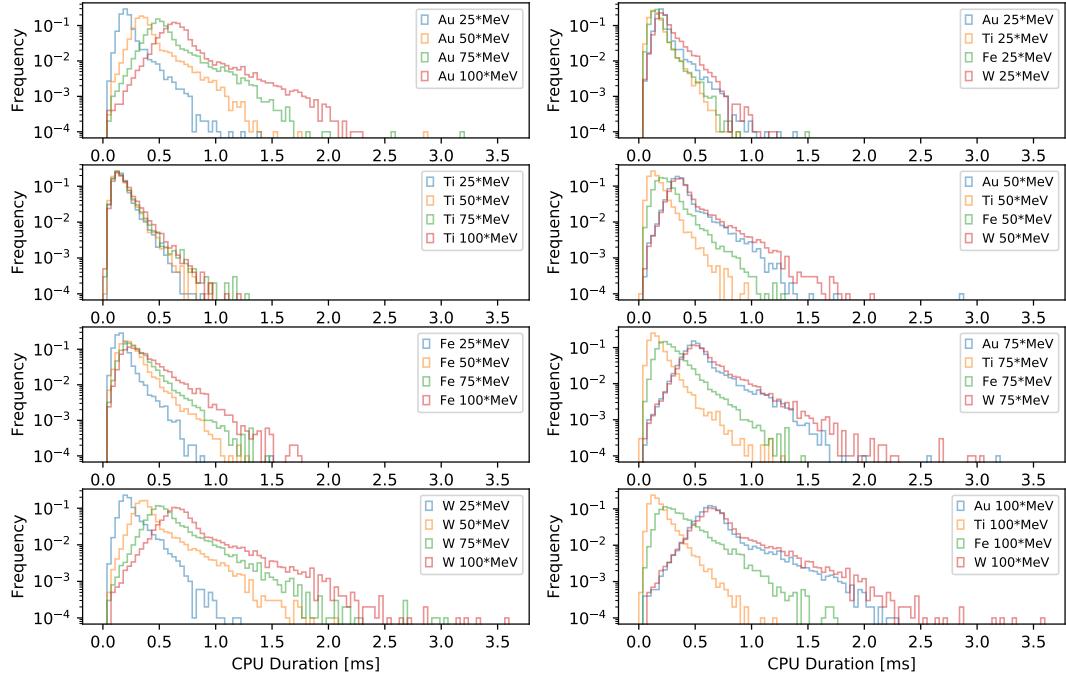
When creating meshed solids, you have the choice of material. Figure 29 shows the CPU duration time distributions for electrons interactions with Geant4 spheres constructed of different Geant4 materials across a range of energies in BDSIM. The energy range is relatively low (25 MeV → 100 MeV), this is due to the run time of the interactions increasing with energy. The run time is heavily linked to the number of secondary particles which is a function of energy. This is proven by the fact that it can be seen that as the energy is increased the width of the distribution increases. This widening is due to the number of secondary particles being produced, the more energetic an interaction the further the particle will penetrate a solid and ionise along the way generating more secondaries.

The dimensions of the spheres used in Figure 29 were set to a minimum radius of 1 micron and a maximum radius of 20 mm. It was then proposed that the radius of thickness could be scaled with respect to the stopping distance of the material it is travelling through, in order to eliminate material as a variable. The radius of thickness  $\Delta R$  can be seen depicted in Figure 30, where  $\Delta R = R_{Max} - R_{Min}$ . The next Section discusses the stopping power of materials in more detail.

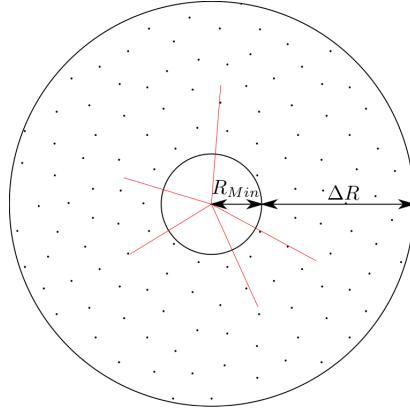
#### 5.3.1 Stopping Power

Stopping power is the force that acts against the motion of a particle within in a material, causing it to lose energy. The Geant4 example “TestEm0” outputs the stopping power and distances for a given material and particle energy. If the energy of the incident particle and the stopping power of the material is known, a stopping distance can be calculated. The values for stopping power in this project are calculated by the TestEm0 example, which extracting values from a Geant4 data lists and then interpolates or extrapolates between them, as the stopping power is a function of. The extracted stopping powers match with values found in other studies, such as [13].

