Code for Figures S6 and S7

August 28, 2016

1 Get the combined datasets for all the scenarios

Load the necessary libraries:

```
library(ggplot2)
library(clusterGeneration)

## Loading required package: MASS
source("functions.R")
```

Load the files representing the summary for each scenario and save the results in a single dataframe, VarsAll:

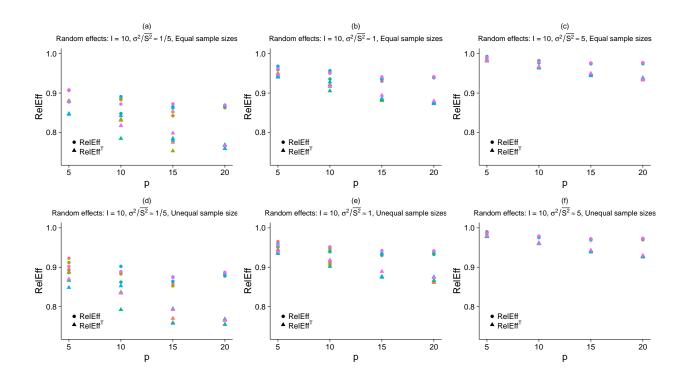
```
allFiles <- list.files("simResultsComb")</pre>
##save the three Vars for the different combinations
VarsAll \leftarrow expand.grid(p = c(5,10,15,20),
                        randVar = 1:5,
                        het = c(0.2, 1, 5),
                        sampleType = c("same", "diff"),
                        I = c(10,20)
VarsAll$known <- VarsAll$unknown <- VarsAll$univKnown <- VarsAll$univ <-
 VarsAll$knownEmpWithin <- VarsAll$univKnownEmpWithin <- NA
for(file in 1:length(allFiles))
    load(paste("simResultsComb", allFiles[file], sep="/"))
    rowNr <- gsub("combine_cost_of_estimation_post_SIM", "", allFiles[file])</pre>
    rowNr <- gsub(".RData", "", rowNr)</pre>
    rowNr <- as.numeric(rowNr)</pre>
    VarsAll[rowNr, c("p","randVar","het","sampleType","I",
                      "univ", "univKnown",
                      "unknown", "known")] <-
      Vars[rowNr, c("p","randVar","het","sampleType","I",
                     "univ", "univKnown",
                     "unknown", "known")]
    ##get number of studies, number of parameters, scenario number, etc
    p <- VarsAll[rowNr, "p"]</pre>
```

```
randVar <- VarsAll[rowNr, "randVar"]</pre>
   het <- VarsAll[rowNr, "het"]</pre>
    sampleType <- VarsAll[rowNr, "sampleType"]</pre>
    I <- VarsAll[rowNr, "I"]</pre>
    ##get theoretical variances of multivariate and univariate estimators
    varMult <- varUniv <- varUnivT1 <- varUnivT2 <- matrix(0, p, p)</pre>
    ##simulate Sigma again
    ##set.seed(381048+1940*randVar)
    ##Sigma <- cov2cor(genPositiveDefMat(p)$Sigma)*het
    D <- diag(diag(Sigma))</pre>
    for(site in 1:I)
      ##StudyEmpVars[[site]] <- StudyEmpVars[[site]] + Sigma
      varMult <- varMult+solve(StudyEmpVars[[site]]+Sigma)</pre>
      Uisite <- diag(diag(StudyEmpVars[[site]]))</pre>
      varUnivT1 <- varUnivT1+solve(Uisite+D)</pre>
      varUnivT2 <- varUnivT2+</pre>
        solve(Uisite+D) %*% (StudyEmpVars[[site]]+Sigma) %*% solve(Uisite+D)
    varMult <- solve(varMult)</pre>
    varUnivT1 <- solve(varUnivT1)</pre>
    varUniv <- varUnivT1 %*% varUnivT2 %*% varUnivT1</pre>
    VarsAll[rowNr, c("knownEmpWithin","univKnownEmpWithin")] <-</pre>
      c(varMult[1], varUniv[1])
VarsAll$Ratio <- VarsAll$known/VarsAll$unknown
VarsAll$RelEff <- VarsAll$unknown/VarsAll$univ
VarsAll$RelEffT <- VarsAll$known/VarsAll$univKnown
VarsAll$RelEffTAsympt <- VarsAll$knownEmpWithin/VarsAll$univKnownEmpWithin
range(VarsAll$Ratio)
## [1] 0.8521896 0.9982430
```

```
##get the minimum value for Sigma^2 = 5
min(VarsAll$RelEff[VarsAll$Sigma2 == "Sigma^2 = 5"])
## [1] 0.9404613
##change format so it's ggplot-friendly
RelEffSame <-
  rbind(cbind(as.matrix(VarsAllSame[,c("p", "I", "randVar", "RelEff"),]), "RelEff"),
        cbind(as.matrix(VarsAllSame[,c("p", "I", "randVar", "RelEffT"),]),"RelEffT"),
        cbind(as.matrix(VarsAllSame[,c("p", "I", "randVar", "RelEffTAsympt"),]),"RelEffTAsympt"))
colnames(RelEffSame)[5] <- "Estimate"</pre>
RelEffSame <- as.data.frame(RelEffSame)</pre>
RelEffSame$Sigma2 <- factor(c(as.character(VarsAllSame$Sigma2), as.character(VarsAllSame$Sigma2),
                               as.character(VarsAllSame$Sigma2)),
                             levels = c("Sigma^2 = 1/5", "Sigma^2 = 1", "Sigma^2 = 5"))
RelEffSame$p <- as.numeric(as.character(RelEffSame$p))</pre>
RelEffSame$RelEff <- as.numeric(as.character(RelEffSame$RelEff))</pre>
##
RelEffDiff <-
  rbind(cbind(as.matrix(VarsAllDiff[,c("p", "I", "randVar", "RelEff"),]),"RelEff"),
        cbind(as.matrix(VarsAllDiff[,c("p", "I", "randVar", "RelEffT"),]),"RelEffT"),
        cbind(as.matrix(VarsAllDiff[,c("p", "I", "randVar", "RelEffTAsympt"),]),"RelEffTAsympt"))
colnames(RelEffDiff)[5] <- "Estimate"</pre>
RelEffDiff <- as.data.frame(RelEffDiff)</pre>
RelEffDiff$Sigma2 <- factor(c(as.character(VarsAllDiff$Sigma2), as.character(VarsAllDiff$Sigma2),</pre>
                               as.character(VarsAllDiff$Sigma2)),
                             levels = c("Sigma^2 = 1/5", "Sigma^2 = 1", "Sigma^2 = 5"))
RelEffDiff$p <- as.numeric(as.character(RelEffDiff$p))</pre>
RelEffDiff$RelEff <- as.numeric(as.character(RelEffDiff$RelEff))</pre>
##take out the asymptotic relative efficiency
RelEffSame <- RelEffSame[RelEffSame$Estimate != "RelEffTAsympt",]</pre>
RelEffDiff <- RelEffDiff[RelEffDiff$Estimate != "RelEffTAsympt",]</pre>
```