Material CPU Duration Time Dist of e- and G4 sphere for n=10000



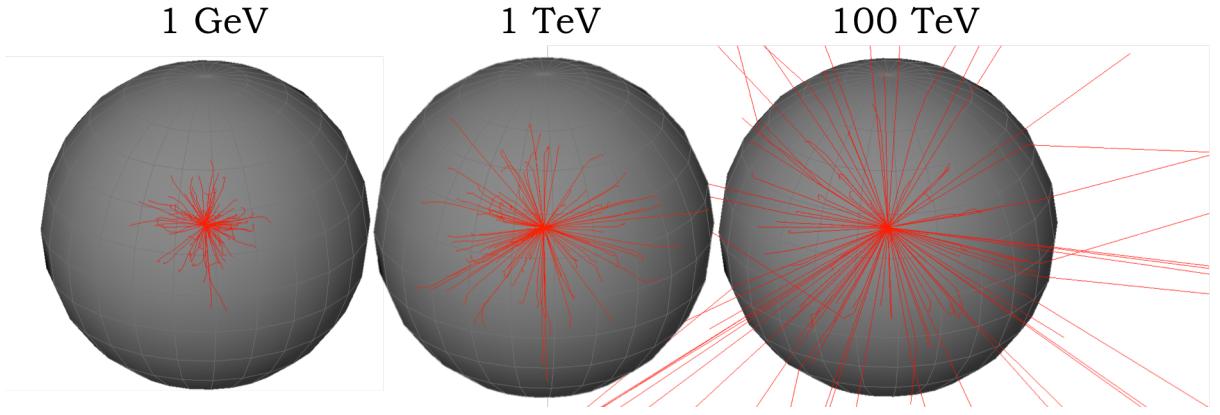
**Figure 29:** Histograms showing the CPU duration distributions of varying Geant4 materials and particle energies in BDSIM on a Geant4 sphere. The left 4 histograms show the distributions show the varying of energy upon each material. The right 4 histograms show the varying of material at each set energy. Each plot is normalised by the initial 10,000 electrons in each event.



**Figure 30:** A diagram depicting a cross section of a sphere, which has a minimum and maximum radius. The diagram was drawn using the CAD software Inkscape.

Figure 31 shows a sphere made of G4\_W, undergoing interactions with batches of 100 electrons at 3 different energies. The spheres radius of thickness is set to the be the stopping distance for G4\_W interacting with a 1 TeV electron. It can be seen that when the energy of the electrons is 1 GeV, which is below the 1 TeV (the stopping distance energy for this situation), the tracks of the interactions are all contained within the sphere. The opposite happens when the electrons energies are more than 1 TeV, where most if not all of the particle tracks leave the sphere.

With the stopping power in mind Figure 29 was reproduced, but instead of using the same dimensions for each sphere,  $\Delta R$  was scaled by the stopping distance. The radius of thickness is set to be the extracted stopping distance for a 100 MeV electron interacting with the material in question. The



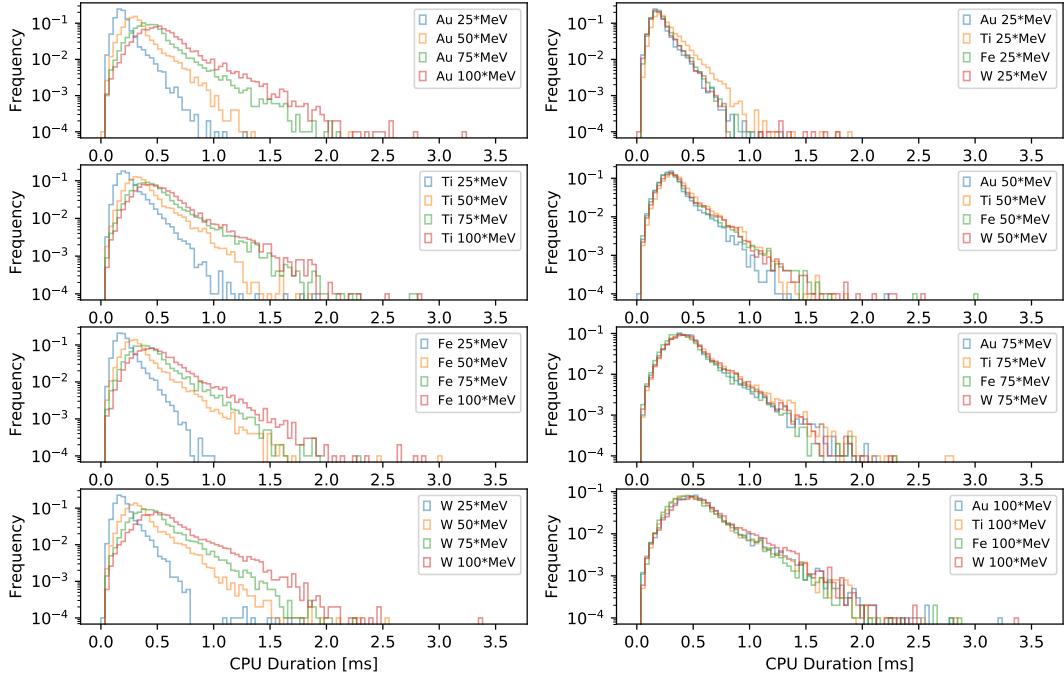
**Figure 31:** Screenshots of 1 GeV, 1 TeV & 100 TeV electrons interacting with a tungsten sphere. Where the radius of thickness is set to the extracted Geant4 stopping distance of a 1 TeV electron in tungsten.

values of  $\Delta R$  are shown in Table 3.

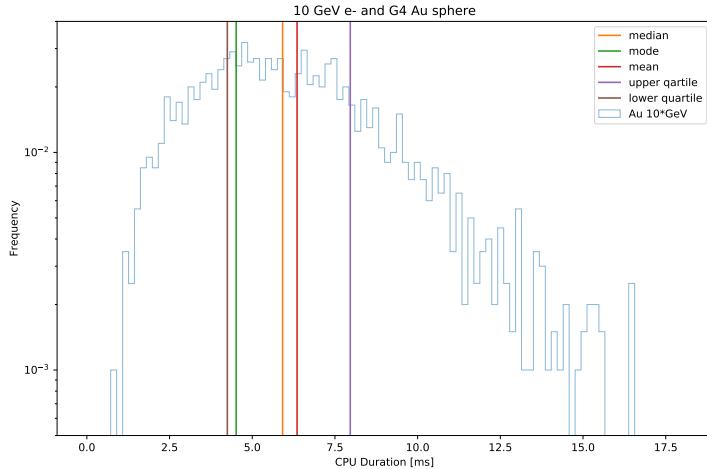
Material	$\Delta R$ [mm]
G4_Au	9.89382
G4_Ti	33.6854
G4_Fe	62.3434
G4_W	10.1631

**Table 2:** A table showing the values of  $\Delta R$  used in Figure 32.

It can be seen that in Figure 32, the scaling of radius relative to stopping distances, generates histograms which act extremely similar at the same particle energies irrespective of the material it propagates through. This is very interesting as it means that for any further analysis, material can be ruled out as a variable and only energy needs to be varied.



**Figure 32:** Histograms showing the CPU duration distributions of varying materials and particle energies in BDSIM on a Geant4 sphere. The left 4 histograms show the distributions show the varying of energy on each material. The right 4 histograms show the varying of material at a set energy. Each plot is normalised by the initial 10,000 electrons in each event.