2 Make Figure S6

```
I, " = ", 10, ", ",
                                          sigma^2/bar(S^2), phantom() %~~% phantom() , 1, ", ",
                                          "Equal sample sizes"))))
I_10_Same_Panel_C <- panelFigS6S7(I=10, subsetSigma2 = "Sigma^2 = 5", RelEffSubs = RelEffSame) +
  labs(color="", shape="",
       title=expression(atop("(c)", paste("Random effects: ",
                                          I, " = ", 10, ", ",
                                          sigma^2/bar(S^2), phantom() %~~% phantom(), 5, ", ",
                                          "Equal sample sizes"))))
I_10_Diff_Panel_A <- panelFigS6S7(I=10, subsetSigma2 = "Sigma^2 = 1/5", RelEffSubs = RelEffDiff) +
  labs(color="", shape="",
       title=expression(atop("(d)", paste("Random effects: ",
                                          I, " = ", 10, ", ",
                                          sigma^2/bar(S^2), phantom() %~~% phantom(), 1/5, ", ",
                                          "Unequal sample sizes"))))
I_10_Diff_Panel_B <- panelFigS6S7(I=10, subsetSigma2 = "Sigma^2 = 1", RelEffSubs = RelEffDiff) +
  labs(color="", shape="",
       title=expression(atop("(e)", paste("Random effects: ",
                                          I, " = ", 10, ", ",
                                          sigma^2/bar(S^2), phantom() %~~% phantom() , 1, ", ",
                                          "Unequal sample sizes"))))
I_10_Diff_Panel_C <- panelFigS6S7(I=10, subsetSigma2 = "Sigma^2 = 5", RelEffSubs = RelEffDiff) +
  labs(color="", shape="",
       title=expression(atop("(f)", paste("Random effects: ",
                                          I, " = ", 10, ", ",
                                          sigma^2/bar(S^2), phantom() %~~% phantom() , 5, ", ",
                                          "Unequal sample sizes"))))
   Put all 6 panels together for Figure S6:
multiplot(I 10 Same Panel A, I 10 Diff Panel A,
          I_10_Same_Panel_B, I_10_Diff_Panel_B,
          I_10_Same_Panel_C, I_10_Diff_Panel_C,
          cols=3)
## Loading required package: grid
```