**Figure 33:** Meshing Development for Tubs (Solid & Mesh View)

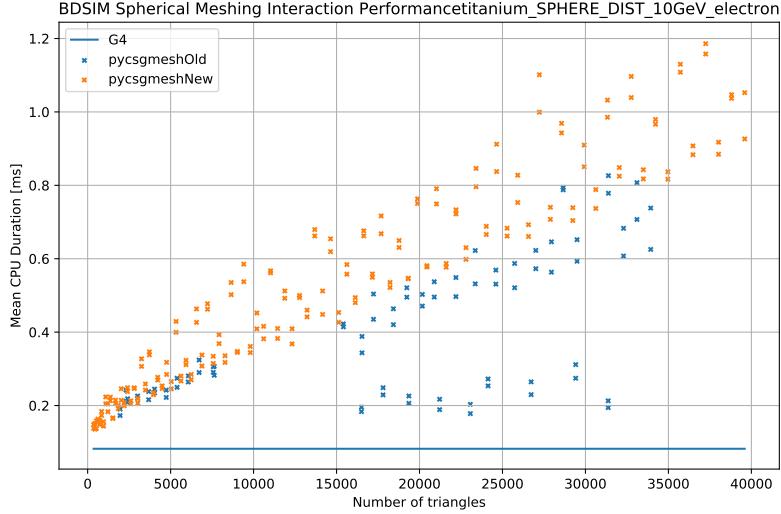
## 5.4 Titanium Sphere Interactions & Spherical Beam Distribution

### 5.5 Interactions with CAD

As a final goal to round off the project, an imported CAD model was compared with a compound boolean meshed solid of a generic bolt, shown in Figure 37. The CAD bolt was downloaded as a STEP format from a free online database GradCAD [14]. The downloaded model was converted to GDML format with the material G4\_STAINLESS-STEEL using python. The dimensions of the CAD model

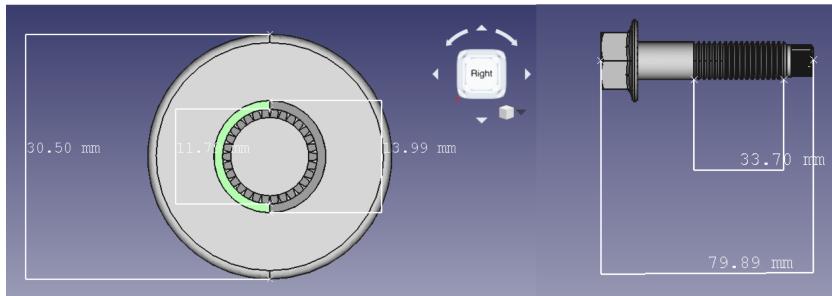
Property	value
$R_{Min}$	0.01 [mm]
$R_{Max}$	10.00 [mm]
Particle	$e^-$
Energy	10 [GeV]
ngenerate	?

**Table 3:** TODO

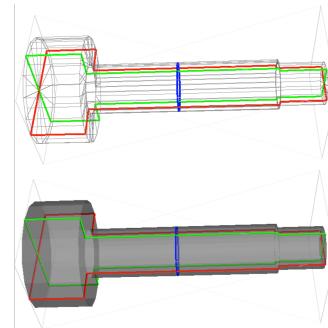


**Figure 34:** TODO

were gained by using the measuring tool within the Freecad GUI as shown Figure 35. The CAD was then approximately recreated by the constructed of basic primitive solids with boolean operations in Pyg4ometry and can be seen in Figure 36.

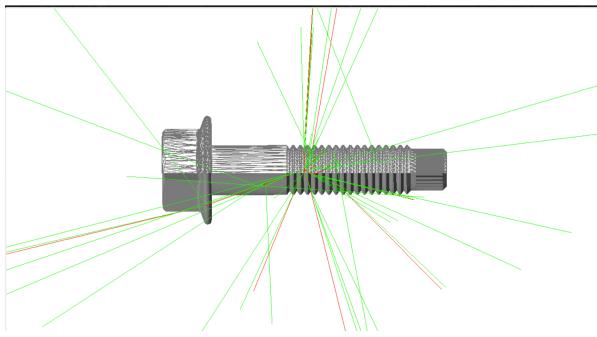


**Figure 35:** TODO

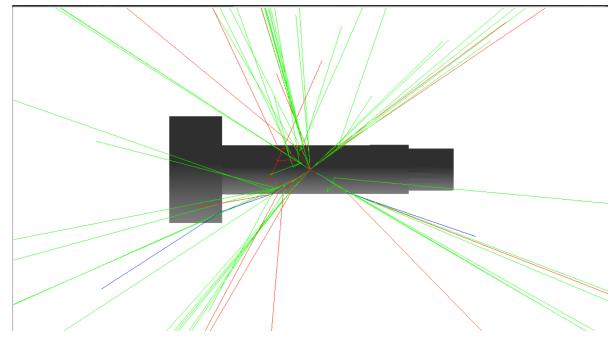


**Figure 36:** TODO

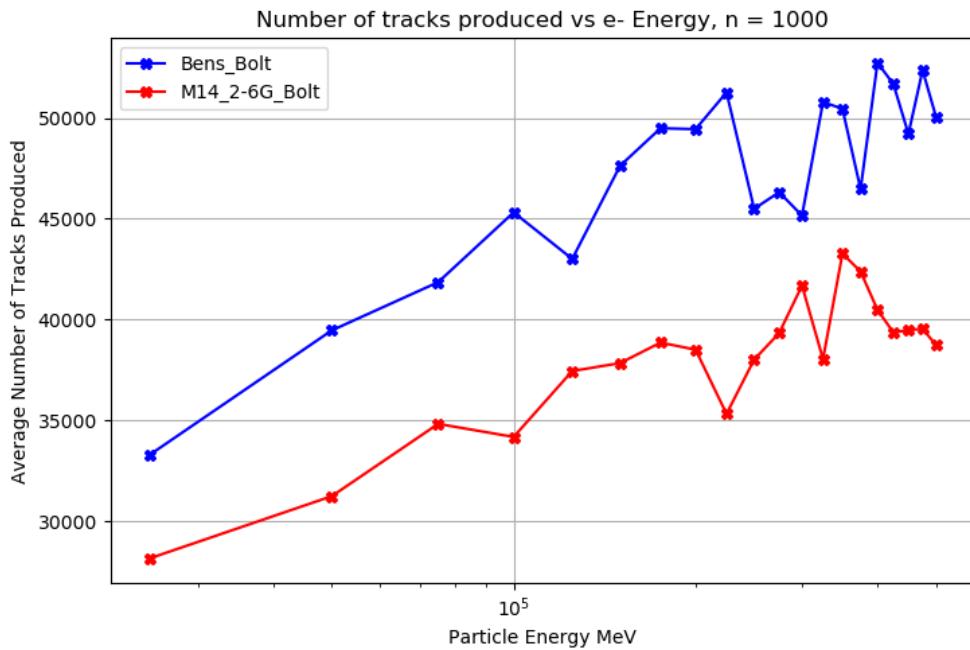
Both were then ran in BDSIM for a variety of energies



**Figure 37:** TODO



**Figure 38:** TODO



**Figure 39:** TODO

## 6 Conclusion & Summary

### 6.1 Improvements

meshing is quicker

BDSIM interactions are quicker but still slower than G4 solid (as expected) improved coverage unit test speeds

meshing is neater and more uniform in structure

higher meshing density = closer to true solid as expected with BDISM interactions

quote graphs and sections

### 6.2 Applications

BDSIM and Pyg4ometry are both very powerful software packages that can be used to aid not only the scientific research community of particle physicist, but also help everyday people by improving medical treatment. Thanks to the software being open source and its wide range of file compatibilities it can be used to simulate a growing number of projects. This report demonstrates this by CAD magnet modelling.

### **6.3 Extension**

If given more time ...  
prototype magnet in appendix

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# A Appendix (Python scripts)

## A.1 Sphere BDSIM Vary Mesh Test

```
from string import Template
2 import Target_Sphere as t
import numpy as np
4 import pybdsim

6 #####
8 def run_gdml_spheres_same_slice_and_stack(min,max):
10 """
11     generate a .txt wth four lists of data , number of slices & runtimes ,
12     from a minimum and maximum number of slices and stacks
13 """
14
15     Meshing_ver = "New"
16
17     for val in range(min,max+1):
18
19         # create gdml
20         t.Test(False, False, n_slice = val, n_stack = val)
21
22         #make gmad
23         f = open('Template.gmad', 'r')
24         contents = f.read()
25         f.close()
26         template = Template(contents)
27         d = {'value': str("gdml://../GDMILs/" + Meshing_ver + "/Target_Sphere_" + str(
28             val) + "_" + str(val) + ".gdml")}
29         rendered = template.substitute(d)
30         gmadfilename = "GMADs/" + Meshing_ver + "/slice_" + str(val) + "_stack_" + str(val)
31         + ".gmad"
32         f = open(gmadfilename, 'w')
33         f.write(rendered)
34         f.close()
35
36         # use gmad and gdml to get root output
37         pybdsim.Run.RunBdsim(gmadfilename, "root_outputs/" + Meshing_ver + "/" + str(
38             val) + "_" + str(val))
39
40         #load in root file to do analysis ...
41
42         print "{}%".format((val-min+1)/(max-min)))
43 #####
44
45 run_gdml_spheres_same_slice_and_stack(10,100)
```