3 Make Figure S7

```
I_20_Same_Panel_A <- panelFigS6S7(I=20, subsetSigma2 = "Sigma^2 = 1/5", RelEffSubs = RelEffSame) +
  labs(color="", shape="",
       title=expression(atop("(a)", paste("Random effects: ",
                                          I, " = ", 20, ", ",
                                          sigma^2/bar(S^2), phantom() %~~% phantom(), 1/5, ", ",
                                          "Equal sample sizes"))))
I_20_Same_Panel_B <- panelFigS6S7(I=20, subsetSigma2 = "Sigma^2 = 1", RelEffSubs = RelEffSame) +
  labs(color="", shape="",
       title=expression(atop("(b)", paste("Random effects: ",
                                          I, " = ", 20, ", ",
                                          sigma^2/bar(S^2), phantom() %~~% phantom() , 1, ", ",
                                          "Equal sample sizes"))))
I_20_Same_Panel_C <- panelFigS6S7(I=20, subsetSigma2 = "Sigma^2 = 5", RelEffSubs = RelEffSame) +
  labs(color="", shape="",
       title=expression(atop("(c)", paste("Random effects: ",
                                          I, " = ", 20, ", ",
                                          sigma^2/bar(S^2), phantom() %~~% phantom() , 5, ", ",
                                          "Equal sample sizes"))))
I_20_Diff_Panel_A <- panelFigS6S7(I=20, subsetSigma2 = "Sigma^2 = 1/5", RelEffSubs = RelEffDiff) +
  labs(color="", shape="",
       title=expression(atop("(d)", paste("Random effects: ",
```

```
I, " = ", 20, ", ",
                                                              sigma^2/bar(S^2), phantom() %~~% phantom(), 1/5, ", ",
                                                              "Unequal sample sizes"))))
I_20_Diff_Panel_B <- panelFigS6S7(I=20, subsetSigma2 = "Sigma^2 = 1", RelEffSubs = RelEffDiff) +
   labs(color="", shape="",
          title=expression(atop("(e)", paste("Random effects: ",
                                                              I, " = ", 20, ", ",
                                                              sigma^2/bar(S^2), phantom() %~~% phantom() , 1, ", ",
                                                              "Unequal sample sizes"))))
I_20_Diff_Panel_C <- panelFigS6S7(I=20, subsetSigma2 = "Sigma^2 = 5", RelEffSubs = RelEffDiff) +
   labs(color="", shape="",
          title=expression(atop("(f)", paste("Random effects: ",
                                                              I, " = ", 20, ", ",
                                                              sigma^2/bar(S^2), phantom() %~~% phantom() , 5, ", ",
                                                              "Unequal sample sizes"))))
    Put all 6 panels together for Figure S7:
multiplot(I_20_Same_Panel_A, I_20_Diff_Panel_A,
               I_20_Same_Panel_B, I_20_Diff_Panel_B,
               I_20_Same_Panel_C, I_20_Diff_Panel_C,
               cols=3)
      Random effects: I = 20, \sigma^2/\overline{S^2} \approx 1/5, Equal sample sizes
                                                   Random effects: I = 20, \sigma^2/\overline{S^2}\approx 1, Equal sample sizes
                                                                                               Random effects: I = 20, \sigma^2/\overline{S^2}\approx 5, Equal sample sizes
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     Random effects: I = 20, \sigma^2/\overline{S^2} \approx 1/5, Unequal sample size
                                                  Random effects: I = 20, \sigma^2/\overline{S^2} \approx 1, Unequal sample sizes
                                                                                              Random effects: I = 20, \sigma^2/\overline{S^2} \approx 5, Unequal sample sizes
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    RelEff

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