Scripts//Run\_New\_Meshes.py

## B All Meshed Solids and Polygon Count Plots

The following Figures are the meshing and polygon data for each primitive solid constructed in Pyg4ometry 3.1. The first Figure for each solid is a screenshot of the old meshing and new meshing visualized in VTK. They show the before and after of each primitive solid in both "solid view" and "mesh view". The second Figures Show the number of polygons and triangles produced by the solid as you increase the slice across a range of 10-100 (if there is a stack it is kept at a constant 10). The polygon data plots are generate using python 2.7. The naming convention is the one used by Geant4 3.2.

### B.0.1 Cons

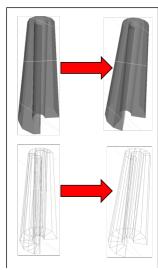


Figure 40

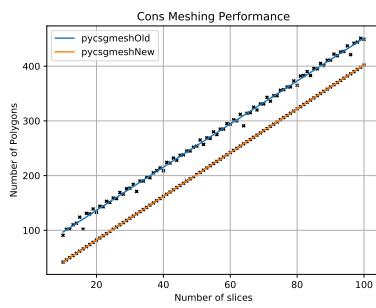


Figure 41

### B.0.4 EllipticalCone

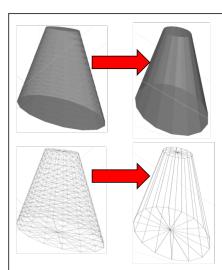


Figure 46

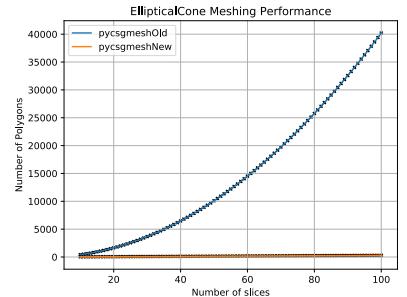


Figure 47

### B.0.2 CutTubs

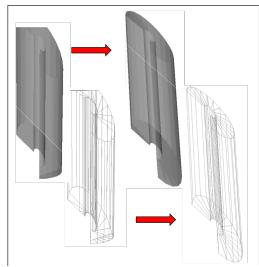


Figure 42

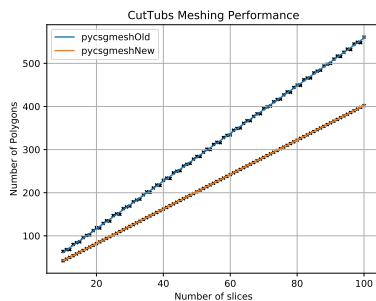


Figure 43

### B.0.5 EllipticalTube

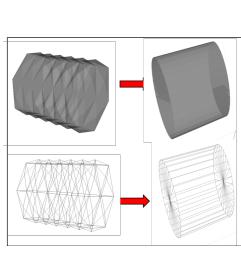


Figure 48

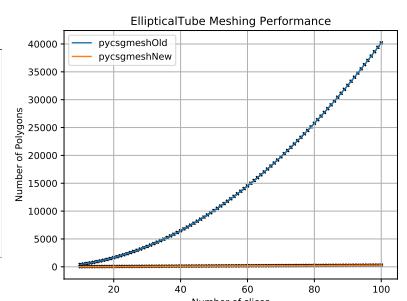


Figure 49

### B.0.3 Ellipsoid

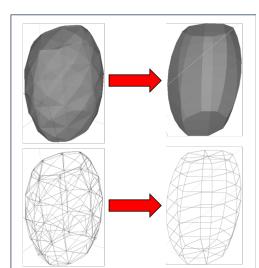


Figure 44

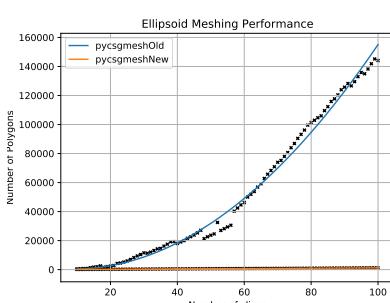


Figure 45

### B.0.6 Hyperboloid

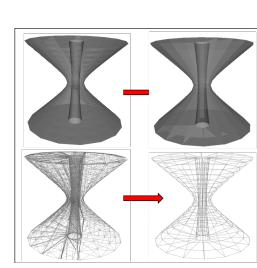


Figure 50

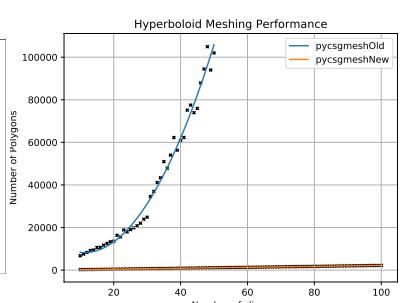


Figure 51

### B.0.7 Orb

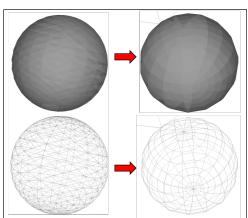


Figure 52

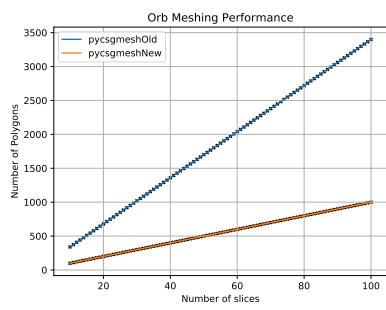


Figure 53

### B.0.10 Sphere

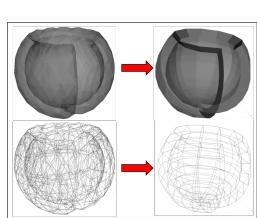


Figure 58

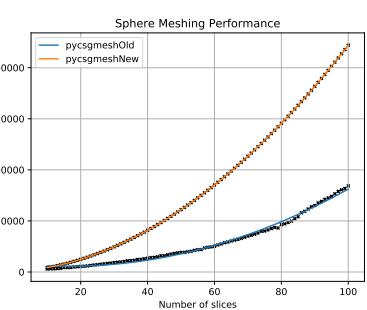


Figure 59

### B.0.8 Paraboloid

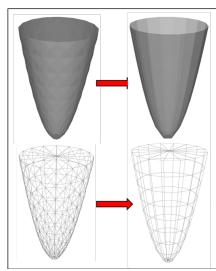


Figure 54

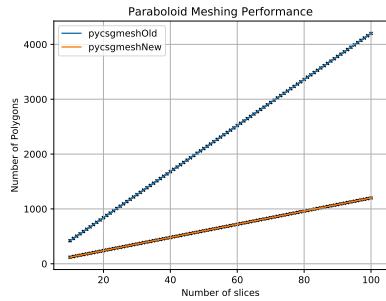


Figure 55

### B.0.11 Torus

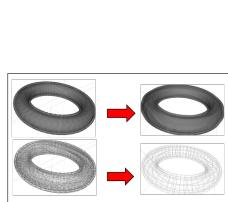


Figure 60

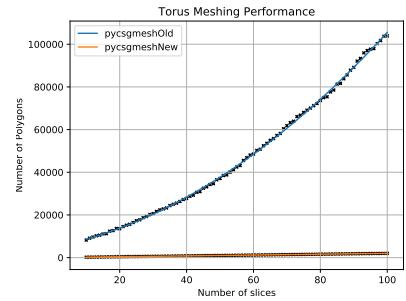


Figure 61

### B.0.9 Polycone

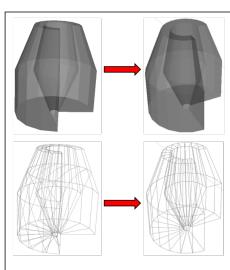


Figure 56

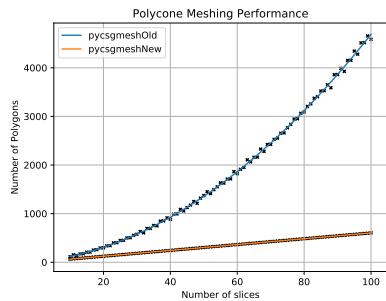


Figure 57

### B.0.12 Tubs

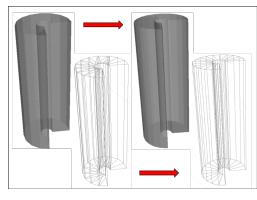


Figure 62

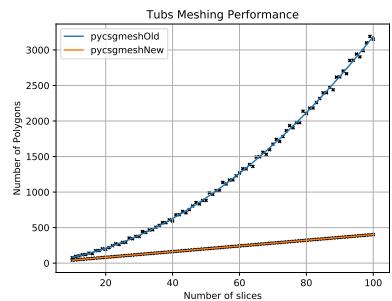


Figure 63

## C Quadratic Parameters for polygon count plots

The quadratic fit where its parameters are of the form:

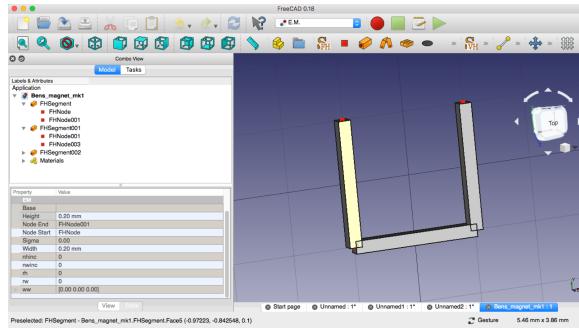
$$ax^2 + bx + c = 0 \quad (5)$$

**Table 4:** A Table showing the parameters to the quadratic fits for the polygon count plot.

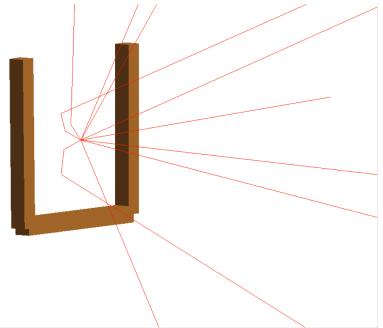
Curved Primitive Solid	Old a	Old b	Old c	New a	New b	New c
Cons	-2.74E-04	3.97E+00	5.72E+01	-3.83E-17	4.00E+00	2.00E+00
CutTubs	2.19E-04	5.50E+00	6.30E+00	-3.83E-17	4.00E+00	2.00E+00
Ellipsoid	18.65090372	-333.5688153	1919.792901	1.61E-17	1.20E+01	0.00E+00
EllipticalCone	4.00E+00	2.00E+00	2.41E-12	4.03E-18	3.00E+00	0.00E+00
EllipticalTube	-1.94E-16	4.20E+01	-5.72E-13	4.03E-18	3.00E+00	0.00E+00
Hyperboloid	64.83177713	-1452.629624	16378.18198	4.84E-17	2.20E+01	-9.53E-14
Orb	-6.45E-17	3.40E+01	-1.91E-13	-8.06E-18	1.00E+01	-4.77E-14
Paraboloid	-1.94E-16	3.40E+01	-1.91E-13	1.61E-17	1.20E+01	0.00E+00
Polycone	0.39682347	7.13011557	7.42466252	-4.03E-17	6.00E+00	4.00E+00
Sphere	10.82154926	-356.6329124	8557.249195	2.00E+01	2.20E+02	1.98E-11
Torus	7.01776508	304.8746037	4899.196225	-1.61E-17	2.00E+01	-9.53E-14
Tubs	0.27241769	4.58191175	8.33675211	-3.83E-17	4.00E+00	2.00E+00

## D Prototype Freecad Magnet

First attempt at a prototype magnet made using Freecad GUI (Figure 64) and exported as a STEP file, which was then converted to a GDML format with Geant4 material G4\_Cu using python. A magnet field was then mapped on to the shape using a preset dipole field in BDSIM, in which you can see electrons repelling in Figure 65.



**Figure 64:** Freecad screenshot



**Figure 65:** BDSIM screenshot